



## CHAPTER 4

# LISTS

# 鏈結表示法



- 如果常常需要在串列中做加入和刪除的動作，那麼使用陣列來表示串列就不合適
- 串列元素可以用任意的順序存放在記憶體內
- 使用一種清楚明白的資訊(稱為鏈結)從一個元素走到(追蹤到)下一個元素



# Introduction

- Array

- successive items locate a fixed distance

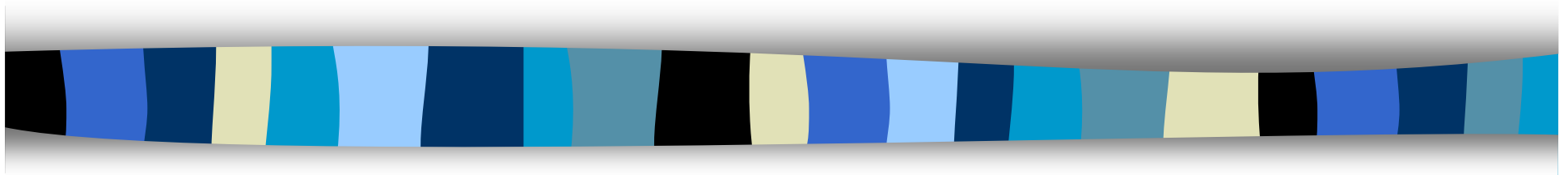
- disadvantage

- data movements during insertion and deletion
  - waste space in storing n ordered lists of varying size

- possible solution

- linked list

指標



Pointer



# 基本觀念

- 指標是一個用來指示資料存在於記憶體中的位址標示器
- 在指標的運用中，我們可瞭解到資料與位址間的關係，進而對記憶體配置有很大的幫助。
- 在C語言中,若某變數所含的是一個記憶體位址，此變數稱為指標變數。

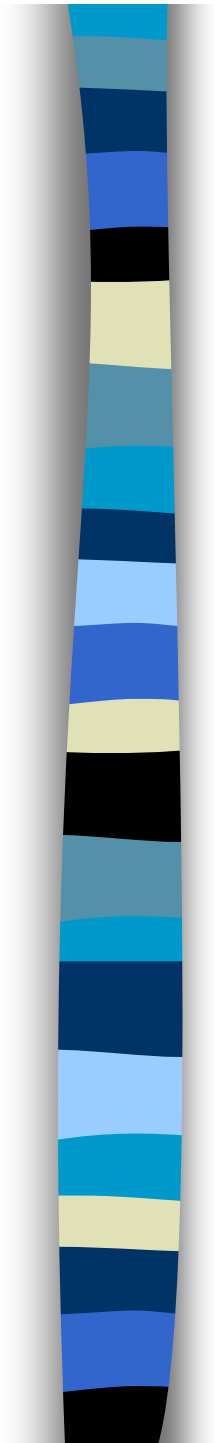


# 指標變數的宣告

變數資料型態\*變數名稱;

Int \*ptr;

- ptr為指標變數
- ptr代表一個位址



**p  
tr**  
為  
指  
標  
變  
數

→變數ptr→

0800H

0802H

....

1010H

1010H
...
16
記憶體

←\*ptr



# 注意事項

- ptr為指標變數，ptr代表一個位址
- \*ptr代表此位址內的資料
- ptr所指向此位址之變數型態為整數 (int)
- 指標變數宣告的關鍵字為"\*"；指標變數的資料型態也分為整數 (int)、浮點數 (float)、字元 (char)
- “&”為另一重要符號，“&”為一個特殊運算子，目的為傳回運算元之位址
- scanf()中之所有引數變數一定要加上“&”符號.



# 動態記憶體配置-說明

- 動態記憶體配置不同於陣列的靜態記憶體配置

- 靜態記憶體配置是在編譯階段就配置記憶體空間，
- 動態記憶體配置是等到執行階段，才向作業系統要求配置所需的記憶體空間，可以讓程式設計者靈活運用程式所需的記憶體空間。

- 在C語言<stdlib.h>標頭檔的標準函式庫提供兩個函數：`malloc()`和`free()`，可以配置和釋放程式所需的記憶體空間。

# 動態記憶體配置-malloc()

## malloc()函數：配置記憶體空間

- C語言的程式碼可以呼叫malloc()函數向作業系統取得一塊可用的記憶體空間，函數的語法，如下所示：

fp = (資料型態\*) malloc(sizeof(資料型態));

- 上述語法因為函數傳回void通用型指標，所以需要加上型態迫換，將函數傳回的指標轉換成指定資料型態的指標，sizeof運算子可以計算指定資料型態的大小。例如：配置一個浮點數變數的記憶體空間，如下所示：

fp = (float \*) malloc(sizeof(float));

struct test \*score;

score=(struct test \*) malloc(num\*sizeof(struct test));

# 動態記憶體配置-free()

free()函數：釋放配置的記憶體空間

- free()函數可以釋放malloc()函數配置的記憶體空間，例如：指標fp是一個指向malloc()函數傳回的浮點數記憶體空間的指標，呼叫free()函數釋放這塊記憶體，如下所示：  
free(fp);
- 上述程式碼的指標fp可以是float浮點數指標，也可以是malloc()函數傳回的其它資料型態指標、陣列或結構指標。



### 4.1.1 Pointer Can Be Dangerous

pointer

```
int i, *pi, *pf;
```

```
pi = &i;          i=10 or *pi=10
```

```
pi= malloc(size of(int));
```

```
/* assign to pi a pointer to int */
```

```
pf=(float *) pi;
```

```
/* casts an int pointer to a float pointer */
```



## 4.1.2 Using Dynamically Allocated Storage

```
int i, *pi;  
float f, *pf;  
pi = (int *) malloc(sizeof(int));  
pf = (float *) malloc (sizeof(float));  
*pi =1024;  
*pf =3.14;  
printf("an integer = %d, a float = %f\n", *pi, *pf);  
free(pi);  
free(pf);
```

request memory

return memory

**\*Program4.1:Allocation and deallocation of pointers (p.138)**



# 鏈結串列的定義

- 鏈結串列(Linkedlist)也是常用的資料結構裡面的元素稱為節點(node)
- 有兩個節點比較特別，就是串列的頭(head)與尾(tail)
- 每個節點除了含有一些成員屬性之外，還包含了一個指向下一節點的鏈結(link)。

- 有次序排列之資料稱為串列(List)，如一年四季，數字0~9
- 陣列、堆疊及佇列皆屬於串列(List)的結構
- 鏈結串列(Linked List)的頭與尾決定於串列中的節點所在的位置，對於串列的處理，都是從頭節點開始，然後一一地找到其他的節點。

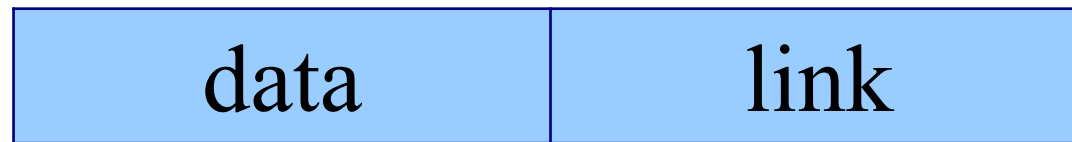
# 鏈結串列特點

- 由節點所串成(利用鏈結)的串列稱之。
- 鏈結串列是一種有順序的串列，可以用陣列，也可以用結構。
- 鏈結串列各元素在記憶體之位置是不連續、隨機(Random)的。它是由動態記憶體分配節點(Node)串接而成。

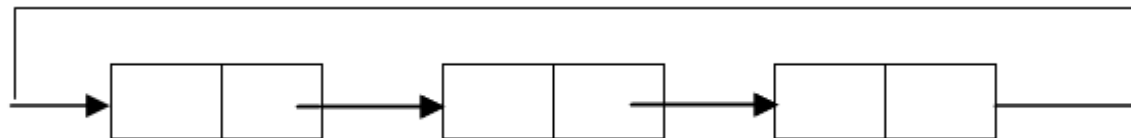


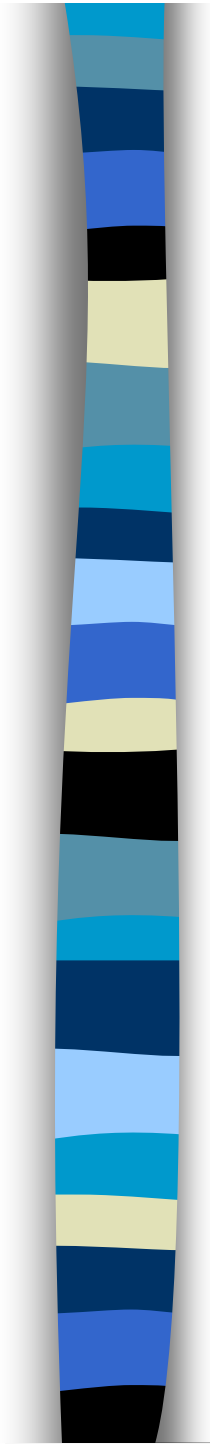
# 鏈結串列的種類

- 單向鏈結：它的節點包含資料（data）及鏈結（link）兩個欄位



- 環狀鏈結 = > 一個鏈結串列之最後一個節點指向鏈結串列之最前端。



- 
- 雙向鏈結 = > 節點至少包含資料及左右兩個結鏈。



# 陣列與鏈結串列的比較

陣列製作串列	
優點	缺點
1.易製作，宣告即可 2.亦存取資料，利用所以對應	1.刪除、插入及易動資料會造成資料移動頻繁，減少系統效率 2.宣告記憶體空間、造成不必要之浪費

鏈結製作串列	
優點	缺點
補足陣列串列之缺點	缺乏陣列串列之優點

# 動態配置之鍵結串列

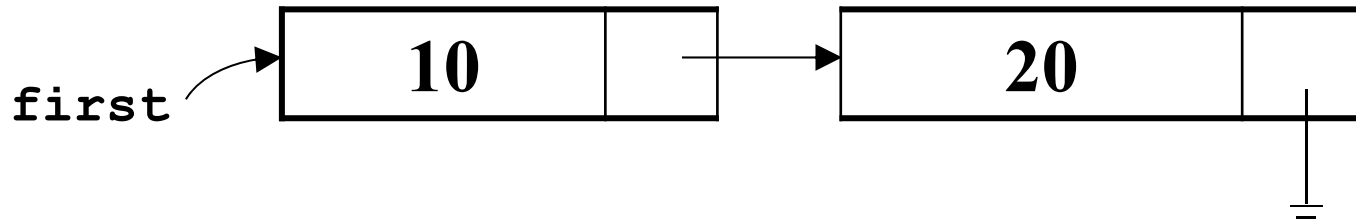
- 鍵結串列有順序的關係，包括至少二種類型的資訊：
  - 內含的元素。
  - 下一項元素所在位置的資訊。
- 鍵結是由指標或位址來構成，比起陣列link的使用更具一般性。

## 程式： 結構的宣告

```
1 define maxchar 20
2 struct FruitType
3 { char name[maxchar];
4   struct FruitType *link;
5 };
6 struct FruitType *head;
```

- 在程式第2~5行中我們宣告了新的資料型態 **struct FruitType**，它包括了一組長度為20的字元 **name**，和指向 **struct FruitType** 此型態的指標（位址） **\*link**，它成為鏈結串列的基本型態，可稱之為節點。

# 範例



## 程式

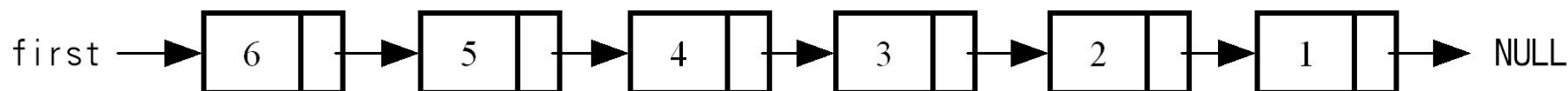
```
1 struct node
2 {   int data;
3     struct node *next;
4 };
5 struct node *first;
6 void construct()
7 {   first = (node *) malloc (sizeof(node));    //
8     first->data = 10;
9     first->next = (node *)  malloc (sizeof(node));
10    first->next->data = 20;
11    first->next->next = NULL;
12 }
```

## 4-2 單向鏈結串列

- 建立和走訪單向鏈結串列
- 刪除單向鏈結串列的節點
- 加入單向鏈結串列的節點

# 單向鏈結串列-說明

- 單向鏈結串列是最簡單的一種鏈結串列，因為節點指標都是指向同一個方向，依序從前一個節點指向下一個節點，然後最後1個節點指向NULL，所以稱為單向鏈結串列，如下圖所示：





# 單向鏈結串列-標頭檔

```
01: /* 程式範例: Ch4-3.h */
02: struct Node {          /* Node節點結構 */
03:     int data;           /* 結構變數宣告 */
04:     struct Node *next; /* 指向下一個節點 */
05: };
06: typedef struct Node LNode; /* 串列節點的新型態 */
07: typedef LNode *List;      /* 串列的新型態 */
08: List first = NULL;       /* 串列的開頭指標 */
09: /* 抽象資料型態的操作函數宣告 */
10: extern void creatList(int len, int *array);
11: extern int isListEmpty();
12: extern void printList();
13: extern List searchNode(int d);
14: extern int deleteNode(List ptr);
15: extern void insertNode(List ptr, int d);
```

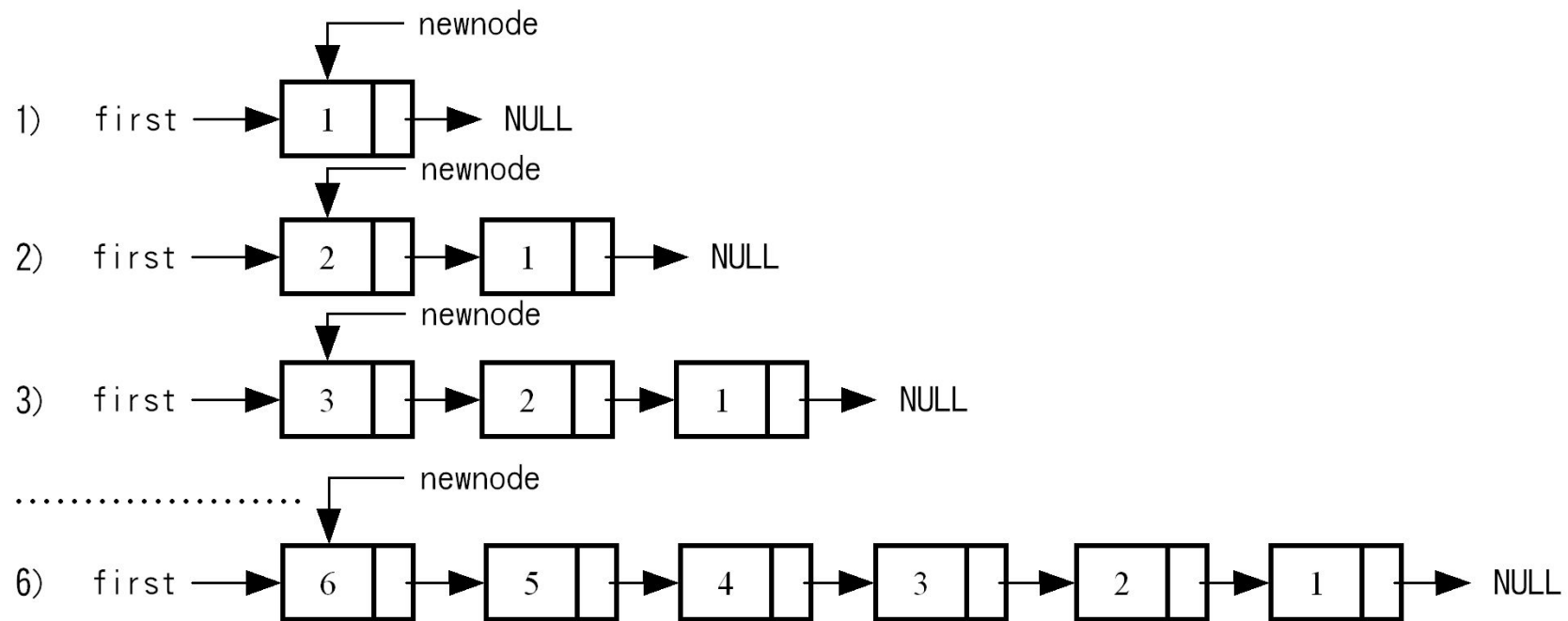
# 建立和走訪單向鏈結串列-建立(說明)

## 建立單向鏈結串列

- 在**createList()**函數是使用**for**迴圈將取得的陣列值建成立串列節點，每執行一次迴圈，就在串列開頭插入一個新節點，如下所示：

```
for ( i = 0; i < len; i++ ) {  
    newnode = (List) malloc(sizeof(LNode));  
    newnode->data = array[i];  
    newnode->next = first;  
    first = newnode;  
}
```

# 建立和走訪單向鏈結串列-建立 (圖例)



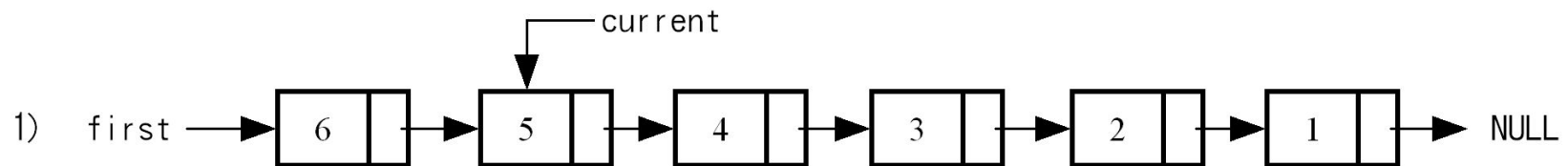
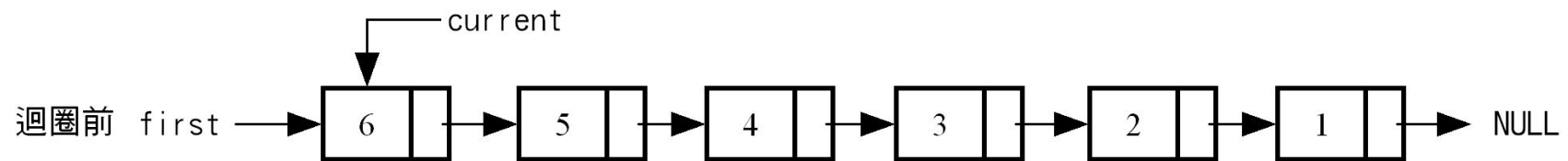
# 建立和走訪單向鏈結串列-走訪 (說明)

## 單向鏈結串列的走訪

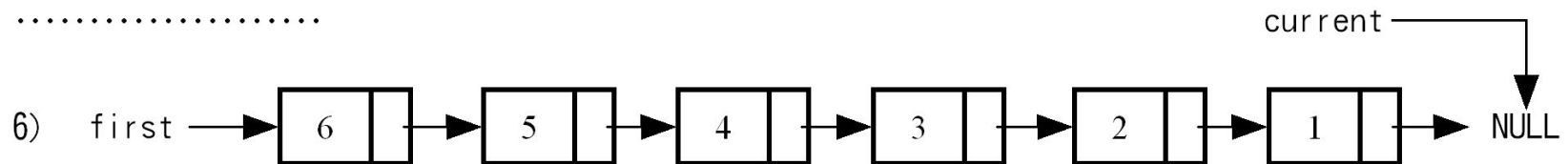
- 單向鏈結串列的「走訪」( **Traverse** ) 和一維陣列的走訪十分相似，其差異在於陣列是遞增索引值來走訪陣列，串列是使用指標運算來處理節點的走訪，如下所示：

```
List current = first;  
while ( current != NULL ) {  
    .....  
    current = current->next;  
}
```

# 建立和走訪單向鏈結串列-走訪 (圖例)

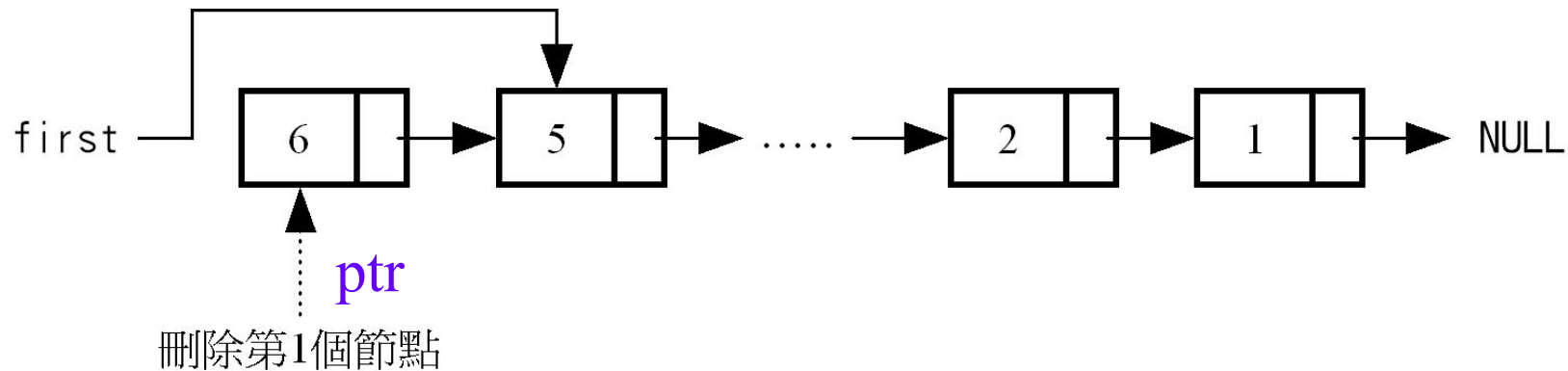


.....



# 刪除單向鏈結串列的節點-情況1

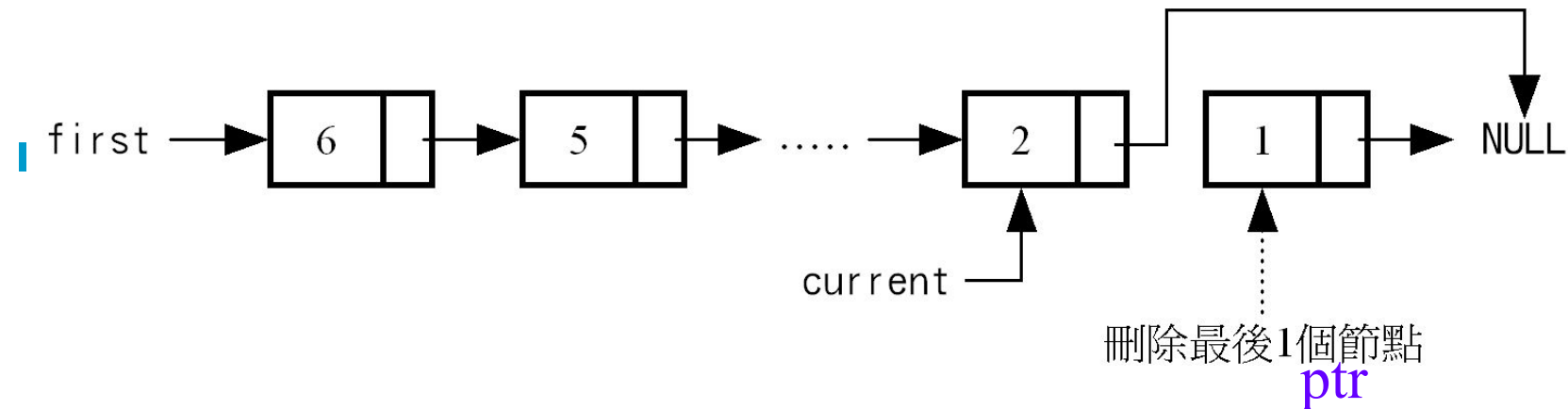
- 刪除串列的第1個節點：只需將串列指標 `first` 指向下一個節點，如下圖所示：



```
ptr = first;  
first = first->next;  
free(ptr);
```

## 刪除單向鏈結串列的節點-情況2

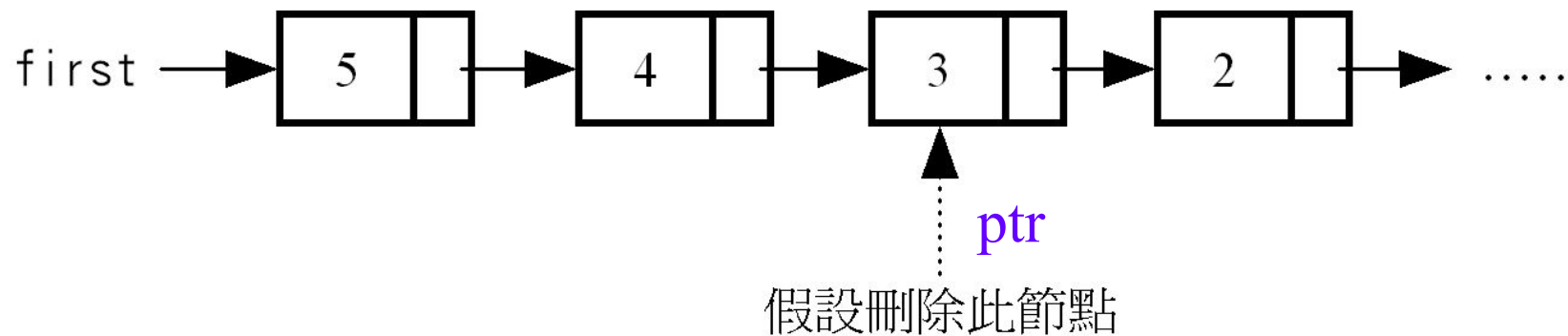
- 刪除串列的最後1個節點：只需將最後1個節點ptr的前一個節點指標指向NULL，如下圖所示：



```
while (current->next!=ptr)
    current = current->next;
free(ptr);
current->next = NULL;
```

# 刪除單向鏈結串列的節點-情況3(1)

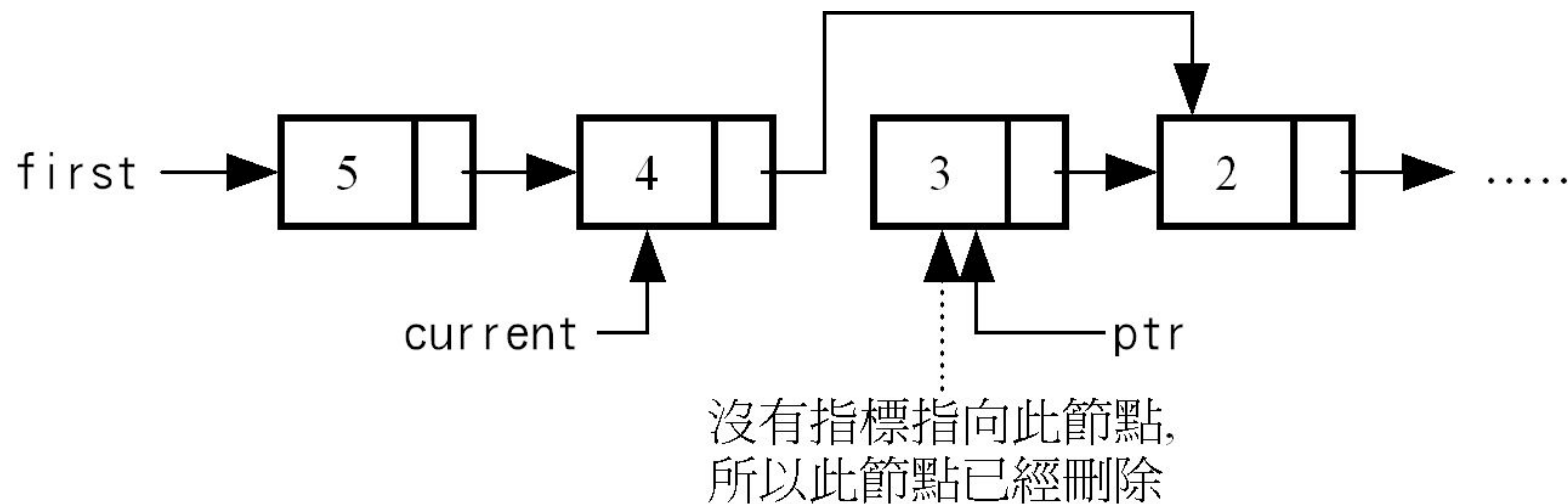
- 刪除串列的中間節點：將刪除節點前一個節點的next指標，指向刪除節點下一個節點，例如：刪除節點3，如下圖所示：





## 刪除單向鏈結串列的節點-情況3(2)

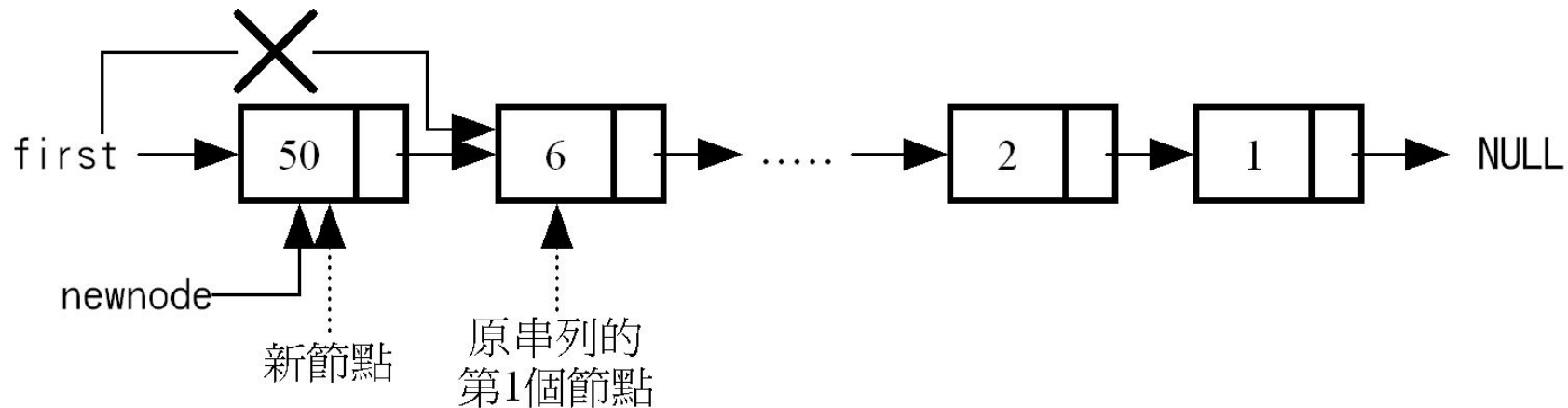
- 在執行刪除節點3操作後的串列圖形，如下所示：



```
while (current->next!=ptr)
    current = current->next;
current->next = ptr->next;
free(ptr);
```

# 加入單向鏈結串列的節點-情況1

- 將節點插入串列第1個節點之前：只需將新節點 `newnode` 的指標指向串列的第1個節點 `first`，新節點就成為串列的第1個節點，如下圖所示：

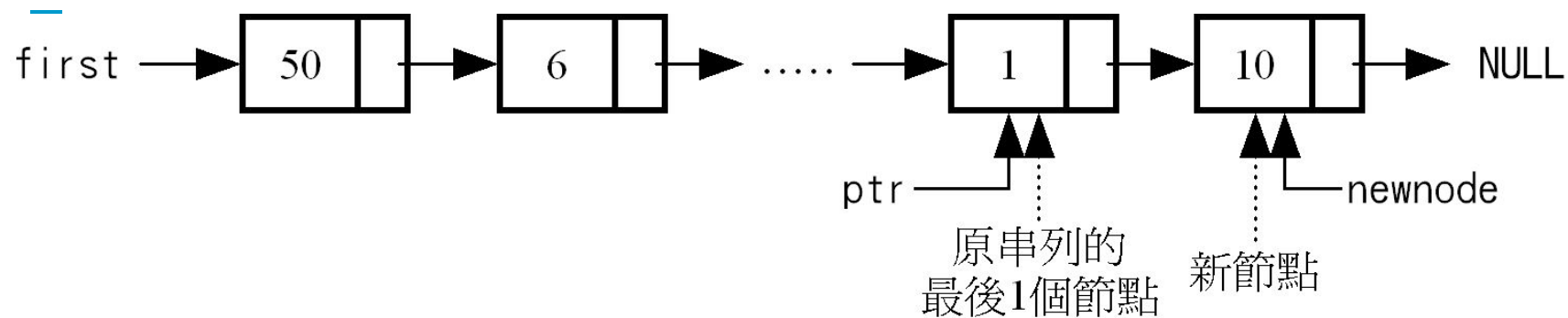


`newnode->next = first;`

`first = newnode;`

## 加入單向鏈結串列的節點-情況2

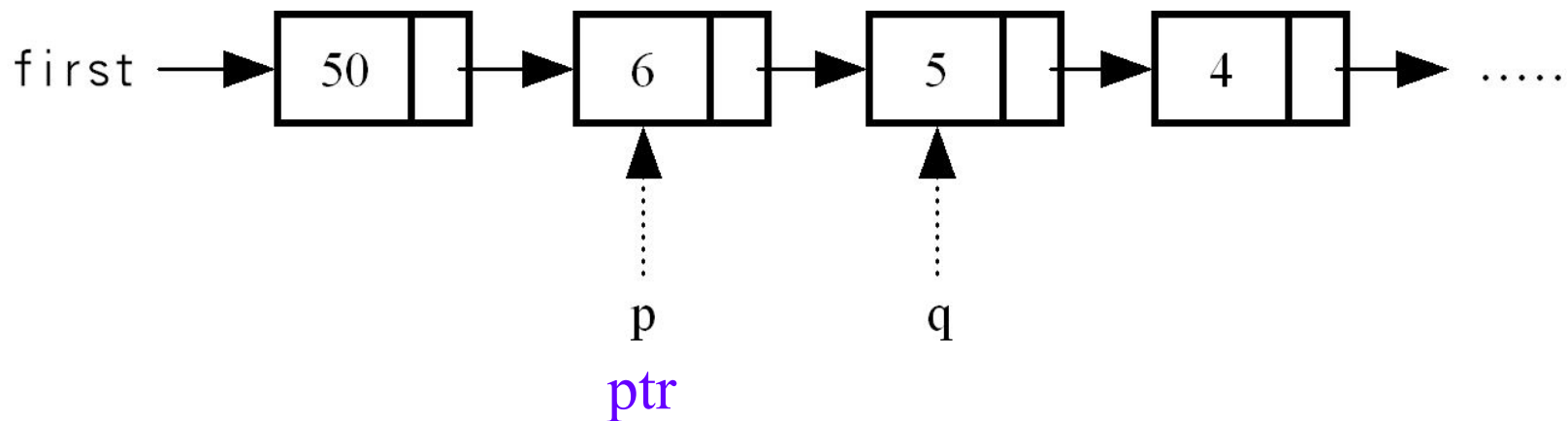
- 將節點插在串列的最後1個節點之後：只需將原來串列最後1個節點的指標指向新節點newnode，新節點指向NULL，如下圖所示：



```
ptr->next = newnode;  
newnode->next = NULL;
```

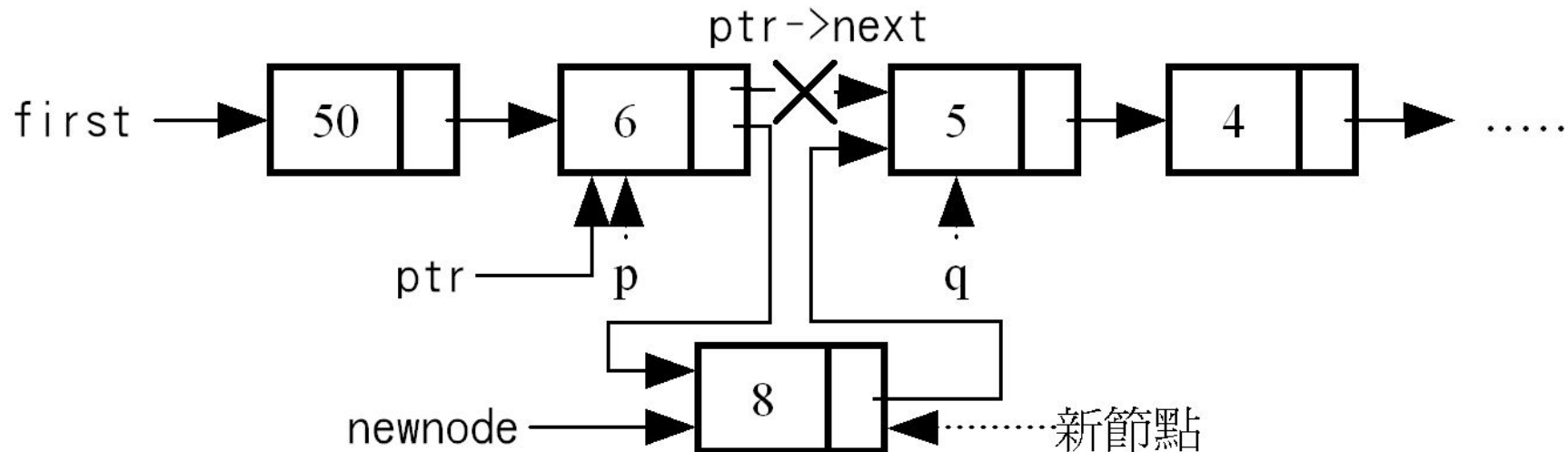
## 加入單向鏈結串列的節點-情況3(1)

- 將節點插在串列的中間位置：假設節點是插在ptr和q兩個節點之間，ptr是q的前一個節點，如下圖所示：



## 加入單向鏈結串列的節點-情況3(2)

- 只需將新節點指標指向q (ptr->next)，然後將 ptr->next指標指向新節點 newnode，就可以插入新節點，如下圖所示：



```
newnode->next=ptr->next;
```

```
ptr->next = newnode;
```

# 反向串接一串列

「鍵結串列的指標反向連接」將使原來串列內資料的順序完全對調。

## 程式4-7反向串接一串列

```
1 struct Node
2 {   int data;
3     struct Node *link;
4 }
5 struct Node *first;
6 void Invert ()
7 {   struct Node *r, *s, *t ;
8     r = first;
9     s = NULL;
10    while (r != NULL)
11    {   t = s;
12        s = r;
13        r = r->link;
14        s->link = t;
15    }
16    first = s;
17 }
```

**r:** 指向目前處理之node

→準備指向下一個node

**t:** 指向目前處理node(r 指向) 的前一個node

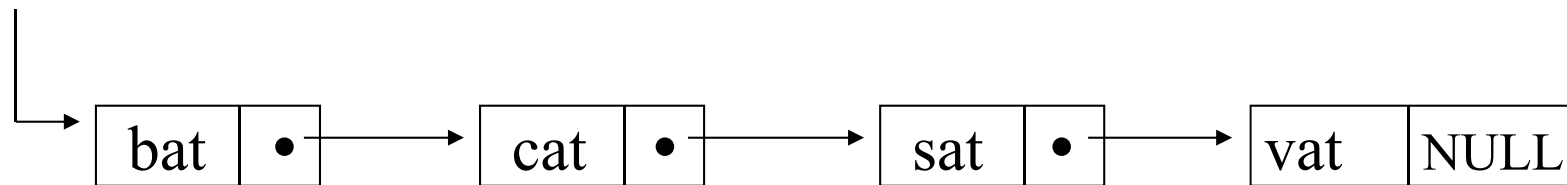
**s:** 將目前處理之node，改指向前一個node( t 指向)

## 串接兩個鏈接串列

程式： 串接兩個鏈接串列

```
1 struct Node
2 { int data;
3   struct Node *link;
4 }
5 struct Node *a_first, *b_first, first;
6 struct Node * Concatenate
7 (struct Node * a_first, struct Node * b_first);
8 { struct Node *p ;
9   if (a_first == NULL)
10    return b_first ;
11   else
12   { for(p=first; p->link!=NULL; p=p->link);
13     p->link = b_first ;
14     return a_first ;
15   }
16 }
```

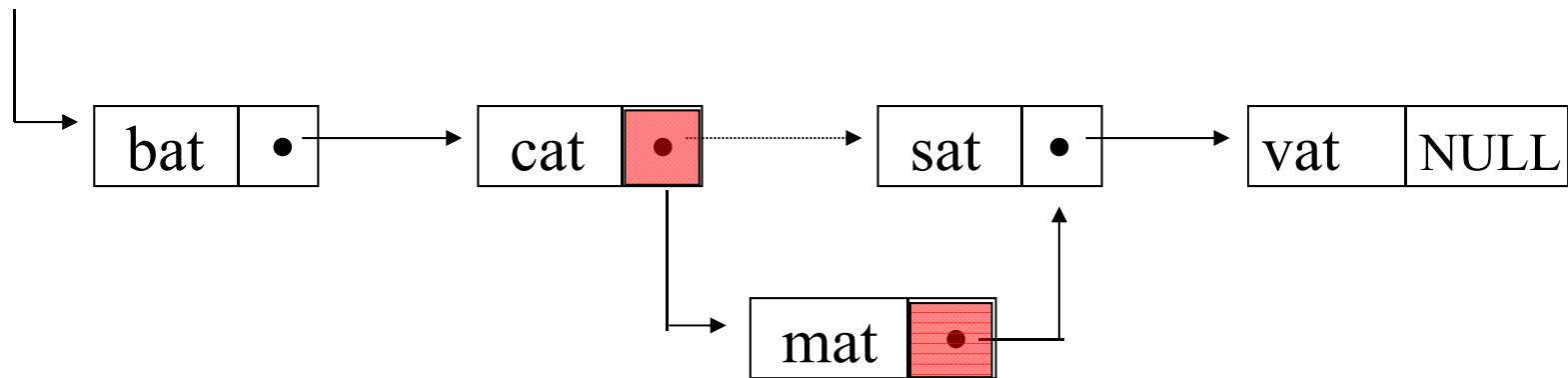
## 4.2 SINGLY LINKED LISTS



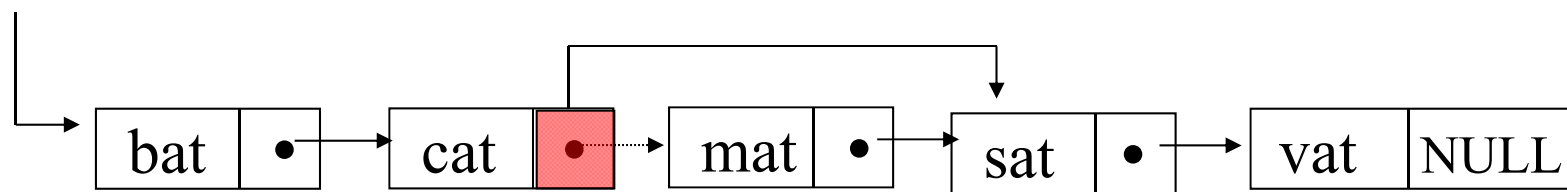
**\*Figure 4.2:** Usual way to draw a linked list (p.147)



## Insertion

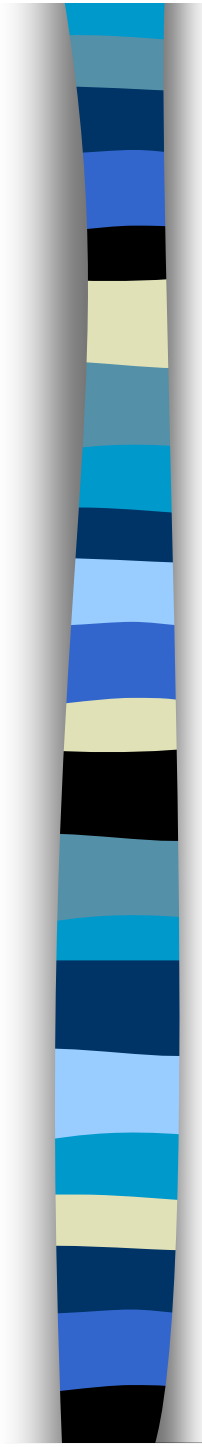


**\*Figure 4.3: Insert mat after cat (p.148)**



dangling  
reference

\*Figure 4.4: Delete *mat* from list (p.149)



## Example 4.1: create a linked list of words

### Declaration

```
typedef struct list_node, *list_pointer;  
typedef struct list_node {  
    char data [4];  
    list_pointer link;  
};
```

### Creation

```
list_pointer ptr =NULL;
```

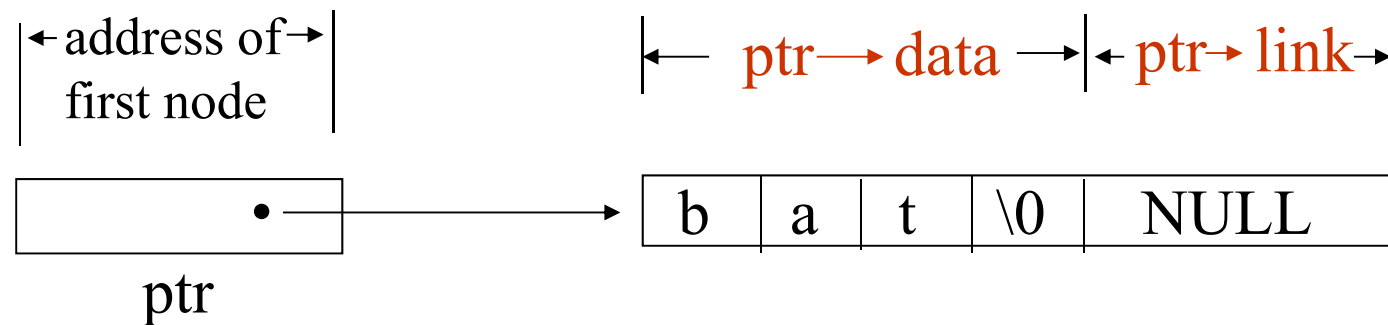
### Testing

```
#define IS_EMPTY(ptr) (!(ptr))
```

### Allocation

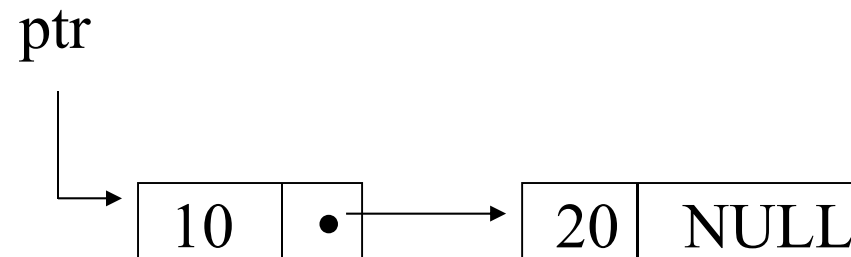
```
ptr=(list_pointer) malloc (sizeof(list_node));
```

$e \rightarrow \text{name} \Leftrightarrow (*e).\text{name}$   
`strcpy(ptr -> data, "bat");`  
`ptr -> link = NULL;`



**\*Figure 4.5: Referencing the fields of a node(p.151)**

## Example: create a two-node list



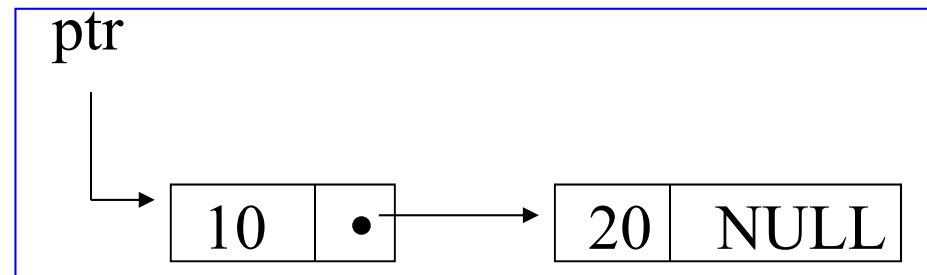
```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    int data;  
    list_pointer link;  
};  
list_pointer ptr = NULL
```

Example 4.1: (p.149)

```

list_pointer create2( )
{
/* create a linked list with two nodes */
list_pointer first, second;
first = (list_pointer) malloc(sizeof(list_node));
second = (list_pointer) malloc(sizeof(list_node));
second -> link = NULL;
second -> data = 20;
first -> data = 10;
first -> link = second;
return first;
}

```



**\*Program 4.1: Create a two-node list (p.152)**

## List Insertion:

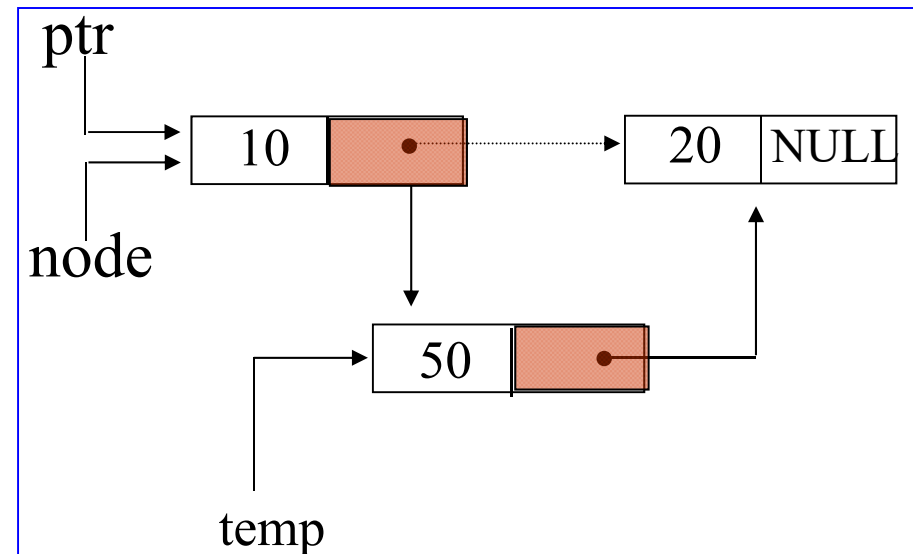
### Insert a node after a specific node

```
void insert(list_pointer *ptr, list_pointer node)
{
    /* insert a new node with data = 50 into the list ptr after node */
    list_pointer temp;
    temp = (list_pointer) malloc(sizeof(list_node));
    if (IS_FULL(temp)){
        fprintf(stderr, "The memory is full\n");
        exit (1);
    }
}
```

```

temp->data = 50;
if (*ptr) { noempty list
    temp->link = node ->link;
    node->link = temp;
}
else { empty list
    temp->link = NULL;
    *ptr = temp;
}
}

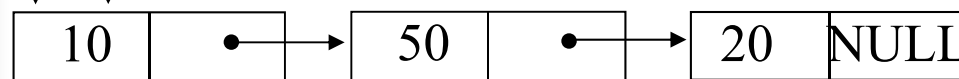
```



**\*Program 4.2:** Simple insert into front of list (p.153)

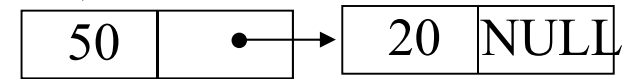


ptr node trail = NULL



(a) before deletion

ptr

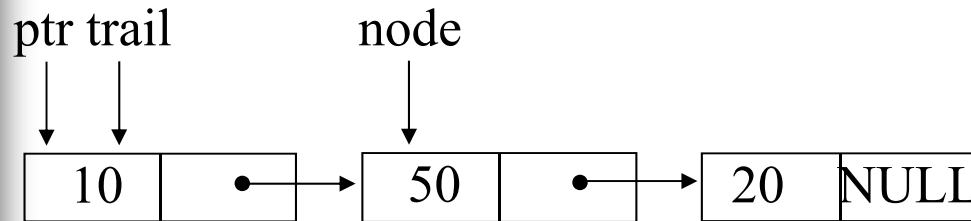


(b) after deletion

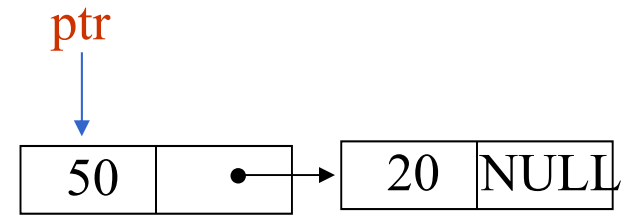
**\*Figure 4.8:** List after the function call *Delete(&ptr, NULL.ptr);*(p.154)

## List Deletion

Delete the first node.

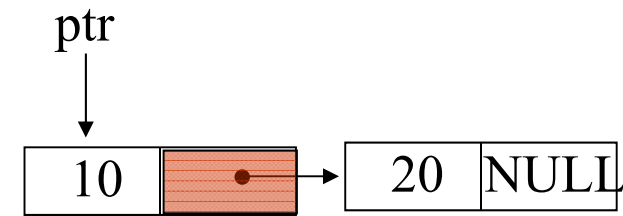
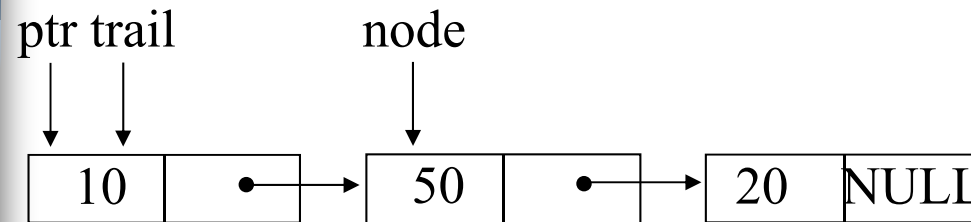


(a) before deletion



(b) after deletion

Delete the node other than the first node.



```
void delete(list_pointer *ptr, list_pointer trail,
            list_pointer node)
```

```
{
/* delete node from the list, trail is the preceding node
ptr is the head of the list */
```

```
if (trail)
```

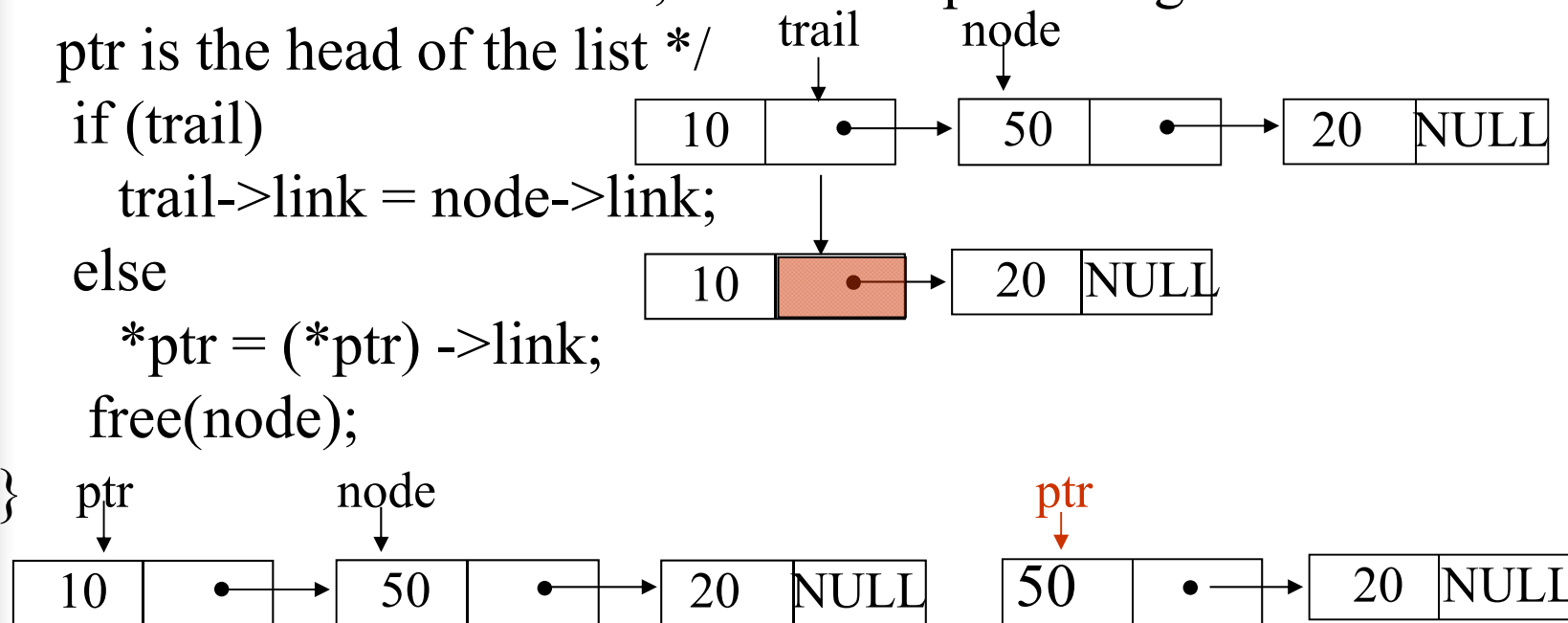
```
    trail->link = node->link;
```

```
else
```

```
    *ptr = (*ptr) ->link;
```

```
    free(node);
```

```
}
```





## Print out a list (traverse a list)

```
void print_list(list_pointer ptr)
{
    printf("The list contains: ");
    for ( ; ptr; ptr = ptr->link)
        printf("%4d", ptr->data);
    printf("\n");
}
```

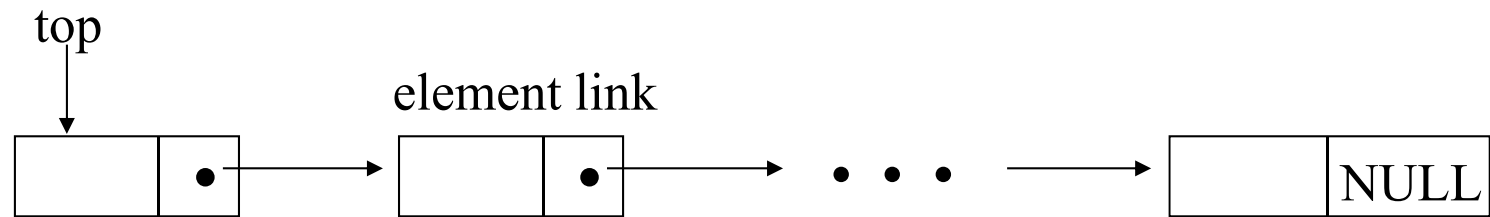
**\*Program 4.4: Printing a list (p.155)**



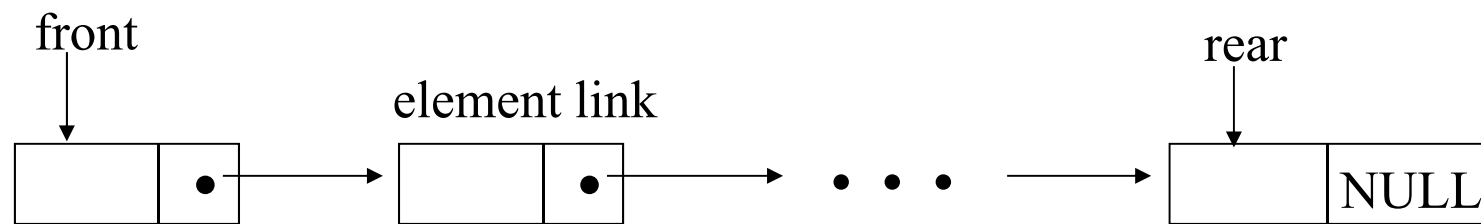
# 作業

- Pp.154: ex6

## 4.3 DYNAMICALLY LINKED STACKS AND QUEUES



(a) Linked Stack



(b) Linked queue

**\*Figure 4.11:** Linked Stack and queue (p.157)

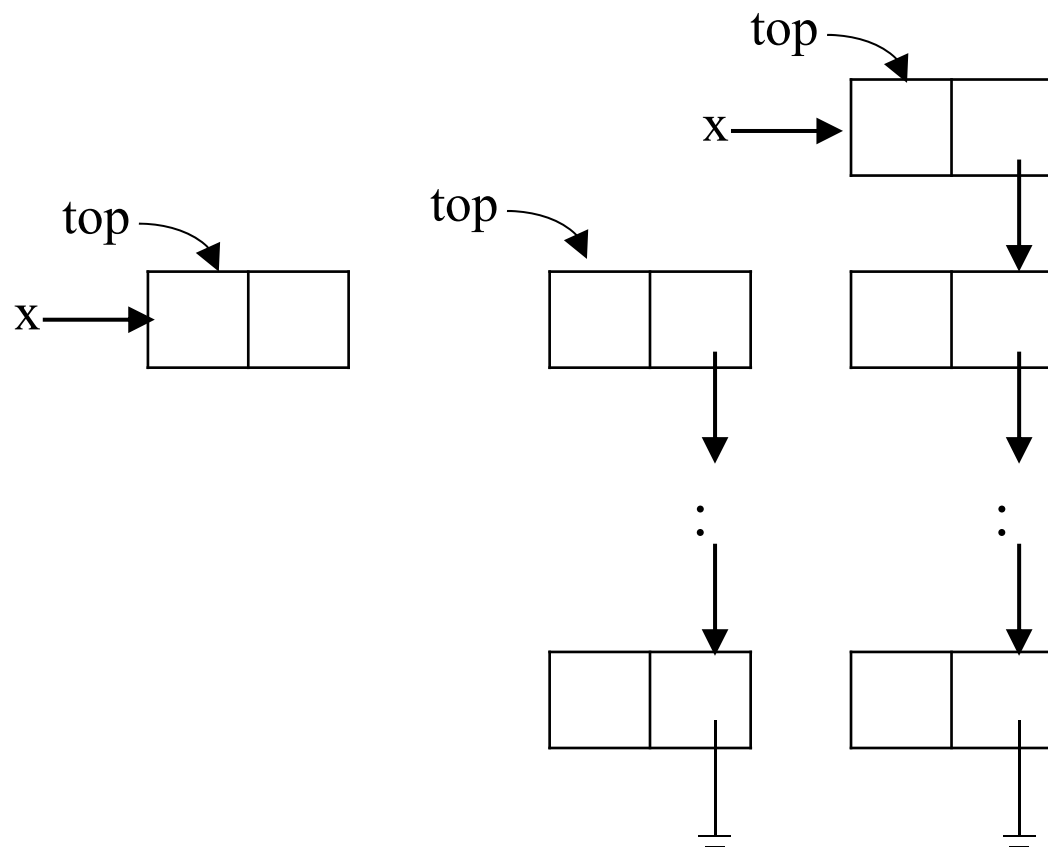
# 鏈結堆疊

利用陣列來實作堆疊的確方便，但是陣列在宣告時即得定義大小，宣告太大形成空間的浪費，宣告太小又怕不敷使用。改用動態配置的鏈結堆疊，即可解決使用陣列造成的缺點。

## 程式 鏈結堆疊

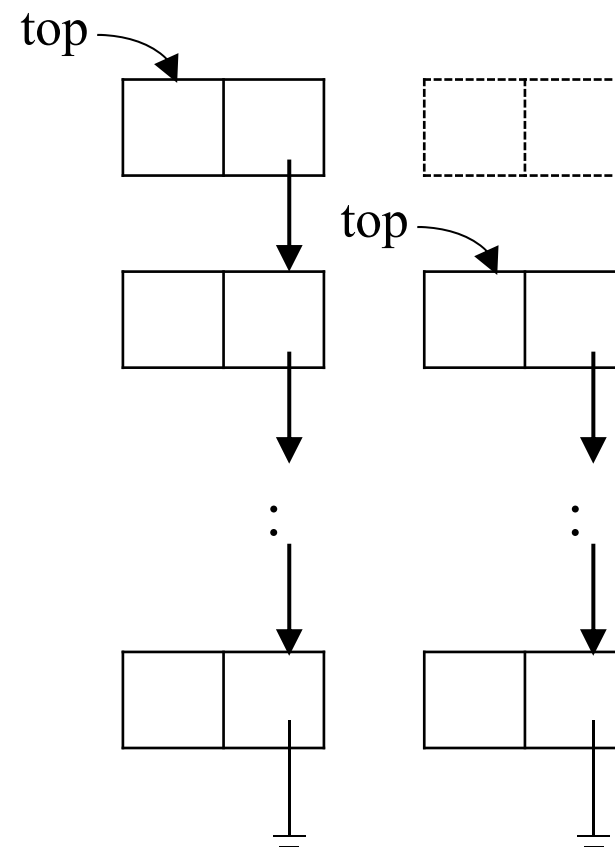
```
1 struct StackNode
2 { int data;
3   struct StackNode *link;
4 }
5 struct StackNode *top;
```

# 鏈結堆疊執行push和pop的過程



(a) push  $x$  至空堆疊

(b) push  $x$  至堆疊



(c) pop 堆疊



## 程式鍵結堆疊 (續)

```
6 struct Stacknode *NewNode(int element)
7 {   struct StackNode *p;
8     p = (struct StackNode *)
          malloc (sizeof(StackNode)) ;
9     p->data = element;
10     p->link = NULL;
11     return p;
12 }
13 void PushStack(int element)
14 {   struct StackNode *x ;
15     x = NewNode(element) ;
16     if (top==NULL) top = x;
17     else
18     {   x->link = top;
19         top = x;
20     }
21 }
```



## Represent n stacks

```
#define MAX_STACKS 10 /* maximum number of stacks */
typedef struct {
    int key;
    /* other fields */
} element;
typedef struct stack *stack_pointer;
typedef struct stack {
    element item;
    stack_pointer link;
};
stack_pointer top[MAX_STACKS];
```



## Push in the linked stack

```
void add(stack_pointer *top, element item)
{
    /* add an element to the top of the stack */
    stack_pointer temp =
        (stack_pointer) malloc (sizeof (stack));
    if (IS_FULL(temp)) {
        fprintf(stderr, " The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = *top;
    *top= temp;
}
```

**\*Program 4.6: Add to a linked stack (p.149)**



## pop from the linked stack

```
element delete(stack_pointer *top) {  
    /* delete an element from the stack */  
    stack_pointer temp = *top;  
    element item;  
    if (IS_EMPTY(temp)) {  
        fprintf(stderr, "The stack is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *top = temp->link;  
    free(temp);  
    return item;  
}
```

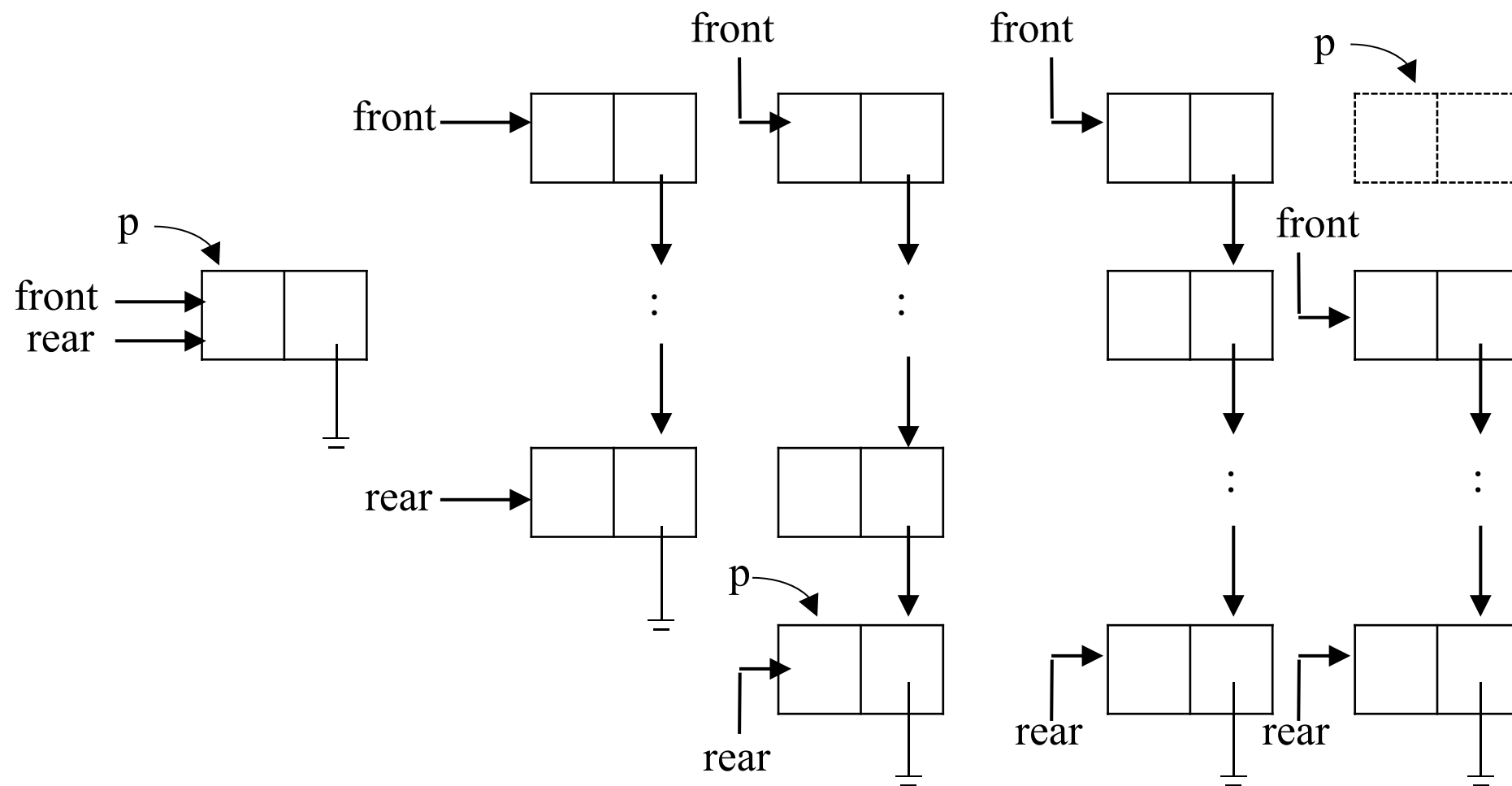
**\*Program 4.7:** Delete from a linked stack (p.149)



## Represent n queues

```
#define MAX_QUEUES 10 /* maximum number of queues */  
typedef struct queue *queue_pointer;  
typedef struct queue {  
    element item;  
    queue_pointer link;  
};  
queue_pointer front[MAX_QUEUE], rear[MAX_QUEUES];
```

# 鏈結佇列執行新增和刪除的過程



(a) 新增節點至空佇列

(b) 新增節點至佇列

(c) 刪除佇列節點

# 鏈結佇列

## 程式鏈結佇列

```
1 struct QueueNode
2 {   char data ;
3     struct QueueNode *next ;
4 }
5 struct QueueNode *front, *rear ;
6 struct QueueNode * NewQNode (char element)
7 {   struct QueueNode *p;
8     p = (struct QueueNode *)
9         malloc (sizeof(QueueNode )) ;
10    p->data = element;
11    P->next = NULL;
12 }
13 void AddQueue(char element)
14 {   struct QueueNode *p;
15     p = NewQNode(element) ;
16     if (rear == NULL)
17         front = p;
18     else
```

## 程式結佇列 (續)

```
18             rear->next = p;
19         rear = p;
20     }
21     char DeleteQueue()
22     {
23         struct QueueNode *p;
24         char element;
25         if (front == NULL)
26         {
27             QueueEmpty( );
28             return "#";
29         }
30         else
31         {
32             p = front;
33             front = front->next;
34             element = p->data;
35             free(p);
36             return element;
37         }
38     }
39 }
```





## enqueue in the linked queue

```
void addq(queue_pointer *front, queue_pointer *rear, element item)
{ /* add an element to the rear of the queue */
    queue_pointer temp =
        (queue_pointer) malloc(sizeof (queue));
    if (IS_FULL(temp)) {
        fprintf(stderr, " The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = NULL;
    if (*front) (*rear) -> link = temp;
    else *front = temp;
    *rear = temp; }
```



**dequeue** from the linked queue (similar to push)

```
element deleteq(queue_pointer *front) {  
    /* delete an element from the queue */  
    queue_pointer temp = *front;  
    element item;  
    if (IS_EMPTY(*front)) {  
        fprintf(stderr, "The queue is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *front = temp->link;  
    free(temp);  
    return item;  
}
```

# Polynomials

$$A(x) = a_{m-1}x^{e_{m-1}} + a_{m-2}x^{e_{m-2}} + \dots + a_0x^{e_0}$$

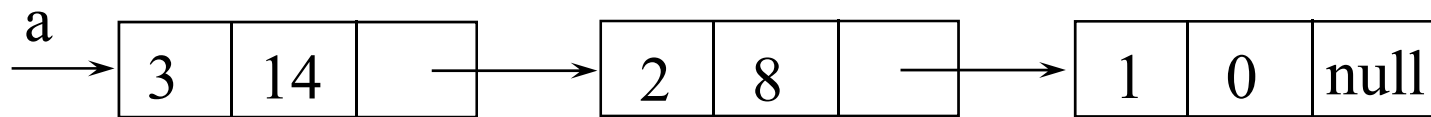
## Representation

```
typedef struct poly_node *poly_pointer;  
typedef struct poly_node {  
    int coef;  
    int expon;  
    poly_pointer link;  
};  
poly_pointer a, b, c;
```

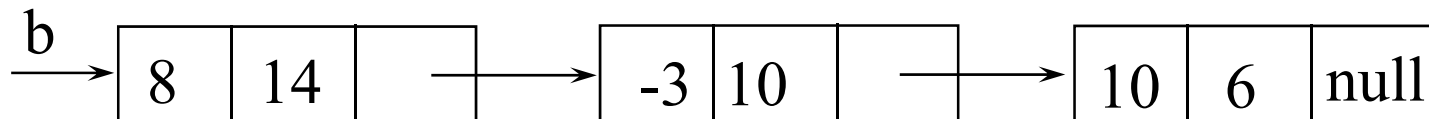
coef	expon	link
------	-------	------

## Examples

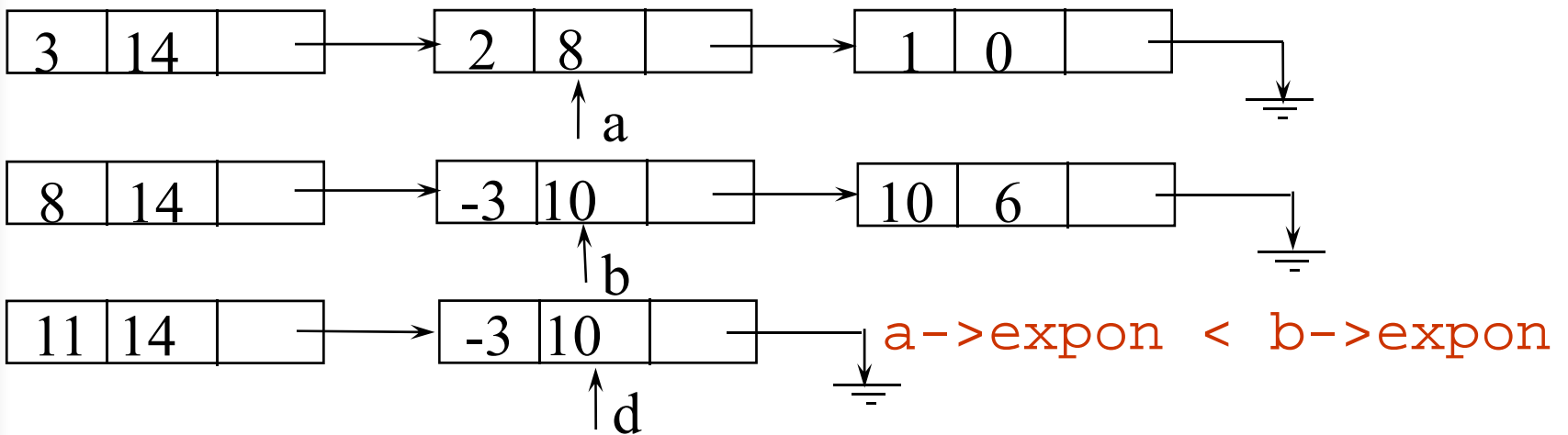
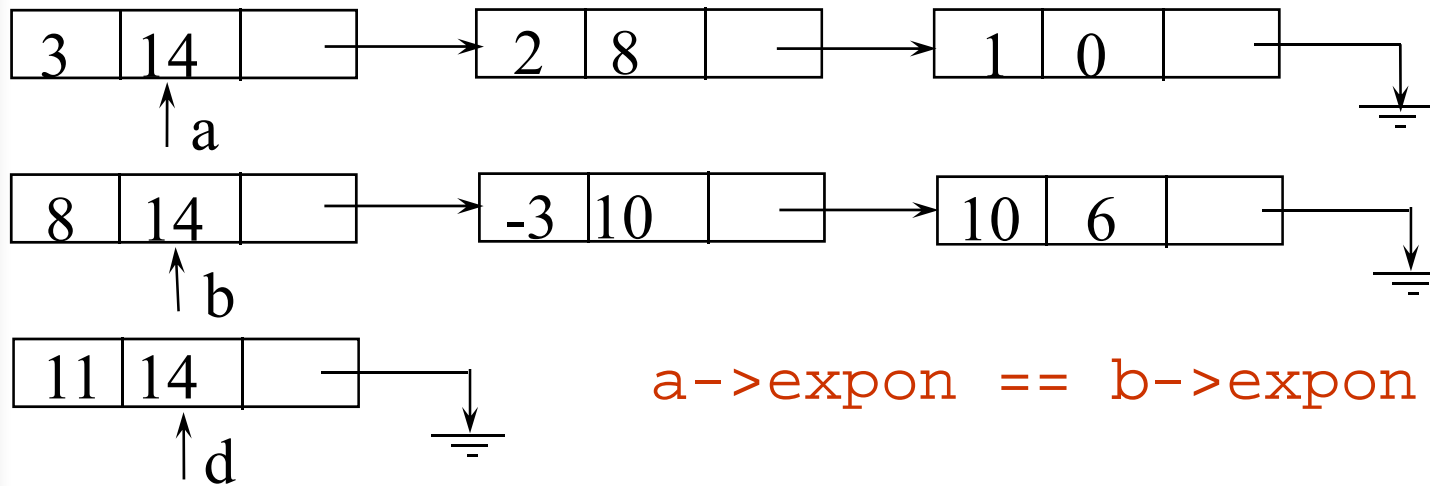
$$a = 3x^{14} + 2x^8 + 1$$



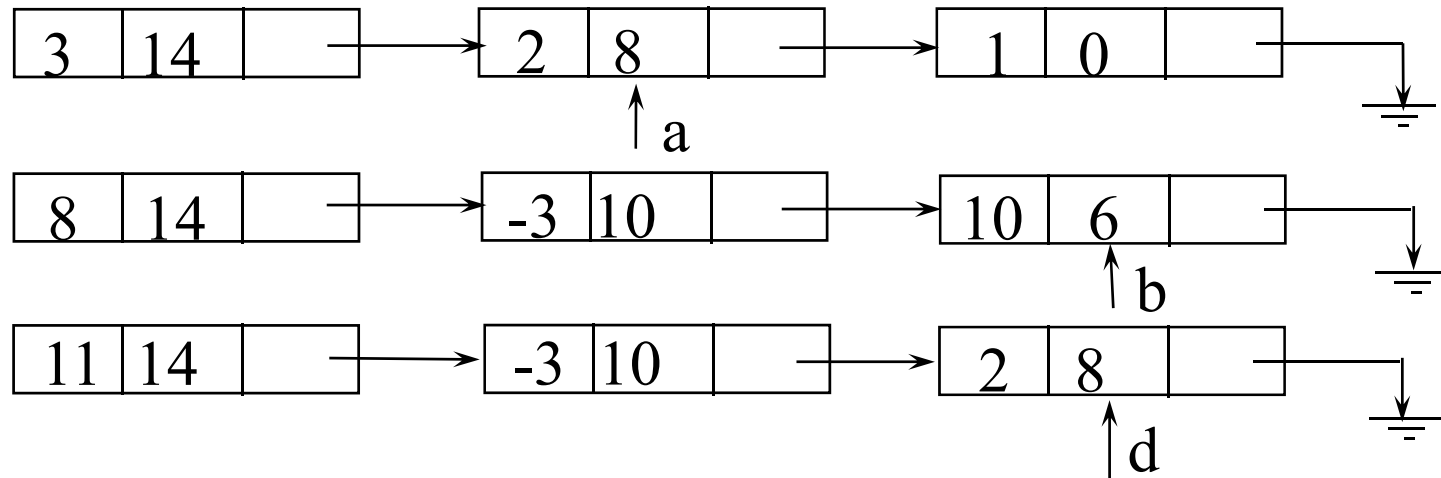
$$b = 8x^{14} - 3x^{10} + 10x^6$$



# Adding Polynomials



## Adding Polynomials (Continued)

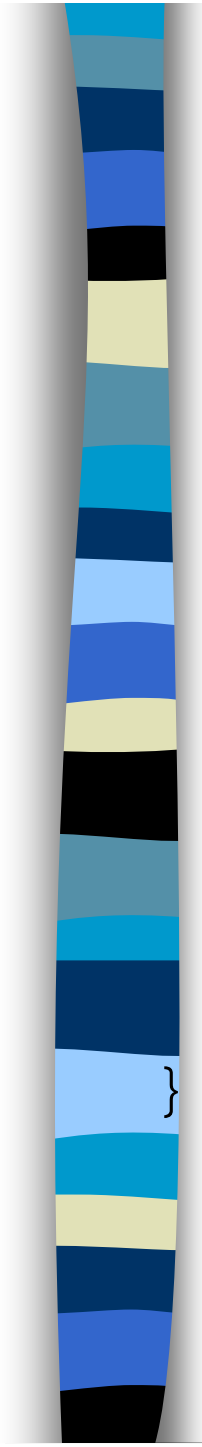


a->expon > b->expon



# Algorithm for Adding Polynomials

```
poly_pointer padd(poly_pointer a, poly_pointer b)
{
    poly_pointer front, rear, temp;
    int sum;
    rear = (poly_pointer)malloc(sizeof(poly_node));
    if (IS_FULL(rear)) {
        fprintf(stderr, "The memory is full\n");
        exit(1);
    }
    front = rear;
    while (a && b) {
        switch (COMPARE(a->expon, b->expon)) {
```



```

    case -1: /* a->expon < b->expon */
        attach(b->coef, b->expon, &rear);
        b = b->link;
        break;
    case 0: /* a->expon == b->expon */
        sum = a->coef + b->coef;
        if (sum) attach(sum, a->expon, &rear);
        a = a->link;    b = b->link;
        break;
    case 1: /* a->expon > b->expon */
        attach(a->coef, a->expon, &rear);
        a = a->link;
}
}
for (; a; a = a->link)
    attach(a->coef, a->expon, &rear);
for (; b; b = b->link)
    attach(b->coef, b->expon, &rear);
rear->link = NULL;
temp = front;    front = front->link;    free(temp);
return front;
}

```

Delete extra initial node.





# Analysis

- (1) coefficient additions  
 $0 \leq \text{additions} \leq \min(m, n)$   
where  $m$  ( $n$ ) denotes the number of terms in  $A$  ( $B$ ).
- (2) exponent comparisons  
extreme case  
 $e_{m-1} > f_{m-1} > e_{m-2} > f_{m-2} > \dots > e_0 > f_0$   
 $m+n-1$  comparisons
- (3) creation of new nodes  
extreme case  
 $m + n$  new nodes  
summary  $O(m+n)$



# Attach a Term

```
void attach(float coefficient, int exponent,
            poly_pointer *ptr)
{
    /* create a new node attaching to the node pointed to
       by ptr. ptr is updated to point to this new node. */
    poly_pointer temp;
    temp = (poly_pointer) malloc(sizeof(poly_node));
    if (IS_FULL(temp)) {
        fprintf(stderr, "The memory is full\n");
        exit(1);
    }
    temp->coef = coefficient;
    temp->expon = exponent;
    (*ptr)->link = temp;
    *ptr = temp;
}
```

# A Suite for Polynomials

$$e(x) = a(x) * b(x) + d(x)$$

```
poly_pointer a, b, d, e;  
...  
a = read_poly();  
b = read_poly();  
d = read_poly();  
temp = pmult(a, b);  
e = padd(temp, d);  
print_poly(e);
```

```
read_poly()  
print_poly()  
padd()  
psub()  
pmult()
```

temp is used to hold a partial result.  
By returning the nodes of temp, we  
may use it to hold other polynomials



# Erase Polynomials

```
void earse(poly_pointer *ptr)
{
    /* erase the polynomial pointed to by ptr */

    poly_pointer temp;

    while (*ptr) {
        temp = *ptr;
        *ptr = (*ptr)->link;
        free(temp);
    }
}
```

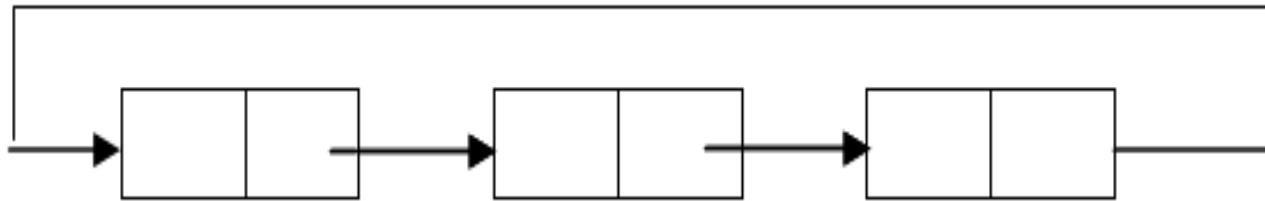
$O(n)$

# 環狀鏈結串列

(Circular Linked Lists)

# 定義

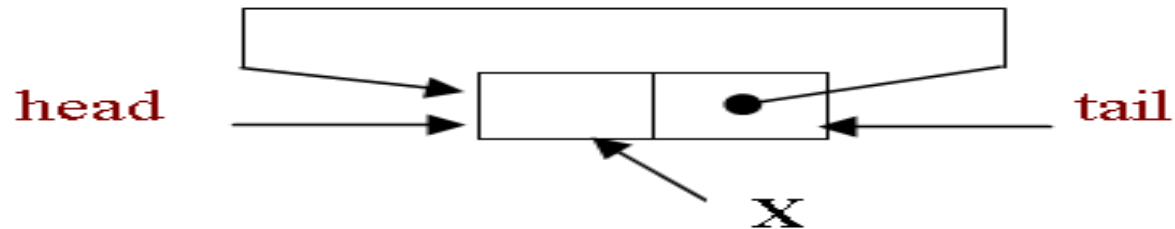
- 一個鏈結串列之最後一個節點指向鏈結串列之最前端，則形成一個環狀鏈結串列，如下圖所示：



# 基本運算與圖解

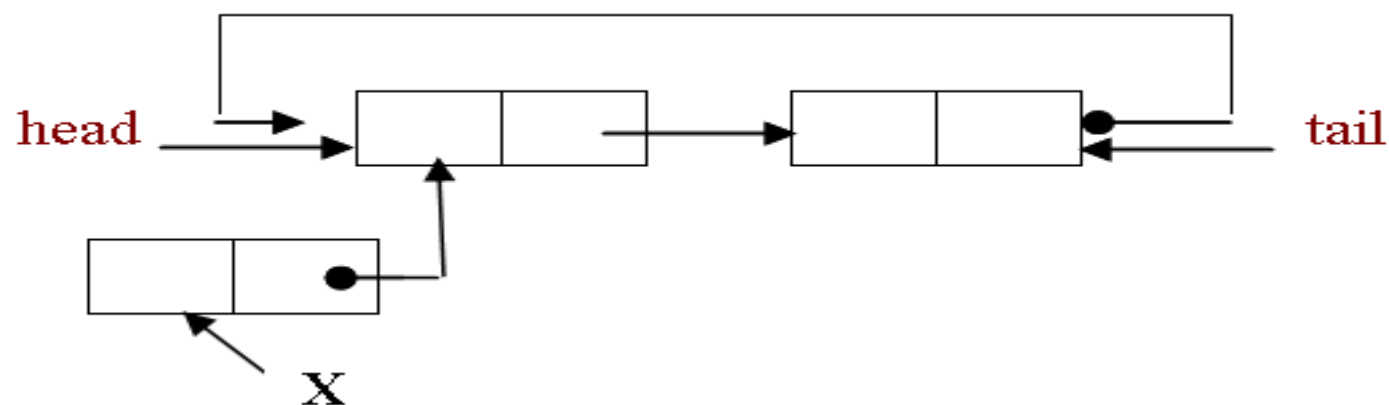
# 加入動作

- 加入節點於前端
  - 當  $\text{head} == \text{NULL}$  時
  - $\text{head} = \text{x}; \text{tail} = \text{x};$

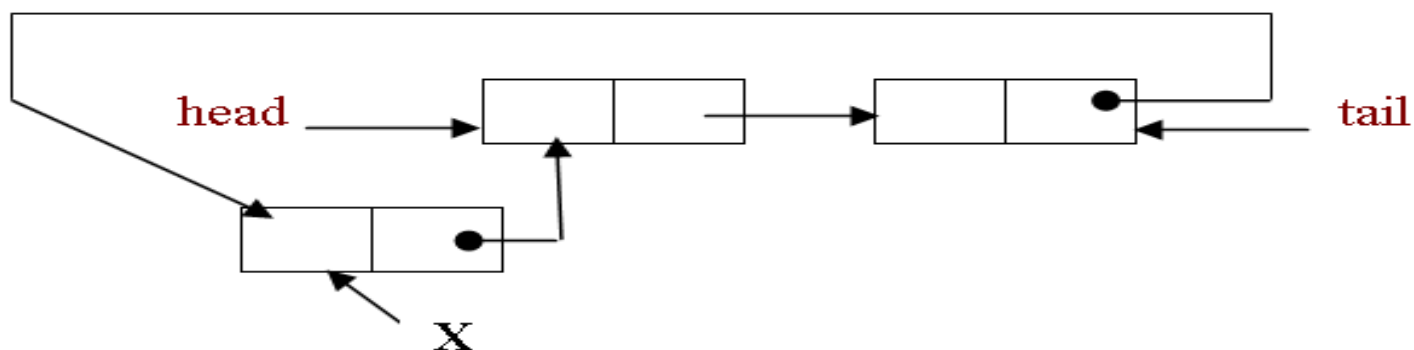




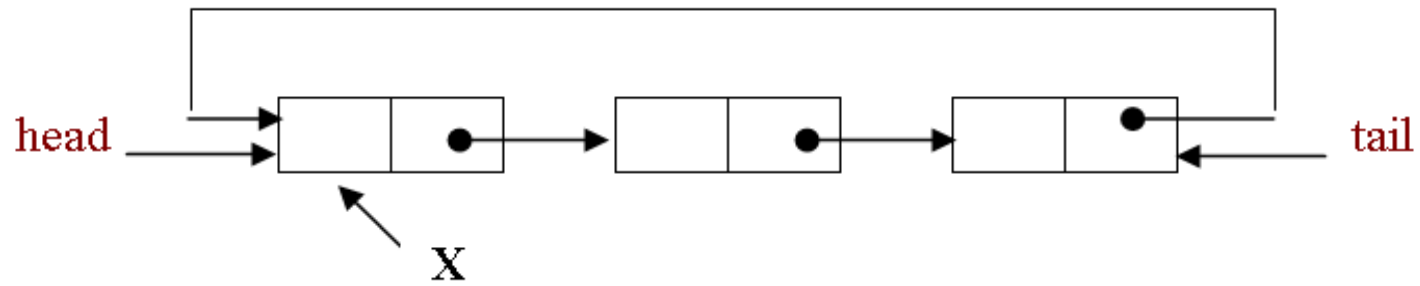
- 當  $\text{head} \neq \text{NULL}$  時
- $x \rightarrow \text{next} = \text{head};$



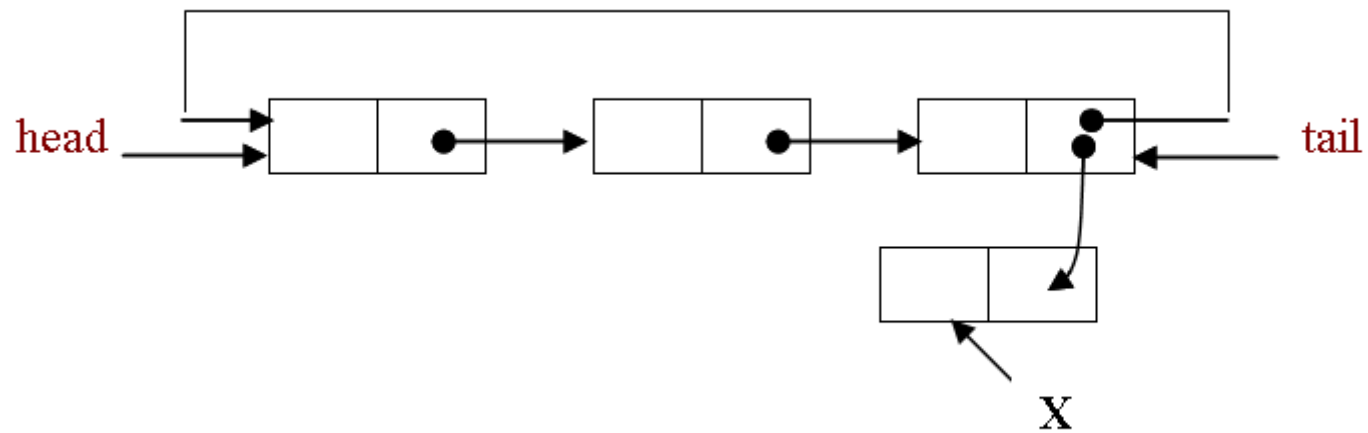
- $\text{tail} \rightarrow \text{next} = x;$



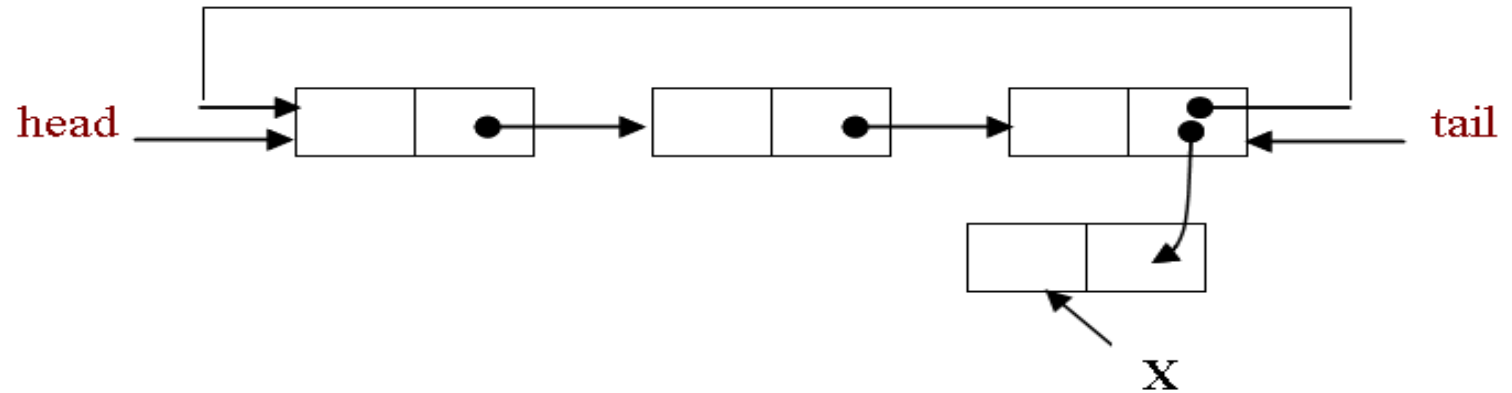
head= x;



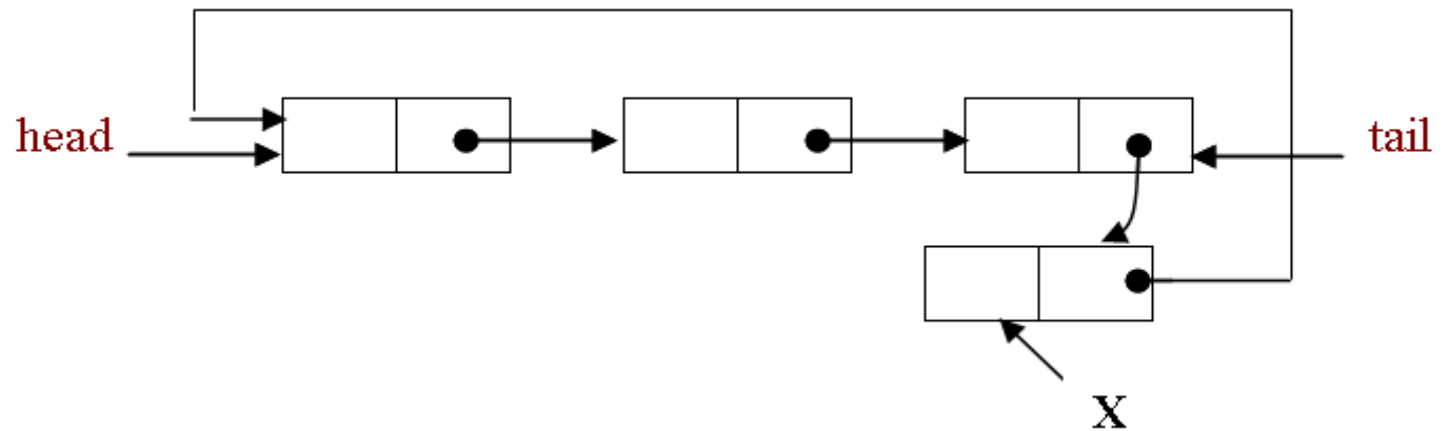
- 加入節點於尾端
  - $\text{tail} \rightarrow \text{next} = x;$



–  $x \rightarrow \text{next} = \text{head};$



–  $\text{tail} = x;$



# 刪除動作

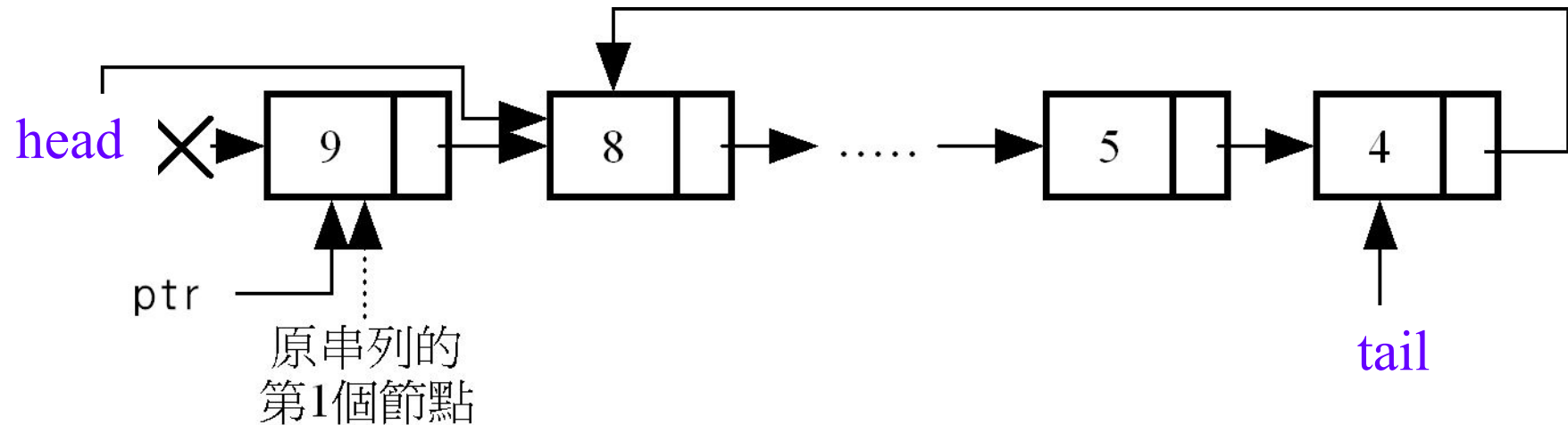
刪除節點於前端

$\text{tail} \rightarrow \text{next} = \text{head} \rightarrow \text{next};$

$\text{ptr} = \text{head};$

$\text{head} = \text{head} \rightarrow \text{next};$

$\text{free}(\text{ptr});$



# 刪除動作

- 刪除環狀串列的中間節點，例如：刪除節點 `ptr` 分成二個步驟，如下所示：

- Step 1：先找到節點 `ptr` 的前一個節點 `previous`。

`previous = head;`

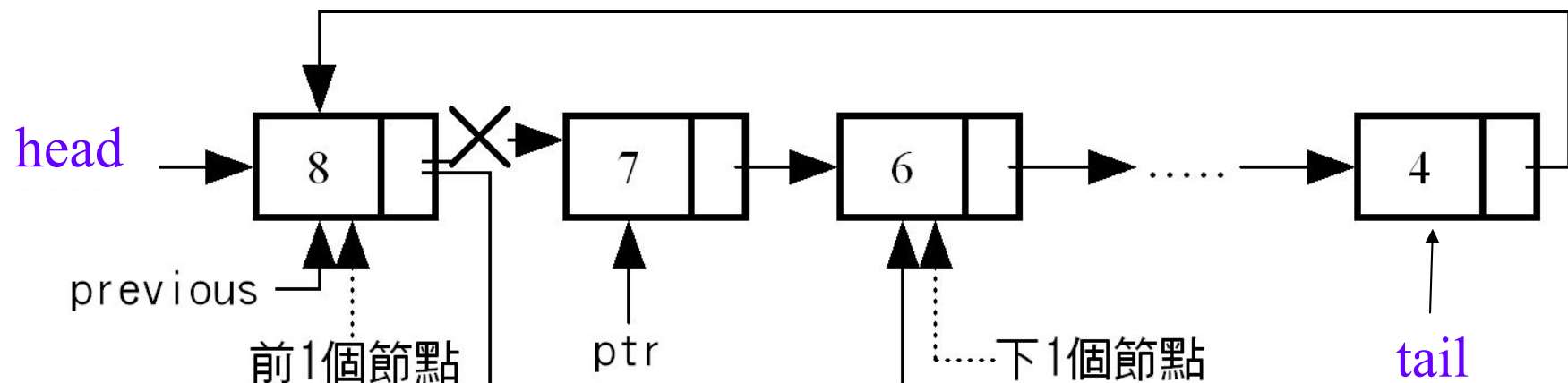
`while ( previous->next != ptr )`

`previous = previous->next;`

- Step 2：將前節點的指標指向節點 `ptr` 的下節點。

`previous->next = ptr->next;`

`free(ptr);`



# 基本運算之演算法及程式

# 加入動作

```
void insert_node (struct node *ptr, struct node *head,  
                  struct node *tail)  
{  
    struct node *prev; *this  
    if (head == NULL)  
    { /*加入資料為第一筆  
        ptr -> next = ptr;  
        head = ptr;  
        tail = ptr;  
    }  
    this = head;
```



```
if (ptr ->key < this ->key)
{ /*加入前端
ptr -> next = this;
head = ptr;
tail -> next = head;
}
else
{
while (this -> next != head)
{
prev = this;
this = this ->next;
```

```
if (ptr->key < this->key)
{ /*加入於特定節點*/
ptr ->next = this;
prev ->next = ptr;
break;
}
}
if (ptr->key >= tail->key)
{ /*加入尾端*/
ptr->next = head;
this->next = ptr;
tail = ptr;
}
}
}
```

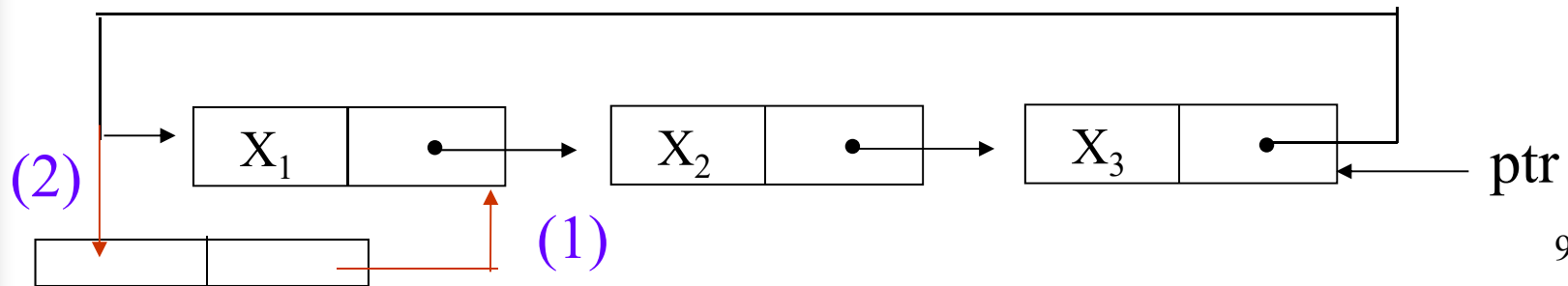
# 刪除動作

## 計算環狀鏈結串列之長度

```
int Clength (NODE *CL )
/*此函數計算環狀鏈結串列之長度*/
{
    int num=0;
    NODE *p;
    if (p != CL) {
        p=CL;
        do {
            num ++;
            p = p->next;
        } while (p != CL);
    }
    return(num);
}
```

# Operations for Circular Linked Lists

```
void insert_front (list_pointer *ptr, list_pointer
node)
{
    if (IS_EMPTY(*ptr)) {
        *ptr= node;
        node->link = node;
    }
    else {
        node->link = (*ptr)->link;    (1)
        (*ptr)->link = node;         (2)
    }
}
```





## Length of Linked List

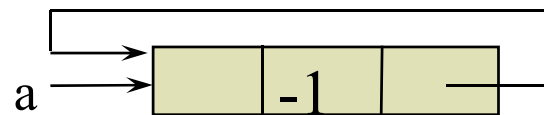
```
int length(list_pointer ptr)
{
    list_pointer temp;
    int count = 0;
    if (ptr) {
        temp = ptr;
        do {
            count++;
            temp = temp->link;
        } while (temp!=ptr);
    }
    return count;
}
```

#### 4.4.4 Representing Polynomials As Circularly Linked Lists

Head Node

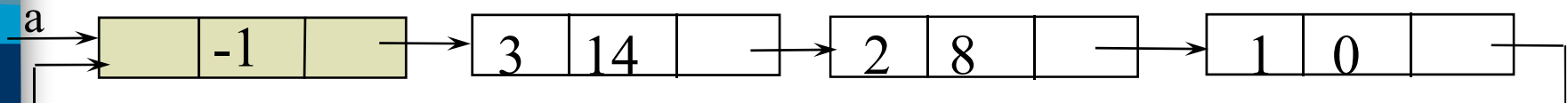
Represent polynomial as circular list.

(1) zero



Zero polynomial

(2) others



$$a = 3x^{14} + 2x^8 + 1$$



## Additional List Operations

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    char data;  
    list_pointer link;  
};
```

Invert single linked lists

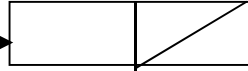
Concatenate two linked lists

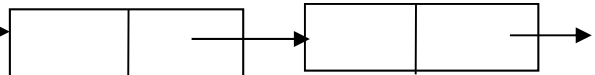
# Invert Single Linked Lists

Use two extra pointers: middle and trail.

```
list_pointer invert(list_pointer lead)
{
    list_pointer middle, trail;
    middle = NULL;
    while (lead) {
        trail = middle;
        middle = lead;
        lead = lead->link;
        middle->link = trail;
    }
    return middle;
}
```

0: null

1: lead →  ...

≥2: lead → 





## Concatenate Two Lists

```
list_pointer concatenate(list_pointer
                        ptr1, list_pointer ptr2)
{
    list_pointer temp;
    if (IS_EMPTY(ptr1)) return ptr2;
    else {
        if (!IS_EMPTY(ptr2)) {
            for (temp=ptr1; temp->link; temp=temp->link);
            temp->link = ptr2;
        }
        return ptr1;
    }
}
```

$O(m)$  where  $m$  is # of elements in the first list



# 作業

- Pp.172: ex1



## 4.8 雙向鏈結串列

# Doubly Linked List

Move in forward and backward direction.

Singly linked list (in one direction only)

How to get the preceding node during deletion or insertion?

Using 2 pointers

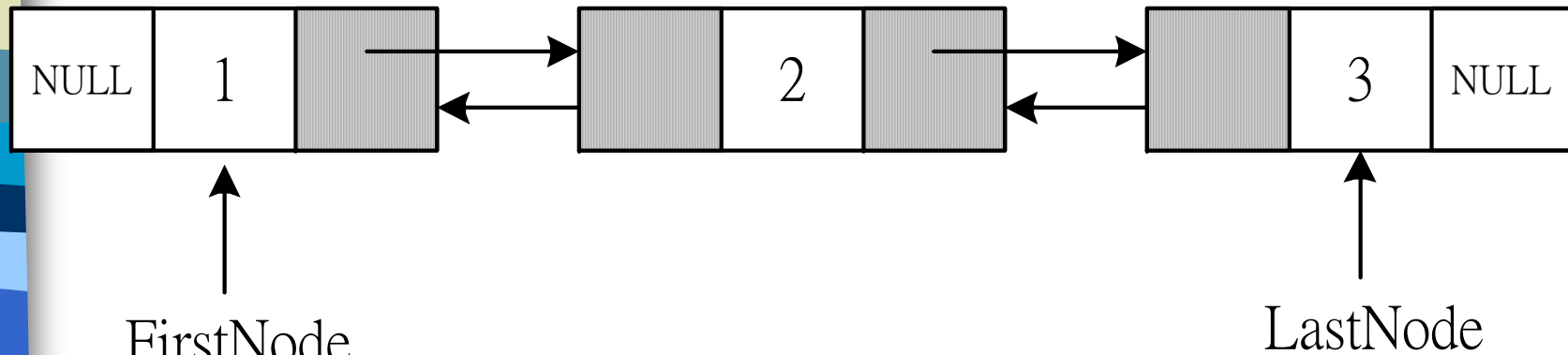
Node in doubly linked list

left link field (llink)

data field (item)

right link field (rlink)

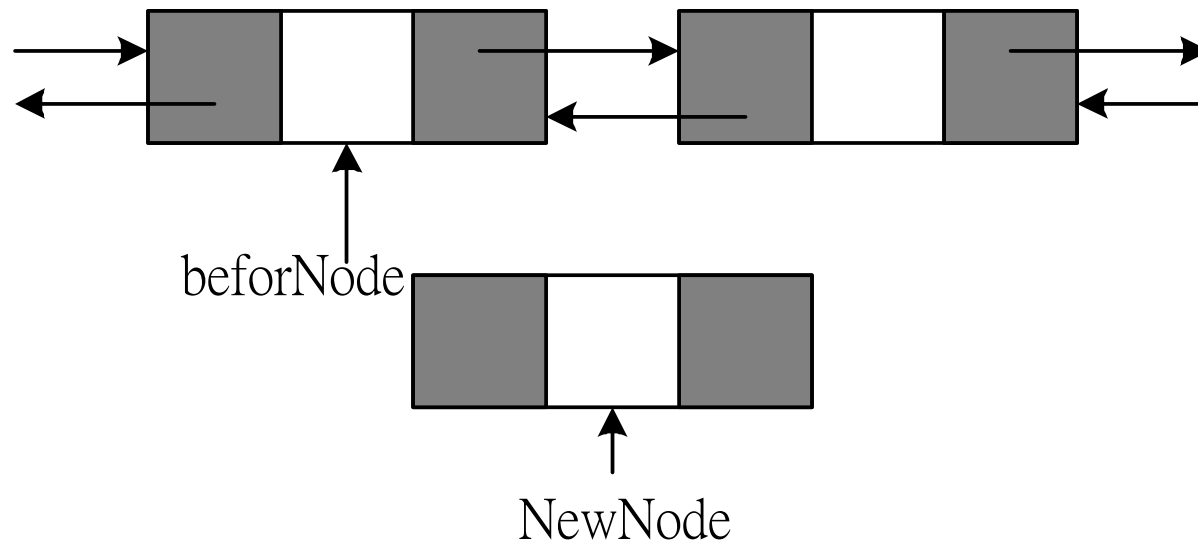
# 雙向鏈結串列



```
typedef struct dlist_node
{
    struct dlist_node *left;
    int                data;
    struct dlist_node *right;
} Dnode;
```

# 插入節點

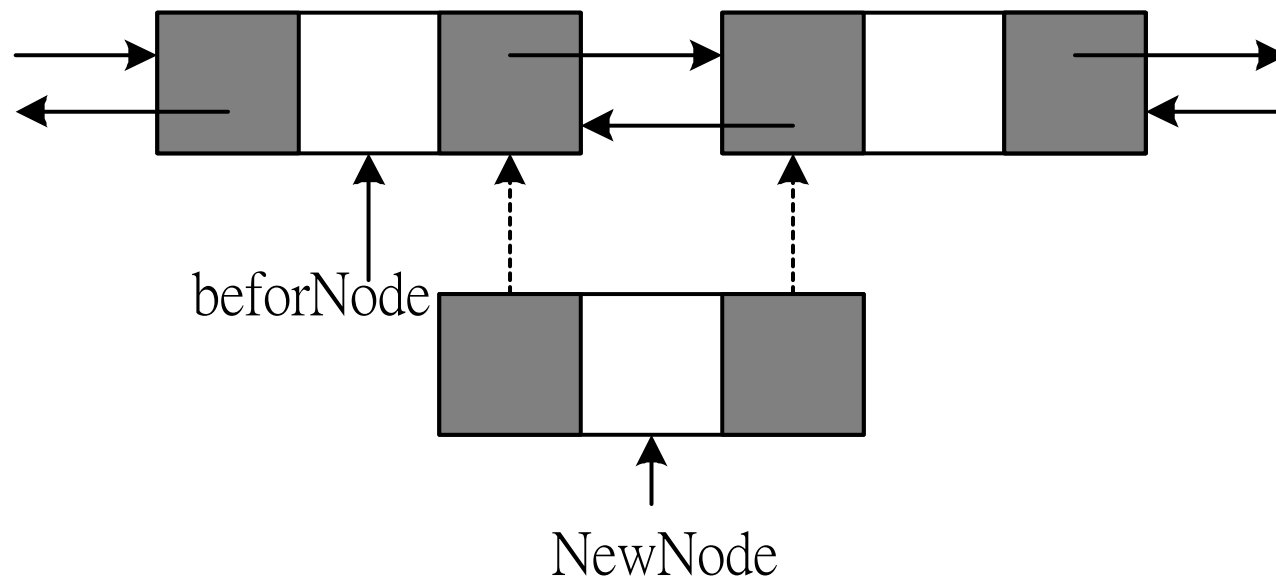
- 要將一個新節點(由newnode指標所指到)，插入beforeNode指標節點之右



# 插入節點

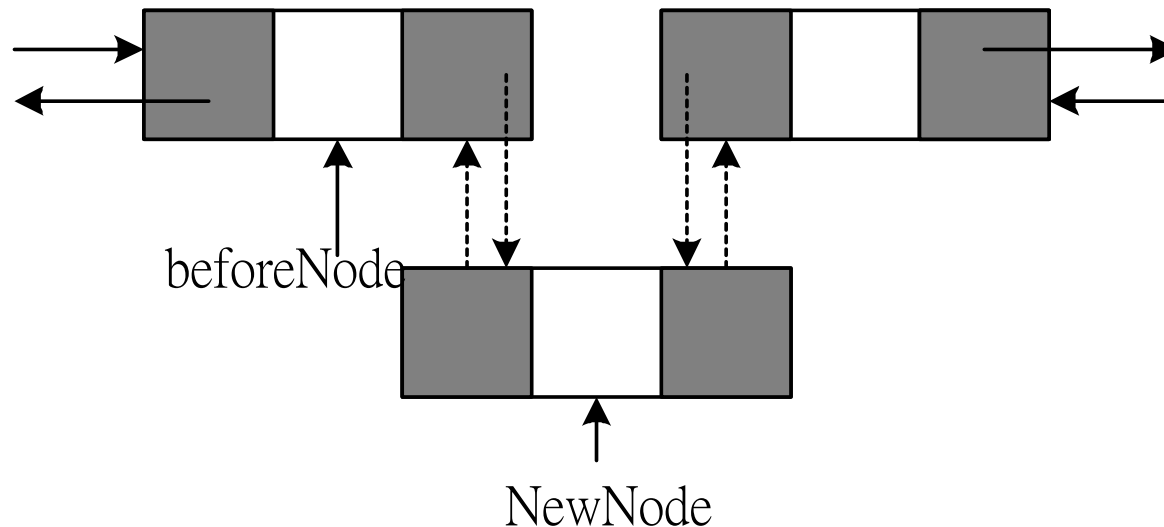
## ■ 處理新節點上的兩個鏈結：

- 左鏈結：NewNode->left=beforeNode;
- 右鏈結：NewNode->right=beforeNode->right;



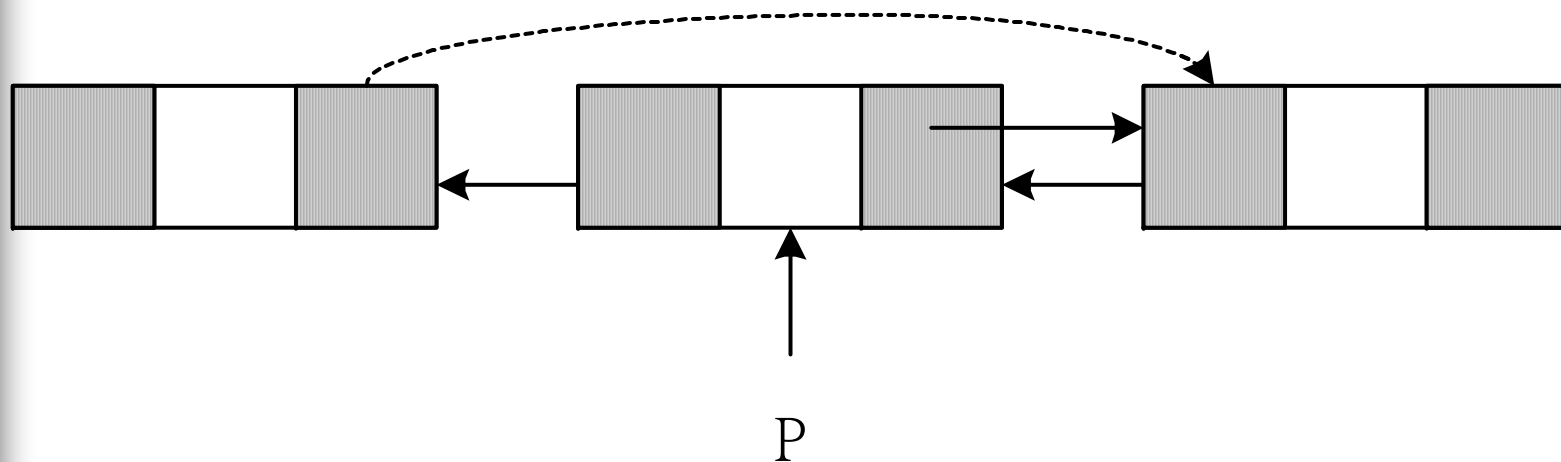
# 插入節點

- 改變舊節點的鏈結，讓它們指向新節點：
  - `beforeNode->right->left=NewNode;`
  - `beforeNode->right=NewNode;`



# 刪除節點

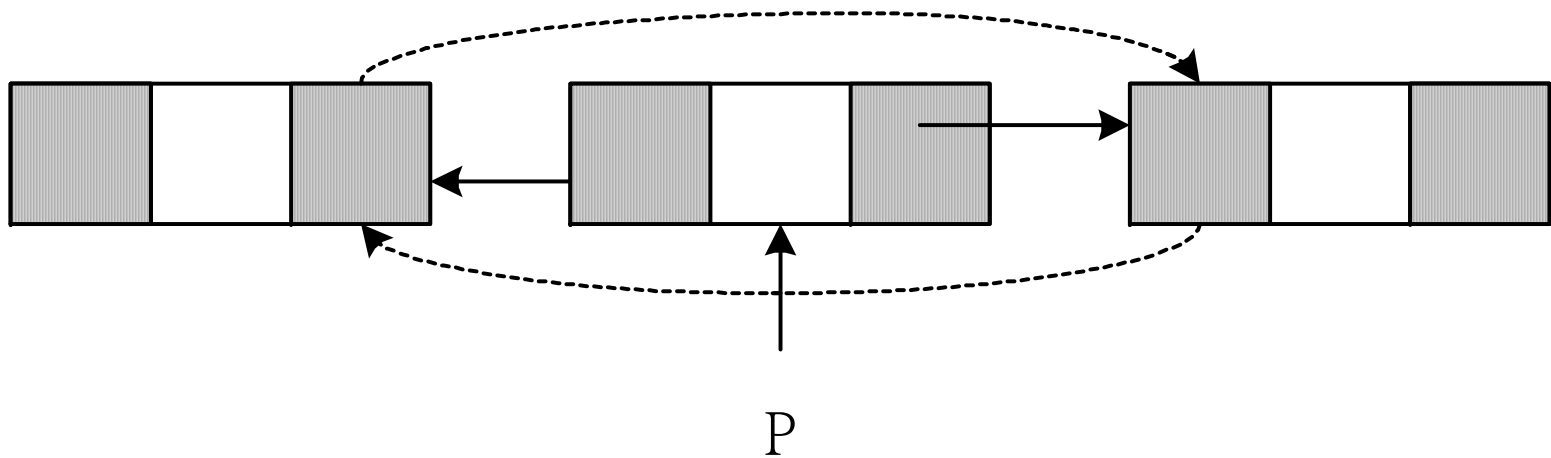
- 改變左邊節點的右指標使它越過舊節點：
  - $p \rightarrow \text{left} \rightarrow \text{right} = p \rightarrow \text{right};$





# 刪除節點

- 改變右邊節點的左指標使它越過舊節點：  
–  $p \rightarrow \text{right} \rightarrow \text{left} = p \rightarrow \text{left};$



# 刪除節點

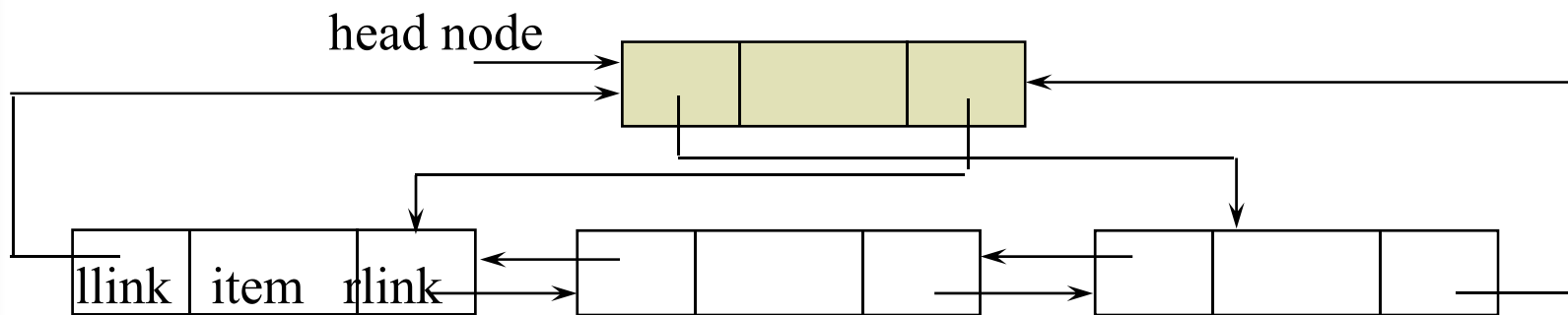
- 刪除舊節點
  - `free(p);`

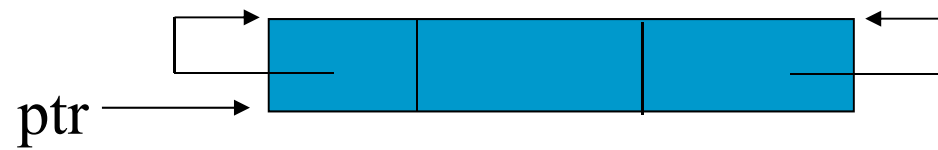


# Doubly Linked Lists

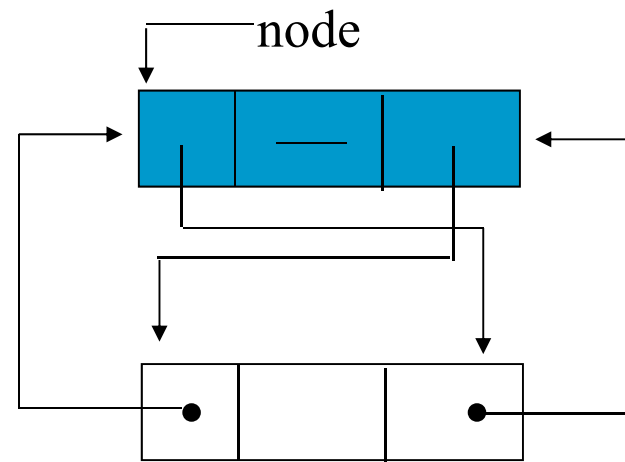
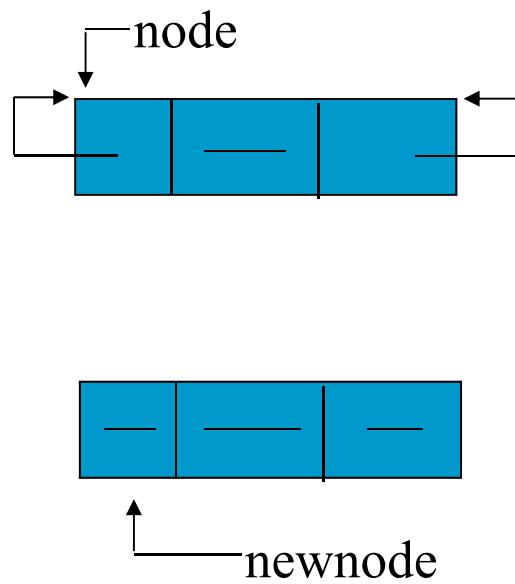
```
typedef struct node *node_pointer;  
typedef struct node {  
    node_pointer llink;  
    element item;  
    node_pointer rlink;  
}
```

ptr  
= ptr->rlink->llink  
= ptr->llink->rlink





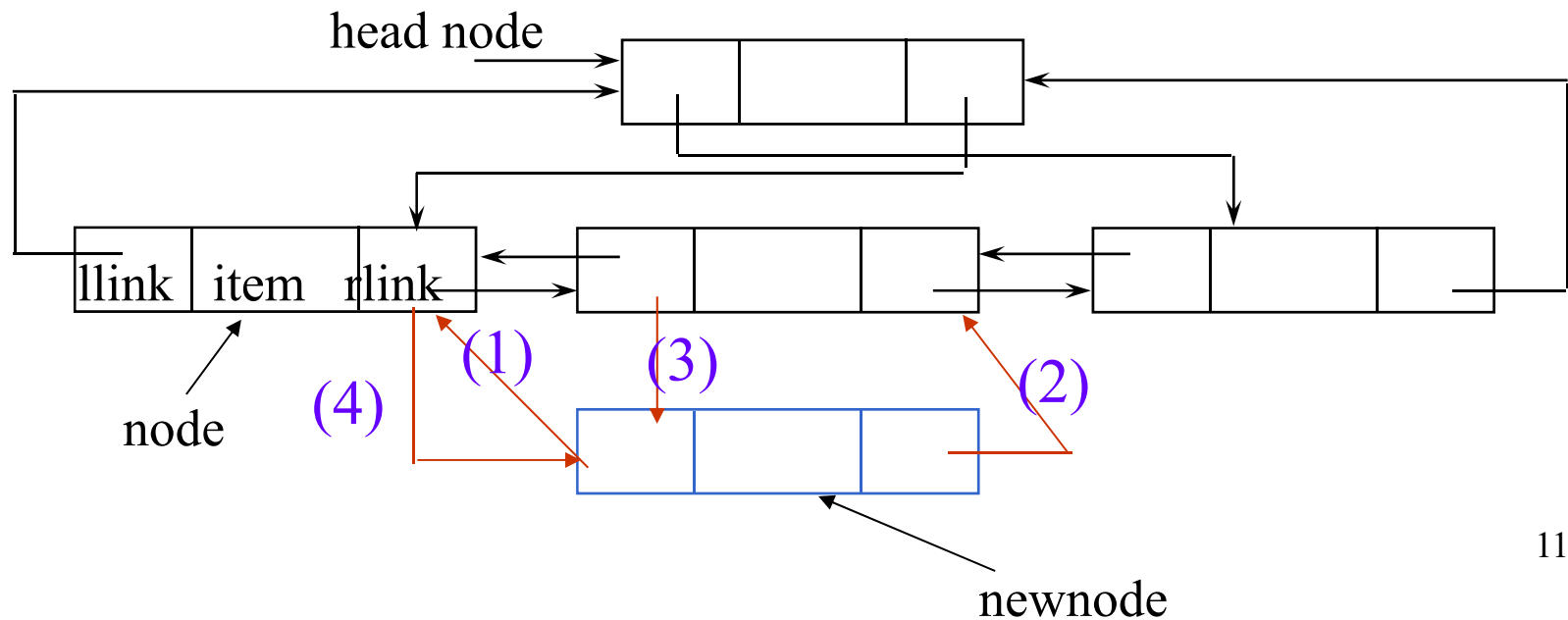
**\*Figure 4.22:Empty doubly linked circular list with head node (p.188)**



**\*Figure 4.25:** Insertion into an empty doubly linked circular list (p.18?)

## Insert

```
void dininsert(node_pointer node, node_pointer newnode)
{
    (1) newnode->llink = node;
    (2) newnode->rlink = node->rlink;
    (3) node->rlink->llink = newnode;
    (4) node->rlink = newnode;
}
```



## Delete

```
void ddelete(node_pointer node, node_pointer deleted)
{
    if (node==deleted) printf("Deletion of head node
                             not permitted.\n");
    else {
        (1) deleted->llink->rlink= deleted->rlink;
        (2) deleted->rlink->llink= deleted->llink;
        free(deleted);
    }
}
```

