

## Introduction

- ▶ Nanoflare model of Parker [11]: corona heated by impulsive ( $\ll \tau_{cool}$ ), low-energy ( $10^{24}$  erg) events produced by twisting, braiding of field lines rooted in the photosphere
- ▶ “Smoking gun” of nanoflare heating is the faint, high-temperature component of the emission measure distribution,  $EM(T)$  [5, 8]
- ▶ While “hot” (i.e.  $> 10^{6.6}$  K) part of  $EM(T)$  poorly constrained observationally [14], measurements of the cool ( $10^6 < T < 10^{6.6}$  K) part of  $EM(T)$  in AR cores are consistent with loop models heated by intermediate frequency nanoflares [12, 6].
- ▶ Fundamental question: **what is the frequency of energy release in the solar corona?** Two extreme cases:
  - ▶ Low-frequency heating: Time between successive events is much greater than typical loop cooling time (i.e. approaches single nanoflare case)
  - ▶ High-frequency heating: Time between successive events is much smaller than typical loop cooling time (i.e. approaches steady heating case)
- ▶ **Goal:** Use hydrodynamic loop models to better understand how different heating properties, including the heating frequency, affect the “hot” part of the emission measure distribution.

## Hydrodynamic Modeling

- ▶ Zero-dimensional Enthalpy-based Thermal Evolution of Loops (EBTEL) model of Klimchuk et al. [10], Cargill et al. [7] allows for efficient modeling of many thousands of loops
- ▶ We use a modified form of the EBTEL model to treat the electron and ion populations separately [for more details, see 1, submitted]
- ▶ Applying the “EBTEL method” to the two-fluid hydrodynamic equations [as given in 3], the modified two-fluid EBTEL equations are,

$$\frac{d}{dt}\bar{p}_e = \frac{\gamma-1}{L}[\psi_{TR} - (\mathcal{R}_{TR} + \mathcal{R}_C)] + k_B\bar{n}\nu_{ei}(\bar{T}_i - \bar{T}_e) + (\gamma-1)\bar{Q}_e, \quad (1)$$

$$\frac{d}{dt}\bar{p}_i = -\frac{\gamma-1}{L}\psi_{TR} + k_B\bar{n}\nu_{ei}(\bar{T}_e - \bar{T}_i) + (\gamma-1)\bar{Q}_i, \quad (2)$$

$$\frac{d}{dt}\bar{n} = \frac{c_2(\gamma-1)}{c_3\gamma L k_B \bar{T}_e}(\psi_{TR} - F_{ce,0} - \mathcal{R}_{TR}), \quad (3)$$

where  $c_1 = \mathcal{R}_{TR}/\mathcal{R}_C$ ,  $c_2 = \bar{T}/T_a = 0.9$ ,  $c_3 = T_0/T_a = 0.6$ ,  $\psi_{TR}$  is a term included to maintain charge and current neutrality, and  $\nu_{ei}$  is the electron-ion binary Coulomb collision frequency

- ▶ Assume quasi-neutrality,  $n_e = n_i = n$ , and closed by equations of state:  $p_e = k_B n T_e$  and  $p_i = k_B n T_i$

## Single-nanoflare Results

- ▶ Single nanoflare is the most extreme low-frequency case, loop allowed to undergo complete heating and cooling cycle
- ▶ In Barnes et al. [1, submitted], we investigated the effect of pulse duration ( $\tau$ ), heat flux limiting, electron versus ion heating, and non-equilibrium ionization (NEI) on the resulting emission measure distribution,  $EM(T)$
- ▶ We found that,
  - ▶ While very short pulses ( $\tau = 20, 40$  s) lead to significant emission above 10 MK, comparisons with field-aligned models [e.g. HYDRAD, 3] show that EBTEL gives an artificially fast rise in density and thus an excess of hot emission for these very short heating times; longer pulses ( $\tau = 200, 500$  s) show a cutoff near 10 MK.
  - ▶ Compared to pure Spitzer thermal conduction, heat flux limiting (using  $f = 1/6$ ) extends  $EM(T)$  to  $> 10$  MK; extreme values of  $f$  (e.g.  $f = 1/30$ ) lead to significant emission  $> 20$  MK.
  - ▶ For the case in which the ions are heated, no emission is visible above 8 MK, independent of the pulse duration
  - ▶ Including effects due to NEI shows that, even for very short pulses, there is little to no emission visible above 10 MK, for the single-fluid, electron heating, and ion heating cases
- ▶ Conclusion:  **$EM(T)$  signature of loop plasma heated by a single nanoflare is most likely found in the temperature range  $T_m < T < 10^7$  K, where the temperature of maximum emission  $T_m \approx 4$  MK for active region (AR) cores [13]**

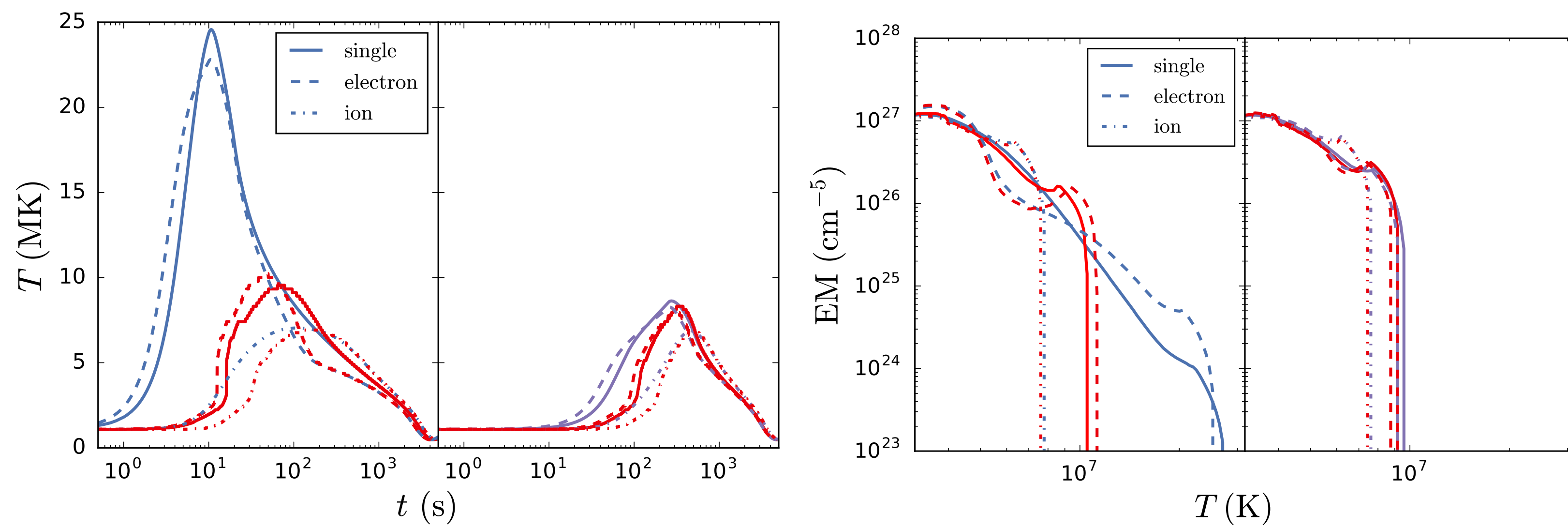


Figure 1: Equilibrium and non-equilibrium (red) ionization results for a single nanoflare lasting 20 s (blue) and 500 s (purple) in the single-fluid case (solid) as well as the case in which only the electrons (dashed) or only the ions (dot-dashed) are heated. **Left:** the electron temperature as a function of time for a 20 s pulse (left) and a 500 s pulse (right). **Right:** corresponding  $EM(T)$  for the equilibrium (left, blue and right, purple) and NEI (red) cases.

## Energy Budget and Heating Statistics

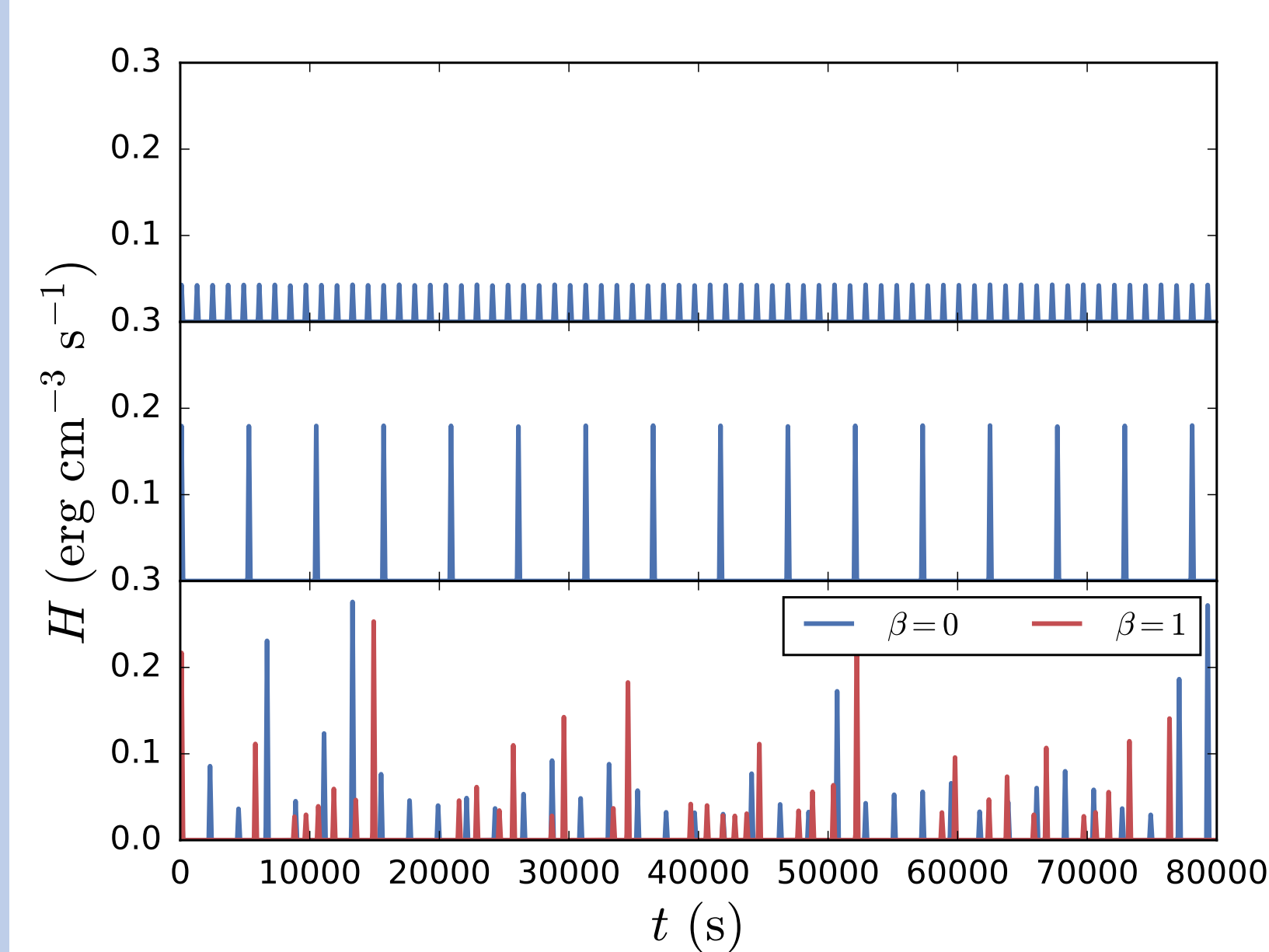


Figure 2: Top (Middle) panel shows Uniform heating amplitudes for  $t_N = 1000$  ( $t_N = 5000$ ) s. Bottom panel shows Heating amplitudes drawn from a power-law distribution with  $\alpha = -1.5$  and mean wait time  $t_N = 2000$  s; the events shown in red (blue) have wait times that depend on the previous event energy (uniform wait times).

- ▶ Loop of half-length  $L = 40$  Mm heated by  $N$  triangular pulses with duration  $\tau = 200$  s over  $t_{total} = 8 \times 10^4$  s.
- ▶ Each event has maximum heating rate  $H_i$  and followed by a waiting time of  $t_{N,i}$ ; static background heating  $H_{bg} = 3.5 \times 10^{-5}$  erg  $\text{cm}^{-3} \text{s}^{-1}$
- ▶  $H_i$  can either be uniform such that  $H_i = H_0$  for all  $i$  or chosen from a power-law distribution with  $\alpha = -1.5, -2.0, -2.5$
- ▶ The total energy injected into the loop is constrained by,

$$H_{eq} = \frac{1}{t_{total}} \sum_{i=1}^N \int_{t_i}^{t_i+\tau} dt Q(t) = \frac{\tau}{2t_{total}} \sum_{i=1}^N H_i, \quad (4)$$

- ▶  $H_{eq} \approx 3.6 \times 10^{-3}$  erg  $\text{cm}^{-3} \text{s}^{-1}$  is the time-averaged heating rate such that  $T_m \approx 4$  MK, consistent with AR core observations [13].
- ▶ Treat  $t_{N,i}$  as time needed for the field to “unwind”, consistent with the Parker [11] nanoflare picture
  - ▶  $\beta = 0$ :  $t_{N,i} = t_N$  for all  $i$ , no dependence on  $H_i$
  - ▶  $\beta = 1$ :  $\varepsilon = LA\tau H_i/2 \propto t_{N,i}$  (see bottom panel of Fig. 2)
- ▶ Total number of events dependent on  $t_N$ ,  $N = t_{total}/(t_N + \tau)$  such that  $N = 16$  when  $t_N = 5000$  s
- ▶ For the power-law cases, require  $NN_R \sim 1 \times 10^4$ , where  $N_R$  is the number of runs for each unique point in the parameter space,  $(\alpha, \beta, t_N)$

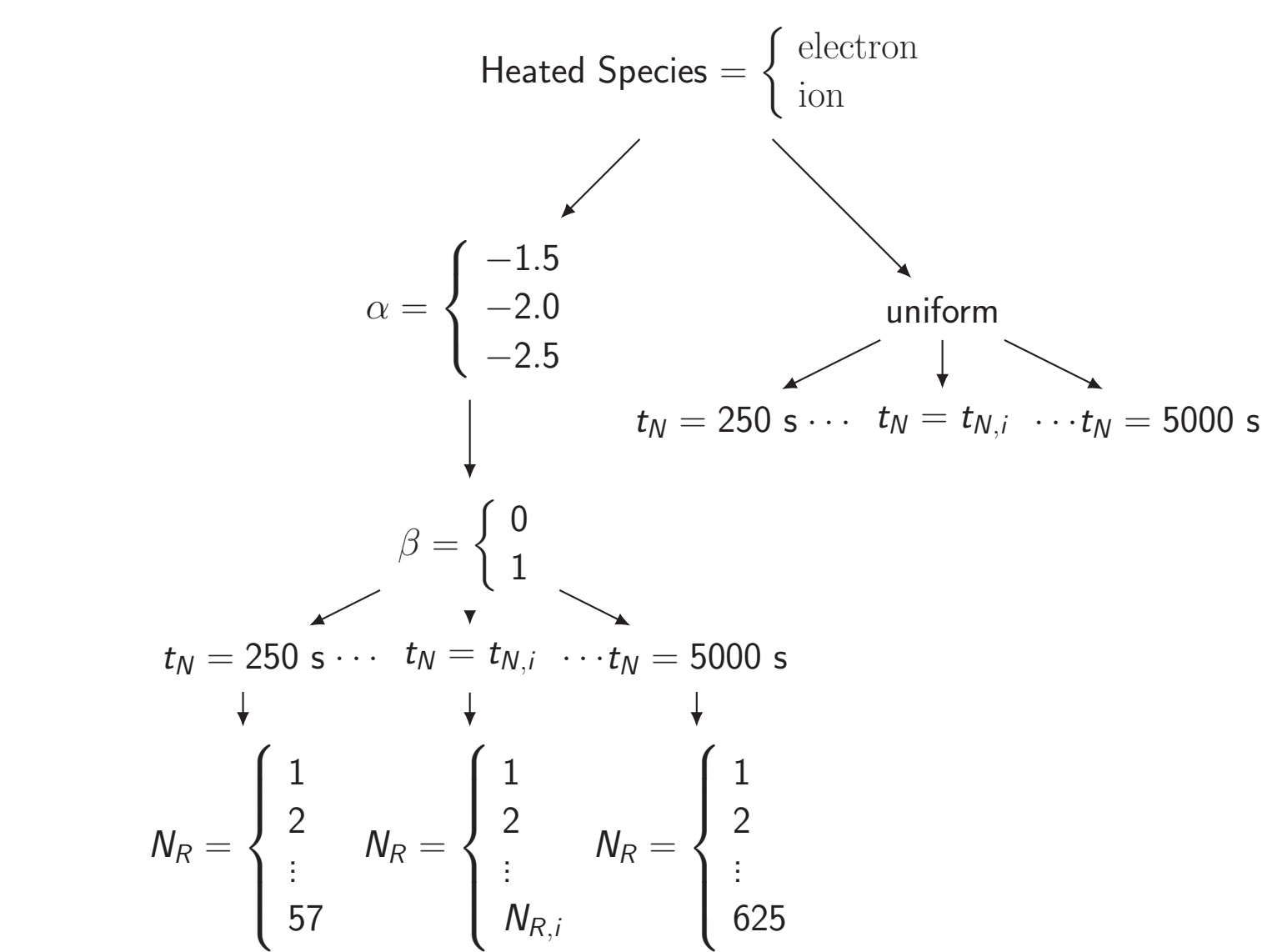


Figure 3: Heating function parameter space. We consider a range of waiting times  $250 < t_N < 5000$  s, in increments of 250 s. In the power-law case, a sufficiently large number of runs,  $N_R$  is required to sample the distribution. For example, when  $t_N = 5000$  s,  $N_R = 625$  such that for each  $(\alpha, \beta, t_N = 5000)$ , we run the model 625 times.

## Emission Measure Distribution

- ▶ Compute solutions to Eqs. 1, 2, and 3 for all  $N_R$  runs for each point in the multidimensional heating parameter space. (Note: for the events of uniform magnitude,  $N_R = 1$ )
- ▶ To account for NEI, we use the numerical code described in Bradshaw [2] to calculate the fractional ionization states for Fe IX through Fe XXVII and calculate  $T_{eff}$ , a temperature that would be measured based on the actual ionization states
- ▶ Given a temperature range  $4 \leq \log T_e \leq 8.5$  with bin widths  $\Delta \log T_e = 0.01$ , at each time  $t_j$ , add  $n_j^2(2L)$  to every bin that falls in the range  $[T_{0e,j}, T_{ae,j}]$ ; time-averaging over the entire run gives  $EM(T)$
- ▶ To calculate  $EM(T_{eff})$ , we use the same procedure, but using  $T_{eff}$  instead of  $T_e$ .

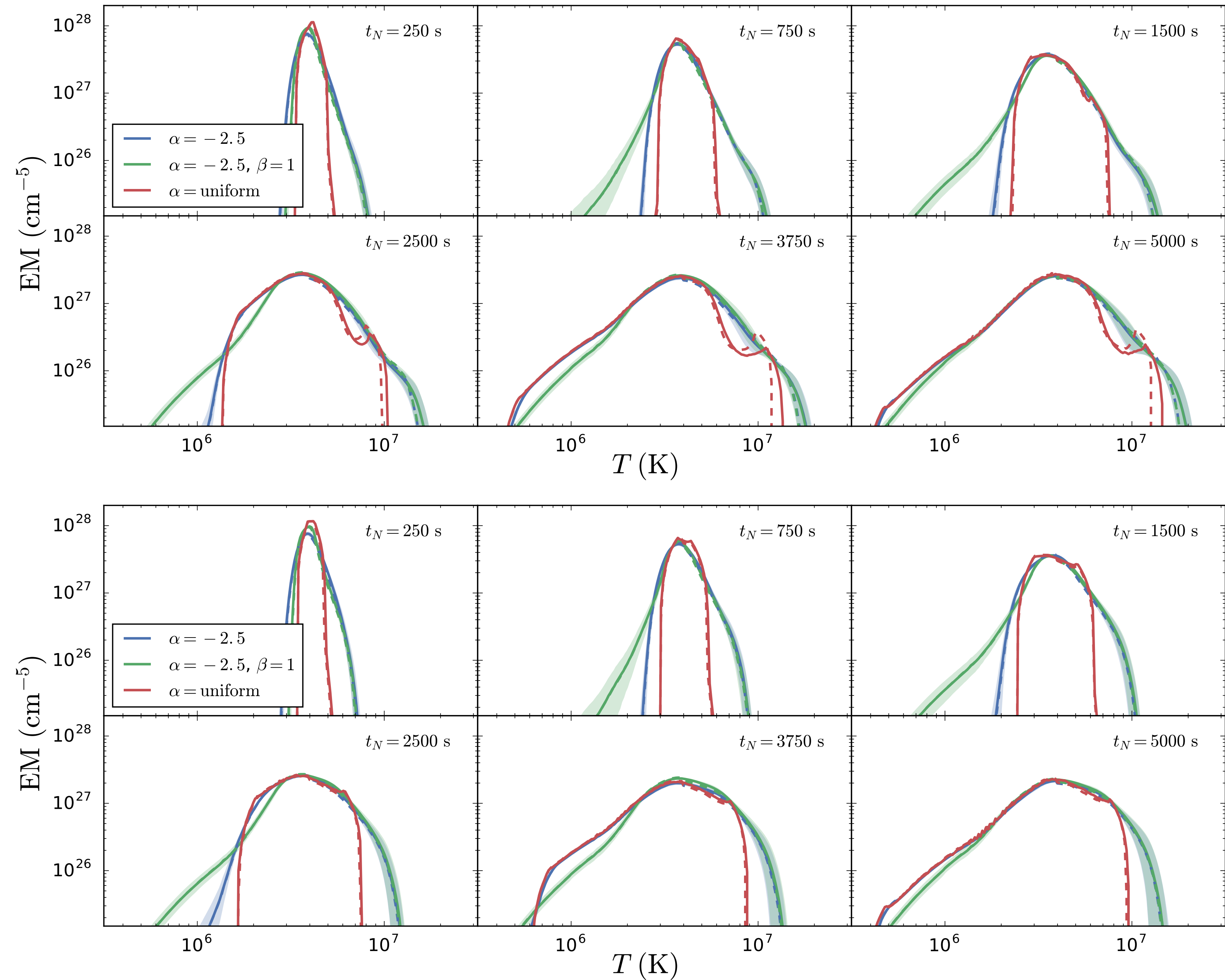


Figure 4: Emission measure distributions for waiting-times  $t_N = 250, 750, 1500, 2500, 3750, 5000$  s in the electron (top) and ion (bottom) heating cases. The three types of heating functions shown are uniform heating rates (red), heating rates chosen from a power-law distribution of  $\alpha = -2.5$  (blue), and heating rates chosen from a power-law distribution of  $\alpha = -2.5$  where the time between successive events is proportional to the heating rate of the preceding event (green). The solid lines in the two power-law cases show the mean  $EM(T)$  over  $N_R$  runs and the shading indicates  $1\sigma$  from the mean. The dashed lines denote the corresponding  $EM(T_{eff})$  distribution. The standard deviation is not included in the NEI results.

## Hot Plasma Diagnostics

- ▶ Well-known cool emission measure scaling  $EM(T) \propto T^a$ ; similar scaling claimed for the hot part of the emission measure distribution,  $EM(T) \propto T^{-b}$  over a temperature range  $T_m \lesssim T \lesssim 10^{7.2}$ .
- ▶ Observations have shown  $7 \lesssim b \lesssim 10$  [13] though measurements of  $b$  are poorly constrained due to lack of spectroscopic data in this temperature range;  $b$  very sensitive to the temperature range over which the fit is performed.
- ▶ Brosius et al. [4] find the ratio of Fe XIX (formed at  $T \approx 10^{6.95}$  K) to Fe XII (formed at  $T \approx 10^{6.2}$  K) intensity to be  $\sim 0.59$  inside AR core compared to  $\sim 0.076$  outside, providing possible evidence for impulsive heating.
- ▶ As a proxy for this intensity ratio and an alternative to  $b$ , we compute an emission measure ratio  $EM(T_{hot})/EM(T_{cool})$ , with  $T_{hot} = 10^{6.95}$  K and  $T_{cool} = 10^{6.3} \approx 2 \times 10^6$  K.

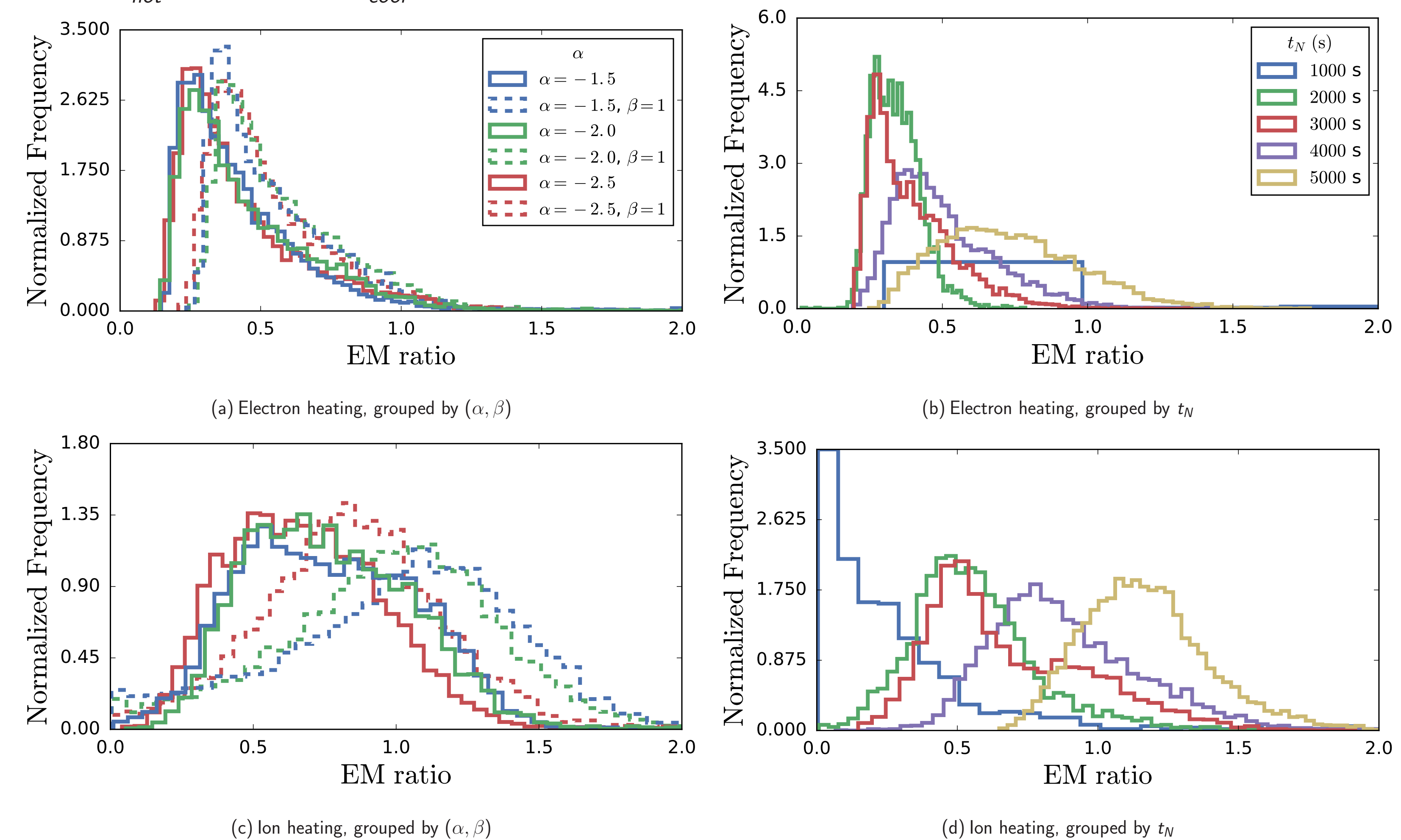


Figure 5: Histograms of emission measure ratios for the entire multidimensional heating parameter space (see Fig. 3). Each histogram is normalized such that for each distribution  $P(x)$ ,  $\int_{-\infty}^{\infty} dx P(x) = 1$  and the bin widths are calculated using the well-known Freedman-Diaconis formula [9]. The top panels show the electron heating cases and the bottom panels show the ion heating cases. In the left panels, each histogram (denoted by linestyle and color) corresponds to a unique heating function  $(\alpha, \beta)$ . The uniform case has not been included here. In the right panels, the emission measure ratios are grouped by  $t_N$ . Here we show only five values of  $t_N$  for aesthetic reasons.

## Conclusions

- ▶ While cool part of  $EM(T)$  more elongated for  $\beta = 1$ , **hot part of emission measure distribution independent of  $\beta$** .
- ▶ For intermediate heating frequencies, power-law cases (compared to uniform case) show significantly more hot emission, for both electron and ion heating
- ▶ Compared to single-nanoflare results, ion heating results show  $EM(T)$  extending to hotter temperatures ( $> 10^7$  K) for intermediate to low heating frequencies
- ▶ **Effects due to NEI only important for uniform heating in electron heating case**, no visible differences in ion heating case
- ▶ Emission measure ratio seems to be largely independent of  $\alpha$ , weakly dependent on  $\beta$ .
- ▶ **In ion heating case, lower  $t_N$  required for consistency with Brosius et al. [4] results as compared to electron heating case.**

## References

- [1] Barnes, W. T., Cargill, P. J., & Bradshaw, S. J. 2016, submitted
- [2] Bradshaw, S. J. 2009, *Astronomy and Astrophysics*, 502, 409
- [3] Bradshaw, S. J., & Cargill, P. J. 2013, *The Astrophysical Journal*, 770, 12
- [4] Brosius, J. W., Daw, A. N., & Rabin, D. M. 2014, *The Astrophysical Journal*, 790, 112
- [5] Cargill, P. J. 1994, *The Astrophysical Journal*, 422, 381
- [6] —, 2014, *The Astrophysical Journal*, 784, 49
- [7] Cargill, P. J., Bradshaw, S. J., & Klimchuk, J. A. 2012, *The Astrophysical Journal*, 752, 161
- [8] Cargill, P. J., & Klimchuk, J. A. 2004, *The Astrophysical Journal*, 605, 911
- [9] Freedman, D., & Diaconis, P. 1981, *Zeitschrift fr Wahrscheinlichkeitstheorie und Verwandte Gebiete*, 57, 453
- [10] Klimchuk, J. A., Patsourakos, S., & Cargill, P. J. 2008, *The Astrophysical Journal*, 682, 1351
- [11] Parker, E. N. 1988, *The Astrophysical Journal*, 330, 474
- [12] Reep, J. W., Bradshaw, S. J., & Klimchuk, J. A. 2013, *The Astrophysical Journal*, 764, 193
- [13] Warren, H. P., Winebarger, A. R., & Brooks, D. H. 2012, *The Astrophysical Journal*, 759, 141
- [14] Winebarger, A. R., Warren, H. P., Schmelz, J. T., et al. 2012, *The Astrophysical Journal Letters*, 746, L17

This work was supported in part by the Big-Data Private-Cloud Research Cyberinfrastructure MRI-award funded by NSF under grant CNS-1338099 and by Rice University.