

## Lecture 8 **Raster Analysis**

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Add xy data as a way to add sampling data  
In the lab, we will talk about viewing spatial  
information using ArcCatalog, or “define projection”

### Raster Analysis

Raster cells store data (nominal, ordinal, interval/ratio)

Complex constructs built from raster data

- Connected cells can be formed into networks

- Related cells can be grouped into neighborhoods or regions

Examples:

- Predict fate of pollutants in the atmosphere

- The spread of disease

- Animal migrations

- Crop yields

- EPA - hazard analysis of urban superfund sites

- Local to global scale forest growth analysis

## Map algebra

### Cell by Cell combination of raster data layers

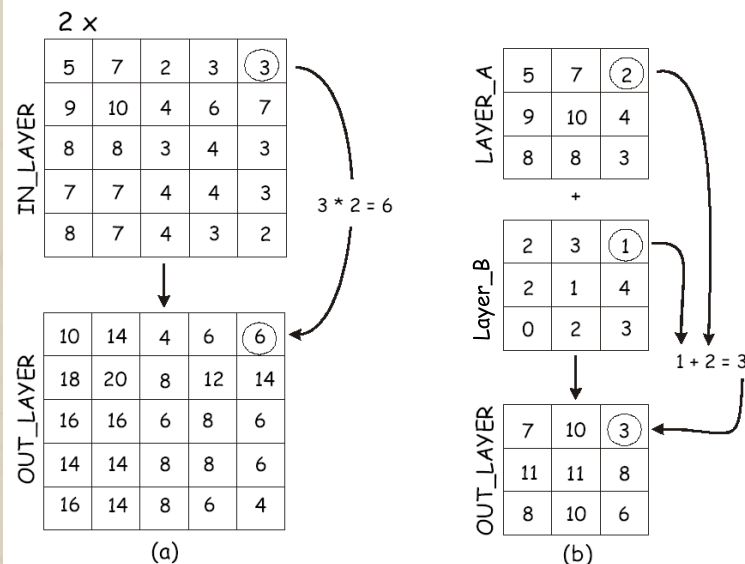
Each number represents a value at a raster cell location

Simple operations can be applied to each number

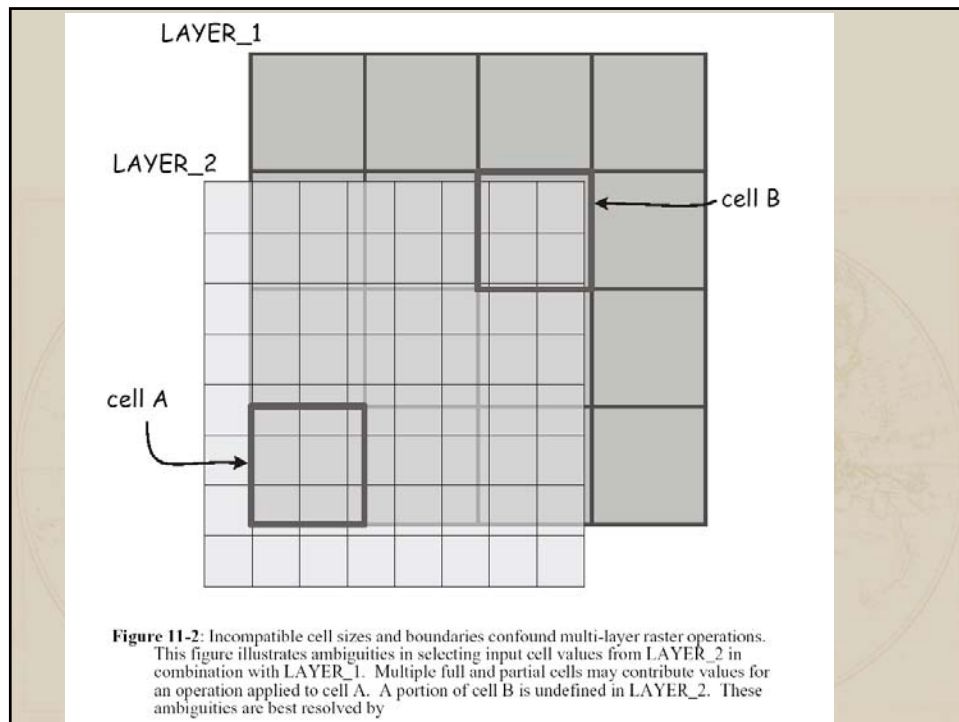
Raster layers may be combined through operations

Addition, subtraction and multiplication

Entails operations applied to one or more raster data layers.

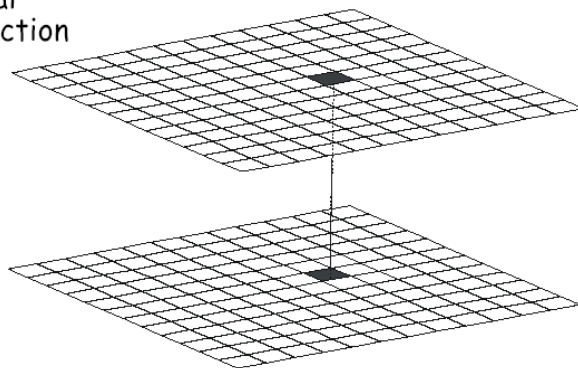


**Figure 11-1:** An example of raster operations. On the left side (a) each input cell is multiplied by the value 2, and the result written stored in the corresponding output location. The right side (b) of the figure illustrates layer addition.



## Scope: Local operations

local  
function



e.g.,

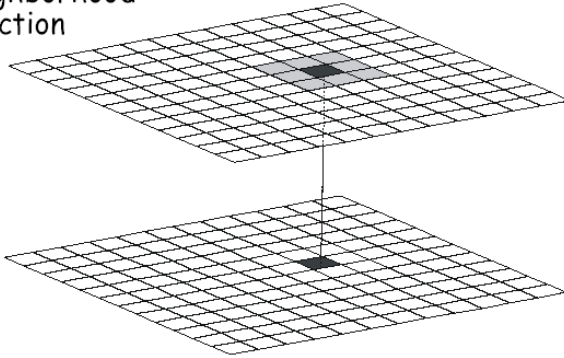
10	12	42
30	9	4
-12	8	15

plus 4

14	16	46
34	13	8
-8	12	19

## Scope: Neighborhood operations

neighborhood  
function



e.g.,

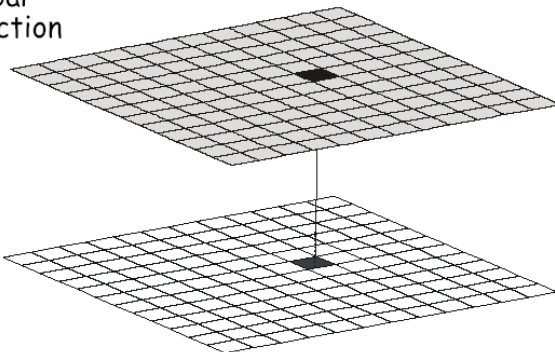
10	12	42
30	9	4
-12	8	15

neighborhood  
maximum

33	42	42
30	42	42
30	30	17

## Scope: Global operation

global  
function



e.g.,

10	12	42
30	9	4
-12	8	15

global  
maximum

42	42	42
42	42	42
42	42	42

## Local Functions

Function	Description
Add, subtract, multiply, and divide	cell-by-cell combination with the arithmetic operation
ABS	Absolute value of each cell
EXP, EXP10, LN, LN10	Applies base e and base 10 exponentiation and logarithms
SIN, COS, TAN, ASIN, ACOS, ATAN	Apply trigonometric functions on a cell-by-cell basis
INT, TRUNC	Truncate cell values, output integer portion
MODULUS	Assigns the decimal portion of each cell
ROUND	Rounds a cell value up or down to nearest integer value
SQRT, ROOT	Calculates the square root or specifies other root of each cell value
POWER	Raises each cell to a defined power

## Logical Operations AND

Non-zero values are “true”, zero values are “false”  
N = null values

Input				Output			
1	3	1	1	0	1	0	1
0	N	2	-1	0	N	1	1
1	2	5	0	0	1	N	0
0	1	N	N	0	1	N	N

AND      =

## Logical Operations OR

Non-zero values are “true”, zero values are “false”  
N = null values

1	3	1	1	OR	0	1	0	9	=	1	1	1	1
0	N	2	-1		0	5	2	5		0	N	1	1
1	2	5	0		0	2	N	2		1	1	N	1
0	1	N	N		0	-3	4	8		0	1	N	N

## Logical Operations NOT

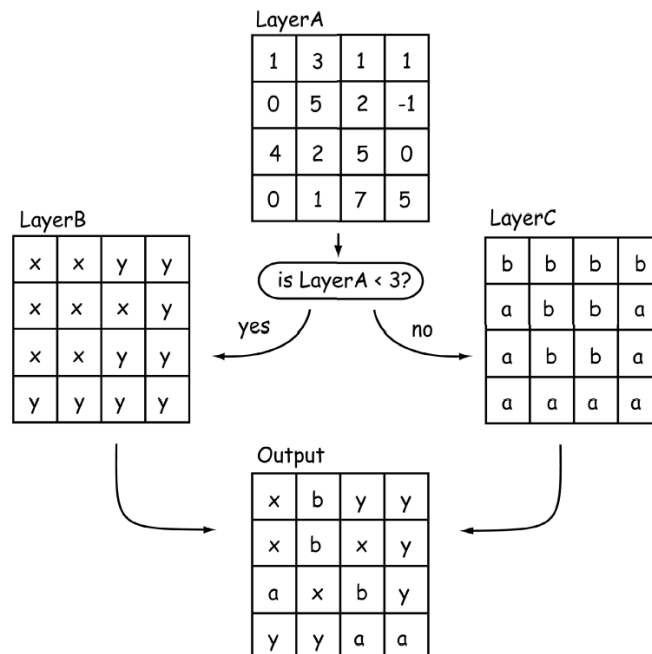
NOT	1	3	1	1	=	0	0	0	0
	0	N	2	-1		1	N	0	0
	1	2	5	0		0	0	0	1
	0	1	N	N		1	0	N	N

## More Local Functions – logical comparisons

	Input		Output																																
a)	<table> <tr><td>1</td><td>3</td><td>1</td><td>1</td></tr> <tr><td>0</td><td>N</td><td>2</td><td>-1</td></tr> <tr><td>1</td><td>2</td><td>5</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>N</td><td>N</td></tr> </table>	1	3	1	1	0	N	2	-1	1	2	5	0	0	1	N	N	less than	<table> <tr><td>0</td><td>1</td><td>0</td><td>9</td></tr> <tr><td>0</td><td>5</td><td>2</td><td>5</td></tr> <tr><td>0</td><td>2</td><td>N</td><td>2</td></tr> <tr><td>0</td><td>-3</td><td>4</td><td>8</td></tr> </table>	0	1	0	9	0	5	2	5	0	2	N	2	0	-3	4	8
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0	1	N	0																																
1	0	N	N																																

### Conditional Function

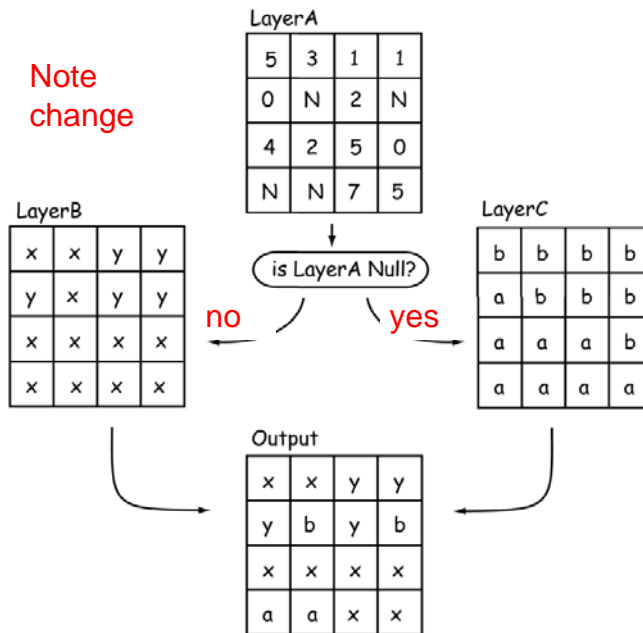
Output = CON (LayerA < 3, LayerB, LayerC)



## Nested Functions

Output = CON(ISNULL(LayerA), LayerC, Layer B)

Note  
change



## Overlay in Raster

### Union and Clip

### Cell by Cell Addition or Multiplication

Attribute combinations corresponding to  
unique cell combinations



## A Problem with Raster Analysis

- Too many cells
- Typically, one-to-one relationship between spatial object and attribute table
- Rasters have multiple cells per feature
- Attribute tables grow to be unwieldy

- a)

b)

A	A	A	A	B	B	B	B	B	B
A	A	A	A	B	B	B	B	B	B
A	A	A	A	B	B	B	B	B	B
A	A	A	B	B	B	B	B	B	B
A	A	A	C	C	B	B	B	B	B
C	C	C	C	C	D	D	D	D	D
C	C	C	C	C	D	D	D	D	D
C	C	C	C	C	D	D	D	D	D
C	C	C	C	C	D	D	D	D	D
C	C	C	C	C	D	D	D	D	D

one to one

ID	type	area
1	A	16.8
2	B	22.2
3	C	18.4
4	D	20.7

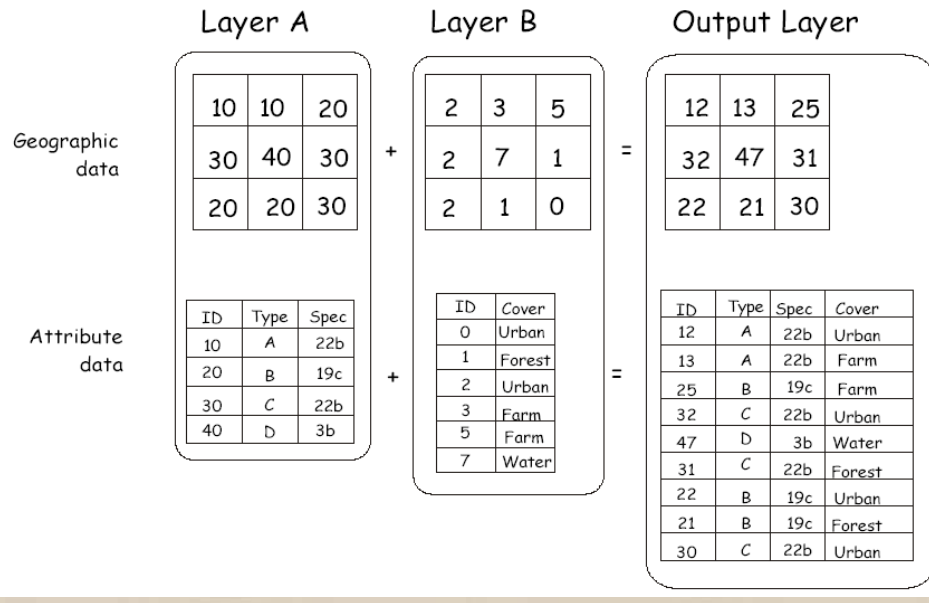
one to many

ID	type	area
1	A	16.8
2	B	22.2
3	C	18.4
4	D	20.7

one to one

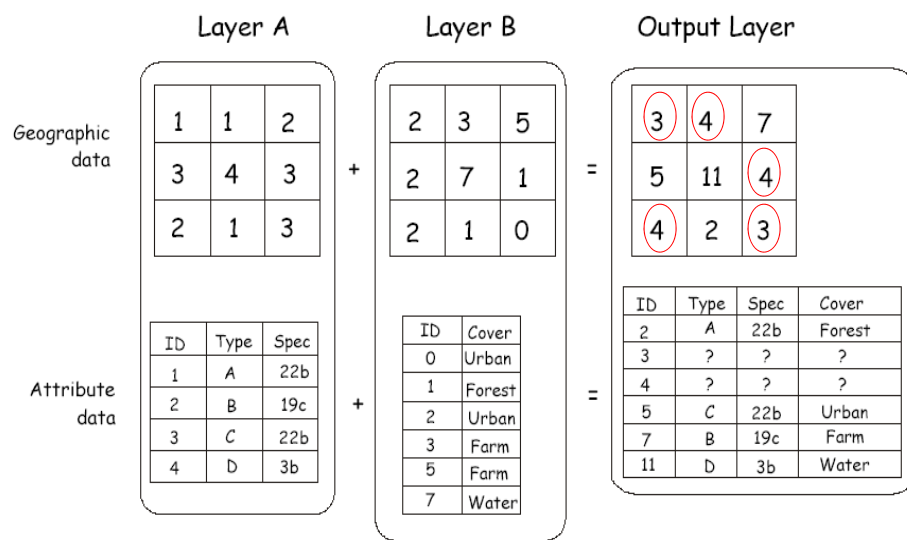
ID	type	area
1	A	0.8
2	A	0.8
3	A	0.8
4	A	0.8
5	B	0.8
6	B	0.8
7	B	0.8
100	D	0.8

## Raster overlay as addition

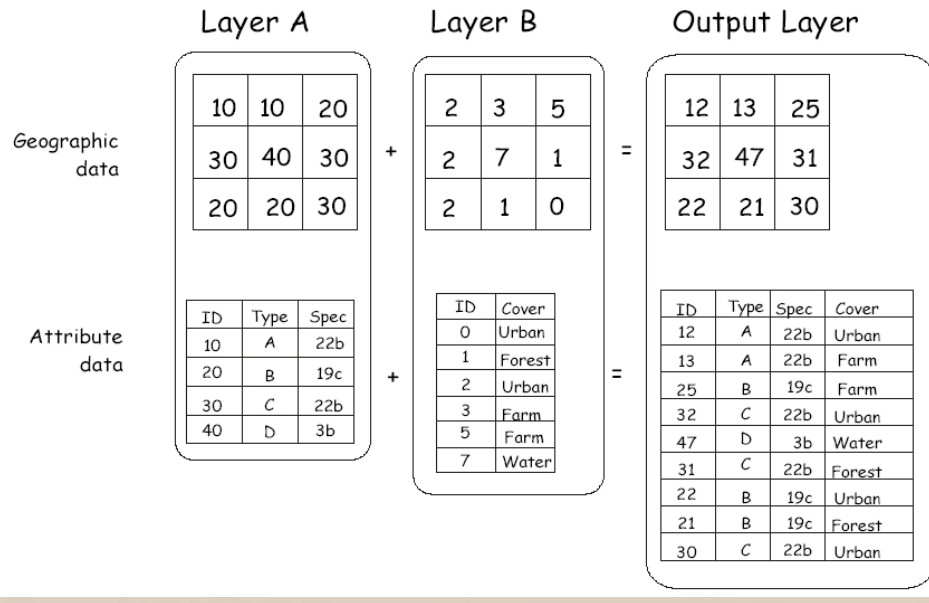


## Raster Overlay

Output layer **DOES NOT**  
have unique records



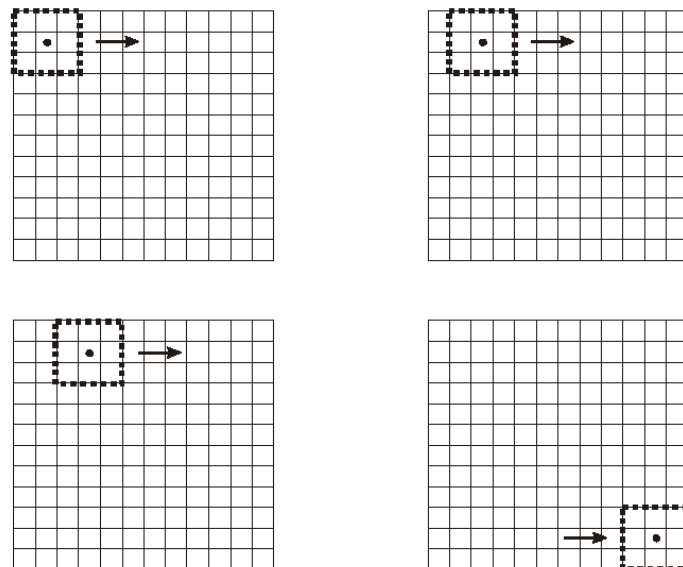
## What to do? First multiply Layer A by 10



## Neighborhood Operations

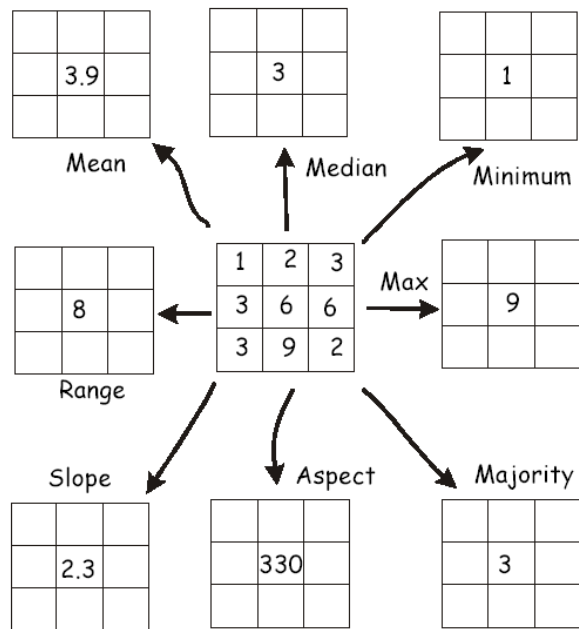
### Moving Windows

(Windows can be any size; often odd to provide a center)

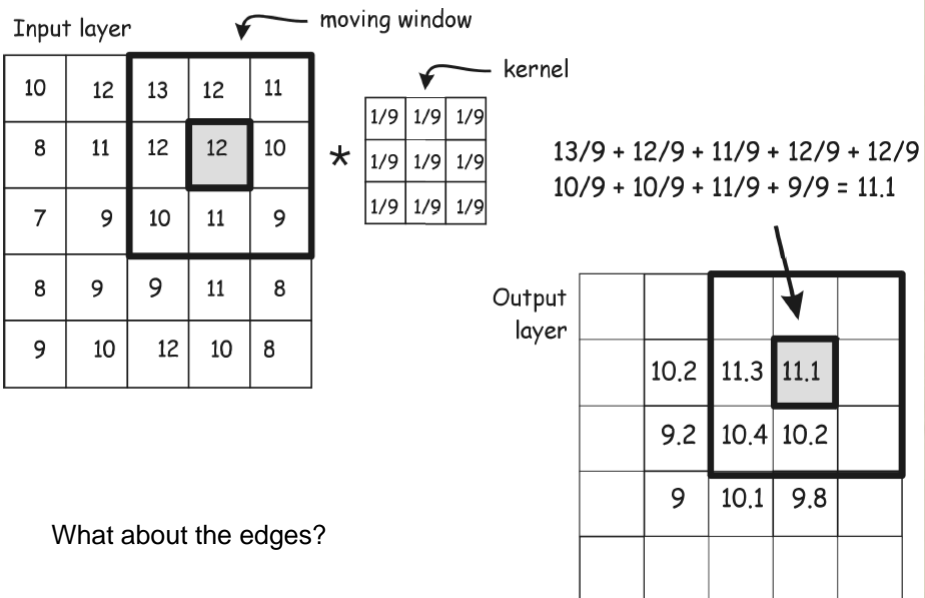


**Figure 11-4:** The concept of a moving window in raster neighborhood operations. Here a 3 by 3 window is swept from left to right and from top to bottom across a raster layer. The window at each location defines the input cells used in the raster operation.

## Neighborhood Operations



## Neighborhood Operations: Mean Function



## Neighborhood Operations:

Separate edge kernels can be used

## Mean function kernels

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

$1/6$	$1/6$	$1/6$
$1/6$	$1/6$	$1/6$

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

example application,  
lower right corner

10	12	13	12	11
8	11	12	12	10
7	9	10	11	9
8	9	9	11	8
9	10	12	10	8

1/6	1/6
1/6	1/6
1/6	1/6

$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$

1/6	1/6
1/6	1/6
1/6	1/6

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

1/6	1/6	1/6
1/6	1/6	1/6

$\frac{1}{4}$	$\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$

$$\frac{1}{4} \cdot 11 + \frac{1}{4} \cdot 8 + \frac{1}{4} \cdot 10 + \frac{1}{4} \cdot 8 = 9\frac{1}{4}$$

		$9\frac{1}{4}$

Example: Identifying spatial differences in a raster layer



980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	940	940			
980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	940	940	940	940	94
980	980	980	980	980	900	900	900	900	90
980	980	980	980	980	900	900	900	900	90
980	980	980	980	980	900	900	900	900	90
980	980	980	980	980	900	900	900	900	90

## Kernels

0	0	0
1	0	-1
0	0	0

horizontal  
difference

0	1	0
0	0	0
0	-1	0

vertical  
difference

Output A

[illegible]

Output B

[illegible]

## Raster Analysis

Moving windows and kernels can be used with a mean kernel to reduce the difference between a cell and surrounding cells. *(done by average across a group of cells)*

Raster data may also contain “noise”; values that are large or small relative to their spatial context.  
*(Noise often requiring correction or smooth(ing))*

Known as “high-pass” filters

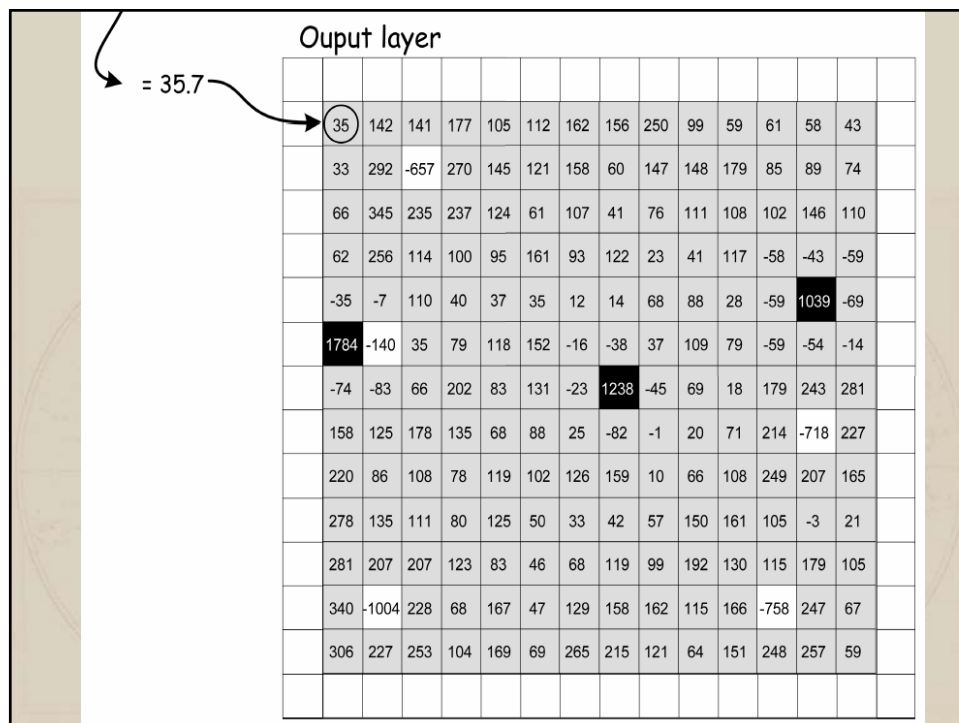
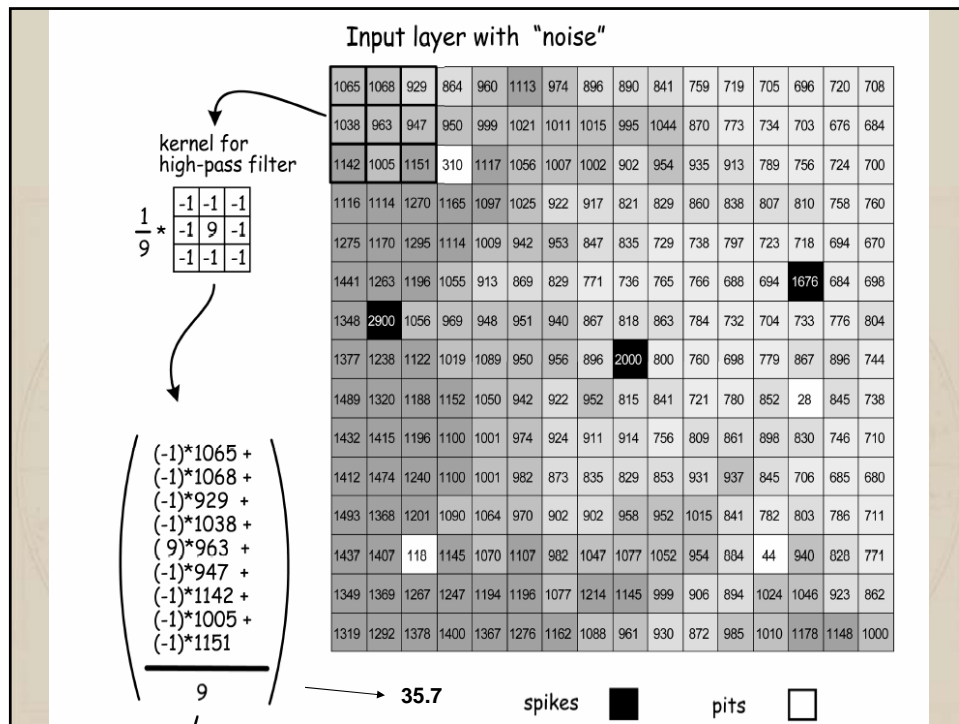
The identified spikes or pits can then be corrected or removed by editing

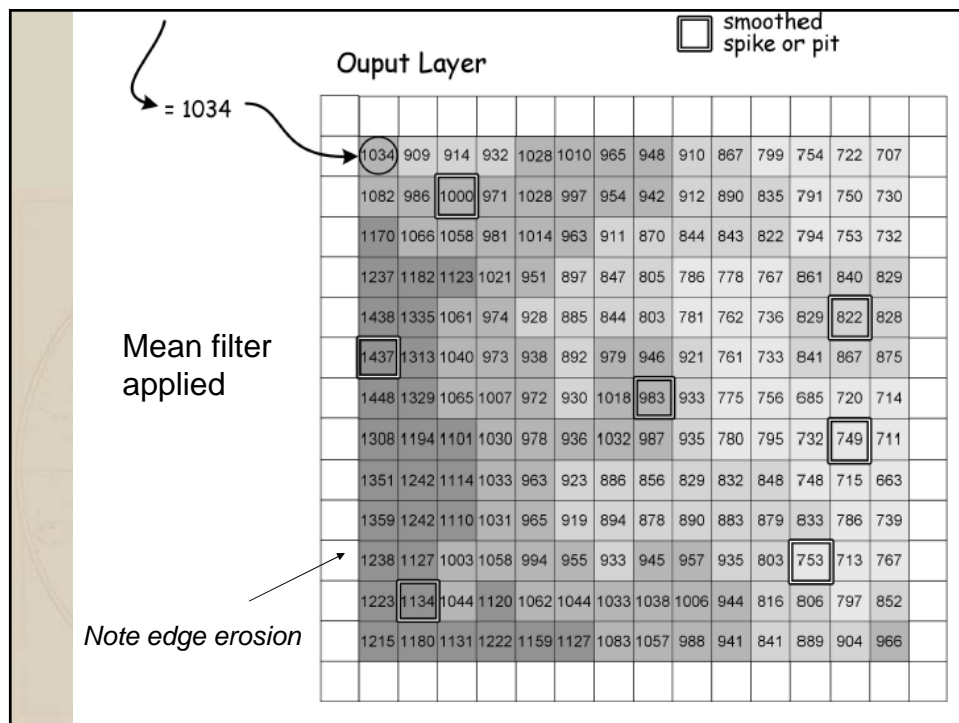
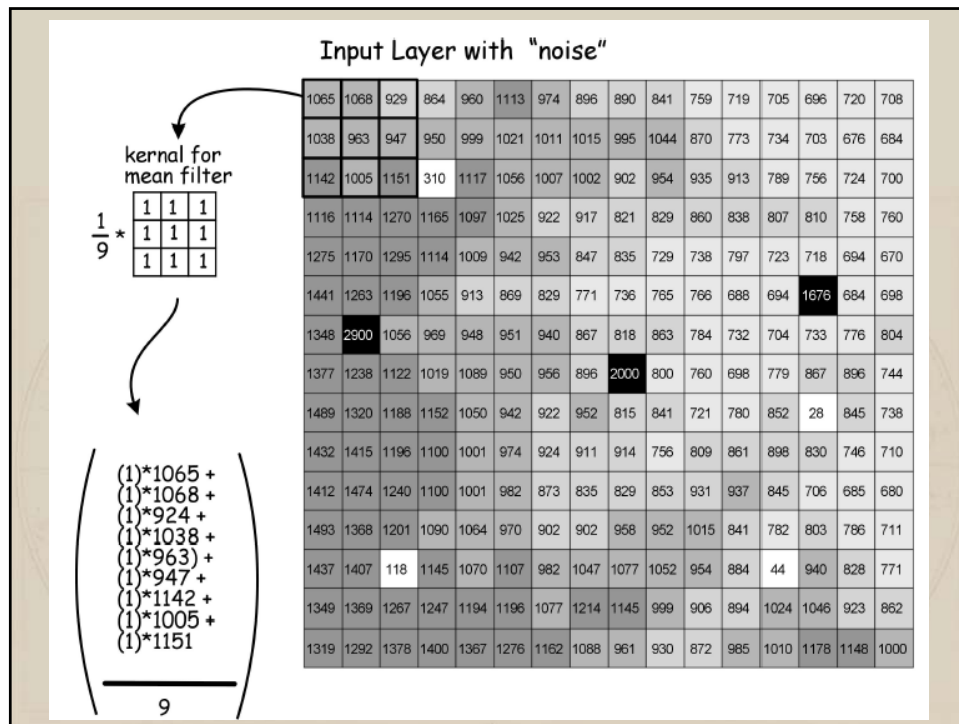
## Raster Analysis

### High pass filters

Return:

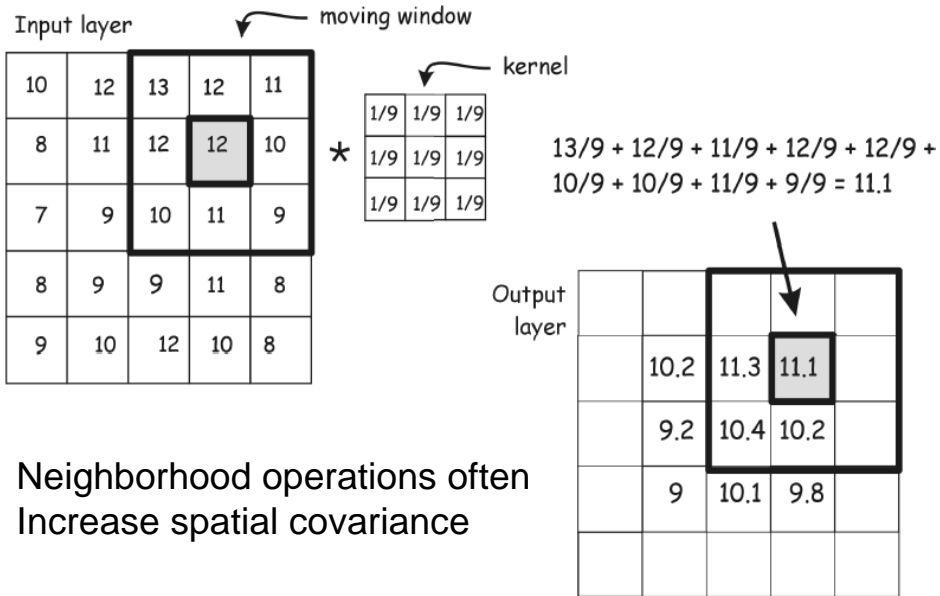
- Small values when smoothly changing values.
- Large positive values when centered on a spike
- Large negative values when centered on a pit







Moving windows: Consider the overlap in cell calculations



## Cost Surface

The minimum cost of reaching cells in a layer **from** one or more sources cells

“travel costs”

*Time to school; hospital;*

*Chance of noxious foreign weed spreading out from an introduction point*

- Units can be money, time, etc.
- Distance measure is combined with a fixed cost per unit distance to calculate travel cost
- If multiple source cells, the lowest cost is typically placed in the output cell

$$\text{Distance} = \sqrt{(x^2 + y^2)}$$

$$\text{e.g., } D_1 = \sqrt{(20^2 + 10^2)} = 22.4$$

20	10	source cell
22.4	14.1	10
28.3	22.4	20

10  
units

$$\text{Cost} = \text{Distance} * \text{fixed cost factor}$$

e.g.

$$\text{Cost} = \text{Distance} * 2$$

40	20	source cell
44.8	28.2	20
56.6	44.8	40

**Figure 11-13:** A cost surface based on a fixed cost per unit distance. Minimum distance from a set of source cells is multiplied by a fixed cost factor to yield a cost surface.

## Friction Surface *(version of a Cost Surface)*

The cell values of a friction surface represent the cost per unit travel distance for crossing each cell – varies from cell to cell

Used to represent areas with variable travel cost.

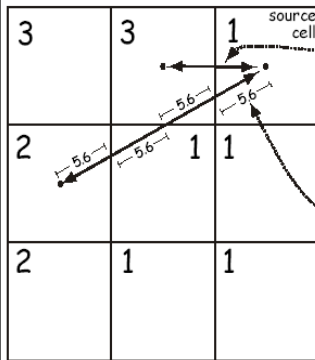
### Notes:

- Barriers can be added.
- Multiple paths are often not allowed
- Cost surfaces are always related to a source cell(s); “from something”
- The center of a cell is always used the distance calculations

cost = cell distance \* friction

output cost surface

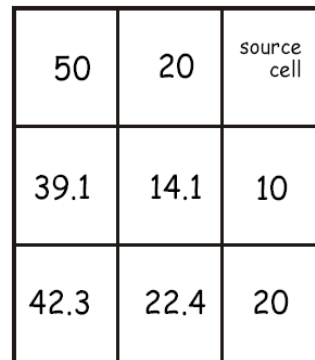
friction surface



$$\begin{aligned} \text{Cost} &= (5 * 1) \\ &+ (5 * 3) \\ &\hline &20 \end{aligned}$$

$$\begin{aligned} \text{Cost} &= (5.6 * 1) \\ &+ (5.6 * 3) \\ &+ (5.6 * 1) \\ &+ (5.6 * 2) \\ &\hline &39.1 \end{aligned}$$

← 10 units →



← 10 units →

**Figure 11-14:** A cost surface based on spatially-variable travel costs. A friction surface specifies the spatially varying cost of travelling through raster cells. The distance traversed through each cell is multiplied by the cost in the friction surface. The values are summed for each path to yield a total cost.