640:250:15 Introduction to Linear Algebra

Instructor: Chenxi Wu Office: Hill 434, Busch Office phone: 848-445-7954 Email: wuchenxi2013@gmail.com

Webpage: https://wuchenxi.github.io/250

Office Hours: M 1-2 pm W 4-5 pm or by appointment

Textbook: Spence, Insel & Friedberg Elementary Linear Algebra: A Matrix Approach, 2nd Edition, ISBN

978-0-13-187141-0, Prentice-Hall, Upper Saddle River, NJ 07458

Prerequisite: CALC2 or 01:640:136 or 138

Course description Vectors in n-space, systems of linear equations, Gaussian elimination, span and linear independence of a set of vectors, matrix algebra, determinants, subspaces of n-space, basis and dimension, eigenvalues and eigenvectors, diagonalization of a matrix, geometry of vectors, projections, orthogonal sets of vectors, symmetric matrices, and applications.

Attendance: Attendance is expected for this course. Please inform me ahead of time, preferably by emails, if you are going to be late or absent in class for a legitimate reason, and also self-report online per university policy. Please turn off your cellphone or keep it in silent mode during the lectures.

Homework and quizzes: Problem-solving is an important part in the study of mathematics, so please finish and hand in homework in time, and make sure that you fully understand the solution of each problem! The homework for each week will be posted online each Thursday, collected on the next Thursday and returned in one week. Sketch of solutions will be posted online after the homework for each week is collected. Only selected problems will be graded. The lowest 2 homework grades will be dropped.

There will be 5 quizzes throughout the semester and the lowest 1 quiz grade will be dropped. The date of the quizzes will not be announced in advance. The quizzes and the exams will be based on homework problems.

Exam dates: Midterms will be on Fridays. The final exam is on Dec. 19, 8-11 pm.

Grading: 10% Homework, 10% Quizzes, 20% Midterm 1, 20% Midterm 2, 40% Final.

Other policies: There will be no make-ups for quizzes and midterms and no late homework allowed. However, if there is a legitimate, documented reason that you miss a homework, quiz or midterm please contact me as soon as possible so I can adjust your grade components accordingly. Make-up for the final exam for is allowed.

Policy and procedures regarding disability are indicated at http://ods.rutgers.edu/. If you need special accommodation, please present the Letter of Accommodation as early in the semester as possible.

All students are expected to be familiar with and abide by the academic integrity policy (http://academicintegrity.rutgers.edu/academic-integrity-at-rutgers). Violations will be taken very seriously.

Class Schedule (Tentative)

| Lecture | Reading | Topics |
|---------|-----------------|--|
| 1 | 1.1, 1.2 | Matrices, Vectors, and Linear Combinations |
| 2 | 1.3 | Systems of Linear Equations; Reduced Row Echelon Form |
| 3 | 1.4 | Gaussian Elimination; Rank and Nullity of a Matrix |
| 4 | 1.6 | Span of a Set of Vectors |
| 5 | 1.7 | Linear Dependence and Linear Independence |
| 6 | 1.7, 2.1 | Homogeneous Systems; Matrix Multiplication |
| 7 | 2.1 | Matrix Algebra |
| 8 | 2.3 | Invertibility and Elementary Matrices; |
| | | Column Correspondence Property |
| | App. E | Uniqueness of Reduced Row Echelon Form |
| 9 | 2.4 | Inverse of a Matrix |
| | 2.5 | Partitioned Matrices and Block Multiplication |
| 10 | 2.6 | LU Decomposition of a Matrix |
| 11 | Midterm | Exam #1 |
| 12 | 3.1 | Determinants; Cofactor Expansions |
| 13 | 3.2 | Properties of Determinants |
| 14 | 4.1 | Subspaces |
| 15 | 4.2 | Basis and Dimension |
| 16 | 4.3 | Column Space, Null Space and Row Space of a Matrix |
| 17 | 5.1 | Eigenvalues and Eigenvectors |
| 18 | 5.2 | Characteristic Polynomial |
| 19 | 5.3 | Diagonalization of a Matrix |
| 20 | 5.5 | Examples of Diagonalization |
| 21 | ${\bf Midterm}$ | Exam # 2 |
| 22 | 6.1 | Geometry of Vectors; Projection onto a Line |
| 23 | 6.2 | Orthogonal Sets of Vectors; |
| | | Gram-Schmidt Process; QR factorization |
| 24 | 6.3 | Orthogonal Projection; Orthogonal Complements |
| | | Projection onto Column Space; Closest Vector Property |
| 25 | 6.4 | Least Squares Method; Normal Equations; Solving Inconsistent Systems |
| 26 | 6.5, 6.6 | Orthogonal Matrices; Diagonalization of Symmetric Matrices |
| 27 | 6.6 | Diagonalization of Quadratic Forms |
| | | Spectral Decomposition for Symmetric Matrices |
| 28 | | Catch up and review |

Student-Wellness Services:

- Just in Case Web App http://codu.co/cee05e Access helpful mental health information and resources for yourself or a friend in a mental health crisis on your smartphone or tablet and easily contact CAPS or RUPD.
- Counseling, ADAP & Psychiatric Services (CAPS) (848) 932-7884 17 Senior Street, New Brunswick NJ 08901 http://www.rhscaps.rutgers.edu/ CAPS is a university mental health support service that includes counseling, alcohol and other drug assistance, and psychiatric services staffed by a team of professionals within Rutgers Health Services to support students' efforts to succeed at Rutgers University. CAPS offers a variety of services that include: individual therapy, group therapy and workshops, crisis intervention, referral to specialists in the community and consultation and collaboration with campus partners.

- Violence Prevention & Victim Assistance (VPVA) (848) 932-1181 3 Bartlett Street, New Brunswick NJ 08901 http://www.vpva.rutgers.edu/ The Office for Violence Prvention and Victim Assistance provides confidential crisis intervention, counceling and advocacy for victims of sexual and relationship violence and stalking to students, staff and faculty. To reach staff during office hours when the university is open or to reach an advocate after hours call 848-932-1181.
- Disability Services (848) 445-6800 Lucy Stone Hall, Suite A145, Livingston Campus, 54 Joyce Kilmer Avenue, Piscataway NJ 08854 https://ods.rutgers.edu/Rutgers University welcomes students with disabilities into all of the university's educational programs. In order to receive consideration for reasonable accommodations, a student with a disability must contact th appropriate disability services office at the campus where you are officially enrolled, participate in an intake interview, and provide documentation (https://ods.rutgers.edu/students/documentation-guidelines). If the documentation supports your request for reasonable accommodations, your campus's disability services office will provide you with a Letter of Accommodation. To begin this process, please complete the Registration form on the ODS website at https://ods.rutgers.edu/students/registration-form.
- Scarlet Listeners (732) 247-5555 http://www.scarletlisteners.com Free and confidential peer counseling and referral hotline, providing a comforting and supportive safe space.