

# COMP 3311 DATABASE MANAGEMENT SYSTEMS

## LECTURE 18 EXERCISES QUERY OPTIMIZATION

# EXAMPLE RELATIONAL DATABASE

Sailor(sailorId, sName, rating, age)

Boat(boatId, bName, color)

Reserves(sailorId, boatId, rDate)

- There are 10,000 Sailor tuples, 100,000 Reserves tuples and 1,000 Boat tuples.
- Assume that for all files there are 10 tuples per page.  
👉  $B_{\text{Sailor}} = 1,000$  pages;  $B_{\text{Reserves}} = 10,000$  pages;  $B_{\text{Boat}} = 100$  pages
- Assume a main memory buffer,  $M$ , of 100 pages.
- Assume that there are the following indexes:
  - hash index on sailorId for Sailor (no overflow buckets).
  - clustering B<sup>+</sup>-tree index on rDate for Reserves (2 levels).
  - hash index on boatId for Boat (no overflow buckets).
- Our goal is to process the query:

```
select *  
from Sailor natural join Reserves natural join Boat  
where rDate = '01-JAN-2020'  
and color = 'red';
```

## Some useful statistics:

- Reserves has 1,000 unique rDates.
- 10% of boats are red.
- A sailor has on average 10 reservations.

# EXERCISE 1

Estimate the query processing cost **using materialization** and the join order

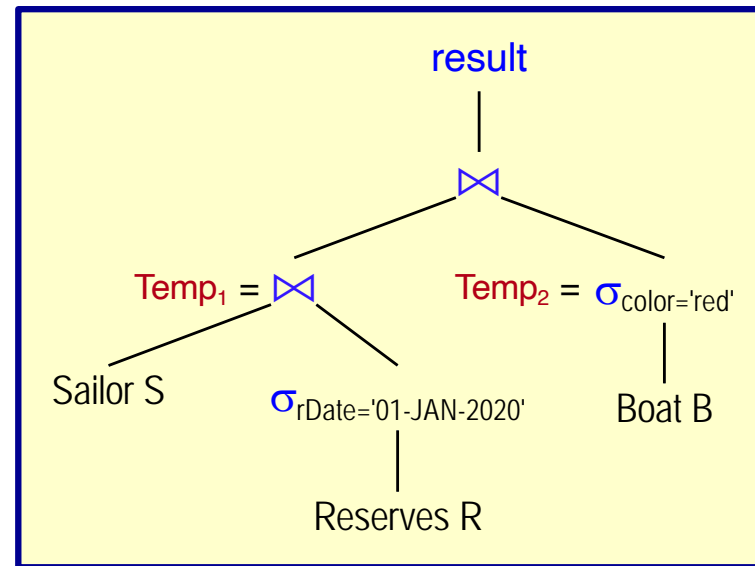
$(\text{Sailor JOIN } \sigma_{R.rDate='01-JAN-2020'} \text{Reserves}) \text{ JOIN } \sigma_{color='red'} \text{Boat}$

$C_1$ : Cost of computing  $\text{Temp}_1 = (\text{Sailor JOIN } \sigma_{R.rDate='01-JAN-2020'} \text{Reserves})$

$C_2$ : Cost of computing  $\text{Temp}_2 = \sigma_{color='red'} \text{Boat}$  (no index on color)

$C_3$ : Cost of  $\text{Temp}_1 \text{ JOIN } \text{Temp}_2$

**Total cost:**  $C_1 + C_2 + C_3$



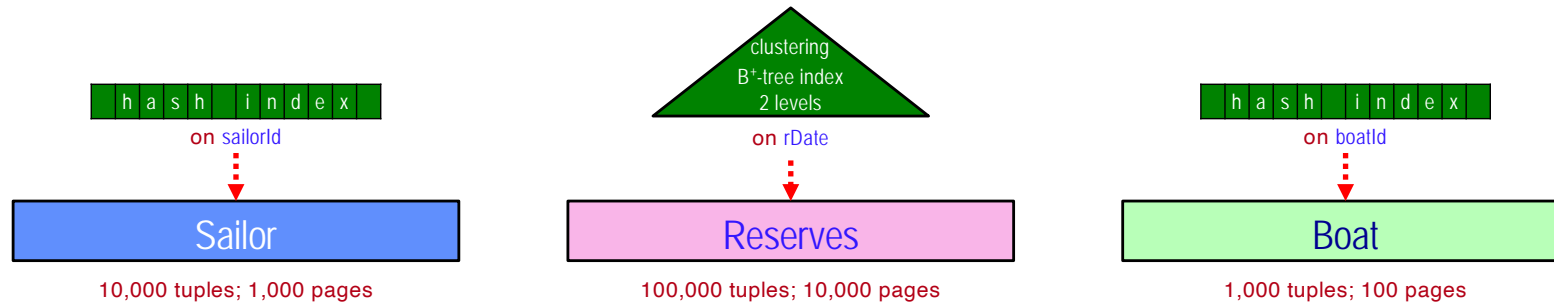
# EXERCISE 1 (CONTD)

Sailor(sailorId, sName, rating, age)

Boat(boatId, bName, color)

Reserves(sailorId, boatId, rDate)

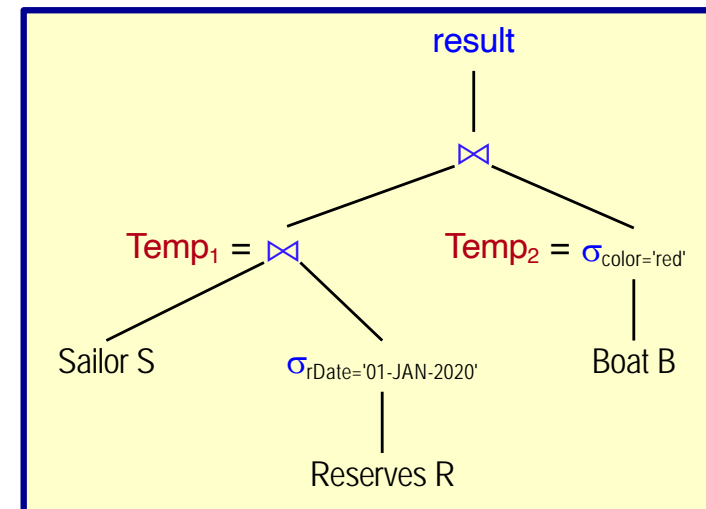
bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
 Hash index: Sailor.sailorId  
 B<sup>+</sup>-tree index: Reserves.rDate (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10



```
select *
from Sailor natural join Reserves natural join Boat
where rDate = '01-JAN-2020'
and color = 'red';
```

## Some useful statistics:

- Reserves has 1,000 unique rDates.
- 10% of boats are red.
- A sailor has on average 10 reservations



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select *
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## EXERCISE 1 (CONTD)

*bf*: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
 Hash index: Sailor.sailorId  
 B+-tree index: Reserves.rDate  
                   (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10

$C_1$ : Cost of computing  $\text{Temp}_1 = (\text{Sailor JOIN } \sigma_{\text{R.rDate}='01\text{-JAN-2020'}} \text{Reserves})$

In order to estimate  $C_1$ , we need to determine the best evaluation plan (sub-plan) for computing  $\text{Temp}_1$ .

Some alternative join strategies:

- block nested-loop – Sailor as outer relation:  $\lceil B_r / (M-2) \rceil * B_s + B_r$ .
- block nested-loop – Reserves as outer relation:  $\lceil B_r / (M-2) \rceil * B_s + B_r$ .
- sort-merge join:  $B_r + B_s + \text{sorting cost: } 2 * B_r * (1 + \lceil \log_{M-1}(B_r/M) \rceil)$ .
- hash join:  $3 * (B_r + B_s)$ .
- indexed nested-loop – Reserves as outer relation:  $B_r + n_r * c$ .

```
select *
from Sailor natural join Reserves natural join Boat
where rDate = '01-JAN-2020'
and color = 'red';
```

## EXERCISE 1 (CONTD)

bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
 Hash index: Sailor.sailorId  
 B+-tree index: Reserves.rDate  
                   (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10

$C_1$ : Cost of computing  $\text{Temp}_1 = (\text{Sailor JOIN } \sigma_{\text{R.rDate}='01\text{-JAN-2020'}} \text{Reserves})$

a) **Strategy:** block nested-loop – Sailor as outer relation.

$$\begin{aligned} \text{Cost: } \lceil B_r / (M-2) \rceil * B_s + B_r &= \lceil 1000 / (100-2) \rceil * 10000 + 1000 \\ &= \underline{110,100} \text{ page I/Os} \end{aligned}$$

b) **Strategy:** block nested-loop – Reserves as outer relation.

$$\begin{aligned} \text{Cost: } \lceil B_r / (M-2) \rceil * B_s + B_r &= \lceil 10000 / (100-2) \rceil * 1000 + 10000 \\ &= \underline{113,000} \text{ page I/Os} \end{aligned}$$

c) **Strategy:** sort-merge join:  $B_r + B_s + \text{sorting cost}$ .

$$\begin{aligned} \text{Sort cost Sailor: } 2 * B_r * (1 + \lceil \log_{M-1}(B_r/M) \rceil) \\ = 2 * 1000 * (1 + \lceil \log_{100-1}(1000/100) \rceil) &= 6000 \end{aligned}$$

$$\begin{aligned} \text{Sort cost Reserves: } 2 * B_r * (1 + \lceil \log_{M-1}(B_r/M) \rceil) \\ = 2 * 10000 * (1 + \lceil \log_{100-1}(10000/100) \rceil) &= 20000 \end{aligned}$$

$$\text{Join cost: } B_r + B_s = 1000 + 10000 = 11000$$

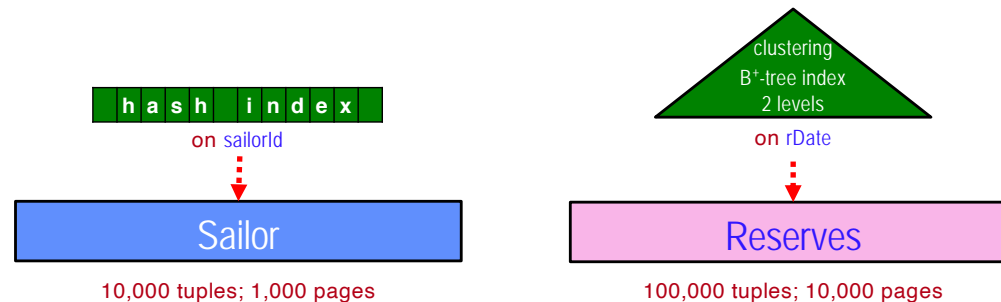
$$\text{Cost: } 6000 + 20000 + 11000 = \underline{37,000} \text{ page I/Os}$$

```
select *
from Sailor natural join Reserves natural join Boat
where rDate = '01-JAN-2020'
and color = 'red';
```

## EXERCISE 1 (CONTD)

bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
 Hash index: Sailor.sailorId  
 B+-tree index: Reserves.rDate (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10

- d) **Strategy:** hash join:  $3 * (B_r + B_s)$ .  
**Cost:**  $3 * (1000 + 10000) = \underline{33,000}$  page I/Os
- e) **Strategy:** indexed nested-loop – Reserves as outer relation.



**Sailor** contains a hash index on the join attribute **sailorId**. Furthermore, we have a selective condition ( $\sigma_{\text{rDate}='01\text{-JAN-2020'}}(\text{Reserves})$ ) and a clustering index on **Reserves.rDate**.

How many reservations do we need to access?

Since there are 100,000 reservations and 1,000 unique **rDates**, on a given **rDate** there are  $100000 / 1000 = 100$  reservations. Therefore, we need to access 100 **Reserves tuples** for 01-JAN-2020.

```
select *
from Sailor natural join Reserves natural join Boat
where rDate = '01-JAN-2020'
and color = 'red';
```

## EXERCISE 1 (CONTD)

bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
 Hash index: Sailor.sailorId  
 B+-tree index: Reserves.rDate (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10

How many pages need to be accessed, to find these reservations?

The index on Reserves.rDate has 2 levels and is ordered on rDate. Since, 10 Reserves tuples fit per page, to retrieve all reservations 2 index pages and 10 Reserves pages need to be accessed = 12 page I/Os. (Assumes all 100 Reserves tuples in the result are in 2 pages.)

For each of the 100 Reserves tuples, the corresponding Sailor tuple is retrieved using the hash index on Sailor.sailorId, with cost  $2 * 100 = 200$  page I/Os. The join result will contain 100 tuples.

**Cost:**  $12 + 200 = 212$  page I/Os

Strategy a)	Strategy b)	Strategy c)	Strategy d)	Strategy e)
110,100	113,000	37,000	33,000	212

Assuming the join result tuple size is twice that of each relation, we can fit 5 tuples per page and the result will occupy  $100 / 5 = 20$  pages.

**Cost:** 20 page I/Os (to write Temp<sub>1</sub>)

**Total cost  $C_1$ :**  $212 + 20 = 232$  page I/Os



```
select *
from Sailor natural join Reserves natural join Boat
where rDate = '01-JAN-2020'
and color = 'red';
```

## EXERCISE 1 (CONTD)

*bf*: 10 tuples/page  
*B*<sub>Sailor</sub>: 1,000 pages  
*B*<sub>Reserves</sub>: 10,000 pages  
*B*<sub>Boat</sub>: 100 pages  
*M*: 100 pages  
 Hash index: Sailor.sailorId  
 B+-tree index: Reserves.rDate  
                     (2 levels)  
 Hash index: Boat.boatId  
 Unique Reserves rDates: 1000  
 Red boat reservations: 10%  
 Reservations/sailor: 10

$C_2$ : Cost of computing  $\text{Temp}_2 = \sigma_{\text{color}='red'} \text{Boat}$  (no index on color)

**Strategy:** file scan

For *Boat*, there is only a hash index on *boatId*. Therefore, to find red boats, a scan of the entire relation (100 pages) is needed.

**Cost:** 100 page I/Os

Since only 10% of the boats are red, we expect to retrieve  $10\% * 1000 = 100$  *Boat* tuples, which can fit on  $100 / 10 = 10$  pages.

**Cost:** 10 page I/Os (to write  $\text{Temp}_2$ )

**Total cost  $C_2$ :**  $100 + 10 = 110$  page I/Os

```
select *  
from Sailor natural join Reserves natural join Boat  
where rDate = '01-JAN-2020'  
and color = 'red';
```

## EXERCISE 1 (CONTD)

*bf*: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1,000 pages  
 $B_{\text{Reserves}}$ : 10,000 pages  
 $B_{\text{Boat}}$ : 100 pages  
 $M$ : 100 pages  
Hash index: Sailor.sailorId  
B+-tree index: Reserves.rDate (2 levels)  
Hash index: Boat.boatId  
Unique Reserves rDates: 1000  
Red boat reservations: 10%  
Reservations/sailor: 10

$C_3$ : Cost of  $\text{Temp}_1 \text{ JOIN } \text{Temp}_2$  ( $\text{Temp}_1$  is 20 pages;  $\text{Temp}_2$  is 10 pages)

**Strategy:** block nested-loop join

We need to read the 20 pages of  $\text{Temp}_1$ .

**Cost:** 20 page I/Os

We need to read the 10 pages of  $\text{Temp}_2$ .

**Cost:** 10 page I/Os

Since there are 100 memory pages, we can simply do the join in memory after reading both relations.

**Total cost**  $C_3$ : 30 page I/Os

**Total cost:**  $C_1 + C_2 + C_3 = 232 + 110 + 30 = 372$  page I/Os

## EXERCISE 2

Estimate the query processing cost **using materialization** and the join order

Sailor JOIN ( $\sigma_{rDate='01-JAN-2020'}$ Reserves JOIN  $\sigma_{color='red'}$ Boat)

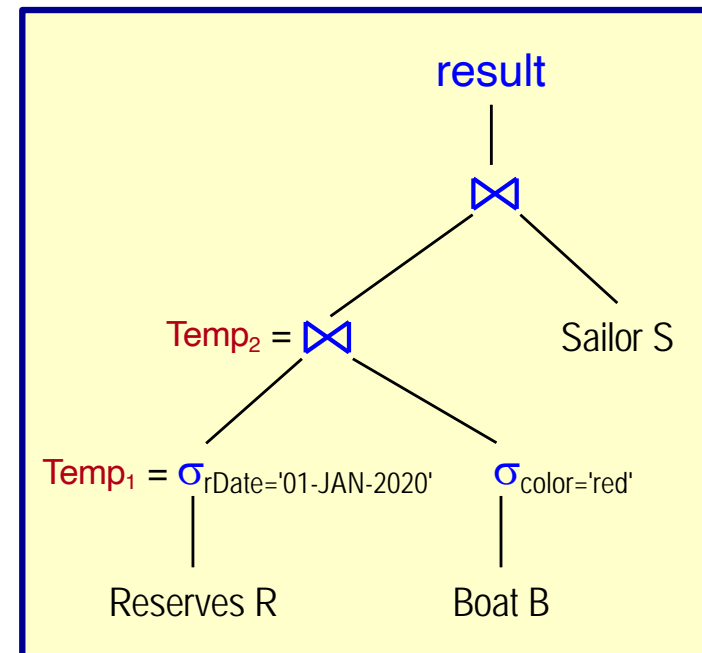
$C_1$ : Cost of computing  $Temp_1 = \sigma_{R.rDate='01-JAN-2020'}Reserves$

$C_2$ : Cost of computing  $Temp_2 = Temp_1$  JOIN  $\sigma_{color='red'}Boat$  (no index on color)

$C_3$ : Cost of Sailor JOIN  $Temp_2$

**Total cost:**  $C_1 + C_2 + C_3$

```
select *  
from Sailor natural join Reserves natural join Boat  
where rDate = '01-JAN-2020'  
and color = 'red';
```



## EXERCISE 2 (CONTD)

bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1000  
 $B_{\text{Reserves}}$ : 10000  
 $B_{\text{Boat}}$ : 100  
 $M$ : 100 pages  
Hash index: Sailor.sailorId  
B+-tree index: Reserves.rDate  
Hash index: Boat.boatId  
Unique Reserves rDates: 1000  
Red boat reservations: 10%  
Reservations/sailor: 10

$C_1$ : Cost of computing  $\text{Temp}_1 = \sigma_{R.rDate='01-JAN-2020'} \text{Reserves}$   
(no index on color)

**Strategy:** index lookup using B+-tree index on Reserves.rDate

As previously determined, to find all reservations on '01-JAN-2020' we retrieve 2 index pages and 10 Reserves pages.

**Cost:** 10 + 2 = 12 page I/Os

The 100 result Reserves tuples occupy  $100 / 10 = 10$  pages.

**Cost:** 10 page I/Os (to write  $\text{Temp}_1$ )

**Total cost  $C_1$ :** 12 + 10 = 22 page I/Os

## EXERCISE 2 (CONTD)

bf: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1000  
 $B_{\text{Reserves}}$ : 10000  
 $B_{\text{Boat}}$ : 100  
 $M$ : 100 pages  
Hash index: Sailor.sailorId  
B+-tree index: Reserves.rDate  
Hash index: Boat.boatId  
Unique Reserves rDates: 1000  
Red boat reservations: 10%  
Reservations/sailor: 10

$C_2$ : Cost of computing  $\text{Temp}_2 = \text{Temp}_1 \text{ JOIN } \sigma_{\text{color}='red'} \text{Boat}$

**Strategy:** block nested-loop join

We need to read the 10 pages of  $\text{Temp}_1$ .

**Cost:** 10 page I/Os

Do not use the hash index on Boat. Instead, we use block nested loop to join Boat with  $\text{Temp}_1$  and discard tuples where the color is not red.

(Note that the cost to use the hash index on Boat is 2 pages I/Os — 1 to the hash index plus 1 to access the Boat tuple — per reservation for a total cost of  $2 \times 100 = 200$  page I/Os).

**Cost:** 100 = 100 page I/Os

Assuming the join result tuple size is twice that of each relation, we can fit 5 tuples per page and the result will occupy  $10\% \times 100 / 5 = 2$  pages.

**Cost:** 2 page I/Os (to write  $\text{Temp}_2$ )

**Total cost**  $C_2$ :  $10 + 100 + 2 = 112$  page I/Os.

## EXERCISE 2 (CONTD)

*bf*: 10 tuples/page  
 $B_{\text{Sailor}}$ : 1000  
 $B_{\text{Reserves}}$ : 10000  
 $B_{\text{Boat}}$ : 100  
 $M$ : 100 pages  
Hash index: Sailor.sailorId  
B+-tree index: Reserves.rDate  
Hash index: Boat.boatId  
Unique Reserves rDates: 1000  
Red boat reservations: 10%  
Reservations/sailor: 10

$C_3$ : Cost of Sailor JOIN  $\text{Temp}_2$

**Strategy:** indexed nested-loop join using Sailor.sailorId hash index

We need to read the 2 pages of  $\text{Temp}_2$  to do the join for  $C_3$ .

**Cost:** 2 page I/Os

For the 10 ( $10\% * 100$ ) reservations that satisfy the first two operations, we use the hash index on sailorId to find the information about the sailor.

The cost is 2 page I/Os (1 to the hash index and 1 to access the Sailor tuple) per reservation.

**Cost:**  $2 * 10 = 20$  page I/Os

**Total cost  $C_3$ :**  $2 + 20 = 22$  page I/Os

**Total Cost:**  $C_1 + C_2 + C_3 = 22 + 112 + 22 = 156$  page I/Os