

Term variables, x, y, z variables
Type variables, a, b type variables
Integer, i

| | | |
|---------------------------|---|--|
| Monotypes, τ | $::=$ $ $ Int $ $ a $ $ $\tau_1 \rightarrow \tau_2$ | Monotypes |
| Rho-types, ρ | $::=$ $ $ τ $ $ (ρ) | Rho-types S |
| Polytypes, σ | $::=$ $ $ ρ $ $ $\forall a. \sigma$ $ $ $[a \mapsto \tau] \sigma$ | bind a in σ M |
| Terms, t, u | $::=$ $ $ i $ $ x $ $ $\lambda x. t$ $ $ $t u$ $ $ $\lambda(x :: \sigma). t$ $ $ let $x = u$ in t $ $ $t :: \sigma$ $ $ (t) $ $ $t[x \rightsquigarrow t']$ | Literal Variable Abstraction Application Typed abstraction Local binding Type annotation S M |
| <i>value</i> , v | $::=$ $ $ i $ $ $\lambda x. t$ $ $ $\lambda(x :: \sigma). t$ | bind x in t bind x in t |
| Typing contexts, Γ | $::=$ $ $ ϵ $ $ $\Gamma, x : \sigma$ | empty context assumption |
| fv | $::=$ $ $ $fv(t)$ | M |
| $ftvany$ | $::=$ $ $ $ftv(\tau)$ $ $ $ftv(\rho)$ $ $ $ftv(\sigma)$ $ $ $ftv(\Gamma)$ | M M M M |
| <i>terminals</i> | $::=$ $ $ \longrightarrow $ $ \rightarrow $ $ $::$ $ $ fv $ $ ftv | |

| | | |
|--------------------|-------|----------------------------|
| | | \in |
| | | \notin |
| | | \vdash |
| <i>formula</i> | $::=$ | |
| | | <i>judgement</i> |
| | | value v |
| | | uniq Γ |
| | | closed σ |
| | | $a \notin ftvany$ |
| | | $x : \sigma \in \Gamma$ |
| <i>JTyping</i> | $::=$ | |
| | | $\Gamma \vdash t : \sigma$ |
| <i>JStep</i> | $::=$ | |
| | | $t \longrightarrow u$ |
| <i>judgement</i> | $::=$ | |
| | | <i>JTyping</i> |
| | | <i>JStep</i> |
| <i>user_syntax</i> | $::=$ | |
| | | Term variables |
| | | Type variables |
| | | Integer |
| | | Monotypes |
| | | Rho-types |
| | | Polytypes |
| | | Terms |
| | | <i>value</i> |
| | | Typing contexts |
| | | <i>fv</i> |
| | | <i>ftvany</i> |
| | | <i>terminals</i> |
| | | <i>formula</i> |

$\Gamma \vdash t : \sigma$

$$\begin{array}{c}
\frac{}{\Gamma \vdash i : \mathbf{Int}} \quad \text{TYP_INT} \\
\\
\frac{\text{uniq } \Gamma \quad x : \sigma \in \Gamma}{\Gamma \vdash i : \sigma} \quad \text{TYP_VAR} \\
\\
\frac{\Gamma, x : \tau_1 \vdash t : \tau_2}{\Gamma \vdash (\lambda x. t) : (\tau_1 \rightarrow \tau_2)} \quad \text{TYP_ABS} \\
\\
\frac{\Gamma \vdash t : \tau_1 \rightarrow \tau_2 \quad \Gamma \vdash u : \tau_1}{\Gamma \vdash t u : \tau_2} \quad \text{TYP_APP}
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma \vdash u : \sigma \quad \Gamma, x : \sigma \vdash t : \rho}{\Gamma \vdash \text{let } x = u \text{ in } t : \rho} \text{ TYP_LET} \\
\\
\frac{\text{closed } \sigma \quad \Gamma \vdash t : \sigma}{\Gamma \vdash (t :: \sigma) : \sigma} \text{ TYP_ANNOT} \\
\\
\frac{\Gamma \vdash t : \rho}{\Gamma \vdash t : \forall a. \rho} \text{ TYP_GEN} \\
\\
\frac{\Gamma \vdash t : \forall a. \rho}{\Gamma \vdash t : [a \mapsto \tau] \rho} \text{ TYP_INST}
\end{array}$$

$$\boxed{t \longrightarrow u}$$

$$\begin{array}{c}
\frac{u \longrightarrow u'}{\text{let } x = u \text{ in } t \longrightarrow \text{let } x = u' \text{ in } t} \text{ STEP_LET1} \\
\\
\frac{}{\text{let } x = v \text{ in } t \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_LET} \\
\\
\frac{t \longrightarrow t'}{t \ u \longrightarrow t' \ u} \text{ STEP_APP1} \\
\\
\frac{u \longrightarrow u'}{(\lambda x. t) \ u \longrightarrow (\lambda x. t) \ u'} \text{ STEP_APP2} \\
\\
\frac{}{(\lambda x. t) \ v \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_APP} \\
\\
\frac{u \longrightarrow u'}{(\lambda(x :: \sigma). t) \ u \longrightarrow (\lambda(x :: \sigma). t) \ u'} \text{ STEP_ANNOT_APP2} \\
\\
\frac{}{(\lambda(x :: \sigma). t) \ v \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_ANNOT_APP} \\
\\
\frac{}{t :: \sigma \longrightarrow t} \text{ STEP_ERASE}
\end{array}$$

Definition rules: 16 good 0 bad
 Definition rule clauses: 31 good 0 bad