

Term variables, x, y, z variables
Type variables, a, b type variables
Integer, i

Monotypes, τ	$::=$ $ $ Int $ $ a $ $ $\tau_1 \rightarrow \tau_2$	Monotypes
Rho-types, ρ	$::=$ $ $ τ $ $ (ρ) S $ $ $[a \mapsto \tau] \mathbf{rhp}$ M	Rho-types
Polytypes, σ	$::=$ $ $ ρ $ $ $\forall a. \sigma$ bind a in σ $ $ $[a \mapsto \tau] \sigma$ M	
Terms, t, u	$::=$ $ $ i Literal $ $ x Variable $ $ $\lambda x. t$ bind x in t Abstraction $ $ $t u$ Application $ $ $\lambda(x :: \sigma). t$ bind x in t Typed abstraction $ $ let $x = u$ in t bind x in t Local binding $ $ $t :: \sigma$ Type annotation $ $ (t) S $ $ $t [x \rightsquigarrow t']$ M	
value, v	$::=$ $ $ i $ $ $\lambda x. t$ bind x in t $ $ $\lambda(x :: \sigma). t$ bind x in t	
Typing contexts, Γ	$::=$ $ $ ϵ empty context $ $ $\Gamma, x : \sigma$ assumption	
fv	$::=$ $ $ $fv(t)$ M	
$ftvany$	$::=$ $ $ $ftv(\tau)$ M $ $ $ftv(\rho)$ M $ $ $ftv(\sigma)$ M $ $ $ftv(\Gamma)$ M	
terminals	$::=$ $ $ \longrightarrow $ $ \rightarrow $ $ $::$ $ $ fv	

		ftv
		\in
		\notin
		\vdash
$formula$	$::=$	
		$judgement$
		$value\ v$
		$\text{uniq}\ \Gamma$
		$\text{lc}\ \sigma$
		$a \notin \text{ftvany}$
		$x : \sigma \in \Gamma$
$JTyping$	$::=$	
		$\Gamma \vdash t : \sigma$
$JStep$	$::=$	
		$t \longrightarrow u$
$JInst$	$::=$	
		$\vdash^{\text{inst}} \sigma \leq \rho$
$judgement$	$::=$	
		$JTyping$
		$JStep$
		$JInst$
$user_syntax$	$::=$	
		Term variables
		Type variables
		Integer
		Monotypes
		Rho-types
		Polytypes
		Terms
		$value$
		Typing contexts
		fv
		ftvany
		$terminals$
		$formula$

$$\boxed{\Gamma \vdash t : \sigma}$$

$$\begin{array}{c}
\frac{}{\Gamma \vdash i : \text{Int}} \quad \text{TYP_INT} \\
\\
\frac{\text{uniq}\ \Gamma \quad x : \sigma \in \Gamma}{\Gamma \vdash x : \sigma} \quad \text{TYP_VAR} \\
\\
\frac{\Gamma, x : \tau_1 \vdash t : \tau_2}{\Gamma \vdash (\lambda x. t) : (\tau_1 \rightarrow \tau_2)} \quad \text{TYP_ABS}
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma \vdash t : \tau_1 \rightarrow \tau_2 \quad \Gamma \vdash u : \tau_1}{\Gamma \vdash t u : \tau_2} \text{ TYP_APP} \\
\\
\frac{\Gamma \vdash u : \sigma \quad \Gamma, x : \sigma \vdash t : \rho}{\Gamma \vdash \text{let } x = u \text{ in } t : \rho} \text{ TYP_LET} \\
\\
\frac{\text{lc } \sigma \quad \Gamma \vdash t : \sigma}{\Gamma \vdash (t :: \sigma) : \sigma} \text{ TYP_ANNOT} \\
\\
\frac{\Gamma \vdash t : \rho}{\Gamma \vdash t : \forall a. \rho} \text{ TYP_GEN} \\
\\
\frac{\Gamma \vdash t : \forall a. \rho}{\Gamma \vdash t : [a \mapsto \tau] \rho} \text{ TYP_INST}
\end{array}$$

$$\boxed{t \longrightarrow u}$$

$$\begin{array}{c}
\frac{u \longrightarrow u'}{\text{let } x = u \text{ in } t \longrightarrow \text{let } x = u' \text{ in } t} \text{ STEP_LET1} \\
\\
\frac{}{\text{let } x = v \text{ in } t \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_LET} \\
\\
\frac{t \longrightarrow t'}{t u \longrightarrow t' u} \text{ STEP_APP1} \\
\\
\frac{u \longrightarrow u'}{(\lambda x. t) u \longrightarrow (\lambda x. t) u'} \text{ STEP_APP2} \\
\\
\frac{}{(\lambda x. t) v \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_APP} \\
\\
\frac{u \longrightarrow u'}{(\lambda(x :: \sigma). t) u \longrightarrow (\lambda(x :: \sigma). t) u'} \text{ STEP_ANNOT_APP2} \\
\\
\frac{}{(\lambda(x :: \sigma). t) v \longrightarrow t[x \rightsquigarrow v]} \text{ STEP_ANNOT_APP} \\
\\
\frac{t \longrightarrow t'}{t :: \sigma \longrightarrow t' :: \sigma} \text{ STEP_ERASE1} \\
\\
\frac{}{t :: \sigma \longrightarrow t} \text{ STEP_ERASE}
\end{array}$$

$$\boxed{\vdash^{\text{inst}} \sigma \leq \rho}$$

$$\begin{array}{c}
\frac{\text{lc } \rho}{\vdash^{\text{inst}} \rho \leq \rho} \text{ INST_REFL} \\
\\
\frac{\vdash^{\text{inst}} [a \mapsto \tau] \sigma \leq \rho}{\vdash^{\text{inst}} \forall a. \sigma \leq \rho} \text{ INST_POLY}
\end{array}$$

Definition rules: 19 good 0 bad
 Definition rule clauses: 37 good 0 bad