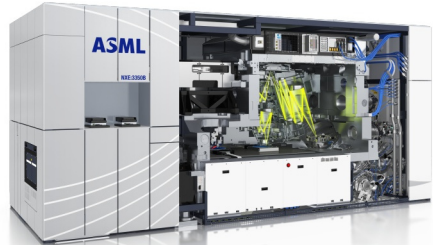
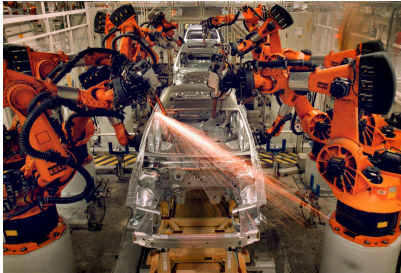


# Compositional Specification of Functionality and Timing of Manufacturing Systems

Bram van der Sanden, João Bastos, Jeroen Voeten,  
Marc Geilen, Michel Reniers, Twan Basten,  
Johan Jacobs, and Ramon Schiffelers



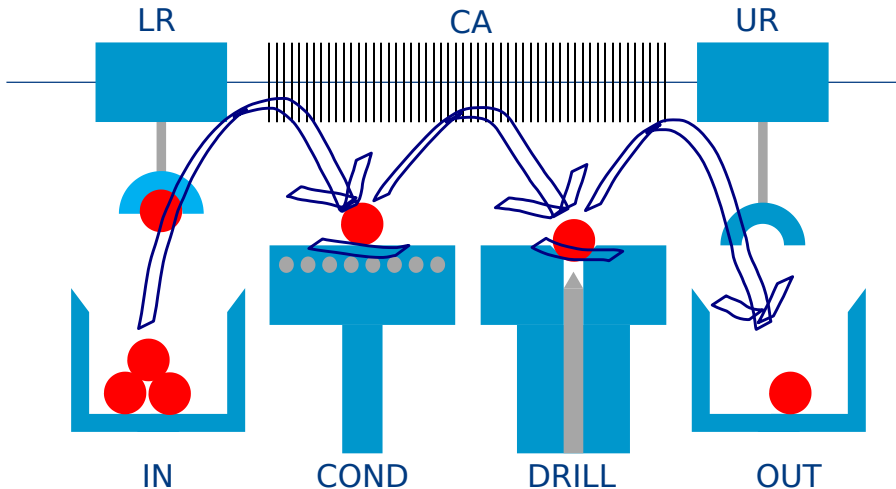


## Goal:

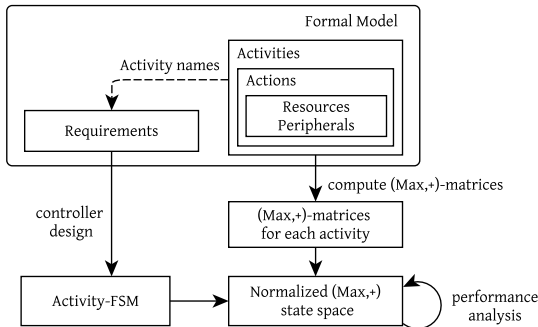
- ▶ Formal modeling approach for manufacturing systems with **Compositional** Specification of **Functionality** and **Timing**.

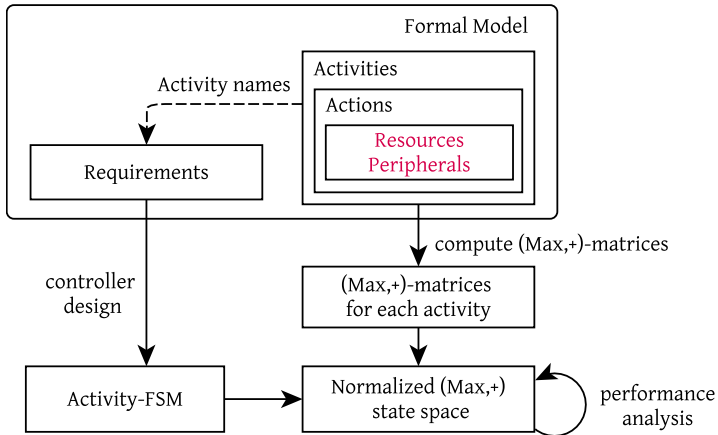
# Example Manufacturing System

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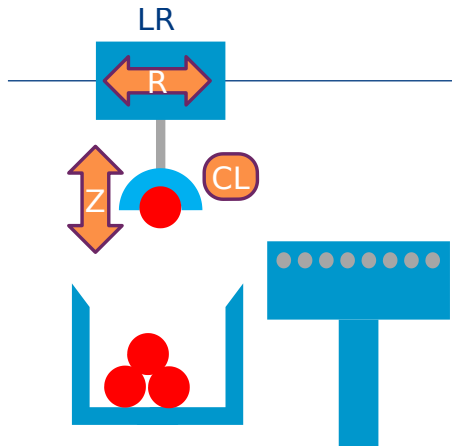


**Modeling** and **Analysis** to find a throughput-optimal safe controller for nominal behavior.



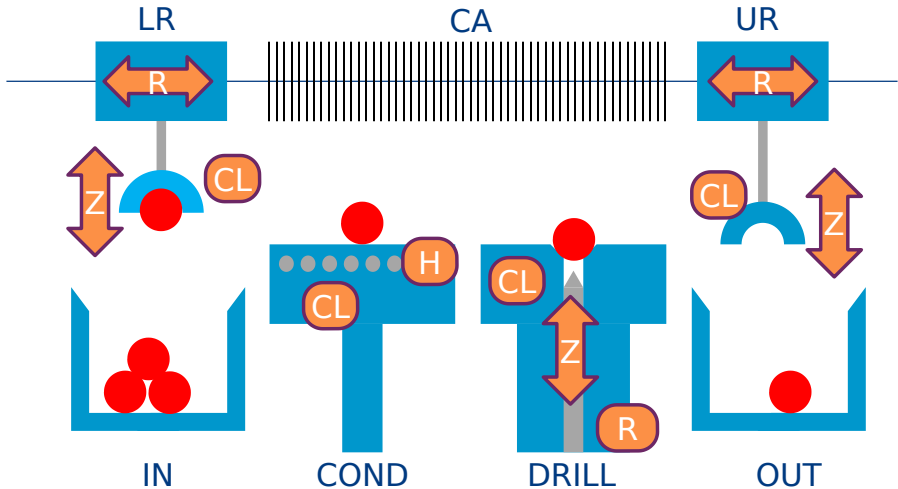


- ▶ Set of peripherals that can execute a number of actions.
- ▶ Peripherals are aggregated into resources.
- ▶ Resource Load Robot LR has peripherals motor R, motor Z, clamp CL.



# Formal Model: Resources and Peripherals

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Resources and peripherals: model the system components.

System behavior is modeled on three levels:

1. **Actions** executed by peripherals.



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System behavior is modeled on three levels:

1. **Actions** executed by peripherals.
2. **Activities** to describe scenarios of end-to-end deterministic behavior.

An activity consists of a set of actions and dependencies among these actions.

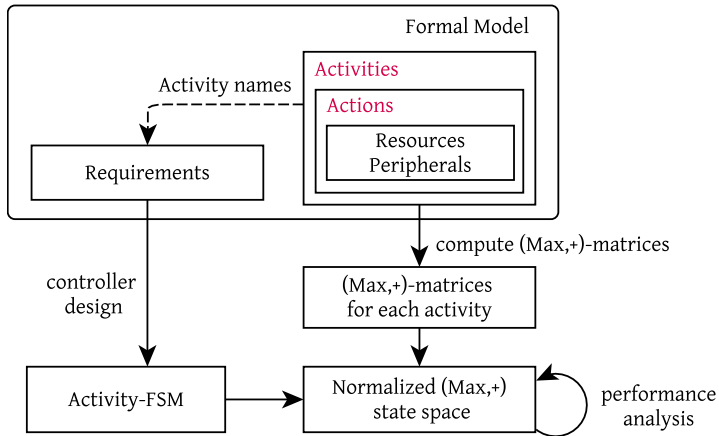
Resources and peripherals: model the system components.

System behavior is modeled on three levels:

1. **Actions** executed by peripherals.
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An activity consists of a set of actions and dependencies among these actions.

3. **Activity sequences** describe orderings of activities.



**Activities** in the Twilight system:

Operations on a product:

- ▶ Condition
- ▶ Drill

Moving a product:

- ▶ LR\_PickFromInput
- ▶ LR\_PickFromCond
- ▶ LR\_PickFromDrill
- ▶ LR\_PutOnCond
- ▶ LR\_PutOnDrill
- ▶ UR\_PickFromCond
- ▶ UR\_PickFromDrill
- ▶ UR\_PutOnCond
- ▶ UR\_PutOnDrill
- ▶ UR\_PutOnOutput

**Activities** in the Twilight system:

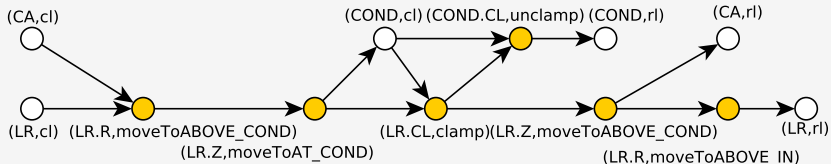
Operations on a product:

- ▶ Condition
- ▶ Drill

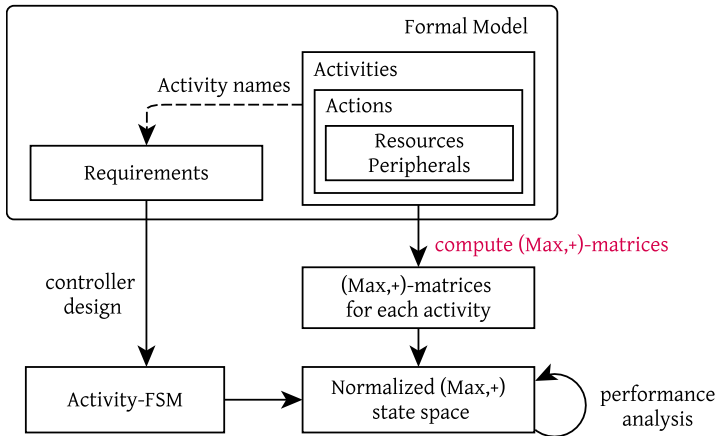
Moving a product:

- ▶ LR\_PickFromInput
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- ▶ UR\_PutOnCond
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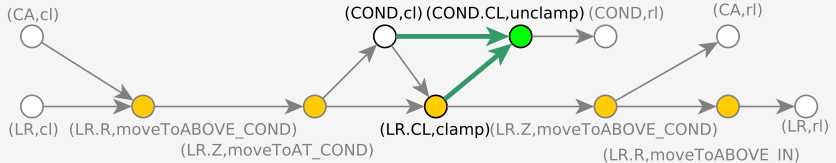
LR\_PickFromCond



- ▶ **Function of activity:**  
Move LR to COND, pick up the ball, move back to home position
- ▶ **Actions:** *cl* claim, *rl* release, unclamp, clamp, moves
- ▶ **Involved resources:**  
Collision Area (CA), Load Robot (LR), Conditioner (COND)



## LR\_PickFromCond

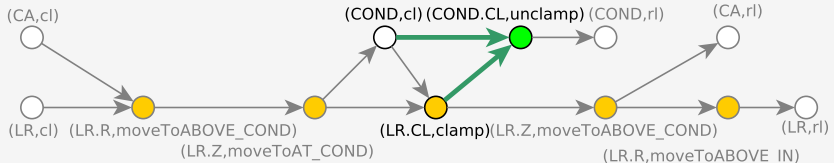


Two essential characteristics in activity execution:

1. **synchronization**: waits for incoming dependencies to finish



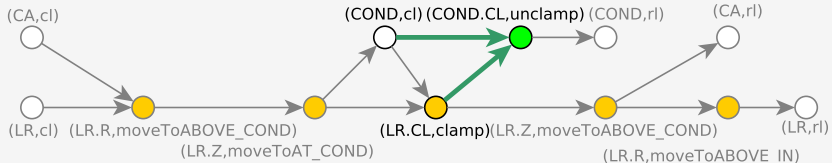
## LR\_PickFromCond



Two essential characteristics in activity execution:

1. **synchronization**: waits for incoming dependencies to finish
2. **delay**: duration of execution before completion

LR\_PickFromCond

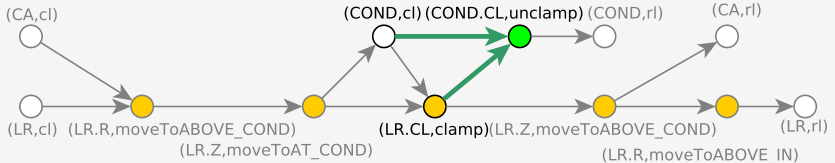


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These characteristics correspond well to the  $(\max,+)$  operators **max** and **addition** in  $(\max,+)$  algebra.

LR\_PickFromCond



Two essential characteristics in activity execution:

1. **synchronization**: waits for incoming dependencies to finish
2. **delay**: duration of execution before completion

These characteristics correspond well to the  $(\max,+)$  operators **max** and **addition** in  $(\max,+)$  algebra.

We use this algebra to capture the timing behavior of the activity in a  $(\max,+)$  **matrix**.

► (max,+) **matrix**:  $M_{LR\_PickFromCond} = \begin{bmatrix} .. & .. & .. \\ .. & .. & .. \\ .. & .. & .. \end{bmatrix}$

- ▶ (max,+) **matrix**:  $M_{LR\_PickFromCond} = \begin{bmatrix} .. & .. & .. \\ .. & .. & .. \\ .. & .. & .. \end{bmatrix}$
- ▶ resource availability vector:  $\gamma_{begin} = \begin{bmatrix} \gamma_{begin}(\text{CA}) \\ \gamma_{begin}(\text{LR}) \\ \gamma_{begin}(\text{COND}) \end{bmatrix}$

- ▶ (max,+) **matrix**:  $M_{LR\_PickFromCond} = \begin{bmatrix} .. & .. & .. \\ .. & .. & .. \\ .. & .. & .. \end{bmatrix}$
- ▶ resource availability vector:  $\gamma_{begin} = \begin{bmatrix} \gamma_{begin}(\text{CA}) \\ \gamma_{begin}(\text{LR}) \\ \gamma_{begin}(\text{COND}) \end{bmatrix}$
- ▶ New vector  $\gamma_{end}$  by matrix multiplication in (max,+) algebra:

$$\begin{bmatrix} \gamma_{end}(\text{CA}) \\ \gamma_{end}(\text{LR}) \\ \gamma_{end}(\text{COND}) \end{bmatrix} = \begin{bmatrix} .. & .. & .. \\ .. & .. & .. \\ .. & .. & .. \end{bmatrix} \otimes \begin{bmatrix} \gamma_{begin}(\text{CA}) \\ \gamma_{begin}(\text{LR}) \\ \gamma_{begin}(\text{COND}) \end{bmatrix}$$

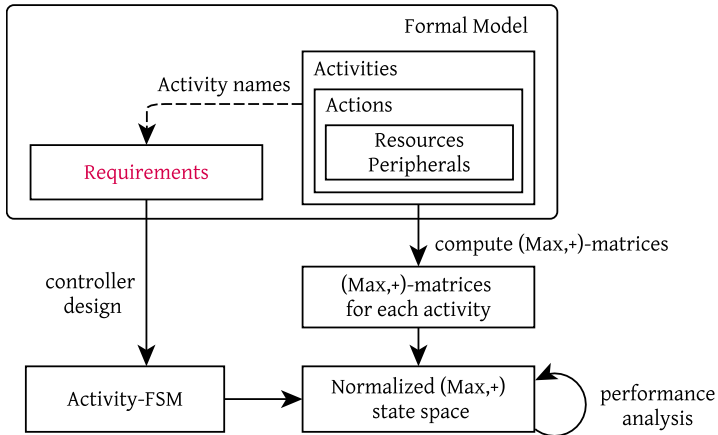
$\gamma_{end} \qquad M_{LR\_PickFromCond} \qquad \gamma_{begin}$

Now consider an **activity sequence**, for instance:

Condition ; LR\_PickFromCond.

Then, given begin system state  $\gamma_{begin}$ ,  
the end system state  $\gamma_{end}$  is given by:

$$\gamma_{end} = M_{LR\_PickFromCond} \otimes M_{Condition} \otimes \gamma_{begin}.$$





What we have so far:

- ▶ **Activities:** specify scenarios of deterministic behavior.
- ▶ **Activity sequences:** to describe orderings of activities.

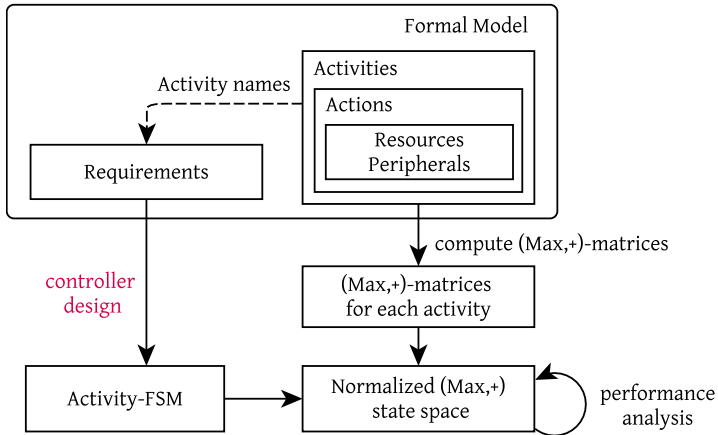
What we have so far:

- ▶ Activities: specify scenarios of deterministic behavior.
- ▶ Activity sequences: to describe orderings of activities.

Not all orderings are however valid. We need **requirements** on allowed orderings to enforce:

- ▶ No product collisions at product locations.
- ▶ No collisions of robots.
- ▶ **Life cycle of products.**





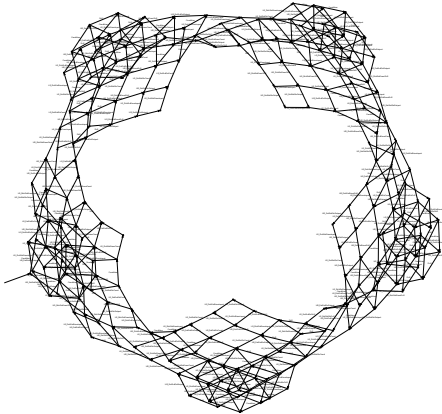
Formal Model specifies:

- ▶ Activities in system.
- ▶ Requirements on allowed activity orderings.

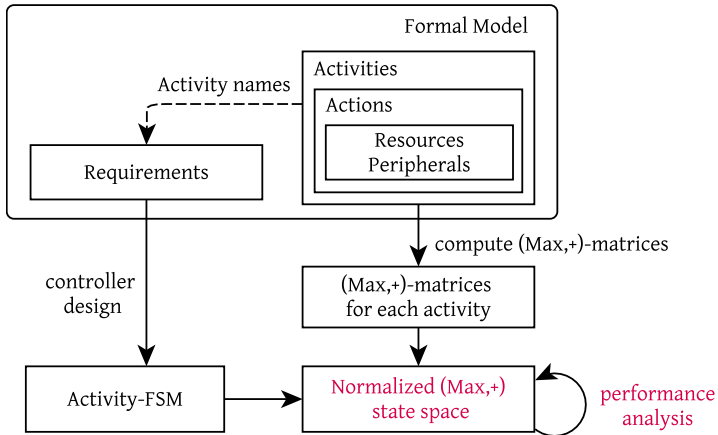
Controller Design:

- ▶ Design a controller that respects the requirements.
- ▶ For our example, we use **supervisory controller synthesis** to obtain an Activity-FSM of all allowed activity sequences.
- ▶ Activity-FSM is guaranteed to be deadlock-free and functionally correct with respect to the requirements.
- ▶ In this step we can **abstract from the timing** !

**Activity-FSM** after synthesis (245 locations, 510 transitions):



Models all allowed activity sequences.



What we have achieved so far:

- ▶ Activity-FSM that models all allowed activity sequences.
- ▶ Timing matrix for each activity.

Now:

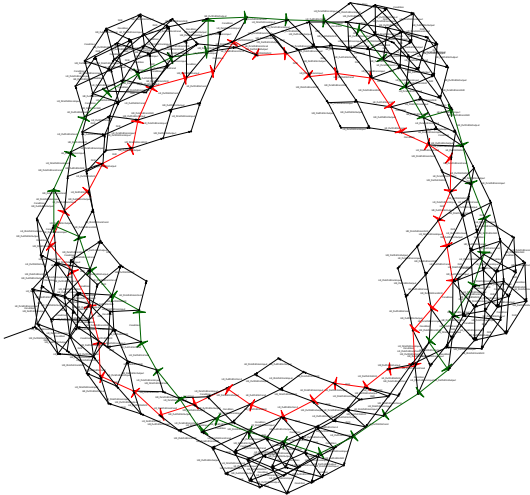
- ▶ Combine the (max,+) timing matrices and Activity-FSM.
- ▶ Explore **normalized (max,+) state space**, which is finite.
- ▶ Find optimal controller by **performance analysis** on traces in the state space.



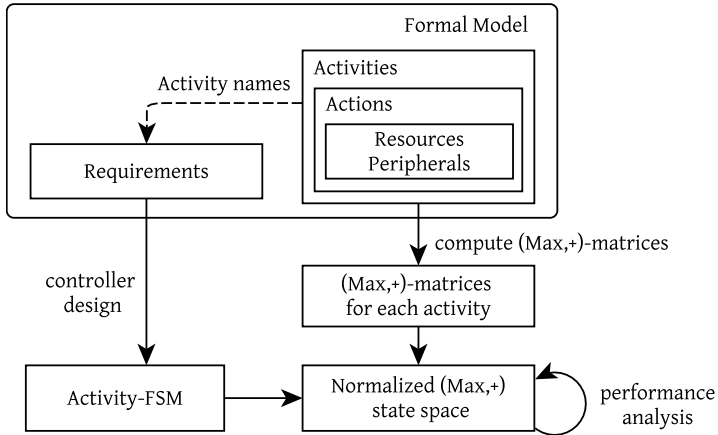
# Performance Analysis on Twilight System

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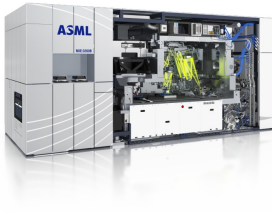
Using **performance analysis** algorithm to find guaranteed throughput and optimal controller.



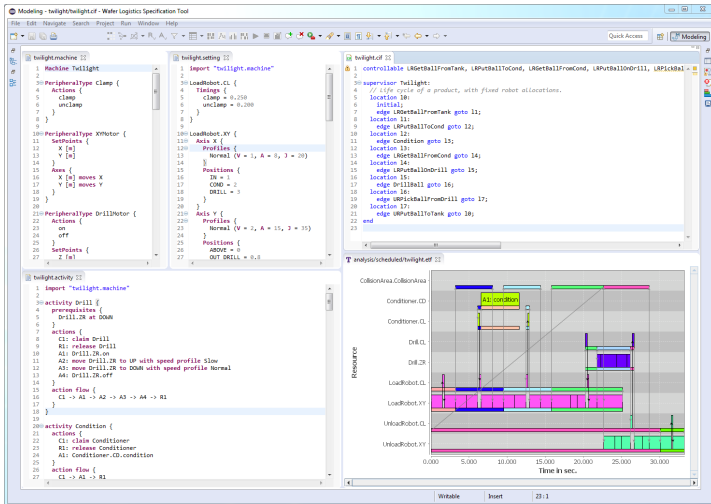
## Compositional Specification of **Functionality** and **Timing**.



- ▶ Semantic underpinning of **wafer handling specification tool**.
- ▶ Model resources, peripherals, actions, activities.
- ▶ But also: motion paths of robots, symbolic positions.
- ▶ Calculate timing of move actions from the specification.
- ▶ Current research: specification of wafer logistics for nominal behavior.



# ASML



## Research directions:

- ▶ Size of state space: modular synthesis techniques.
- ▶ More intuitive requirement modeling using state-based expressions.
- ▶ Uncontrollable behavior: extend formalism, new throughput analysis and optimization techniques.

- ▶ **Compositional** Specification of **Functionality** and **Timing**.
- ▶ **Functionality:**
  - Describe deterministic behavior using **activities**.
  - Controller choices determine the **order of these activities**.
  - Separation between deterministic behavior and nondeterministic behavior.
  - Controller design on activity level, **abstraction from timing**.
- ▶ **Timing:**
  - Fixed timing for actions.
  - Timing behavior of activities captured in **matrices**.
  - System behavior: **max-plus state space**, timing analysis.