Math 481

Instructor: Chenxi Wu wuchenxi2013@gmail.com

Office: Hill 434

Office hours: 10-11 am Tu, Wed or by appointment

Grading policy: 10% weekly homework (lowest dropped), 20%

each of the two midterms, 50% final exam.

Main topics we will cover:

- ► Review of probability
- ▶ Point estimate
- p-values and hypothesis testing
- Confidence intervals
- Bayesian statistics

Bayesian and non-Bayesian approaches to statistics

- Non-Bayesian approach: Set up a null hypothesis and try to show that observation is highly unlikely if null hypothesis is true.
- ► Bayesian approach: Assume prior distribution of some parameter, calculate posterior via Bayes formula

DID THE SUN JUST EXPLODE? (IT'S NIGHT, 50 WE'RE NOT SURE.)



FREQUENTIST STATISTICIAN:

BAYESIAN STATISTICIAN:

THE PROBABILITY OF THIS RESULT HAPPENING BY CHANCE IS \$\frac{1}{3c}\$=0.027.

SINCE P<0.05, I. CONCLUDE THAT THE SUN HAS EXPLODED.



Some review of basic probability

- ► Two random events A and B are called **independent** if $P(A \cap B) = P(A)P(B)$
- ▶ If A and B are two random events, P(A) > 0. The conditional probability of B when A is given is $P(B|A) = P(A \cap B)/P(A)$.

Example

Suppose you are given a coin, you flip it 5 times and get head on all 5 of them.

- Suppose the coin is fair, what is the odds that it gets head for 5 times in 5 flips?
- Null hypothesis
- p-value

- ▶ Suppose the coin is biased and gets head at probability p.
 - ▶ What is the probability that it gets head for 5 times in 5 flips?
 - ▶ What is the *p* that maximizes this probability?
 - ► What is the range of *p* such that the probability for 5 heads in 5 flips is no less than 0.05?
- Maximum likelihood estimate (MLE)
- Confidence interval

- ➤ Suppose you pick the coin among a pile of 100 coins, 99 of which is fair and 1 has head on both sides. What is the chance of the coin being unfair given the results of the 5 flips?
- Prior and posterior
- ► Maximum a posteriori (MAP) estimate

➤ Suppose the odds for getting a head is uniformly distributed in [0,1], given the results of the 5 flips, what do you think is the most likely value for *p*?









WE FOUND NO









WE FOUND NO LINK BETWEEN BLUE JELLY BEANS AND ACNE (P>0.05).



WE FOUND NO LINK BETWEEN TEAL JELLY BEANS AND ACNE (P > 0.05)



GREY JELLY BEANS AND ACNE (P > 0.05).



TAN JELLY BEANS AND ACNE (P>0.05),



CYAN JELLY
BEANS AND ACNE
(P>0.05)



GREEN JELLY BEANS AND ACNE (P<0.05)



MAUVE JELLY BEANS AND ACNE (P>0.05),



WE FOUND NO LINK BETWEEN BEIGE JELLY BEANS AND ACNE (P > 0.05).



WE FOUND NO LINK BETWEEN LICAC JELLY BEANS AND ACNE (P>0.05).



WE FOUND NO LINK BETWEEN BLACK JELLY BEANS AND ACNE (P > 0.05)



WE FOUND NO LINK BETWEEN PEACH JELLY BEANS AND ACNE (P>0.05),



WE FOUND NO LINK BETWEEN ORANGE JELLY BEANS AND ACNE (P > 0.05)



