

Math 481

Instructor: Chenxi Wu

wuchenxi2013@gmail.com

Office: Hill 434

Office hours: 10-11 am Tu, Wed or by appointment

Grading policy: 10% weekly homework (lowest dropped), 20% each of the two midterms, 50% final exam.

Main topics we will cover:

- ▶ Review of probability
- ▶ Point estimate
- ▶ p-values and hypothesis testing
- ▶ Confidence intervals
- ▶ Bayesian statistics

Bayesian and non-Bayesian approaches to statistics

- ▶ Non-Bayesian approach: Set up a null hypothesis and try to show that observation is highly unlikely if null hypothesis is true.
- ▶ Bayesian approach: Assume prior distribution of some parameter, calculate posterior via Bayes formula

DID THE SUN JUST EXPLODE?

(IT'S NIGHT, SO WE'RE NOT SURE.)

THIS NEUTRINO DETECTOR MEASURES
WHETHER THE SUN HAS GONE NOVA.

THEN, IT ROLLS TWO DICE. IF THEY
BOTH COME UP SIX, IT LIES TO US.
OTHERWISE, IT TELLS THE TRUTH.

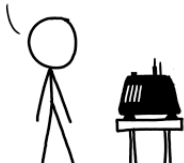
LET'S TRY.

DETECTOR! HAS THE
SUN GONE NOVA?



FREQUENTIST STATISTICIAN:

THE PROBABILITY OF THIS RESULT
HAPPENING BY CHANCE IS $\frac{1}{36} = 0.027$.
SINCE $p < 0.05$, I CONCLUDE
THAT THE SUN HAS EXPLODED.



BAYESIAN STATISTICIAN:

BET YOU \$50
IT HASN'T.



Some review of basic probability

- ▶ Two random events A and B are called **independent** if $P(A \cap B) = P(A)P(B)$
- ▶ If A and B are two random events, $P(A) > 0$. The conditional probability of B when A is given is $P(B|A) = P(A \cap B)/P(A)$.

Example

Suppose you are given a coin, you flip it 5 times and get head on all 5 of them.

- ▶ Suppose the coin is fair, what is the odds that it gets head for 5 times in 5 flips?
- ▶ Suppose the coin is biased and gets head at probability p .
 - ▶ What is the probability that it gets head for 5 times in 5 flips?
 - ▶ What is the p that maximizes this probability?
 - ▶ What is the range of p such that the probability for 5 heads in 5 flips is no less than 0.05?
- ▶ Suppose you pick the coin among a pile of 100 coins, 99 of which is fair and 1 has head on both sides. What is the chance of the coin being unfair given the results of the 5 flips?
- ▶ Suppose the odds for getting a head is uniformly distributed in $[0, 1]$, given the results of the 5 flips, what do you think is the most likely value for p ?

JELLY BEANS
CAUSE ACNE!

SCIENTISTS!
INVESTIGATE!

BUT WE'RE
PLAYING
MINECRAFT!

... FINE.



WE FOUND NO
LINK BETWEEN
JELLY BEANS AND
ACNE ($P > 0.05$).



THAT SETTLES THAT.

I HEAR IT'S ONLY
A CERTAIN COLOR
THAT CAUSES IT.

SCIENTISTS!

BUT
MINECRAFT!



WE FOUND NO
LINK BETWEEN
PURPLE JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
BROWN JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
PINK JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
BLUE JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
TEAL JELLY
BEANS AND ACNE
($P > 0.05$).



LINK BETWEEN
GREY JELLY
BEANS AND ACNE
($P > 0.05$).



LINK BETWEEN
TAN JELLY
BEANS AND ACNE
($P > 0.05$).



LINK BETWEEN
CYAN JELLY
BEANS AND ACNE
($P > 0.05$).



LINK BETWEEN
GREEN JELLY
BEANS AND ACNE
($P < 0.05$).

WHOA!



LINK BETWEEN
MAUVE JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
BEIGE JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
LILAC JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
BLACK JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
PEACH JELLY
BEANS AND ACNE
($P > 0.05$).



WE FOUND NO
LINK BETWEEN
ORANGE JELLY
BEANS AND ACNE
($P > 0.05$).



News

GREEN JELLY BEANS LINKED TO ACNE!

95% CONFIDENCE

ONLY 5% CHANCE
OF COINCIDENCE!



SCIENTISTS...