$\begin{array}{ll} \text{Term variables, } x, \, y, \, z & \text{variables} \\ \text{Type variables, } a, \, b & \text{type variables} \\ \text{Integers, } i & \end{array}$ 

```
Monotypes, \tau
                                                                                                Monotypes
                                       ::=
                                                {\tt Int}
                                                a
                                                \tau_1 \to \tau_2
Rho-types, \rho
                                                                                                Rho-types
                                               	au(
ho)
                                                                           S
Polytypes, \sigma
                                       ::=
                                                \forall a.\sigma
                                                                           \mathsf{bind}\ a\ \mathsf{in}\ \sigma
                                                                            Μ
                                                [a \mapsto \tau] \sigma
Terms, t, u
                                       ::=
                                                i
                                                                                                    Literal
                                                                                                     Variable
                                                \boldsymbol{x}
                                                \lambda x.t
                                                                            bind x in t
                                                                                                    Abstraction
                                                                                                     Application
                                                t u
                                                \lambda(x::\sigma).t
                                                                           \mathsf{bind}\ x\ \mathsf{in}\ t
                                                                                                    Typed abstraction
                                                \mathtt{let}\; x = u \; \mathtt{in} \; t
                                                                           \mathsf{bind}\;x\;\mathsf{in}\;t
                                                                                                    Local binding
                                                t :: \sigma
                                                                                                    Type annotation
                                                                           S
                                                (t)
                                                t[x \leadsto t']
                                                                           Μ
value, v
                                                \lambda x.t
                                                                           \mathsf{bind}\ x\ \mathsf{in}\ t
                                                \lambda(x::\sigma).t
                                                                            \mathsf{bind}\;x\;\mathsf{in}\;t
Typing contexts, \Gamma
                                                \epsilon
                                                                                                    empty context
                                                \Gamma, x : \sigma
                                                                                                     assumption
fv
                                                fv(t)
                                                                           Μ
ftvany
                                       ::=
                                                \mathrm{ftv}(\tau)
                                                                            Μ
                                                ftv(\rho)
                                                                            Μ
                                                ftv(\sigma)
                                                                           Μ
                                                \mathrm{ftv}(\Gamma)
                                                                            Μ
terminals
                                                ::
                                                fv
```

ftv

fv ftvany terminals formula

## $\Gamma \vdash t : \sigma$

$$\begin{array}{l} \overline{\Gamma \vdash i : \mathtt{Int}} & \mathtt{TYP\_INT} \\ \\ \underline{uniq} \, \Gamma \\ \underline{x : \sigma \in \Gamma} \\ \overline{\Gamma \vdash i : \sigma} & \mathtt{TYP\_VAR} \\ \\ \underline{\Gamma, x : \tau_1 \vdash t : \tau_2} \\ \overline{\Gamma \vdash (\lambda x.t) : (\tau_1 \to \tau_2)} & \mathtt{TYP\_ABS} \\ \\ \underline{\Gamma \vdash t : \tau_1 \to \tau_2} \\ \underline{\Gamma \vdash u : \tau_1} \\ \overline{\Gamma \vdash t \ u : \tau_2} & \mathtt{TYP\_APP} \end{array}$$

$$\begin{array}{l} \Gamma \vdash u : \sigma \\ \hline \Gamma, x : \sigma \vdash t : \rho \\ \hline \Gamma \vdash \mathsf{let} \ x = u \ \mathsf{in} \ t : \rho \\ \hline \end{array} \quad \begin{array}{l} \mathsf{TYP\_LET} \\ \\ \mathsf{closed} \ \sigma \\ \hline \Gamma \vdash t : \sigma \\ \hline \hline \Gamma \vdash (t :: \sigma) : \sigma \\ \hline \end{array} \quad \begin{array}{l} \mathsf{TYP\_ANNOT} \\ \hline \\ \hline \Gamma \vdash t : \forall a. \rho \\ \hline \hline \Gamma \vdash t : \forall a. \rho \\ \hline \hline \Gamma \vdash t : [a \mapsto \tau] \ \rho \\ \hline \end{array} \quad \begin{array}{l} \mathsf{TYP\_INST} \\ \hline \end{array}$$

 $t \longrightarrow u$ 

$$\frac{u \longrightarrow u'}{\text{let } x = u \text{ in } t \longrightarrow \text{let } x = u' \text{ in } t} \quad \text{STEP\_LET1}$$

$$\frac{1}{\text{let } x = v \text{ in } t \longrightarrow t \left[x \leadsto v\right]} \quad \text{STEP\_LET}$$

$$\frac{t \longrightarrow t'}{t \ u \longrightarrow t' \ u} \quad \text{STEP\_APP1}$$

$$\frac{u \longrightarrow u'}{(\lambda x.t) \ u \longrightarrow (\lambda x.t) \ u'} \quad \text{STEP\_APP2}$$

$$\frac{u \longrightarrow u'}{(\lambda (x::\sigma).t) \ u \longrightarrow (\lambda (x::\sigma).t) \ u'} \quad \text{STEP\_APP}$$

$$\frac{u \longrightarrow u'}{(\lambda (x::\sigma).t) \ u \longrightarrow (\lambda (x::\sigma).t) \ u'} \quad \text{STEP\_ANNOT\_APP2}$$

$$\frac{(\lambda (x::\sigma).t) \ v \longrightarrow t \left[x \leadsto v\right]}{t :: \sigma \longrightarrow t} \quad \text{STEP\_ERASE}$$

Definition rules: 16 good 0 bad Definition rule clauses: 31 good 0 bad