Consider a dataset  $D=\{(x_i,y_i)\}^N$  of N data points, where  $x_i=(x_{i1},x_{i2},\cdots,x_{iM})$  is a feature vector with M features, and  $y_i$  is the target, i.e., the response, variable. Let  $x_j$  denote the jth variable in feature space. A typical linear regression model can then be expressed mathematically as:

$$\mathbf{y} = \beta_0 + \beta_1 \mathbf{x}_1 + \beta_2 \mathbf{x}_2 + \dots + \beta_M \mathbf{x}_M$$

This model assumes that the relationships between the target variable  $y_i$  and features  $x_j$  are linear and can be captured in slope terms  $\beta_1, \beta_2, \ldots, \beta_M$ .