

*with(LinearAlgebra) :*

*# Mat represents all the matrices in the set  $R := \{I, R_u^k, R_v^k, R_w^k \mid k \text{ in } \{1, 2, 3\}\}$ .*

*Id :=  $\langle \langle 1, 0, 0 \rangle \mid \langle 0, 1, 0 \rangle \mid \langle 0, 0, 1 \rangle \rangle$  : Rx :=  $\langle \langle 1, 0, 0 \rangle \mid \langle 0, 0, 1 \rangle \mid \langle 0, -1, 0 \rangle \rangle$  : Ry :=  $\langle \langle 0, 0, -1 \rangle \mid \langle 0, 1, 0 \rangle \mid \langle 1, 0, 0 \rangle \rangle$  : Rz :=  $\langle \langle 0, 1, 0 \rangle \mid \langle -1, 0, 0 \rangle \mid \langle 0, 0, 1 \rangle \rangle$  :*

*Mat := [Id, Rx, Rx . Rx, Rx . Rx . Rx, Ry, Ry . Ry, Ry . Ry . Ry, Rz, Rz . Rz, Rz . Rz . Rz] :*

*#variable list of a triangle ABC, A(a1,a2,a3), B(b1,b2,b3), C(c1,c2,c3).*

*vars :=  $\langle a1, a2, a3, b1, b2, b3, c1, c2, c3 \rangle$  :*

*# loop all the combinations of edge types for a triangle*

**for i from 1 to 10 do**

*A := Id - Mat[i] :*

**for j from i to 10 do**

*B := Id - Mat[j] :*

**for k from j to 10 do**

*C := Id - Mat[k] :*

*M := Matrix(9, 9) : # M represents the linear system as shown in Eqn. (8) in the paper*

**for s from 1 to 3 do**

**for t from 1 to 3 do**

*M[s, t] := A[s, t] : M[s, 3 + t] := -A[s, t] :*

*M[s + 3, t] := B[s, t] : M[s + 3, 6 + t] := -B[s, t] :*

*M[s + 6, t + 3] := C[s, t] : M[s + 6, 6 + t] := -C[s, t] :*

**od:**

**od:**

*RM := RowSpace(M) : # compute the basis of M*

**if nops(RM) > 0 then**

*# use the basis of M to eliminate the polynomial of the area of the triangle*

*G := Groebner[Basis]( {Determinant( $\langle \langle a1, a2, a3 \rangle \mid \langle b1, b2, b3 \rangle \mid \langle c1, c2, c3 \rangle \rangle$ )},  
seq(RM[i] . vars, i = 1 ..nops(RM)) }, tdeg(a1, a2, a3, b1, b2, b3, c1, c2, c3)) :*

*#If the area of the triangle can be eliminated, it means that the area of triangle is always zero.*

*#We print the encode of the combination of edge types.*

**if nops(G) = nops(RM) then**

*print(i - 1, j - 1, k - 1);*

**fi:**

**fi:**

**od:** *#end for k*

**od:** *#end for j*

**od:** *#end for i*