APSTA-2013: Final Project

William Spagnola 3/15/2019

Part A: Introduction

Dataset

My dataset is a subset of the Behavioral Risk Factor Surveillance System (BRFSS), which I obtained from the naniar package. I kept four of the 34 variables from the original datset: age, BMI, health insurance coverage (health_cover), and self-reported general health (health_general). Age and BMI are continuous variables and are self-explanatory. Health_cover is a binary variable that is coded 1 for subjects who reported having health insurance and 0 for subjects who did not have insurance. Health_general was an ordinal factor that was measured on a five point scale: Poor, Fair, Good, Very Good and Excellent. In order to simplify my analysis, I recoded health_general as a binary variable called health_good. A health_general rating of 'fair' or 'poor' was coded as 0 and'good', 'very good', and 'excellent' rating was coded as 1.

Analysis

My analysis plan was to predict 'good health' (health_good) based on each subject's age, BMI, and health insurance coverage (health_cover). Since health_good was a binary variable, I opted to fit a binomial logistic regression model on the data to accomplish this goal.

```
set.seed(2013)
### Load Data
risk_sub <- read.csv('data/risk_sub.csv')
rownames(risk_sub) <- NULL</pre>
#Convert Health_general and health_cover to binary variables coded 1 and 0
risk_sub$health_cover <- ifelse(risk_sub$health_cover=='Yes', 1, 0)
risk_sub$health_good <- ifelse(risk_sub$health_general %in% c('Excellent', 'VeryGood', 'Good'), 1, 0)
#Drop Id, Healh_general and Smoking Variables
risk_sub <- risk_sub[, -which(names(risk_sub) %in% c('id', 'health_general', 'smoke_days'))]
head(risk sub)
##
           bmi health_cover health_good
## 1
     49 32.68
                                       1
                          1
## 2 48 25.90
                          1
                                       0
## 3 55 28.04
                          1
                                       0
## 4 42 29.59
                          1
                                       1
     66 24.74
                          1
## 5
                                       1
## 6 66 23.72
                                       1
```

Missing Data

In the original dataset, all the variables were completely observed except BMI, in which 4.5% cases were missing. Consequently, I had to generate missing data in order to explore different imputation methods.

Use Ampute Function

I used the ampute function from the mice package to generate missing data at random. After generating the missing data, I replaced the age variable with the completely observed column from the original dataset. Having one completely observed continuous variable was necessary in order to perform all the imputation methods.

Examine Missing Data

After using the ampute function to generate missing data at random, 22.4% of the *bmi* values were missing, 16.3% of the *health_cover* values were missing and 16.3% of the *health_good* values were missing. *Age* was completely observed. Out of all the cases, 44.9% were completely observed. Overall, 13.8% of the values were missing.

```
miss_prop_summary(risk_MAR)
## # A tibble: 1 x 3
##
        df
            var case
##
     <dbl> <dbl> <dbl>
## 1 0.138 0.75 0.551
miss var summary(risk MAR)
## # A tibble: 4 x 3
##
     variable
                 n_miss pct_miss
##
     <chr>>
                   <int>
                             <dbl>
## 1 bmi
                      55
                             22.4
## 2 health_cover
                             16.3
                      40
## 3 health_good
                      40
                             16.3
## 4 age
                       0
                               0
```

Part B: Methods

Since there were very few missing variables in the original dataset, I decided to first fit a model on the full dataset for comparison. Then I fit models using listwise deletion, mean/mode imputation, random imputation, the dummy variable method, hotdecking, regression imputation, stochastic imputation (regression with noise), and multiple imputation using the mi package. For each model, I printed out a table of the coefficient estimates. The tables also included the standard errors of each of the coefficients. In addition, I wrote an equation of the resulting regression equation produced by each model.

Because my data was cross-sectional, I omitted the LVCF method, which is generally used for longitudinal data. In addition, as a caveat, despite setting the seed, the mi function produced slightly different coefficients every time I ran the program. In the fourth section, I explain in further detail the range of numbers produced by the mi function for multiple imputation.

Full Dataset

```
risk_full <- risk_sub[complete.cases(risk_sub) ,]</pre>
fit_full <- glm(formula = health_good ~ health_cover + age + bmi, data = risk_full,
                 family = binomial)
summary(fit_full)
##
## Call:
  glm(formula = health_good ~ health_cover + age + bmi, family = binomial,
##
       data = risk_full)
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                    30
                                            Max
##
  -2.3777
           -0.5527
                      0.6472
                               0.7788
                                         1.3196
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                 3.274852
                            0.969979
                                        3.376 0.000735 ***
## health_cover
                1.187222
                            0.461667
                                        2.572 0.010123 *
## age
                -0.028407
                            0.009978
                                      -2.847 0.004413 **
## bmi
                -0.054041
                            0.023050
                                      -2.345 0.019052 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 264.27
                              on 233
                                      degrees of freedom
## Residual deviance: 247.89
                              on 230
                                      degrees of freedom
  AIC: 255.89
##
## Number of Fisher Scoring iterations: 4
```

1. Listwise deletion.

```
##
## Call:
## glm(formula = health_good ~ bmi + age + health_cover, family = binomial(link = "logit"),
      data = risk_CC)
## Deviance Residuals:
                    Median
                                         Max
      Min
                10
                                  30
## -2.2398 -0.9585 0.5442 0.7835
                                       1.3511
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                          1.40750 2.601 0.009293 **
              3.66105
               -0.02153
                           0.03169 -0.679 0.496924
## bmi
               -0.05366
                           0.01612 -3.328 0.000874 ***
## age
## health_cover 1.18477
                           0.68866 1.720 0.085362 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 126.90 on 109 degrees of freedom
## Residual deviance: 112.32 on 106 degrees of freedom
## AIC: 120.32
## Number of Fisher Scoring iterations: 4
Report Formula for listwise deletion model
```

 $HEALTH_GOOD = 3.36 + -0.02 * BMI + -0.05 * AGE + 1.18 * HEALTH_COVER$

2. Mean/mode imputation.

```
#Function for Mean Imputation
mean.imp <- function (a){</pre>
  missing <- is.na(a)
  a.obs <- a[!missing]</pre>
  imputed <- a
  imputed[missing] <- mean(a.obs)</pre>
  return (imputed)
#Function for Mode
mode = function(x) {
  ta = table(x)
  tam = max(ta)
  if (all(ta == tam))
    mod = NA
  else
    mod = names(ta)[ta == tam]
  return(mod)
}
#Function for Mode Imputation
```

```
mode.imp <- function (a) {</pre>
  missing <- is.na(a)
  a.obs <- a[!missing]</pre>
  imputed <- a
  imputed[missing] <- mode(a.obs)</pre>
  # Output the imputed vector
 return(imputed)
#Create A Duplicate Dataset
risk_imp_mean <- risk_MAR
#Apply Mode Imputation to Indicator Variables (Health_Good & Health_Cover)
risk_imp_mean$health_cover <- as.integer(mode.imp(risk_MAR$health_cover))
risk_imp_mean$health_good <- as.integer(mode.imp(risk_MAR$health_good))
#Apply Mean Imputation to Continuous Variables (BMI)
risk_imp_mean$bmi <- mean.imp(risk_MAR$bmi)</pre>
#Perform Analysis
fit_imp_mean_mode <- glm(health_good ~ health_cover +bmi + age,</pre>
                         data = risk_imp_mean,
                         family = binomial(link = 'logit'))
summary(fit_imp_mean_mode)
##
## Call:
## glm(formula = health_good ~ health_cover + bmi + age, family = binomial(link = "logit"),
##
       data = risk_imp_mean)
##
## Deviance Residuals:
                 10
##
       Min
                     Median
                                   3Q
                                           Max
## -2.2234
           0.4931
                      0.6282
                               0.7073
                                        1.0747
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                 3.059610 1.028552 2.975 0.00293 **
## health_cover 0.630248 0.528898
                                      1.192 0.23341
                -0.042250
                           0.025128 -1.681 0.09268 .
                            0.009943 -1.857 0.06336 .
## age
                -0.018462
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 250.64 on 244 degrees of freedom
## Residual deviance: 244.09 on 241 degrees of freedom
## AIC: 252.09
##
## Number of Fisher Scoring iterations: 4
```

Equation: Mean/Mode Imputation

3. Random imputation.

```
## Simple random imputation
random.imp <- function (a){</pre>
  missing <- is.na(a)
 n.missing <- sum(missing)</pre>
 a.obs <- a[!missing]</pre>
  imputed <- a
  imputed[missing] <- sample(a.obs, n.missing, replace=TRUE)</pre>
  return (imputed)
#Perform Random Imputation
risk_imp_rand <- risk_MAR
risk_imp_rand$bmi <- random.imp(risk_MAR$bmi)</pre>
risk_imp_rand$health_cover <- random.imp(risk_MAR$health_cover)
risk_imp_rand$health_good <- random.imp(risk_MAR$health_good)
#Perform Analysis
fit_imp_rand <- glm(health_good ~ health_cover + bmi + age,
                         data = risk_imp_rand,
                         family = binomial(link = 'logit'))
summary(fit_imp_rand)
##
## Call:
## glm(formula = health_good ~ health_cover + bmi + age, family = binomial(link = "logit"),
##
       data = risk_imp_rand)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                            Max
## -2.1871
           -1.0680
                      0.6781
                               0.8049
                                         1.1441
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                 2.925507
                            0.915556 3.195
                                                0.0014 **
## health_cover 0.512311
                                       1.087
                                                0.2769
                            0.471206
                -0.032535
                            0.020207 -1.610
                                                0.1074
## bmi
                -0.022859
                                               0.0145 *
## age
                            0.009355 - 2.444
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 277.18 on 244 degrees of freedom
## Residual deviance: 268.30 on 241 degrees of freedom
## AIC: 276.3
## Number of Fisher Scoring iterations: 4
```

Equation: Random Imputation

```
HEALTH GOOD = 2.93 + 0.51 * HEALTH COVER + -0.03 * BMI + -0.02 * AGE
```

4. Dummy variable on predictor variables.

```
#Create Indicator Variabler
health_cover_missing <- is.na(risk_MAR$health_cover)*1
bmi_missing <- is.na(risk_MAR$bmi)*1</pre>
risk_dummy <- risk_MAR
#Add arbitrary number for missing values of predictors
risk_dummy[bmi_missing == 1,] <- 0
risk_dummy[health_cover_missing == 1,] <- 0
#Add indicator variables for to inicate rows with missing values on predictor variables
risk dummy$health cover miss <- health cover missing
risk_dummy$bmi_miss <- bmi_missing</pre>
#Remove Rows with Missing Outcome Variable
risk_dummy_cc <- risk_dummy[!is.na(risk_dummy$health_good) , ]</pre>
#Perform Analysis
fit_dummy <- glm(health_good ~ health_cover + bmi + age + health_cover_miss + bmi_miss,
                         data = risk_dummy_cc,
                         family = binomial(link = 'logit'))
summary(fit_dummy)
##
## Call:
## glm(formula = health good ~ health cover + bmi + age + health cover miss +
       bmi_miss, family = binomial(link = "logit"), data = risk_dummy_cc)
##
##
## Deviance Residuals:
       Min
                  1Q
                         Median
                                       3Q
                                                Max
## -2.23976 -0.00008 -0.00008
                                0.56970
                                            1.35114
##
## Coefficients:
                       Estimate Std. Error z value Pr(>|z|)
                       3.66105 1.40754 2.601 0.009294 **
## (Intercept)
## health_cover
                       1.18477
                                   0.68868 1.720 0.085367 .
                       -0.02153
                                   0.03170 -0.679 0.496928
## bmi
## age
                       -0.05366
                                   0.01612 -3.328 0.000874 ***
## health_cover_miss -23.22712 1700.35933 -0.014 0.989101
## bmi_miss
                     -23.22712 1450.07150 -0.016 0.987220
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 275.10 on 204 degrees of freedom
## Residual deviance: 112.32 on 199 degrees of freedom
## AIC: 124.32
```

```
##
## Number of Fisher Scoring iterations: 18
```

Equation: Dummy Variable Method

```
\begin{split} HEALTH\_GOOD &= 3.66 + 1.18*HEALTH\_COVER + -0.02*BMI + -0.05*AGE \\ &+ -23.23*MISSING\_HEALTH\_COVER + -22.23*MISSING\_BMI \end{split}
```

5. LVCF (if applicable to your data).

My data is cross-sectional so the LVCF method is not applicable.

6. Hotdecking (nearest neighbor).

```
# Using Manhattan distance and variance as weight to rescale variables:
risk_hot_deck <- impute.NN_HD(DATA=risk_MAR,
                                 distance="eukl",
                                 donor_limit = 2,
                                 optimal_donor = 'mmin',
                                 weights="var",
                                 diagnose = 'diagnostics')
#Perform Analysis
fit_hot_deck <- glm(health_good ~ health_cover + bmi + age,</pre>
                         data = risk_hot_deck,
                         family = binomial(link = 'logit'))
summary(fit_hot_deck)
##
## Call:
## glm(formula = health_good ~ health_cover + bmi + age, family = binomial(link = "logit"),
       data = risk_hot_deck)
##
##
## Deviance Residuals:
      Min
                1Q
                    Median
                                           Max
## -2.3686 -1.2222
                     0.6727
                               0.8065
                                        1.3169
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                2.210668
                           0.884635
                                       2.499 0.01246 *
## health_cover 1.000239
                           0.420322
                                       2.380 0.01733 *
## bmi
               -0.013103
                            0.021205 -0.618 0.53661
## age
               -0.028896
                            0.009365 -3.086 0.00203 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 287.47 on 244 degrees of freedom
## Residual deviance: 273.10 on 241 degrees of freedom
## AIC: 281.1
## Number of Fisher Scoring iterations: 4
```

Equation: Hotdecking Method

```
HEALTH\_GOOD = 2.21 + 1.00 * HEALTH\_COVER + -0.01 * BMI + -0.03 * AGE
```

7. Regression imputation.

```
risk_imp_reg <- risk_MAR
df_cc <- risk_MAR[complete.cases(risk_MAR) , ] #Subset complete cases (cc)</pre>
#BMI: Regression Imputation
Ry <- as.numeric(!is.na(risk_MAR$bmi))# Missing data indicator</pre>
bmi_miss <- risk_MAR[Ry == 0 , ] #Subset rows with missing BMI values</pre>
mod reg imp <- lm(bmi ~ age + health good + health cover, data = df cc) #Run model on cc data
bmi_imp_reg <- predict(mod_reg_imp, newdata = bmi_miss) #Use model to predict missing values</pre>
risk_imp_reg$bmi[Ry ==0] <- bmi_imp_reg #Replace missing values</pre>
#HEALTH INSURANCE COVERAGE: Regression Imputation
Ry <- as.numeric(!is.na(risk MAR$health cover)) # Missing data indicator
health_cover_miss <- risk_imp_reg[Ry == 0 , ] #Subset rows with missing HEALTH_COVER values
health_cover_mod <- glm(health_cover ~ age + bmi + health_good,
                        data = df_cc,
                        family = binomial(link = 'logit')) #Fit model on cc data
health_cover_probs <- predict(health_cover_mod,
                              newdata = health_cover_miss,
                              type = 'response') #Predict Probability for missing data
heath_cover_imp_reg <- as.integer(round(health_cover_probs)) #Round probs to 0/1
risk_imp_reg$health_cover[Ry == 0] <- heath_cover_imp_reg #Replace missing values</pre>
#GOOD HEALTH: Regression Imputation
Ry <- as.numeric(!is.na(risk_MAR$health_good)) # Missing data indicator
health_good_miss <- risk_imp_reg[Ry == 0 , ] #Subset rows with missing HEALTH_COVER values
health_good_mod <- glm(health_good ~ age + bmi + health_cover,
                        data = df_cc,
                        family = binomial(link = 'logit')) #Fit model on cc data
health_good_probs <- predict(health_good_mod,
                              newdata = health_good_miss,
                              type = 'response') #Predict Probability for missing data
heath_good_imp_reg <- as.integer(health_good_probs) #Round probs to 0/1
risk_imp_reg$health_good[Ry == 0] <- heath_good_imp_reg #Replace missing COVER values
#Perform Analysis
fit_imp_reg <- glm(health_good ~ health_cover + bmi + age,</pre>
                         data = risk_imp_reg,
                         family = binomial(link = 'logit'))
summary(fit_imp_reg)
##
## Call:
## glm(formula = health good ~ health cover + bmi + age, family = binomial(link = "logit"),
       data = risk_imp_reg)
##
##
## Deviance Residuals:
       Min
                 1Q Median
                                   3Q
                                           Max
## -2.0380 -1.2614 0.7869 0.9565
                                       1.4341
```

```
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
              2.100052  0.890315  2.359  0.01834 *
## (Intercept)
## health_cover 0.925836 0.478924
                                  1.933 0.05322 .
             -0.031391 0.022560 -1.391 0.16409
## bmi
             ## age
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 323.26 on 244 degrees of freedom
## Residual deviance: 310.17 on 241 degrees of freedom
## AIC: 318.17
##
## Number of Fisher Scoring iterations: 4
```

Equation: Regression Imputation

```
HEALTH \ GOOD = 2.10 + 0.93 * HEALTH \ COVER + -0.03 * BMI + -0.03 * AGE
```

8. Regression imputation with Noise

Perform only on numerical and dichotomous variables.

```
risk_imp_stoch <- risk_MAR
#BMI: Stochastic Imputation
Ry <- as.numeric(!is.na(risk_MAR$bmi))# Missing data indicator</pre>
bmi_miss <- risk_MAR[Ry == 0 , ] #Subset rows with missing BMI values</pre>
df_cc <- risk_MAR[complete.cases(risk_MAR) , ] #Subset complete cases (cc)</pre>
mod_reg_imp <- lm(bmi ~ age + health_good + health_cover, data = df_cc) #Run model on cc data
bmi_imp <- predict(mod_reg_imp, newdata = bmi_miss) #Use model to predict missing BMI values
noise <- rnorm(length(bmi_imp), 0, summary(mod_reg_imp)$sigma) #Generate noise
bmi_imp_stoch <- bmi_imp + noise #Combine predictions with noise</pre>
risk_imp_stoch$bmi[Ry ==0] <- bmi_imp_stoch #Replace missing values
#HEALTH INSURANCE COVERAGE: Stochastic Imputation
Ry <- as.numeric(!is.na(risk MAR$health cover)) # Missing data indicator
health_cover_miss <- risk_MAR[Ry == 0 , ] #Subset rows with missing HEALTH_COVER values
health_cover_mod <- glm(health_cover ~ age + bmi + health_good,
                        data = df_cc,
                        family = binomial(link = 'logit')) #Fit model on cc data
health_cover_probs <- predict(health_cover_mod,
                              newdata = health_cover_miss,
                              type = 'response') #Predict Probability for missing data
heath_cover_imp_stoch <- rbinom(n = length(health_cover_probs),
                            size = 1,
                            prob = health_cover_probs) #Draw from binomial distribution
risk_imp_stoch$health_cover[Ry == 0] <- heath_cover_imp_stoch #Replace missing values
#GOOD HEALTH: Stochastic Imputation
```

```
Ry <- as.numeric(!is.na(risk_MAR$health_good)) # Missing data indicator</pre>
health_good_miss <- risk_MAR[Ry == 0 , ] #Subset rows with missing HEALTH_COVER values
health_good_mod <- glm(health_good ~ age + bmi + health_cover,
                        data = df cc,
                        family = binomial(link = 'logit')) #Fit model on cc data
health_good_probs <- predict(health_good_mod,
                             newdata = health_good_miss,
                             type = 'response') #Predict Probability for missing data
heath_good_imp_stoch <- rbinom(n = length(health_good_probs),</pre>
                           size = 1,
                           prob = health_good_probs) #Draw from binomial distribution
risk_imp_stoch$health_good[Ry == 0] <- heath_good_imp_stoch #Replace missing COVER values
#Perform Analysis
fit_imp_stoch <- glm(health_good ~ health_cover +bmi + age,
                        data = risk_imp_stoch,
                        family = binomial(link = 'logit'))
summary(fit_imp_stoch)
##
## Call:
## glm(formula = health_good ~ health_cover + bmi + age, family = binomial(link = "logit"),
       data = risk_imp_stoch)
## Deviance Residuals:
                1Q Median
      Min
                                  3Q
                                          Max
## -2.2877 -1.1049 0.6389 0.7925
                                        1.4421
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) 3.232945 0.900385 3.591 0.00033 ***
                                      2.497 0.01252 *
## health_cover 1.145455
                           0.458713
               -0.050673
                           0.020727 -2.445 0.01450 *
## bmi
## age
               -0.031009
                           0.009499 -3.264 0.00110 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
       Null deviance: 289.41 on 244 degrees of freedom
## Residual deviance: 268.42 on 241 degrees of freedom
## AIC: 276.42
## Number of Fisher Scoring iterations: 4
```

Equation: Regression with Noise Imputation

```
HEALTH\_GOOD = 3.23 + 1.15*HEALTH\_COVER + -0.05*BMI + -0.03*AGE
```

Multiple imputation with either mi or mice package:

9. Load your data into the package. Obtain summary, histogram and image of the data.

```
risk_mdf <- missing_data.frame(risk_MAR)</pre>
```

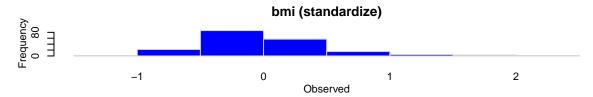
A) Summary

summary(risk_mdf)

##	age	bmi	health_cover	health_good	
##	Min. : 7.00	Min. :14.21	Min. :0.0000	Min. :0.0000	
##	1st Qu.:48.00	1st Qu.:23.25	1st Qu.:1.0000	1st Qu.:1.0000	
##	Median :59.00	Median :26.66	Median :1.0000	Median :1.0000	
##	Mean :58.11	Mean :27.86	Mean :0.8927	Mean :0.7512	
##	3rd Qu.:70.00	3rd Qu.:31.38	3rd Qu.:1.0000	3rd Qu.:1.0000	
##	Max. :97.00	Max. :55.72	Max. :1.0000	Max. :1.0000	
##		NA's :55	NA's :40	NA's :40	

B) Histogram

hist(risk_mdf, ask = F)



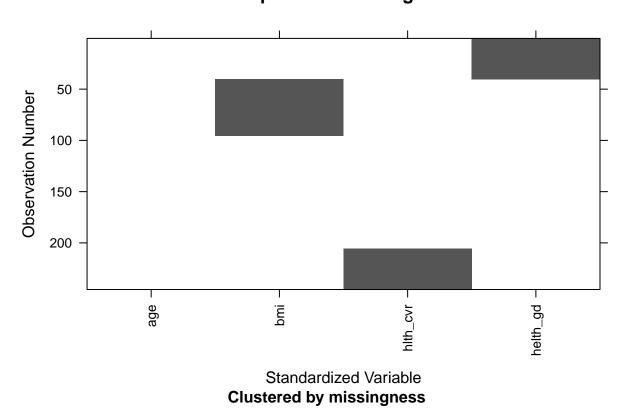




C) Image

image(risk_mdf, grayscale = TRUE)

Dark represents missing data



10. Check your data types and make changes if necessary.

gaussian identity

logit

logit

bmi

health_cover binomial

health_good binomial

There do not seem to be any need for changes. *BMI* is continuous, so the imputation method is the identity link, i.e. regular linear regression. *Health_Cover* and *Health_Good* are both binary variables, so they should be imputed with binomial logistic regression, which uses a logit link. *Age* is not missing any data, so there is no need to impute it, hence the NAs in the table below.

```
show(risk_mdf)
## Object of class missing_data.frame with 245 observations on 4 variables
##
## There are 4 missing data patterns
##
## Append '@patterns' to this missing_data.frame to access the corresponding pattern for every observat
##
##
                       type missing method
                                            model
## age
                                  0
                                      <NA>
                                              <NA>
                continuous
                                       ppd linear
                continuous
                                 55
## bmi
                                 40
## health_cover
                    binary
                                           logit
                                       ppd
## health_good
                    binary
                                       ppd
                                            logit
##
##
                  family
                              link transformation
## age
                     <NA>
                              <NA>
                                      standardize
```

<NA>

<NA>

standardize

11. Run the mi command and check convergence by traceplots.

```
risk_imp_MI <- mi(risk_mdf, n.chains = 5, n.iter = 30, verbose = F, seed = 2013)
```

Trace Plots

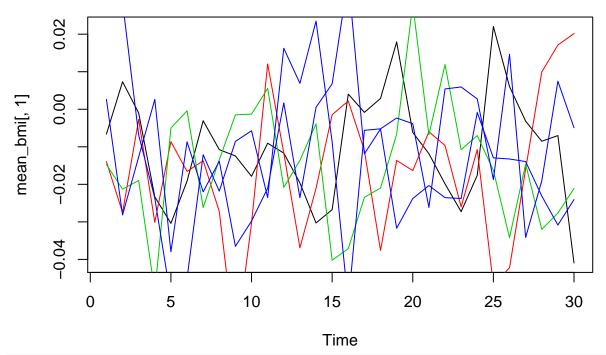
None of the trace plots provide clear evidence of divergence. However, some of the lines extend beyond the y-limits of the plots. Also, I was a little concerned about the red line at the end of the *health_cover* plot. It seems possible that it may diverge at 30.

```
converged <- mi2BUGS(risk_imp_MI)

mean_bmi <- converged[, , 1]
mean_health_cover <- converged[, , 2]
mean_health_good <- converged[, , 3]

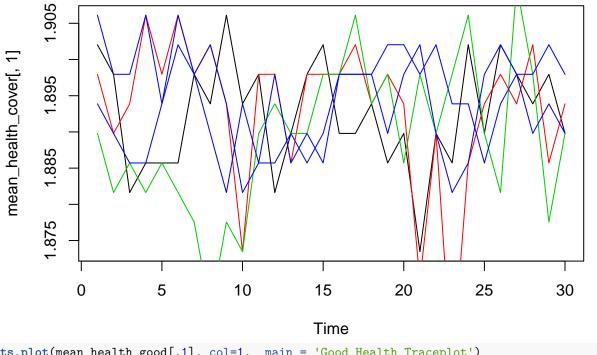
ts.plot(mean_bmi[,1], col=1, main = 'BMI Traceplot')
lines(mean_bmi[,2], col= 2)
lines(mean_bmi[,3], col= 3)
lines(mean_bmi[,4], col= 4)
lines(mean_bmi[,5], col= 4)</pre>
```

BMI Traceplot



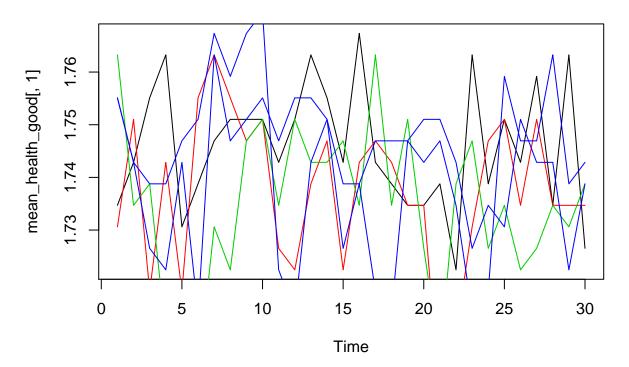
```
ts.plot(mean_health_cover[,1], col=1, main = 'Health Cover Traceplot')
lines(mean_health_cover[,2], col= 2)
lines(mean_health_cover[,3], col= 3)
lines(mean_health_cover[,4], col= 4)
lines(mean_health_cover[,5], col= 4)
```

Health Cover Traceplot



```
ts.plot(mean_health_good[,1], col=1, main = 'Good Health Traceplot')
lines(mean_health_good[,2], col= 2)
lines(mean_health_good[,3], col= 3)
lines(mean_health_good[,4], col= 4)
lines(mean_health_good[,5], col= 4)
```

Good Health Traceplot



12. Check r-hats.

All of the r-hats are close to 1 and less than 1.1, which is a good sign.

```
Rhats(risk_imp_MI)
```

```
## mean_bmi mean_health_cover mean_health_good sd_bmi
## 1.004345 1.011192 1.036500 1.010088
## sd_health_cover sd_health_good
## 1.010309 1.036036
```

13. Increase number of imputations if necessary.

The r-hats were close to one, which was a good sign. Althoug there was no clear sign of divergence from the trace plots, I was a little concern about some of the anomalies I saw, particularly the possible divergence of one of the imputations at the end of the health_cover plot. I decided to increase the number of iterations from 30 to 60 just to be sure that the imputations converged. Because the model was relatively simple and the dataset relatively small, the increase in iterations was not too much of a burden for my computer.

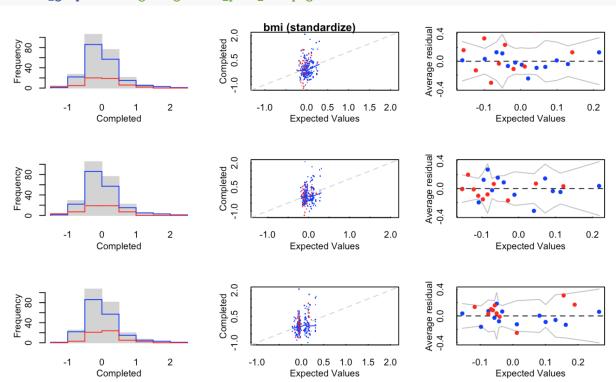
```
set.seed(2013)
risk_imp_mi_60 <- mi(risk_mdf, verbose = F, n.iter = 60, seed = 2013)</pre>
```

14. Plot diagnostics.

The barplots/histograms, scatter plots and residual plots of imputed values seemed to be consistent with the observed values on the three variables with missing data.

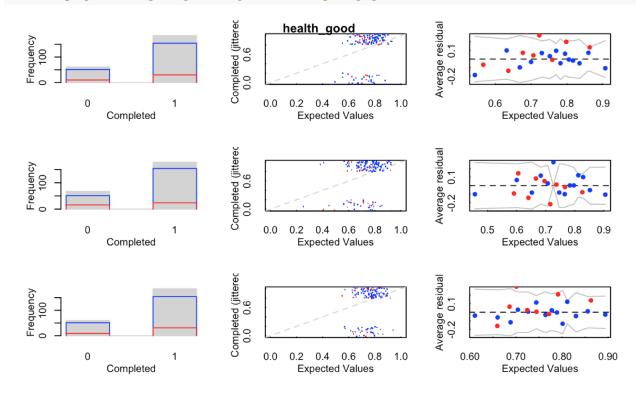
14i. Diagnostic Plot: BMI PLOT





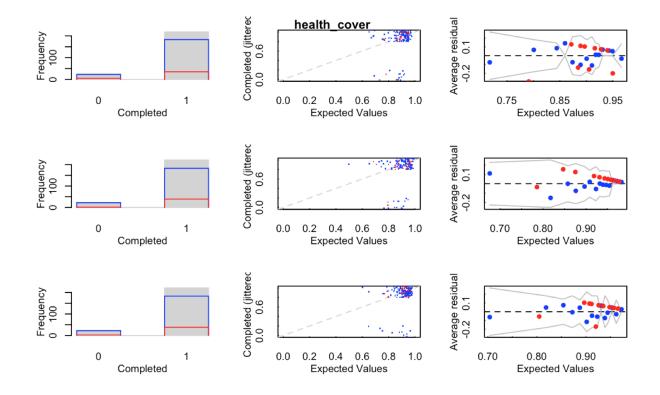
14ii. Diagnostic Plot: Health_Good

include_graphics('img/diagnostic_plot_health_good.png')



14ii. Diagnostic Plot: Health_Cover

include_graphics('img/diagnostic_plot_health_cover.png')



15. Change imputation models if necessary.

Because the imputed data from the second multiple imputation model seemed consistent with the observed data, I decided not to alter the imputation model further.

16. Run pooled analysis.

```
fit_risk_imp_mi_60 <- mi::pool(health_good ~ health_cover + age + bmi, data = risk_imp_mi_60)
display(fit_risk_imp_mi_60)
## bayesglm(formula = health good ~ health cover + age + bmi, data = risk imp mi 60)
                 coef.est coef.se
## (Intercept)
                  2.74
                           1.07
## health_cover1
                  0.95
                           0.76
                           0.01
## age
                 -0.02
## bmi
                 -0.04
                           0.03
## n = 241, k = 4
## residual deviance = 263.5, null deviance = 278.1 (difference = 14.6)
```

Part C: Summary Table

Table with results from all imputation methods.

```
prepare_table <- function(x, model_name, vars = 4){
   require(magrittr)
   estimates <- coef(summary(x))[1:vars, 1] %>% t
   standard_errors <- coef(summary(x))[1:vars, 2] %>% t
   colnames(standard_errors) <- paste('SE', colnames(standard_errors), sep = '_')
   d <- cbind(estimates, standard_errors)</pre>
```

```
d \leftarrow round(d, 2)
  d <- cbind(model name, d)</pre>
  d <- as.data.frame(d)</pre>
  return(d)
}
#Get Coefs from Each Model
listwise_coefs <- prepare_table(fit_list_wise, model_name ='Listwise')</pre>
## Loading required package: magrittr
##
## Attaching package: 'magrittr'
## The following object is masked from 'package:purrr':
##
##
       set_names
## The following object is masked from 'package:tidyr':
##
##
       extract
mean_coefs <-prepare_table(fit_imp_mean_mode, model_name = 'Mean')</pre>
random_coefs <- prepare_table(fit_imp_rand, model_name = 'Random')</pre>
dummy_coefs <- prepare_table(fit_dummy, model_name = 'Dummy')</pre>
hot_deck_coefs <- prepare_table( fit_hot_deck, model_name = 'Hot Deck')</pre>
regression_coefs <- prepare_table(fit_imp_reg, model_name = 'Regression')</pre>
stoch_coefs <- prepare_table(fit_imp_stoch, model_name = 'Stochastic')</pre>
mi_coefs <- prepare_table( fit_risk_imp_mi_60, model_name = 'Multi. Imp.')</pre>
names(mi coefs)[grepl(names(mi coefs), pattern = 'health cover')] <- c("health cover", "SE health cover"</pre>
full_coefs <- prepare_table(fit_full, "Full Data")</pre>
#Bind All Coefficients into One Table
summ_table <- listwise_coefs %>%
                   rbind(mean_coefs) %>%
                   rbind(random_coefs) %>%
                   rbind(dummy_coefs) %>%
                   rbind(hot_deck_coefs) %>%
                   rbind(regression_coefs) %>%
                   rbind(stoch_coefs) %>%
                   rbind(mi_coefs) %>%
                   rbind(full_coefs)
summ_table <- summ_table %>%
  select(model_name, `(Intercept)`, `SE_(Intercept)`, age, SE_age, bmi, SE_bmi,
         health_cover, SE_health_cover)
names(summ_table) <- c('Model', rep(c('Est.', 'SE'), 4))</pre>
kable(summ table) %>%
add_header_above(c(" " = 1, "Intercept" = 2, "Age" = 2, "BMI" = 2,
                    'Health Cover' = 2)) %>%
row_spec(9, italic= T)
```

	Intercept		Age		BMI		Health Cover	
Model	Est.	SE	Est.	SE	Est.	SE	Est.	SE
Listwise	3.66	1.41	-0.05	0.02	-0.02	0.03	1.18	0.69
Mean	3.06	1.03	-0.02	0.01	-0.04	0.03	0.63	0.53
Random	2.93	0.92	-0.02	0.01	-0.03	0.02	0.51	0.47
Dummy	3.66	1.41	-0.05	0.02	-0.02	0.03	1.18	0.69
Hot Deck	2.21	0.88	-0.03	0.01	-0.01	0.02	1	0.42
Regression	2.1	0.89	-0.03	0.01	-0.03	0.02	0.93	0.48
Stochastic	3.23	0.9	-0.03	0.01	-0.05	0.02	1.15	0.46
Multi. Imp.	2.74	1.07	-0.02	0.01	-0.04	0.03	0.95	0.76
Full Data	3.27	0.97	-0.03	0.01	-0.05	0.02	1.19	0.46

PART D: Comparisons

The table above shows all the estimates from all the models including their standard errors. The last row (in *italics*) represents the 'true' estimates and standard errors from the model that was fit on the complete data set (i.e. The original dataset before I applied the ampute function). The 'stochastic' model refers to the regression with noise imputation model.

1) Intercept

Out of all the methods, stochastic imputation generated an estimate of the intercept that was closest to the intercept from the full data model (3.23 versus 3.27). Despite setting a seed, multiple imputation tended to produce different intercept estimates on different runs. Nevertheless, multiple imputation generally resulted in estimates of the intercept that were slightly lower than the full data model's estimate. The listwise deletion, dummy variable method, and stochastic models overestimated the intercept and the regression imputation, hot deck, mean imputation and random imputation models underestimated the intercept.

The listwise deletion and the dummy variable models tended to overestimate the standard errors of the intercept coefficient. The multiple imputation gave a standard error that varied quite a bit but was generally close to 1. This was close to the standard error of the intercept from the full model (0.97). All the other models tended to provide standard errors that were slightly less than the full model and were generally around 0.90.

2) Age

Age was completely observed. Consequently, most of the imputation models performed well by estimating a coefficient that was similar to the one from the model fit on the full dataset (-0.03). The only exceptions were the listwise deletion and dummy variable method models, which overestimated the effect of age (-0.05). The coefficient of the multiple imputation tended to vary between -0.02 and -0.03, which was fairly close to the coefficient estimate from the full data model. All of the models produced estimates of the standard error that were either 0.01 or 0.02, which were all fairly close to the standard error of the full data model (0.01).

3) BMI

The estimate of BMI from the stochastic model matched closely to the full data model (-0.05). The coefficient from the multiple imputation model also generally matched the coefficient from the full data model, varying between -0.04 and -0.05. The other models tended to underestimate the effect of BMI on health and produced coefficients, ranging from -0.01 to -0.03. The standard errors of all the models varied between .02 and .03, which was pretty close to the .02 SE from the full data model.

4) Health Cover

Surprisingly, the listwise deletion method and dummy variable models resulted in an estimates of health_cover that were closest to the full data model (1.18 vs. 1.19). However, the standard error of the coefficient from the listwise deletion model was higher than the standard error from the full data model (0.69 versus 0.46). The next closest estimate was the stochastic imputation model (1.15). The stochastic model also produced a standard error that matched the full data model. The other models generally underestimated the coefficient for health_cover. The random imputation and regression imputation models produced standard errors that were close to the original, whereas the mean imputation model overestimated the standard error (.53) and the hotdecking method underestimated the standard error (.42). The multiple imputation model tended to underestimate the effect of health coverage and overestimate the standard error.

It should be noted that although the listwise deletion model produced a reasonabllu close estimate for the health_cover effect, it probably would not produce accurate predictions for *good_health*, the outcome variable, because the other coefficients were not close to the full data model. The stochastic and the multiple imputation models produced coefficients for BMI, age, and the intercept that were closer to the full data model; consequently, they would likely produce better predictions of health in general.

Note on Standard Errors The stochastic imputation model most closely matched the estimates from the full data model. However, the multiple imputation method produced accurate coefficients for age and bmi. In addition the higher standard errors from the multiple imputation method could reflect the additional uncertainty due to the imputation process. Finally, although the diagnostic plots seemed to be reasonable, increasing the number of iterations or changing the imputation method from post predictive distributions to predictive mean matching may have resulted in stabler estimates.

The listwise deletion model tended to have the highest standard errors. The lower standard errors are a result of this model being fit on only around half of the data. Having a smaller number of observations will result in a higher standard error if everything else is held equal.

Health_Cover From the barplot in section 9B, we can see that among the observed cases, most subjects had health insurance. The fact that there was very little variance on this variable may have caused the multiple imputation method to underestimate its effect.

Other Limitations In order to simplify the interpretation of the models, I dichotimized *health_general*, which was originally a 5-point ordinal variable, into a binary variable coded 1 for 'good health' and 0 for 'fair' or 'poor' health. Although this change simplified the interpretation of the coefficients of the model, some information would have been lost as the result of binning multiple categories together. This could have in turn affected the estimates of the predictor variables across all the variables.

PART E: Wow Factor

1.0207871

##

As I wrote in the previous section, I was concerned about the lack of stability across multiple runs. I decided to convert the imputation method used for health_cover and health_good to predictive mean matching in the hope that this might lead to more stable estimates

Result of Changing Imputation Model The Rhats seemed to be closer to 1. However, the estimates produced still seem to underestimate the effect of health_cover as seen below.

0.9935526

```
fit_risk_imp_mi_wow <- mi::pool(health_good ~ health_cover + age + bmi, data = risk_imp_mi_wow)
display(fit_risk_imp_mi_wow )
## bayesglm(formula = health_good ~ health_cover + age + bmi, data = risk_imp_mi_wow)
##
                 coef.est coef.se
## (Intercept)
                  3.30
                           1.73
## health_cover1 0.51
                           0.84
                           0.01
## age
                 -0.03
## bmi
                 -0.04
                           0.04
## n = 241, k = 4
## residual deviance = 269.9, null deviance = 284.8 (difference = 15.0)
```

Interaction

My next decision was to evaluate whether or not the model should have any interaction terms. I fit new models with interactions between *health_cover* and *age* and *bmi* and then performed likelihood ratio tests to evaluate whether the interaction terms significantly improved the model. Only the model with the *health_cover/bmi* interaction had a statistically significant improvement over the model without interaction

```
risk_sub %>% nrow
## [1] 245
risk_full %>% nrow
## [1] 234
fit_full_1 <- glm(formula = health_good ~ health_cover*age + bmi,</pre>
             data = risk_full,
             family = binomial)
anova(fit_full,fit_full_1, test = 'Chisq')
## Analysis of Deviance Table
##
## Model 1: health_good ~ health_cover + age + bmi
## Model 2: health good ~ health cover * age + bmi
##
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           230
                   247.88
## 2
           229
                   245.31 1
                               2.5742
                                        0.1086
fit_full_2 <- glm(formula = health_good ~ age + health_cover*bmi, data = cc(risk_sub))</pre>
anova(fit_full, fit_full_2, test = 'Chisq')
## Analysis of Deviance Table
##
## Model 1: health_good ~ health_cover + age + bmi
## Model 2: health_good ~ age + health_cover * bmi
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           230
                  247.885
## 2
           229
                   41.084 1
                                206.8 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Comparing Imputation Model with New Interaction Term

I decided to compare the stochastic imputation model with the multiple imputation model using the new formula. I chose these models because stochastic imputation performed the best with the previous main terms only formula despite the fact that multiple imputation is generally considered to be superior.

```
fit_full_interaction <- glm(health_good ~ age + health_cover*bmi, data = risk_full,
            family = binomial)
summary(fit_full_interaction)
##
## Call:
## glm(formula = health_good ~ age + health_cover * bmi, family = binomial,
       data = risk full)
##
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
  -2.3811
           -0.5743
                      0.6461
                               0.7788
                                         1.3032
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     3.126071
                                1.998250
                                           1.564 0.11772
## age
                    -0.028541
                                0.010107
                                          -2.824 0.00475 **
## health_cover
                     1.364788
                                2.139887
                                           0.638 0.52361
## bmi
                    -0.048339
                                0.070839
                                          -0.682 0.49500
## health_cover:bmi -0.006412
                                0.075428
                                          -0.085 0.93225
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 264.27 on 233
                                      degrees of freedom
## Residual deviance: 247.88 on 229
                                      degrees of freedom
## AIC: 257.88
## Number of Fisher Scoring iterations: 4
fit_stoch_interaction <- glm(health_good ~ age + health_cover*bmi, data = risk_imp_stoch,
            family = binomial)
summary(fit_stoch_interaction)
##
## Call:
## glm(formula = health_good ~ age + health_cover * bmi, family = binomial,
##
       data = risk_imp_stoch)
##
## Deviance Residuals:
##
                                   3Q
                                           Max
       Min
                 10
                      Median
                      0.6281
                               0.7967
                                         1.3862
## -2.3100 -1.0586
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                     2.184980
                                1.719509
                                           1.271 0.203835
## age
                    -0.032271
                                0.009714
                                          -3.322 0.000894 ***
                     2.430381
                                1.887232
                                           1.288 0.197815
## health_cover
## bmi
                    -0.012035
                                0.058113 -0.207 0.835932
```

```
## health_cover:bmi -0.044171
                                0.062760 -0.704 0.481555
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 289.41 on 244 degrees of freedom
##
## Residual deviance: 267.95 on 240 degrees of freedom
## AIC: 277.95
##
## Number of Fisher Scoring iterations: 4
fit_mi_interaction <- mi::pool(health_good ~ age + health_cover*bmi, data = risk_imp_mi_60)
display(fit_mi_interaction )
## bayesglm(formula = health_good ~ age + health_cover * bmi, data = risk_imp_mi_60)
                     coef.est coef.se
## (Intercept)
                      2.73
                               1.51
## age
                     -0.02
                               0.01
                               1.32
                      0.95
## health_cover1
## bmi
                     -0.04
                               0.06
## health_cover1:bmi 0.00
                               0.05
## n = 240, k = 5
## residual deviance = 263.4, null deviance = 278.1 (difference = 14.7)
full_row <- prepare_table(fit_full_interaction, model_name = 'Full Data', vars = 5)
stoch_row <- prepare_table(fit_stoch_interaction, model_name = 'Stochastic', vars = 5)</pre>
mi_row <- prepare_table(fit_mi_interaction, model_name = 'Multi. Imp.', vars = 5)
names(mi_row) <- str_replace_all(names(mi_row), pattern = 'health_cover1', replacement = 'health_cover'</pre>
summ_table_interaction <- stoch_row %>%
                              rbind(mi row) %>%
                              rbind(full_row)
summ_table_interaction <- summ_table_interaction %>%
  select(model_name, `(Intercept)`, `SE_(Intercept)`, age, SE_age, bmi, SE_bmi,
         health_cover, SE_health_cover, `health_cover:bmi`, `SE_health_cover:bmi`)
names(summ_table_interaction) <- c('Model', rep(c('Est.', 'SE'), 5))</pre>
kable(summ_table_interaction) %>%
add_header_above(c(" " = 1, "Intercept" = 2, "Age" = 2, "BMI" = 2,
                   'Health Cover' = 2, 'BMI:Health Cover' = 2)) %>%
row_spec(3, italic= T)
```

	Intercept		Age		BMI		Health Cover		BMI:Health Cover	
Model	Est.	SE	Est.	SE	Est.	SE	Est.	SE	Est.	SE
Stochastic	2.18	1.72	-0.03	0.01	-0.01	0.06	2.43	1.89	-0.04	0.06
Multi. Imp.	2.73	1.51	-0.02	0.01	-0.04	0.06	0.95	1.32	0	0.05
Full Data	3.13	2	-0.03	0.01	-0.05	0.07	1.36	2.14	-0.01	0.08

Using the new formula with the interaction term between bmi and $health_cover$, the multiple imputation method generally produces estimates closer to the model fit on the full dataset.

One Final Note The original dataset was almost entirely complete. However, 4% of the BMI values were missing. It is possible that these missing values could affect the model if they were MNAR (Missing Not at Random).