

# Jitter Propagation in Task Chains

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# Outline

1 Background

2 Model

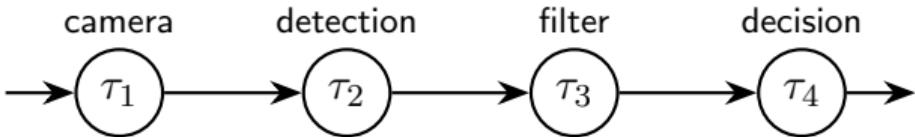
3 Composition

4 Evaluation

5 Conclusion

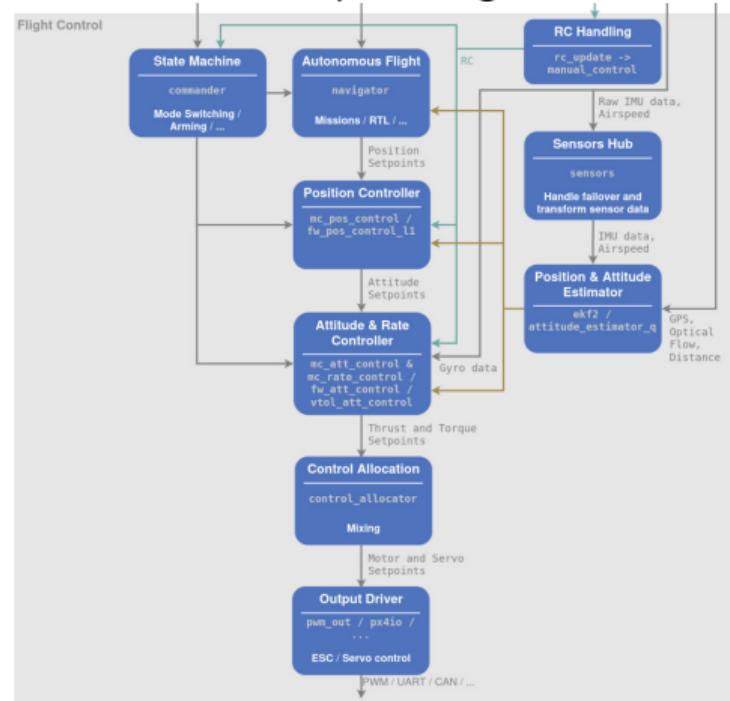
# Motivation

- **Use cases**
  - automotive, avionics, robotics, and UAVs
- **Functionalities delivered by concatenating tasks**
  - Camera records video
  - Object detection
  - Data filtering
  - Decision taking
- **Asynchronous communication**
  - readers do not wait for writers

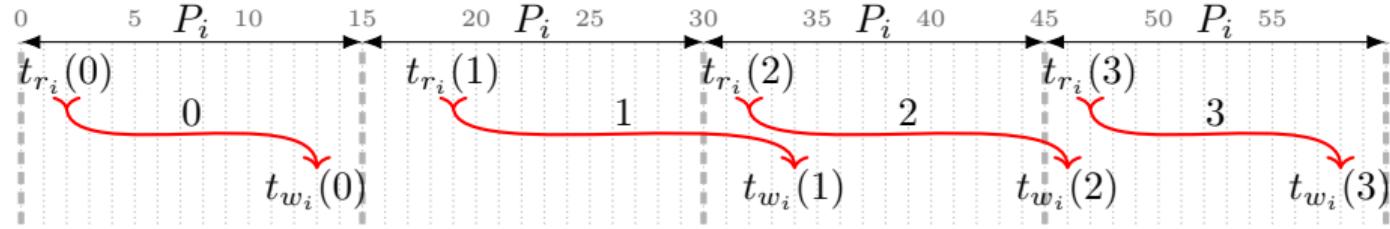


<sup>1</sup>source: <https://docs.px4.io>

## PIX4<sup>1</sup> UAV autopilot, flight controller

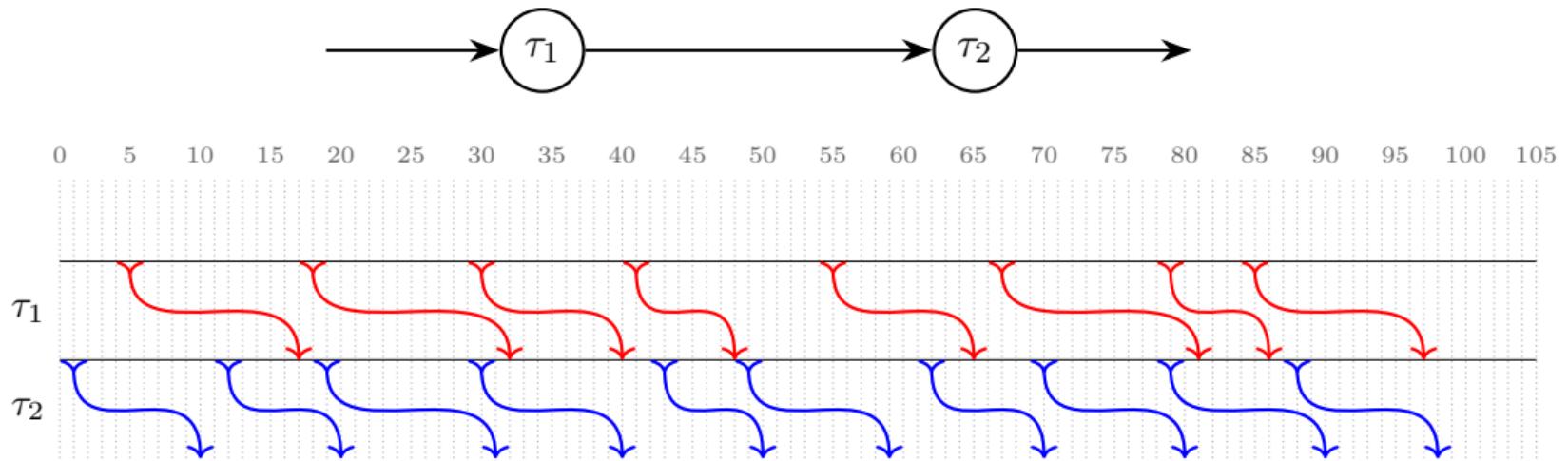


## Standard model of a task $\tau_i$ in chains

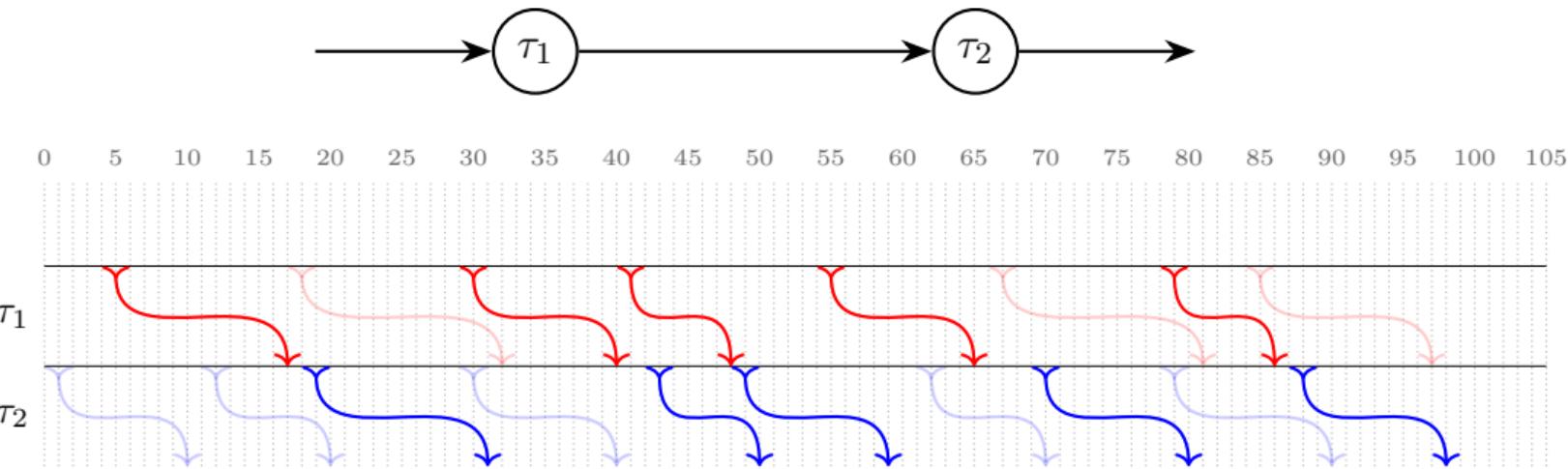


- A task  $\tau_i$  is composed by *jobs* (curvy arrows) indexed by  $0, 1, 2, \dots$
- Jobs are released every *period*  $P_i$
- $t_{r_i}(j)$ , sequence of read instants of  $\tau_i$  jobs
- $t_{w_i}(j)$ , sequence of write instants of  $\tau_i$  jobs
- No need of execution times, scheduling algorithm: we only care of the read/write instants
- A “task” could also be a network message, a bus line in transportation network, etc.

## Chain of tasks: analysis

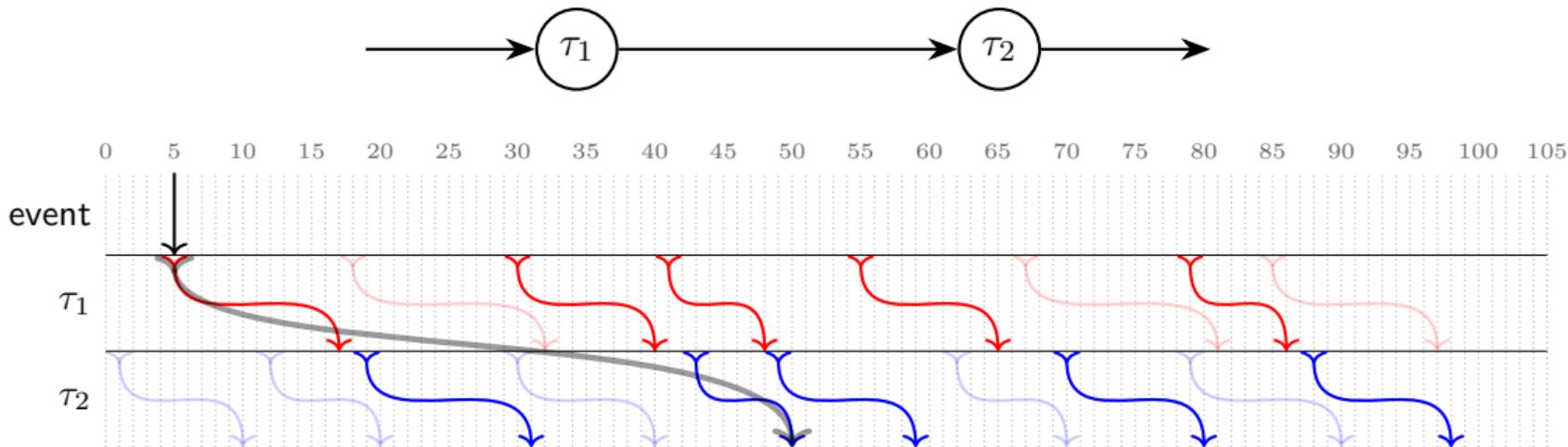


## Chain of tasks: analysis



- We can drop “useless” jobs. A job is useless when
  - it writes data being overwritten by next job of the same task, or when
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- We can drop “useless” jobs. A job is useless when
  - it writes data being overwritten by next job of the same task, or when
  - it reads data already read by the previous job of the same task
- Typical metric: reaction time (45 in the figure)
  - longest time from an external event (at the begin of the chain) to the end
  - other metrics exist (First-to-Last latency, data age, Last-First, etc.), all related to one another
- Useless jobs do not influence the reaction time

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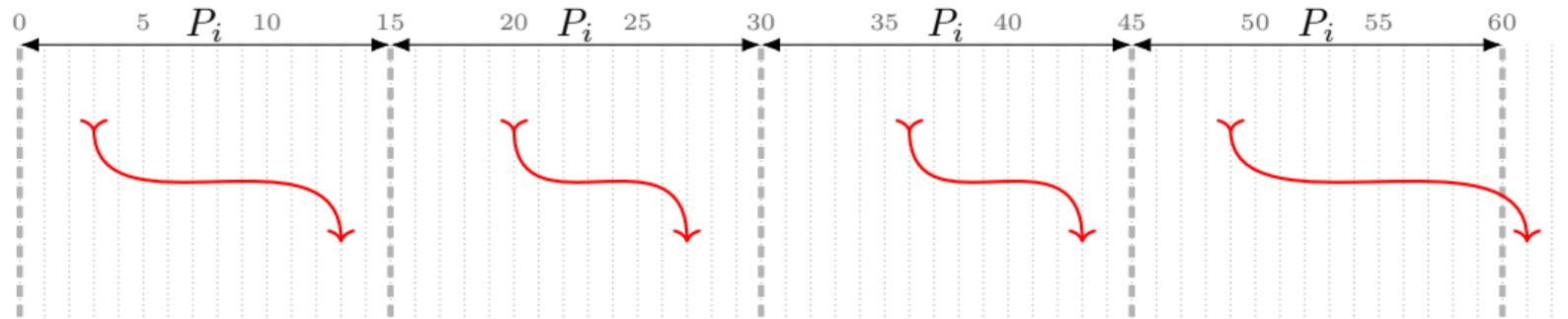
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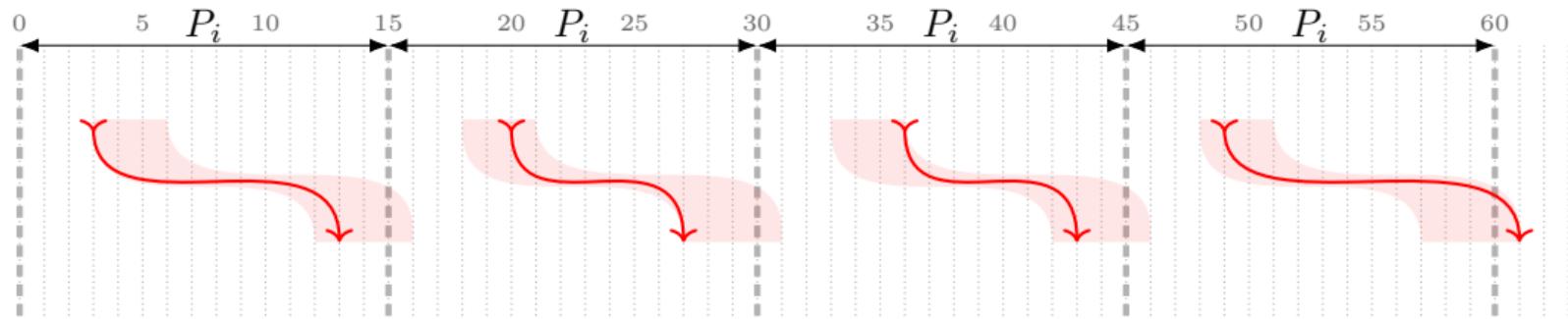
## Task model with uncertain read/write events

- Read/write instants may be subject to uncertainties (exec. times, bus contention, etc.)



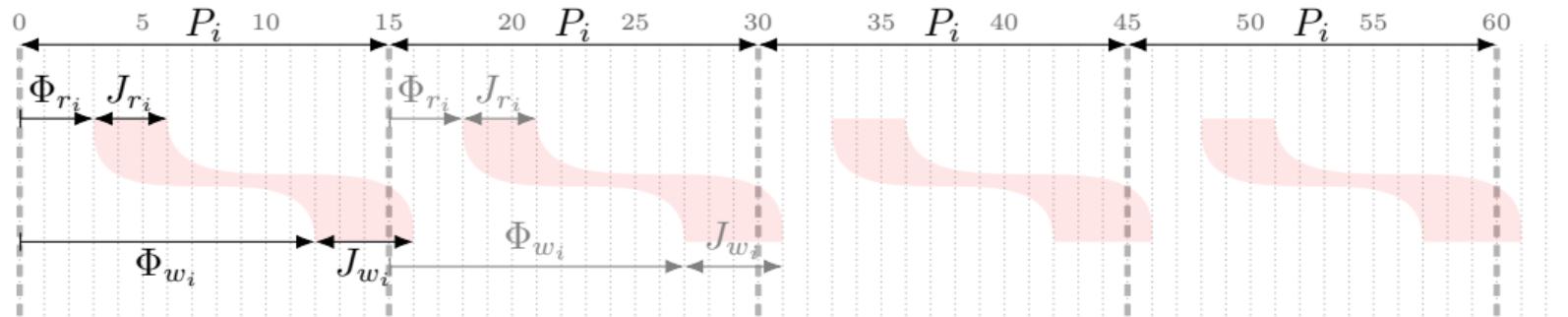
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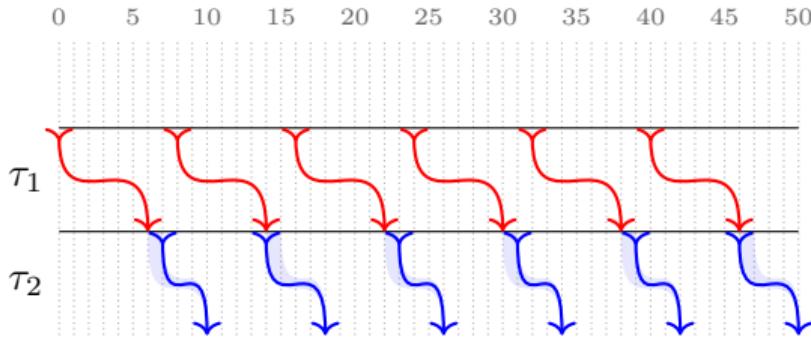
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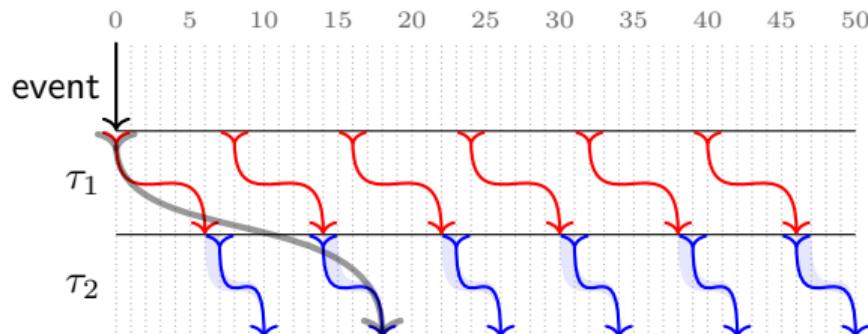


- $P_i$ , period of task  $\tau_i$
- $\Phi_{r_i}$ , read offset of  $\tau_i$ , relative to periodic releases
- $J_{r_i}$ , read jitter
- $\Phi_{w_i}$ , write offset of  $\tau_i$  relative to periodic releases
- $J_{w_i}$ , write jitter
- Intervals are considered closed on both ends

# Impact of uncertainty on reaction time

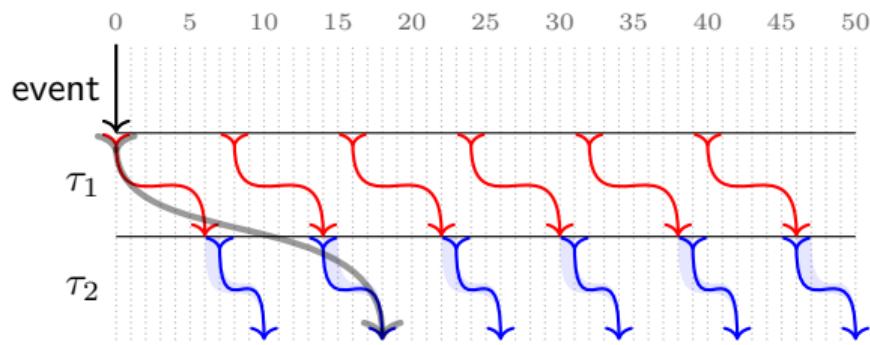


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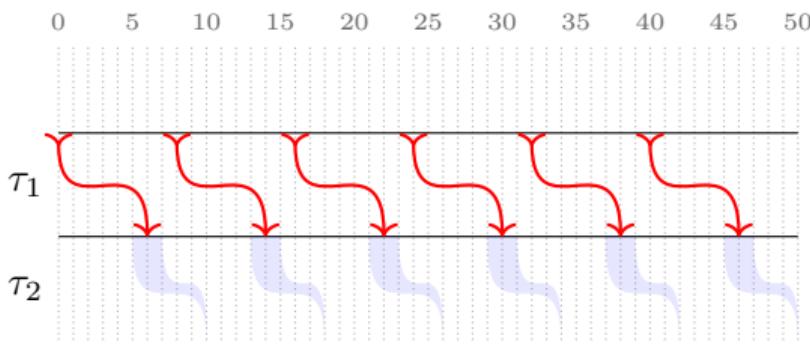


reaction time = 18

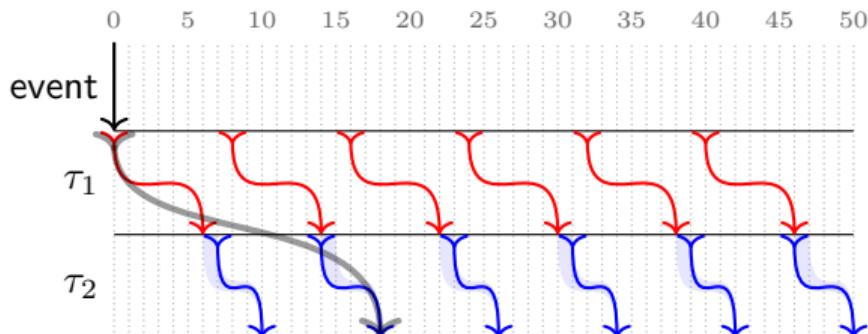
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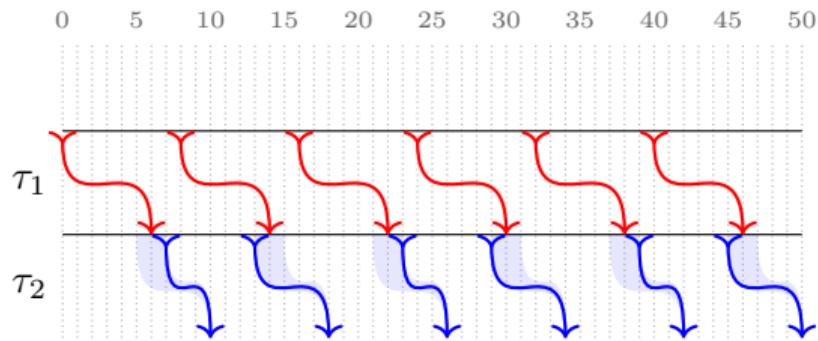
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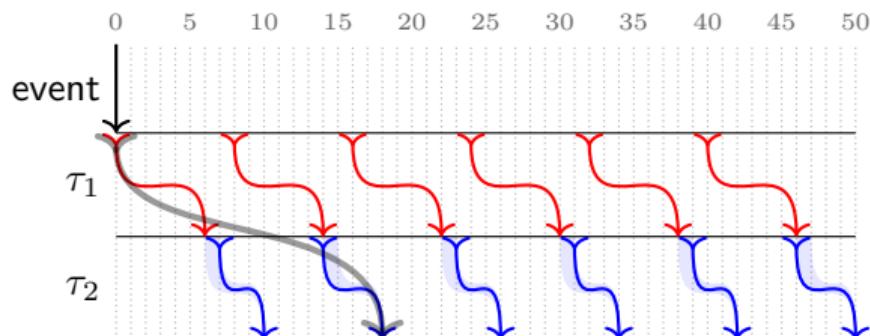
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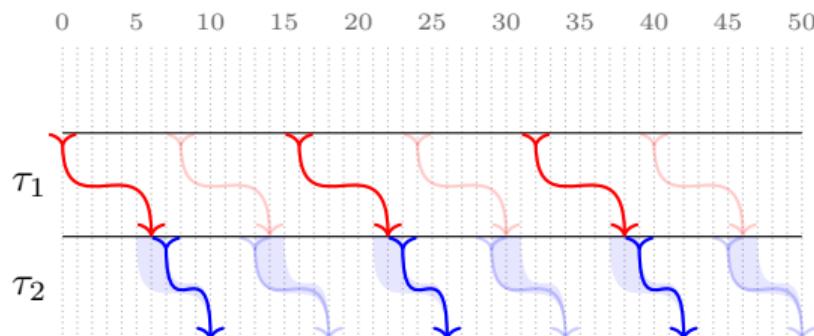
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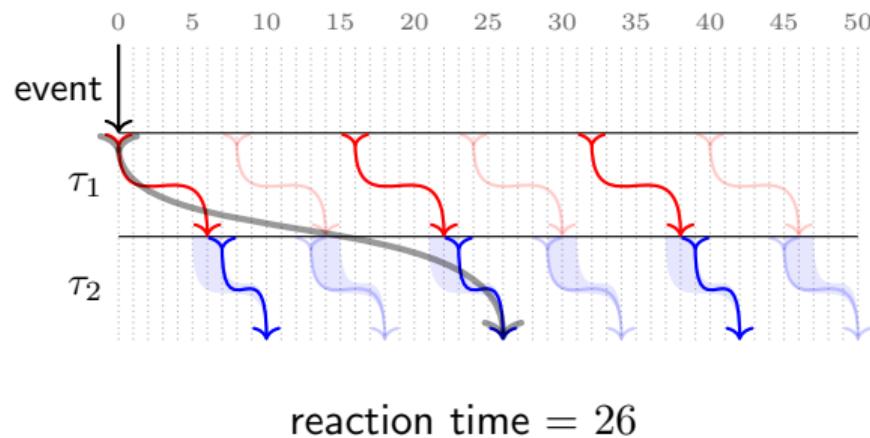
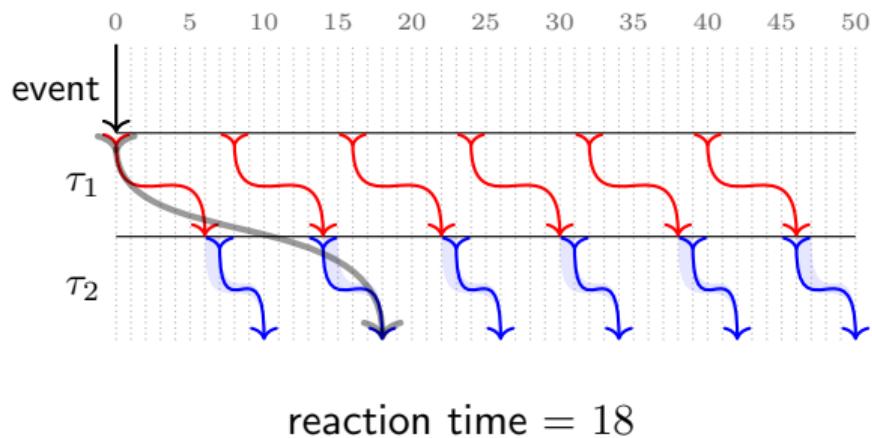
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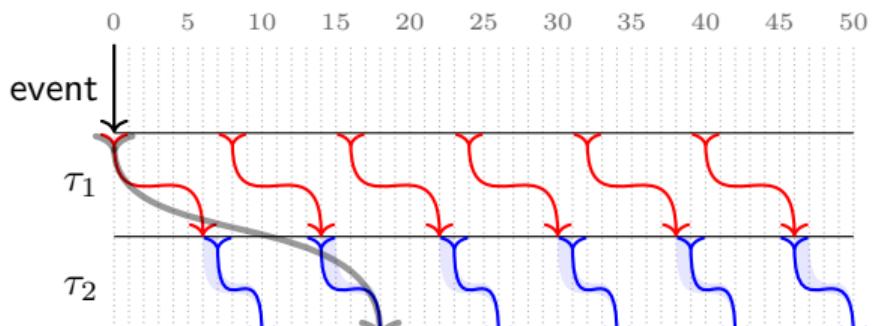
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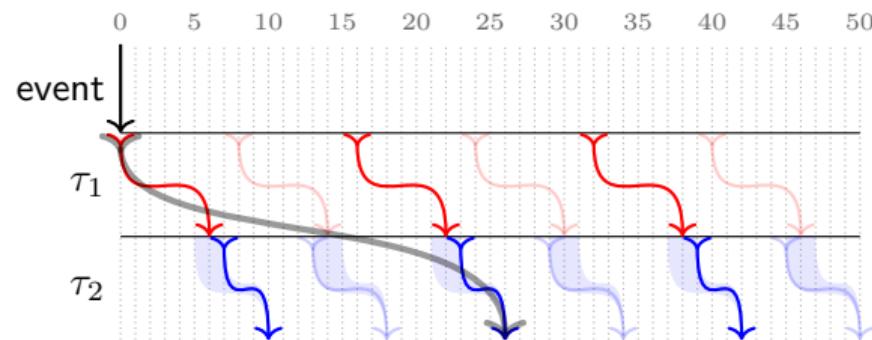
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# Impact of uncertainty on reaction time



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reaction time = 26

- small increase in jitter ( $+ \epsilon$ ) makes big jump in reaction time ( $+8$ )
- worst-case scenario of read instants for max reaction-time is not so intuitive

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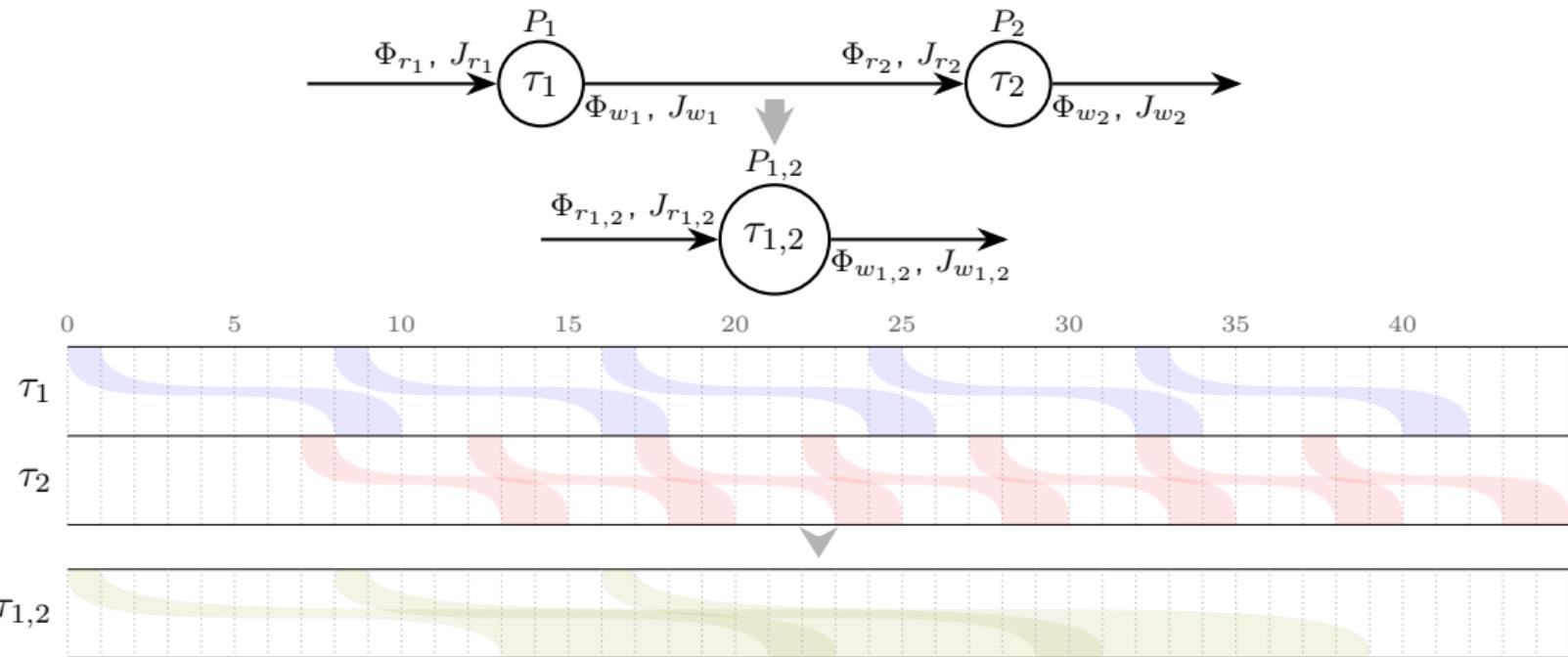
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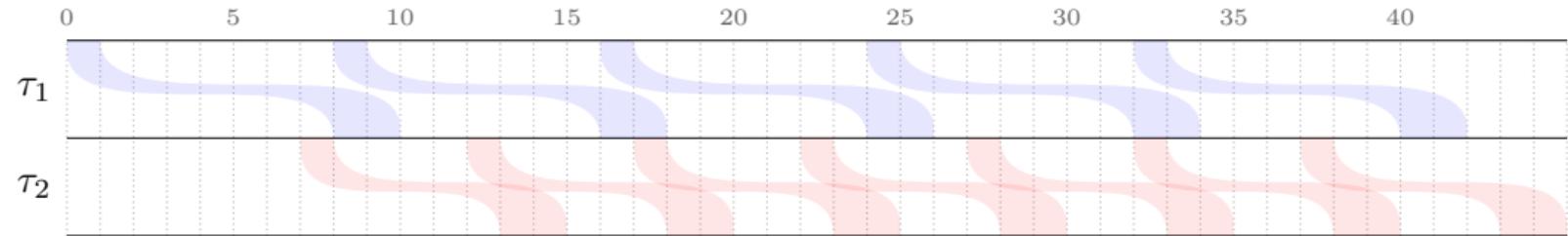
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## Our proposed analysis: composing two tasks into one

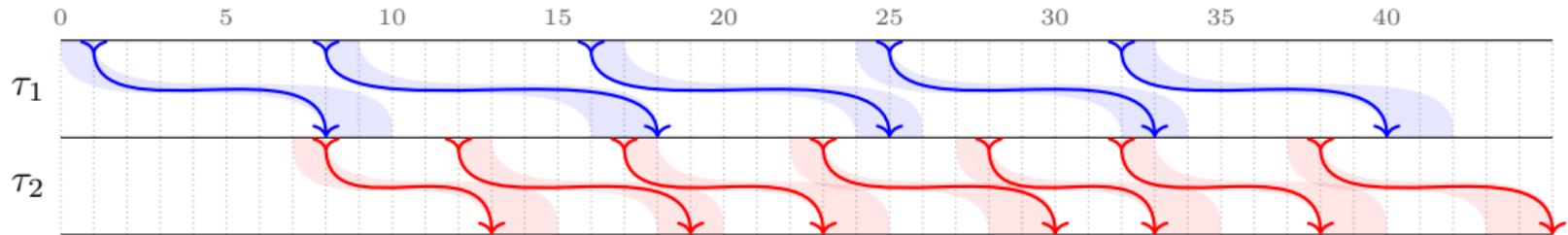


- If we can combine two tasks into one, recursively, we can combine  $n$  tasks into one
- Analysis in linear time, instead of spanning all jobs over the hyperperiod
- Reaction time of one task has a closed expression

# Composing two tasks: how?

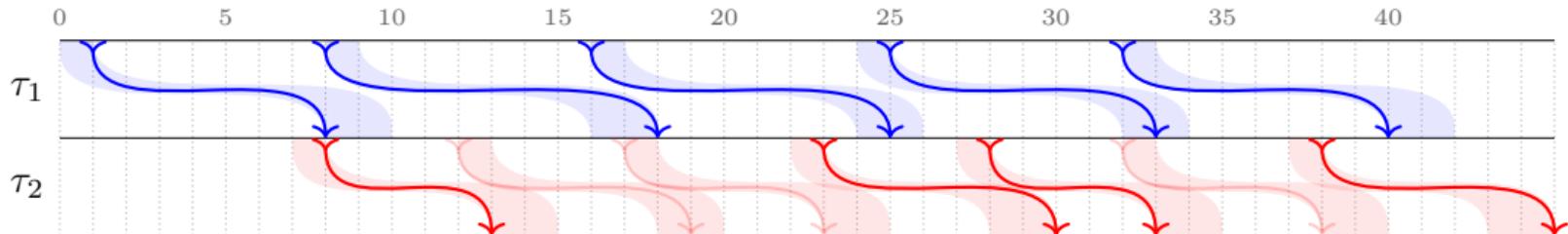


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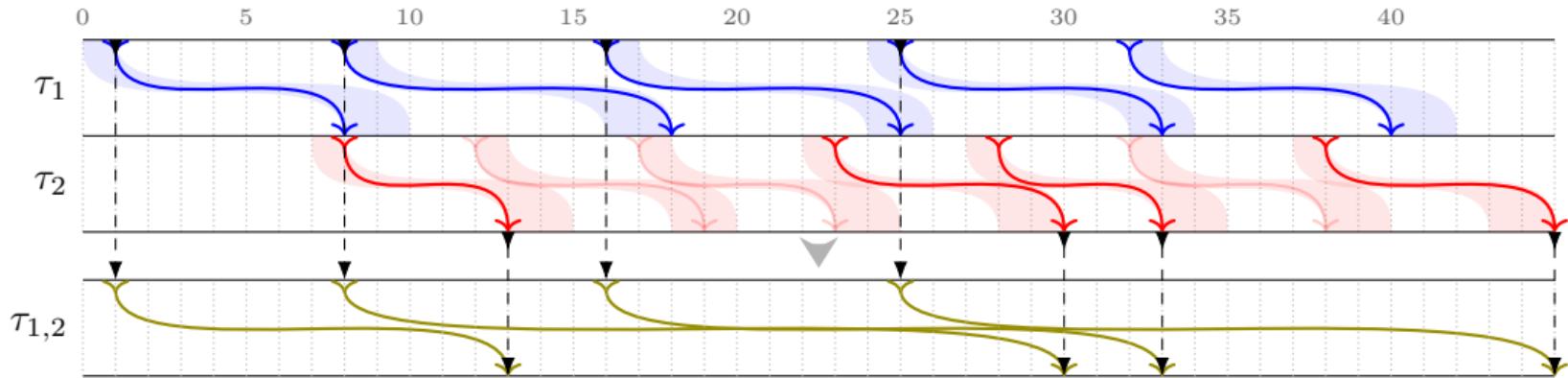
- ① **For all sequences**  $(t_{r_1}, t_{w_1})$  and  $(t_{r_2}, t_{w_2})$  compatible with  $\tau_1$  and  $\tau_2$ , respectively

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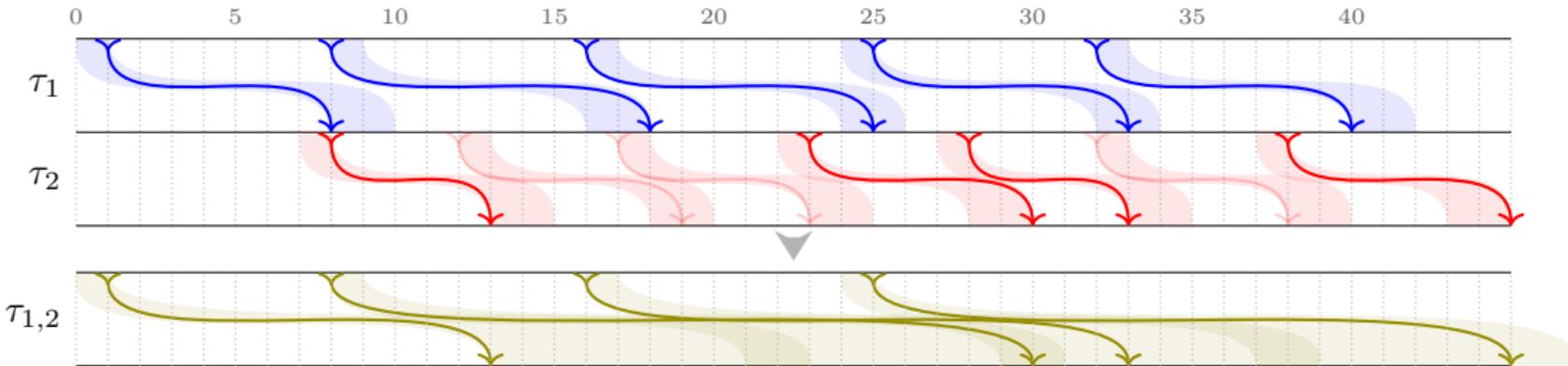
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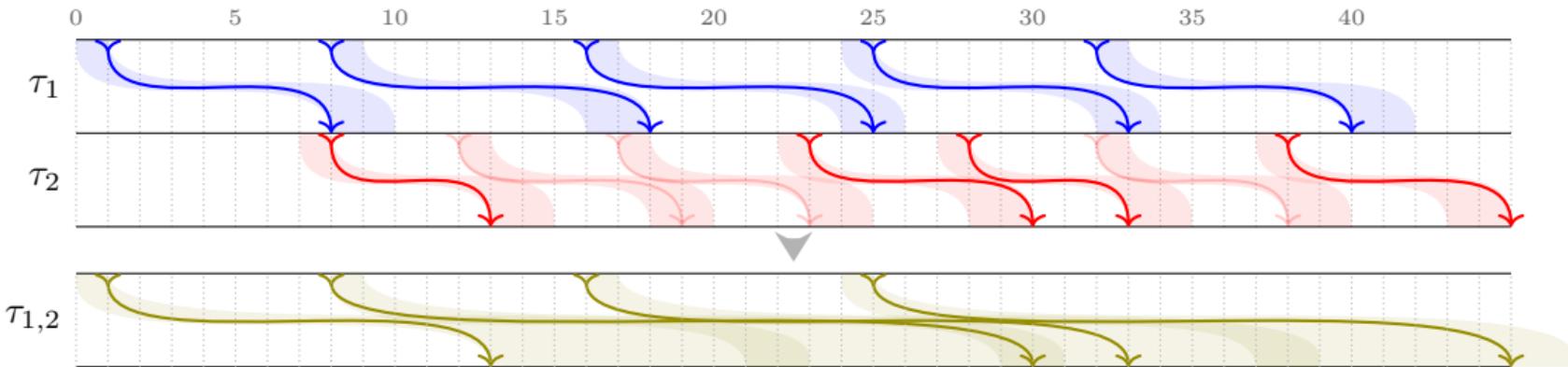
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- ③ We combine the sequences into  $(t_{r_{1,2}}, t_{w_{1,2}})$  with read/write from  $t_{r_1}/t_{w_2}$ , resp.

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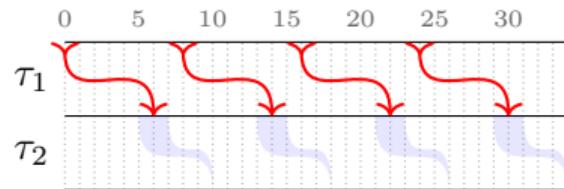
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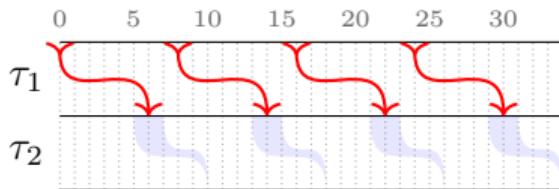
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- ④ We require the sequences  $(t_{r_{1,2}}, t_{w_{1,2}})$  be compatible with  $\tau_{1,2}$
- No recipe for  $\tau_{1,2}$ , only the needed properties
  - Does  $\tau_{1,2}$  always exist? If yes, is it unique?

## Composing two tasks: not always possible...



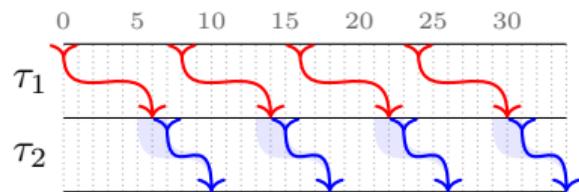
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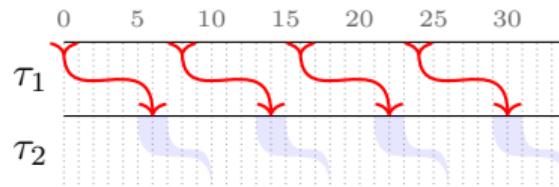


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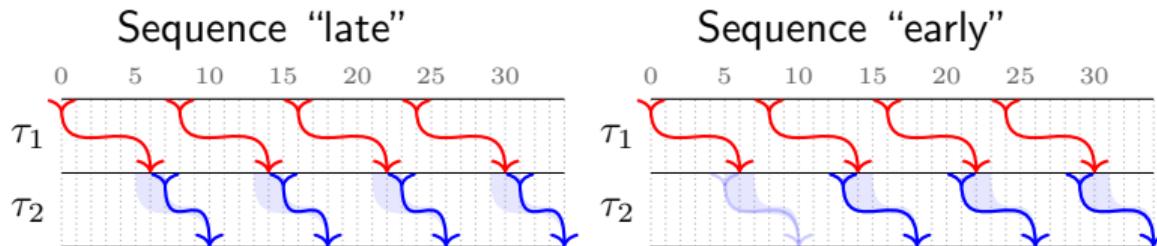
Sequence “late”



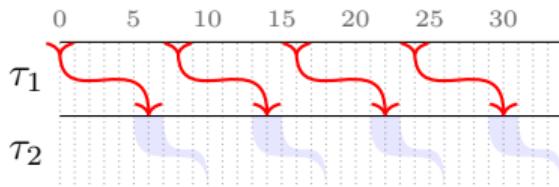
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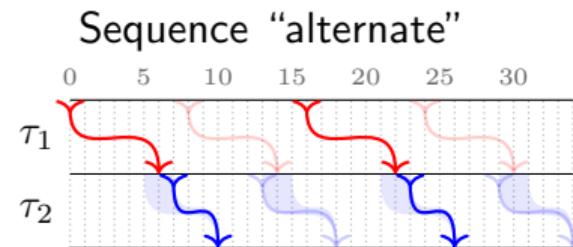
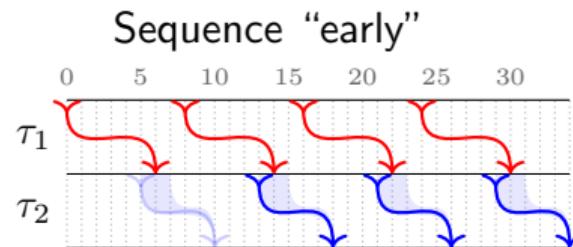
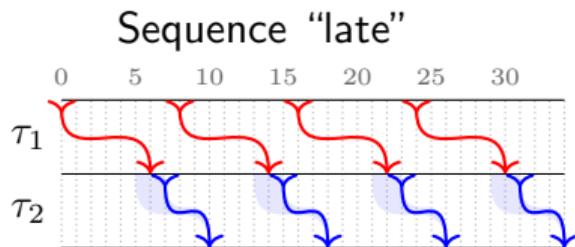
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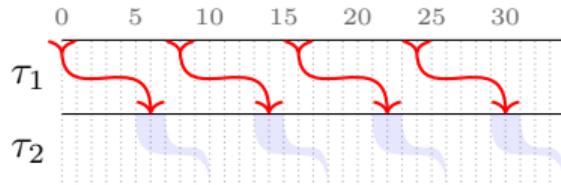
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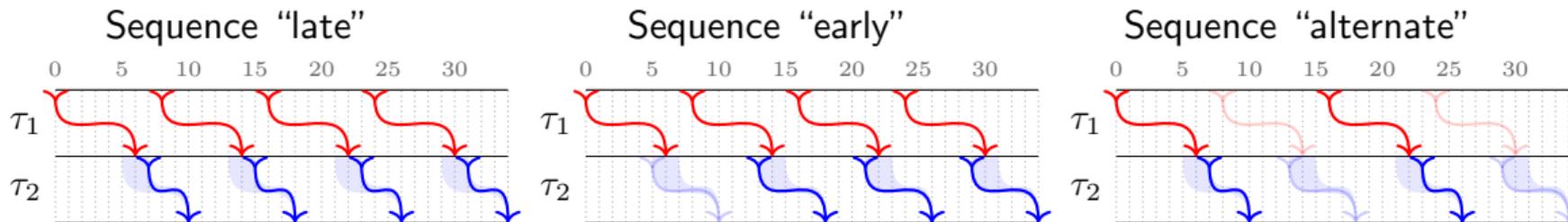
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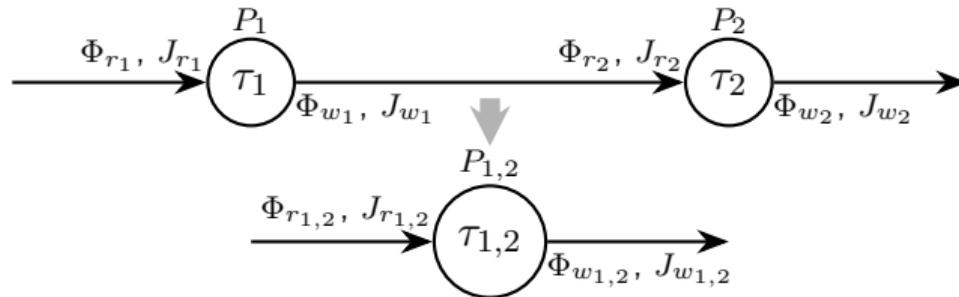


- We need to consider **all** sequences compatible with  $\tau_1$  and  $\tau_2$



- The period  $P_{1,2}$  of  $\tau_{1,2}$  needs to be equal to  $P_1$  and equal to  $2P_1$ : impossible!
- A periodic  $\tau_{1,2}$  which can embrace all possible sequences **may not exist**

# How to resolve this existential problem?



- [3 theorems] “If the following hypotheses hold

$$\begin{cases} J_{w_1} \leq \text{mod}(\Phi_{r_2} - \Phi_{w_1}, P_2) < P_2 - J_{r_2} & P_1 = P_2 \\ P_2 + J_{r_2} \leq P_1 - J_{w_1} & P_1 > P_2 \\ P_1 + J_{w_1} \leq P_2 - J_{r_2} & P_1 < P_2 \end{cases}$$

then  $\tau_{1,2}$  exists and its parameters are [something]

- The conditions are independent of  $J_{r_1}$  and  $J_{w_2}$
- $J_{w_1} = J_{r_2} = 0 \Rightarrow$  conditions true. As  $J_{w_1}$ ,  $J_{r_2}$  grow, the conditions get more stringent
- [something]:  $P_{1,2} = \max\{P_1, P_2\}$ ,  $J_{r_{1,2}} \geq J_{r_1}$ ,  $J_{w_{1,2}} \geq J_{w_2}$

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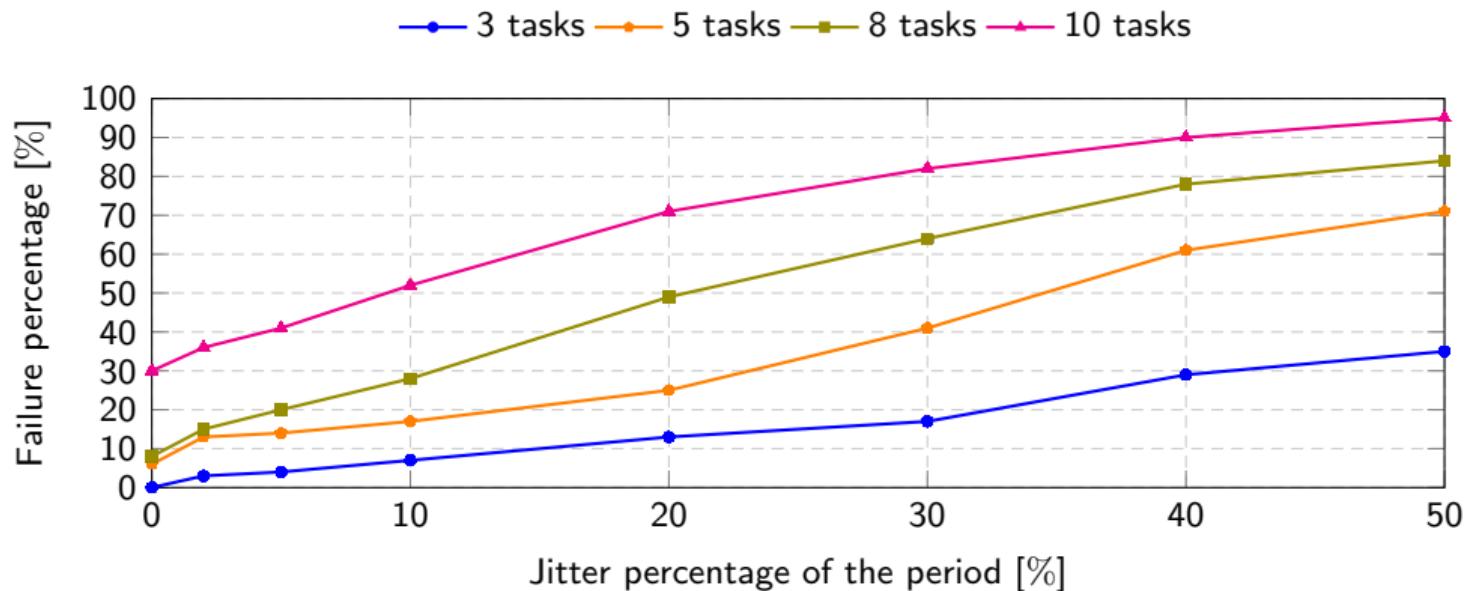
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## Failure percentage: how often the hypotheses do not hold?



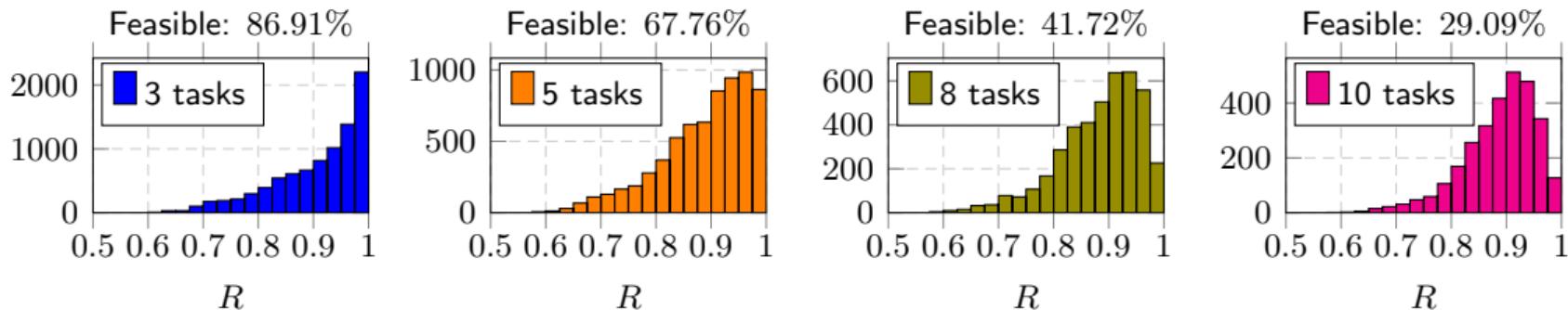
- Growing chain length and jitter reduces the applicability of composition

## Quality of the bound

- After composing the  $n$  tasks into  $\tau_{1,n}$ , we find the maximum reaction time as

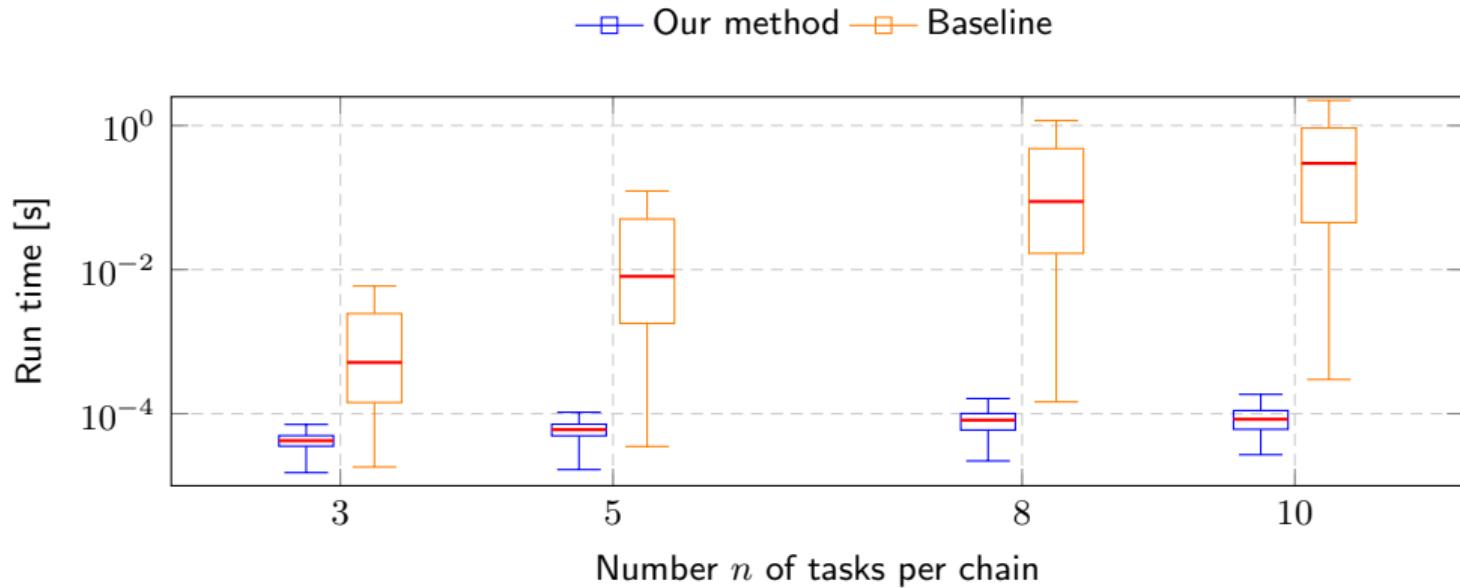
$$P_{1,n} + \Phi_{w_{1,n}} - \Phi_{r_{1,n}} + J_{w_{1,n}}$$

- As baseline for comparison, we use the maximum reaction time by Günzel et al.<sup>2</sup>
- $R = \text{baseline maximum reaction time} / \text{our method maximum reaction time}$



<sup>2</sup>M. Günzel, K.-H. Chen, N. Ueter, G. von der Brüggen, M. Dürr, and J.-J. Chen, "Timing analysis of asynchronized distributed causeeffect chains," in Real Time and Embedded Technology and Applications Symposium (RTAS), 2021.

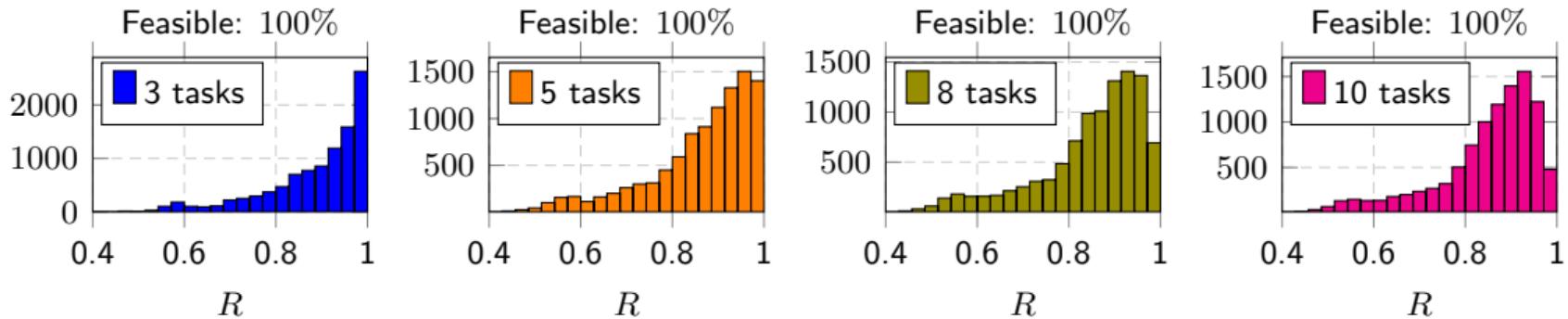
# Running time



- Running time is several orders of magnitude smaller than the baseline
  - our composition has linear time, faster than spanning all jobs over the hyperperiod

# Active analysis

- When the conditions are violated: “active” analysis
  - inserting publisher tasks [Bini et al. IEEE-TC’23] between  $\tau_1$  and  $\tau_2$  to eliminates the jitter



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## Conclusions & future work

- We propose an **new task model** which incorporates the uncertainty in the read/write instants
- A technique (linear-time) to **compose tasks** and then analysed the composed task only
- Active analysis: if jitter too large to compose, reduce it with publisher tasks
- Can the task model be changed to enable a more successful composition?
- What if DAGs instead of chains?

Github repository with code for the analysis

