# Standard Code Library

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## 一切的开始

#### 宏定义

● 需要 C++11

```
#include <bits/stdc++.h>
   using namespace std;
   using LL = long long;
   #define FOR(i, x, y) for (decay < decltype(y) > :: type i = (x), _##i = (y); i < _##i; ++i)
   \#define\ FORD(i,\ x,\ y)\ for\ (decay < decltype(x)>::type\ i\ =\ (x),\ \_\#i\ =\ (y);\ i\ >\ \_\#i;\ --i)
   #ifdef zerol
    #define dbg(x...) do { cout << "\033[32;1m" << \#x << " -> "; err(x); } while (0)
   void err() { cout << "\033[39;0m" << endl; }</pre>
   template<template<typename...> class T, typename t, typename... A>
   void err(T<t> a, A... x) { for (auto v: a) cout << v << ' '; err(x...); }</pre>
   template<typename T, typename... A>
11
   void err(T a, A... x) { cout << a << ' '; err(x...); }</pre>
   #else
13
   #define dbg(...)
   #endif
15
    数据结构
   ST 表
    struct ST{
        int n:
2
        std::vector<array<int,21>> st;
4
        ST(int n):n(n),st(n + 1) {}
        void init(vector<int>& a){
5
            for(int i = 1;i <= n;i ++)st[i][0] = a[i - 1];</pre>
            for(int j = 1;j <= 18;j ++){
                for(int i = 1;i + (1 << j) <= n + 1;i ++){
                     st[i][j] = max(st[i][j - 1], st[i + (1 << (j - 1))][j - 1]);
10
            }
11
        }
12
        int rmq(int l,int r){
            int j = log(r - l + 1)/log(2);
14
            return max(st[l][j],st[r - (1 << j) + 1][j]);</pre>
15
        }
16
   };
17
    线段树
    struct SegTree {
        int l, r;
2
        SegTree *ls, *rs;
3
        ll sum;
        ll plus;
5
        SegTree (const int L, const int R) : l(L), r(R) {
            plus = 0;
            if (L == R) {
                 /*Initial*/
                ls = rs = nullptr;
10
            } else {
                int M = (L + R) >> 1;
12
                 ls = new SegTree (L, M);
13
                rs = new SegTree (M + 1, R);
14
15
                pushup();
            }
17
        void pushup() {
18
            sum = ls->sum + rs->sum;
19
            // std::cerr << "AAA" << l << ' ' << r << ' ' << sum;
20
21
22
        void make_tag(long long w) {
23
            sum += (r - l + 1) * w;
```

```
plus += w;
24
25
         void pushdown() {
26
             if (plus == 0) return;
27
             ls->make_tag(plus);
             rs->make_tag(plus);
29
             plus = 0;
30
31
         void upd(const int L, const int R, const int w) {
32
33
             if ((L > r) || (l > R)) return;
             if ((L <= l) && (r <= R)) {</pre>
34
35
                  make_tag(w);
36
             } else {
                  pushdown();
37
                  ls->upd(L, R, w);
38
                  rs->upd(L, R, w);
39
                  pushup();
             }
41
42
    };
43
    树状数组
    \textbf{template} \hspace{0.1in} < \hspace{-0.1in} \textbf{typename} \hspace{0.1in} \hspace{0.1in} \hspace{0.1in} \hspace{0.1in} \textbf{T} >
2
    struct Fenwick {
        int n;
         std::vector<T> a;
         Fenwick(int n) : n(n), a(n) {}
         void add(int x, T v) {
             for (int i = x + 1; i \le n; i += i \& -i) {
                  a[i - 1] += v;
             }
10
         T sum(int x) {
11
12
             T ans = 0;
             for (int i = x; i > 0; i -= i \& -i) {
13
                 ans += a[i - 1];
14
15
             }
             return ans;
16
17
         T rangeSum(int l, int r) {
18
19
             return sum(r) - sum(l);
20
         int kth(T k) {
21
22
             int x = 0;
             // 先从高位开始取, 如果当前这一位可以取, 那么就考虑下一位是取 1 还是 0
23
             // 到最后找到的就是最大的那个 pos 并且对应的 <=x 的
             for (int i = 1 << std::__lg(n); i; i /= 2) {</pre>
25
                  if (x + i \le n \&\& k \ge a[x + i - 1]) {
26
                      x += i;
27
                      k = a[x - 1];
28
                  }
29
             }
30
31
             return x;
         }//树状数组上倍增本质上是通过倍增来快速找出对应的区间
32
    };
33
    DSU
    struct DSU {
         std::vector<int> f, siz;
2
         DSU(int n) : f(n), siz(n, 1) { std::iota(f.begin(), f.end(), 0); }
3
         int leader(int x) {
             while (x != f[x]) x = f[x] = f[f[x]];
             return x;
         bool same(int x, int y) { return leader(x) == leader(y); }
8
         bool merge(int x, int y) {
             x = leader(x);
10
             y = leader(y);
```

```
if (x == y) return false;
12
            siz[x] += siz[y];
13
             f[y] = x;
14
            return true;
15
        int size(int x) { return siz[leader(x)]; }
17
    };
18
    Splay
    struct Node {
1
      int v, sz, sm;
2
      Node *ch[2], *fa;
      Node(const int V, Node *const f) : v(V), sz(1), sm(1), fa(f) {
        ch[0] = ch[1] = nullptr;
      inline int GetRela(const\ int\ x) { return (v == x) ? -1 : (x > v); }
10
      void pushup() { sm = (ch[0] ? ch[0] -> sm : 0) + (ch[1] ? ch[1] -> sm : 0) + sz; }
11
12
13
      inline void rotate(const int x) {
        auto nrt = ch[x];
14
15
        ch[x] = nrt -> ch[x ^ 1];
        nrt->ch[x ^ 1] = this;
16
        if (ch[x]) ch[x]->fa = this;
17
        nrt->fa = fa; fa = nrt;
        if (nrt->fa) nrt->fa->ch[nrt->fa->GetRela(nrt->v)] = nrt;
19
20
        pushup(); nrt->pushup();
21
22
      void splay(const Node *p) {
23
        while (fa != p) {
24
25
          auto pa = fa->fa;
          if (pa == p) {
26
             fa->rotate(fa->GetRela(v));
27
28
          } else {
             int k1 = fa->GetRela(v), k2 = pa->GetRela(fa->v);
29
30
             if (k1 == k2) {
              pa->rotate(k1);
31
32
               fa->rotate(k1);
            } else {
33
               fa->rotate(k1);
34
35
               fa->rotate(k2);
            }
36
37
          }
        }
38
39
      }
    };
40
    LCT
    struct Node {
      int v, s;
      bool tag;
      Node *ch[2], *fa;
      inline void maketag() {
        tag = !tag;
        std::swap(ch[0], ch[1]);
9
10
      inline void pushup() {
        s = v;
11
        for (auto u : ch) if (u != nullptr) {
          s \wedge = u \rightarrow s;
13
14
        }
15
      inline void pushdown() {
16
17
        if (tag) {
```

```
for (auto u : ch) if (u != nullptr) {
18
19
            u->maketag();
20
          tag = false;
21
22
      }
23
24
      inline int Getson() { return fa->ch[1] == this; }
25
26
      inline bool IsRoot() { return (fa == nullptr) || (fa->ch[Getson()] != this); }
27
28
29
      void rotate(const int x) {
        auto nt = ch[x];
30
        ch[x] = nt->ch[x ^ 1];
31
        nt->ch[x ^ 1] = this;
32
        if (ch[x]) ch[x]->fa = this;
33
34
        nt->fa = fa;
        if (!IsRoot()) { fa->ch[Getson()] = nt; }
35
        fa = nt;
        pushup(); nt->pushup();
37
38
39
      void splay() {
40
        static Node* stk[maxn];
        int top = 0;
42
43
        stk[++top] = this;
        for (auto u = this; !u->IsRoot(); stk[++top] = u = u->fa);
44
        while (top) stk[top--]->pushdown();
45
        while (!IsRoot()) {
          if (fa->IsRoot()) {
47
            fa->rotate(Getson());
48
49
          } else {
            auto pa = fa->fa;
50
51
             int l1 = Getson(), l2 = fa->Getson();
            if (l1 == l2) {
52
53
               pa->rotate(l2);
               fa->rotate(l1);
54
55
            } else {
56
               fa->rotate(l1);
               fa->rotate(l2);
57
58
          }
59
        }
60
61
      }
62
    };
63
    Node *node[maxn], Mem[maxn];
64
    void Cut(const int x, const int y);
    void Link(const int x, const int y);
66
    void Query(const int x, const int y);
67
68
    void Update(const int x, const int y);
69
    void access(Node *u) {
      for (Node *v = nullptr; u; u = (v = u) -> fa) {
71
72
        u->splay();
        u \rightarrow ch[1] = v; u \rightarrow pushup();
73
      }
74
75
    }
76
    void makeroot(Node *const u) {
77
     access(u);
78
79
      u->splay();
80
      u->maketag();
81
82
    void Query(const int x, const int y) {
83
84
      auto u = node[x], v = node[y];
85
      makeroot(u);
      access(v);
86
87
      v->splay();
      qw(v->s, '\n');
88
```

```
}
89
90
    void Link(const int x, const int y) {
91
      auto u = node[x], v = node[y];
92
       makeroot(u);
       access(v); v->splay();
94
       if (u->IsRoot() == false) return;
95
      u->fa = v;
96
97
98
    void Cut(const int x, const int y) {
99
       auto u = node[x], v = node[y];
      makeroot(u); access(v); u->splay();
101
       if ((u->ch[1] != v) || (v->ch[0] != nullptr)) return;
102
      u->ch[1] = v->fa = nullptr;
103
      u->pushup();
104
106
107
    // w[x] \rightarrow y
    void Update(const int x, const int y) {
108
       auto u = node[x];
109
      u->splay();
      u \rightarrow s \land = u \rightarrow v;
111
      u->s ^= (u->v = a[x] = y);
113
    扫描线
    //二维数点
1
    struct Segment{
         int l,r,h,add;
         bool operator <(const Segment a)const{</pre>
             return h < a.h;</pre>
    };
    struct SegTree {
         int l, r;
10
         SegTree *ls, *rs;
         int mn,len;
11
12
         int plus;
         SegTree (const int L, const int R) : l(L), r(R) {
13
14
             plus = 0; len = 0;
             if (L == R) {
15
                  ls = rs = nullptr;
16
17
             } else {
                  int M = (L + R) >> 1;
18
19
                  ls = new SegTree (L, M);
                  rs = new SegTree (M + 1, R);
20
                  pushup();
21
             }
22
23
         void pushup() {
24
             if(plus) len = r - l + 1;
25
26
             else if(l == r)len = 0;
             else len = ls->len + rs->len;
27
28
         void make_tag(int w) {
29
             plus += w;
30
31
         void pushdown() {
32
33
             if (plus == 0) return;
             ls->make_tag(plus);
34
35
             rs->make_tag(plus);
36
             plus = 0;
37
         void update(const int L, const int R, const int w) {
38
             if ((L > r) || (l > R)) {
39
40
                  return;
41
             if ((L <= l) && (r <= R)) {</pre>
42
                  make_tag(w);
```

```
pushup();
44
45
                  return ;
             } else {
46
                  ls->update(L, R, w);
47
                  rs->update(L, R, w);
                  pushup();
49
50
         }
51
    };
52
    //矩形面积并
53
    #include<bits/stdc++.h>
54
55
56
    using namespace std;
     typedef long long ll;
57
     const double eps = 1e-8;
58
     const int maxn = 2e5 + 7;
59
     std::vector<int> x;
     struct Segment{
61
         int l,r,h,add;
62
         bool operator <(const Segment a)const{</pre>
63
             return h < a.h;</pre>
64
65
    };
66
     struct SegTree {
         int l, r;
68
69
         SegTree *ls, *rs;
70
         int mn,len;
         int plus;
71
72
         SegTree (const int L, const int R) : l(L), r(R) {
             plus = 0;len = 0;
73
              if (L == R) {
74
                  ls = rs = nullptr;
75
76
             } else {
77
                  int M = (L + R) >> 1;
                  ls = new SegTree (L, M);
78
79
                  rs = new SegTree (M + 1, R);
                  pushup();
80
             }
81
82
         void pushup() {
83
84
             if(plus) len = x[r] - x[l - 1];
             else if(l == r)len = 0;
85
             else len = ls->len + rs->len;
86
87
         }
         void make_tag(int w) {
88
89
             plus += w;
90
         void pushdown() {
             if (plus == 0) return;
92
93
             ls->make_tag(plus);
             rs->make_tag(plus);
94
             plus = 0;
95
         void update(const int L, const int R, const int w) {
97
98
             if ((L >= x[r]) || (x[l - 1] >= R)) {
99
                  return;
100
             if ((L \leq x[l - 1]) && (x[r] \leq R)) {
101
102
                  make_tag(w);
                  pushup();
103
104
                  return ;
             } else {
105
106
                  //pushdown();
                  ls->update(L, R, w);
107
108
                  rs->update(L, R, w);
                  pushup();
109
110
             }
         }
111
    };
112
113
     int main(){
         ios::sync_with_stdio(false);
114
```

```
cin.tie(0);
115
116
117
         vector<Segment> s;
         int n;
118
         cin >> n;
119
         for(int i = 0;i < n;i ++){</pre>
120
121
              int xa,ya,xb,yb;
             cin >> xa >> ya >> xb >> yb;
122
             x.push_back(xa);
123
              x.push_back(xb);
124
             s.push_back({xa,xb,ya,1});
125
126
              s.push_back({xa,xb,yb,-1});
         }
127
         sort(s.begin(),s.end());
128
129
         sort(x.begin(),x.end());
         x.erase(unique(x.begin(),x.end()),x.end());
130
131
         int N = x.size();
         SegTree Seg(1,N - 1);
132
         ll ans = 0;
133
         if(s.size()){
134
              Seg.update(s[0].l,s[0].r,s[0].add);
135
              for(int i = 1;i < s.size();i ++){</pre>
136
                  ans += 1ll * Seg.len * (s[i].h - s[i - 1].h);
137
                  Seg.update(s[i].l,s[i].r,s[i].add);
138
              }
139
         }
140
         cout << ans << "\n";
141
         return 0;
142
    }
143
```

#### Seg beats

本质上是维护了两棵线段树, A 树维护区间内最大值产生的贡献, B 树维护剩下树的贡献。注意 A 树某节点的孩子不一定全部能贡献到该节点, 因为孩子的最大值不一定是父亲的最大值。所以要注意下传标记时, A 树的孩子下传的可能是 B 的标记。

beats 的部分是,每次让序列里每个数对另一个数 V 取 min,则直接暴力递归到 inRange 且 B 的最大值小于 V 的那些节点上,转化成对 A 那个节点的区间加法(加上  $V-val_A$ )即可。这么做的均摊复杂度是  $O(\log n)$ 。

做区间历史最大值的方法是,维护两个标记  $x,y,\ x$  是真正的加标记,y 是 x 在上次下传结束并清零后的历史最大值。下传时注意先下传 y 再下传 x。实现历史最值是平凡的,不需要 beats。beats 解决的仅是取 min 的操作。

下面五个操作分别是: 区间加, 区间对 k 取 min, 区间求和, 区间最大值, 区间历史最大值。

```
#include <array>
    #include <iostream>
    #include <algorithm>
    typedef long long int ll;
    const int maxn = 500005;
    ll a[maxn];
10
    const ll inf = 0x3f3f3f3f3f3f3f3f3f1l;
11
    struct Node {
13
14
      Node *ls, *rs;
15
      int l, r, maxCnt;
      ll v, add, maxAdd, sum, maxV, maxHistory;
16
17
      Node(const int L, const int R) :
18
          ls(nullptr), rs(nullptr), l(L), r(R), maxCnt(0),
19
20
          v(\theta), add(\theta), maxAdd(\theta), sum(\theta), maxV(-inf), maxHistory(-inf) {}
21
22
      inline bool inRange(const int L, const int R) {
        return L <= l && r <= R;
23
24
      inline bool outRange(const int L, const int R) {
25
        return 1 > R || L > r;
26
27
```

```
28
29
      void addVal(const ll t, int len) {
30
        add += t;
        sum += len * t;
31
        maxV += t;
32
33
34
      void makeAdd(const ll t, int len) {
35
        addVal(t, len);
36
37
        maxHistory = std::max(maxHistory, maxV);
        maxAdd = std::max(maxAdd, add);
38
39
40
    };
41
    void pushup(Node *x, Node *y) {
42
      y->maxV = std::max(y->ls->maxV, y->rs->maxV);
43
44
      y->sum = y->ls->sum + y->rs->sum;
      y->maxHistory = std::max({y->maxHistory, y->ls->maxHistory, y->rs->maxHistory});
45
      if (x->ls->maxV != x->rs->maxV) {
        bool flag = x->ls->maxV < x->rs->maxV;
47
        if (flag) std::swap(x->ls, x->rs);
48
49
        x->maxV = x->ls->maxV;
        x->maxCnt = x->ls->maxCnt;
50
       y->maxV = std::max(y->maxV, x->rs->maxV);
        y->sum += x->rs->sum;
52
53
        x->sum = x->ls->sum;
54
        if (flag) std::swap(x->ls, x->rs);
      } else {
55
        x->maxCnt = x->ls->maxCnt + x->rs->maxCnt;
        x \rightarrow sum = x \rightarrow ls \rightarrow sum + x \rightarrow rs \rightarrow sum:
57
        x->maxV = x->ls->maxV;
58
59
      x-maxHistory = std::max(\{x-ls-\}maxHistory, x-rs-\}maxHistory, x-maxHistory, y-maxHistory);
60
61
62
    void New(Node *&u1, Node *&u2, int L, int R) {
63
      u1 = new Node(L, R);
64
      u2 = new Node(L, R);
65
      if (L == R) {
        u1->v = u1->sum = u1->maxV = u1->maxHistory = a[L];
67
68
        u1->maxCnt = 1;
      } else {
69
        int M = (L + R) >> 1;
70
71
        New(u1->ls, u2->ls, L, M);
        New(u1->rs, u2->rs, M + 1, R);
72
73
        pushup(u1, u2);
      }
74
75
    }
76
    void pushdown(Node *x, Node *y) {
77
      ll val = std::max(x->ls->maxV, x->rs->maxV);
      std::array<Node*, 2> aim({y, x});
79
      Node *curl = aim[x->ls->maxV == val], *curr = aim[x->rs->maxV == val];
      x->ls->maxAdd = std::max(x->ls->maxAdd, x->ls->add + curl->maxAdd);
81
      x->ls->maxHistory = std::max(x->ls->maxHistory, x->ls->maxV + curl->maxAdd);
82
      x->ls->addVal(curl->add, x->ls->maxCnt);
83
      x->rs->maxAdd = std::max(x->rs->maxAdd, x->rs->add + curr->maxAdd);
84
      x->rs->maxHistory = std::max(x->rs->maxHistory, x->rs->maxV + curr->maxAdd);
86
      x->rs->addVal(curr->add, x->rs->maxCnt);
      y->ls->maxAdd = std::max(y->ls->maxAdd, y->ls->add + y->maxAdd);
87
      y->rs->maxAdd = std::max(y->rs->maxAdd, y->rs->add + y->maxAdd);
88
      y->ls->addVal(y->add, x->ls->r - x->ls->l + 1 - x->ls->maxCnt);
      y->rs->addVal(y->add, x->rs->r - x->rs->l + 1 - x->rs->maxCnt);
      x->add = y->add = x->maxAdd = y->maxAdd = 0;
91
92
93
94
    void addV(Node *x, Node *y, int L, int R, ll k) {
95
      if (x->inRange(L, R)) {
        x->makeAdd(k, x->maxCnt);
96
        y->makeAdd(k, x->r - x->l + 1 - x->maxCnt);
97
      } else if (!x->outRange(L, R)) {
```

```
pushdown(x, y);
 99
                 addV(x\rightarrow ls, y\rightarrow ls, L, R, k);
100
                 addV(x\rightarrow rs, y\rightarrow rs, L, R, k);
101
                 pushup(x, y);
102
103
        }
104
105
         std::array<ll, 3> qry(Node *x, Node *y, const int L, const int R) {
106
             if (x-) in Range (L, R)) return \{x-) sum +y-) sum *((x-) r-x-) l+1) l=x-) max l=x-) max l=x-1 max l=x-1
107
108
             else if (x->outRange(L, R)) return {0, -inf, -inf};
             else {
109
110
                 pushdown(x, y);
111
                 auto A = qry(x->ls, y->ls, L, R), B = qry(x->rs, y->rs, L, R);
                 return {A[0] + B[0], std::max(A[1], B[1]), std::max(A[2], B[2])};
112
113
             }
        }
114
115
         void minV(Node *x, Node *y, const int L, const int R, int k) {
116
117
             if (x->maxV <= k) return;</pre>
             if (x-\sin Range(L, R) \&\& y-\cos V < k) {
118
                 ll delta = k - x->maxV;
119
120
                 x->makeAdd(delta, x->maxCnt);
             } else if (!x->outRange(L, R)) {
121
                 pushdown(x, y);
122
                 minV(x->ls, y->ls, L, R, k);
123
                 minV(x->rs, y->rs, L, R, k);
124
125
                 pushup(x, y);
             }
126
127
        }
128
         int main() {
129
             std::ios::sync_with_stdio(false);
130
             std::cin.tie(nullptr);
131
132
             int n, m;
             std::cin >> n >> m;
133
             for (int i = 1; i <= n; ++i) std::cin >> a[i];
134
             Node *rot1, *rot2;
135
             New(rot1, rot2, 1, n);
136
137
             for (int op, l, r; m; --m) {
                 std::cin >> op >> l >> r;
138
139
                 if (op == 1) {
                     std::cin >> op;
140
                     addV(rot1, rot2, l, r, op);
141
142
                 } else if (op == 2) {
                     std::cin >> op;
143
144
                     minV(rot1, rot2, l, r, op);
                 } else {
145
146
                     std::cout << qry(rot1, rot2, l, r)[op - 3] << '\n';
147
                 }
             }
148
149
        }
         珂朵莉树
         auto getPos(int pos) {
             return --s.upper_bound({pos + 1, 0, 0});
 2
 3
 4
         void split(int pos) {
             auto it = getPos(pos);
             auto [l, r, v] = *it;
             s.erase(it);
             if (pos > l) s.insert({l, pos - 1, v});
             s.insert({pos, r, v});
 11
 12
         void add(int l, int r, int v) {
 13
             split(l); split(r + 1);
 14
 15
             for (auto x = getPos(l), y = getPos(r + 1); x != y; ++x) {
                x->v += v;
 16
             }
 17
```

```
}
18
19
    void upd(int l, int r, int v) {
20
      split(l); split(r + 1);
21
      s.erase(getPos(l), getPos(r + 1));
      s.insert({l, r, v});
23
24
    getPos(pos): 找到 pos 所在的迭代器
    split(pos): 把 pos 所在的迭代器区间 [l, r] 分成 [l, pos - 1] 和 [pos, r] 两个
    李超树
    插入线段 kx + b 求某点最值
    constexpr long long INF = 1'000'000'000'000'000'000;
    constexpr int C = 100'000;
    struct Line {
3
        int k:
        long long b;
5
        Line(int k, long long b) : k(k), b(b) {}
    long long f(const Line &line, int x) {
        return 1LL * line.k * x + line.b;
    }
10
11
    struct Node {
        Node *lc, *rc;
12
        Line line;
13
        Node(const Line &line) : lc(nullptr), rc(nullptr), line(line) {}
14
15
    };
    void modify(Node *&p, int l, int r, Line line) {
16
        if (p == nullptr) {
17
18
            p = new Node(line);
            return;
19
20
21
        int m = (l + r) / 2;
        bool le = f(p -> line, l) < f(line, l);</pre>
22
23
        bool mi = f(p -> line, m) < f(line, m);</pre>
        if (!mi)
24
25
            std::swap(p -> line, line);
        if (r - l == 1)
26
            return;
27
        if (le != mi) {
            modify(p -> lc, l, m, line);
29
        } else {
            modify(p -> rc, m, r, line);
31
32
33
    Node *merge(Node *p, Node *q, int l, int r) {
34
35
        if (p == nullptr)
            return q;
36
        if (q == nullptr)
37
38
            return p;
39
        int m = (l + r) / 2;
40
        p \rightarrow lc = merge(p \rightarrow lc, q \rightarrow lc, l, m);
        p -> rc = merge(p -> rc, q -> rc, m, r);
41
42
        modify(p, l, r, q -> line);
        return p;
43
44
    }
45
    long long query(Node *p, int l, int r, int x) {
        if (p == nullptr)
46
47
            return INF;
        long long ans = f(p \rightarrow line, x);
48
        if (r - l == 1)
49
50
            return ans;
        int m = (l + r) / 2;
51
52
        if (x < m) {
            return std::min(ans, query(p -> lc, l, m, x));
53
        } else {
54
55
            return std::min(ans, query(p -> rc, m, r, x));
        }
```

57 }

```
动态维护凸壳
```

```
1
    * Author: Simon Lindholm
    * Date: 2017-04-20
     * License: CC0
    * Source: own work
     * Description: Container where you can add lines of the form kx+m, and query maximum values at points x.
     * Useful for dynamic programming.
     * Time: O(\log N)
     * Status: tested
10
11
12
    struct Line {
     mutable ll k, m, p;
13
14
      bool operator<(const Line &o) const { return k < o.k; }</pre>
     bool operator<(ll x) const { return p < x; }</pre>
15
16
17
    struct LineContainer: multiset<Line, less<>> {
18
      const ll inf = LLONG_MAX;
      ll val_offset = 0;
20
21
      void offset(ll x) {
       val_offset += x;//整体加
22
23
24
      ll div(ll a, ll b) {
       return a / b - ((a^b) < 0 && a%b);
25
26
      bool isect(iterator x, iterator y) {
27
        if (y == end()) {
28
         x->p = inf;
29
          return 0;
30
31
        if (x->k == y->k) {
32
         x->p = (x->m > y->m)? inf: -inf;
33
        } else {
34
35
         x->p = div(y->m - x->m, x->k - y->k);
36
        return x->p >= y->p;
37
38
      void add(ll k, ll m) {
39
        auto z = insert(\{k, m - val\_offset, 0\}), y = z++, x = y;//这里加減看情况
40
41
        while (isect(y, z)) z = erase(z);
        if (x := begin() \&\& isect(--x, y)) isect(x, y = erase(y));
42
43
        while ((y = x) != begin() \&\& (--x)->p >= y->p) isect(x, erase(y));
44
      ll query(ll x) {
45
        assert(!empty());
46
        auto l = *lower_bound(x);
47
48
        return l.k * x + l.m + val_offset;
49
      }
50
    };
51
    LineContainer* merge(LineContainer *S, LineContainer *T) {
52
53
      if (S->size() > T->size())
54
        swap(S, T);
55
      for (auto l: *S) {
       T->add(l.k, l.m + S->val_offset);
56
57
58
      return T;
59
   }
    TODO
```

线段树合并和分裂

#### 图论

#### LCA

```
● 倍增
    void dfs(int u, int fa) {
        pa[u][0] = fa; dep[u] = dep[fa] + 1;
2
        FOR (i, 1, SP) pa[u][i] = pa[pa[u][i - 1]][i - 1];
        for (int& v: G[u]) {
            if (v == fa) continue;
            dfs(v, u);
   }
    int lca(int u, int v) {
10
        if (dep[u] < dep[v]) swap(u, v);</pre>
11
        int t = dep[u] - dep[v];
12
        FOR (i, 0, SP) if (t & (1 << i)) u = pa[u][i];
13
        FORD (i, SP - 1, -1) {
            int uu = pa[u][i], vv = pa[v][i];
15
            if (uu != vv) { u = uu; v = vv; }
16
17
        return u == v ? u : pa[u][0];
18
```

## 计算几何

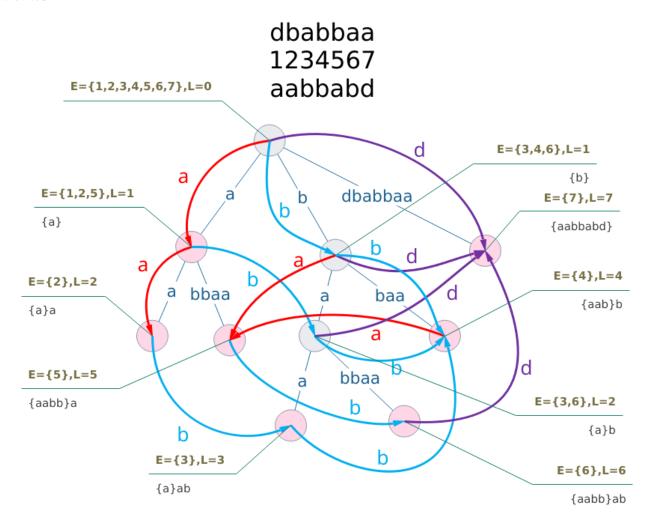
#### 二维几何: 点与向量

```
#define y1 yy1
1
    #define nxt(i) ((i + 1) % s.size())
    typedef double LD;
    const LD PI = 3.14159265358979323846;
    const LD eps = 1E-10;
    int sgn(LD x) { return fabs(x) < eps ? 0 : (x > 0 ? 1 : -1); }
    struct L;
    struct P;
    typedef P V;
10
    struct P {
        LD x, y;
11
        explicit P(LD x = 0, LD y = 0): x(x), y(y) {}
12
        explicit P(const L& l);
13
14
15
    struct L {
        Ps, t;
16
17
        L() {}
        L(P s, P t): s(s), t(t) {}
18
19
20
    P operator + (const P& a, const P& b) { return P(a.x + b.x, a.y + b.y); }
21
    P operator - (const P& a, const P& b) { return P(a.x - b.x, a.y - b.y); }
22
    P operator * (const P& a, LD k) { return P(a.x * k, a.y * k); }
23
    P operator / (const P& a, LD k) { return P(a.x / k, a.y / k); }
    inline bool operator < (const P& a, const P& b) {</pre>
25
        return sgn(a.x - b.x) < 0 \mid \mid (sgn(a.x - b.x) == 0 && sgn(a.y - b.y) < 0);
26
27
    bool operator == (const P& a, const P& b) { return !sgn(a.x - b.x) && !sgn(a.y - b.y); }
28
    P::P(const L& l) { *this = l.t - l.s; }
    ostream &operator << (ostream &os, const P &p) {
30
        return (os << "(" << p.x << "," << p.y << ")");
31
32
    istream &operator >> (istream &is, P &p) {
33
34
        return (is >> p.x >> p.y);
    }
35
    LD dist(const P& p) { return sqrt(p.x * p.x + p.y * p.y); }
37
    LD dot(const V& a, const V& b) { return a.x * b.x + a.y * b.y; }
    LD det(const V& a, const V& b) { return a.x * b.y - a.y * b.x; }
```

```
40 LD cross(const P& s, const P& t, const P& o = P()) { return det(s - o, t - o); }
41 // -------
```

## 字符串

### 后缀自动机



## 杂项

#### STL

copy

```
template <class InputIterator, class OutputIterator>
OutputIterator copy (InputIterator first, InputIterator last, OutputIterator result);
```