

# 人工智能作业二

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## 1

(a)

变量:  $V_{ij}, i = 1, 2, 3, j = 1, 2, 3.$

值域:  $Dom(V_{ij}) = \{1, 2, \dots, 9\}.$

约束:

$$V_{i_1 j_1} \neq V_{i_2 j_2}, (i_1, j_1) \neq (i_2, j_2), i_1, i_2, j_1, j_2 = 1, 2, 3.$$

$$\sum_{p=1}^3 V_{pj} = 15, j = 1, 2, 3.$$

$$\sum_{q=1}^3 V_{iq} = 15, i = 1, 2, 3.$$

$$V_{11} + V_{22} + V_{33} = 15.$$

$$V_{13} + V_{22} + V_{31} = 15.$$

(b)

图 $G=(V,E)$

变量:  $v_i, i = 1, 2, \dots, k$

值域:  $Dom(v_i) = V$

约束:

$$v_m \neq v_n, m \neq n, m, n = 1, 2, \dots, k$$
$$(v_p, v_q) \notin E, p \neq q, p, q = 1, 2, \dots, k$$

(c)

变量:  $I, N, T, L, A$

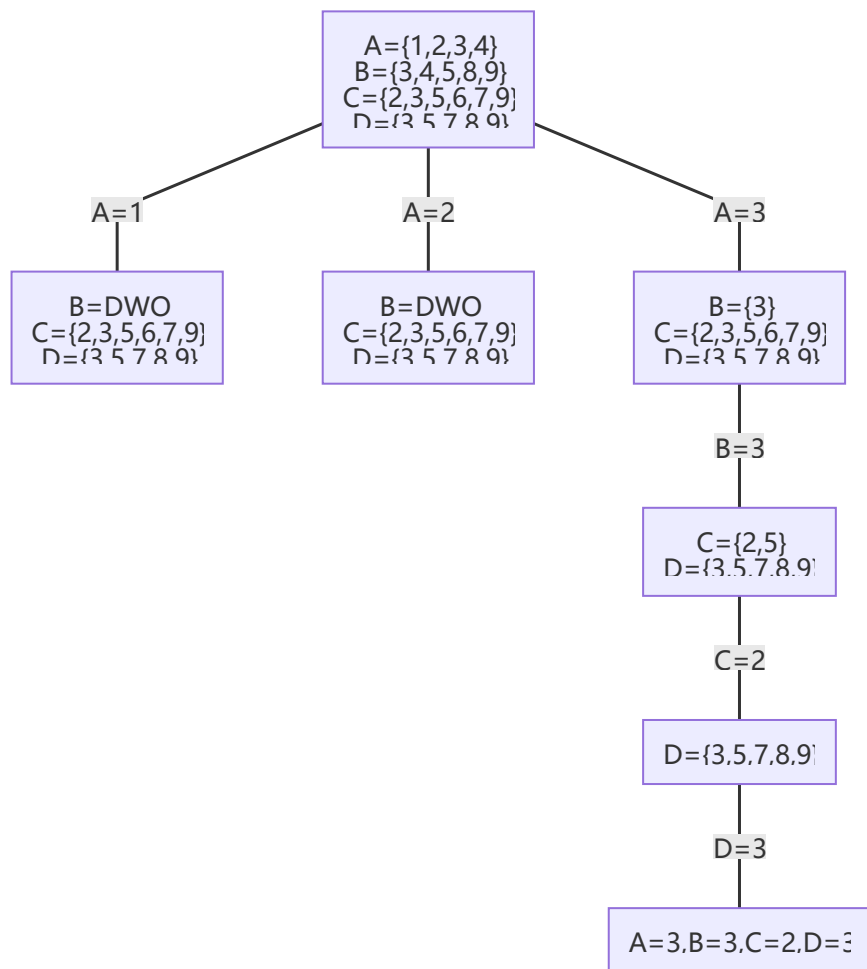
值域:  $Dom(x) = 1, 2, \dots, 9, x = I, N, T, L, A$

约束:

$$(100 * I + 10 * N + T) \times L = 1110 * A + I$$

## 2

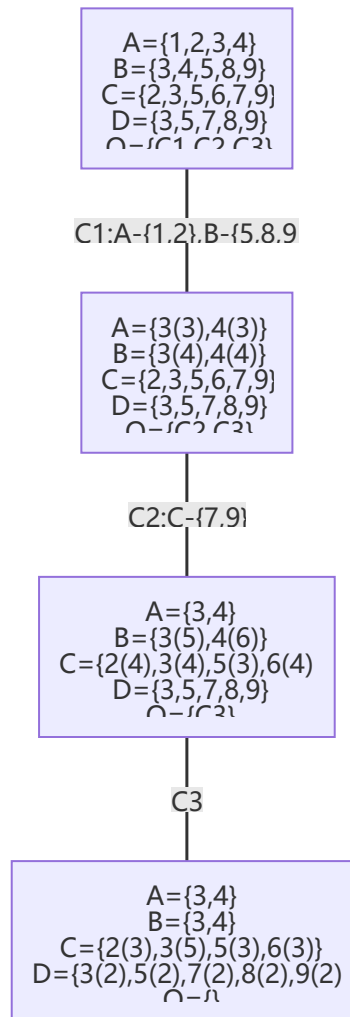
(a)



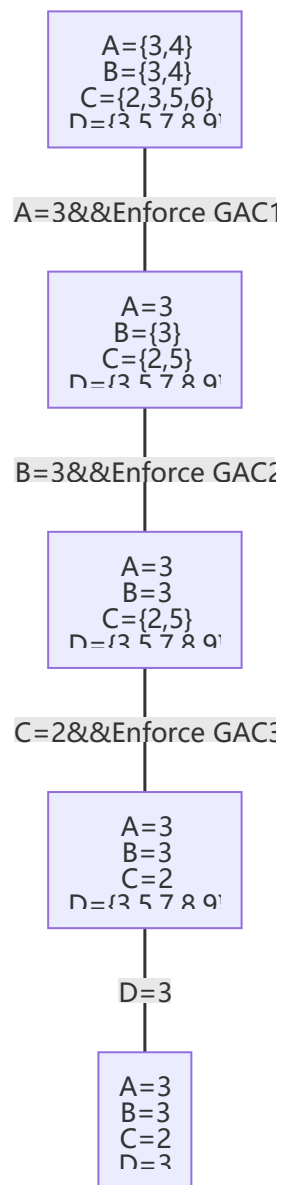
得到了一组解 (3,3,2,3)

(b)

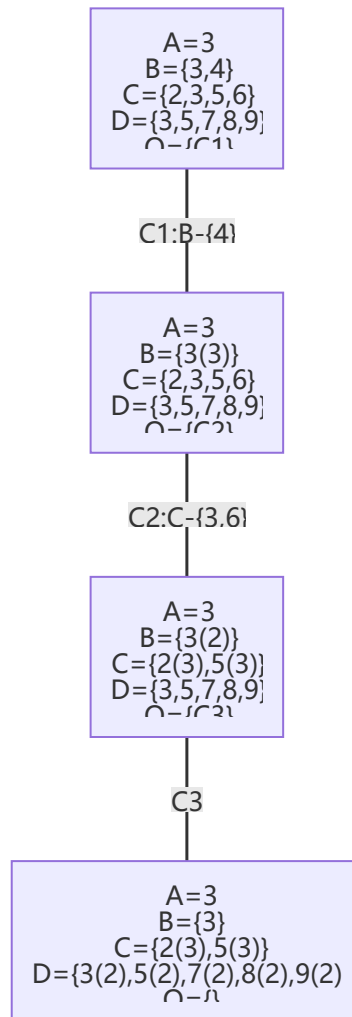
执行Enforce GAC。



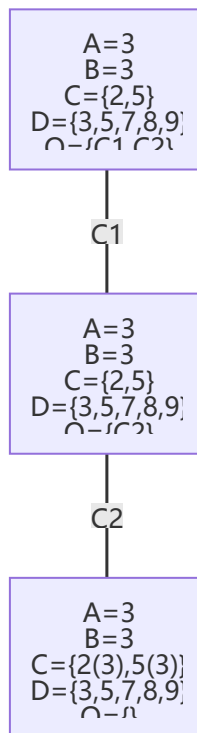
接下来执行GAC算法。



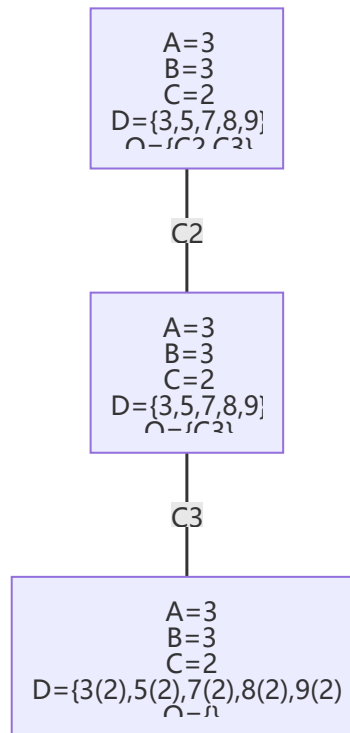
其中Enforce GAC1如下：



Enforce GAC2如下:



Enforce GAC3如下:



得到了一组解 (3,3,2,3)

### 3

(a)

$member(Joe). member(Sally). member(Bill). member(Allen).$   
 $spouse(Allen, Sally).$   
 $brother(Bill, Allen)$   
 $\forall X \forall Y, spouse(X, Y) \rightarrow spouse(Y, X)$   
 $\forall X \forall Y, spouse(X, Y) \wedge member(X) \rightarrow member(Y)$   
 $\forall x, member(x) \rightarrow x = Joe \vee x = Sally \vee x = Bill \vee x = Allen$

逻辑上, Allen可以和Bill结婚, 他们两人都是club成员, 符合规则。所以以上事实不能得出Allen没有结婚。

(b)

添加如下:

$\forall X \forall Y, brother(X, Y) \rightarrow \neg spouse(X, Y)$   
 $\forall X \forall Y, spouse(X, Y) \rightarrow X \neq Y$   
 $\forall X \forall Y \forall Z, spouse(X, Y) \rightarrow \neg spouse(X, Z)$

证明: (反证) 假设Allen结婚了, 即 $spouse(Allen, c)$

$\therefore \forall X \forall Y, spouse(X, Y) \wedge member(X) \rightarrow member(Y)$   
 $\therefore spouse(Ellen, c) \wedge member(Ellen) \rightarrow member(c)$  (全称实例化)  
 $\therefore spouse(Ellen, c) \wedge member(Ellen)$   
 $\therefore member(c)$  (假言推理)  
 $\therefore \forall x, member(x) \rightarrow x = Joe \vee x = Sally \vee x = Bill \vee x = Ellen$   
 $\therefore member(c) \rightarrow c = Joe \vee c = Sally \vee c = Bill \vee c = Ellen$  (全称实例化)  
 $\therefore c = Joe \vee c = Sally \vee c = Bill \vee c = Ellen$   
 1) 若  $c = Joe$   
 $\therefore \forall X \forall Y \forall Z, spouse(X, Y) \rightarrow \neg spouse(X, Z)$   
 $\therefore spouse(Joe, Sally) \rightarrow \neg spouse(Joe, Ellen)$  (全称实例化, 化简律)  
 这与  $spouse(Ellen, Joe)$  矛盾  
 2) 若  $c = Sally$ , 由 (1) 同理矛盾  
 3) 若  $c = Ellen$   
 $\therefore \forall X \forall Y, spouse(X, Y) \rightarrow X \neq Y$   
 $\therefore spouse(Ellen, Ellen) \rightarrow Ellen \neq Ellen$  (全称实例化)  
 矛盾  
 4) 若  $c = Bill$   
 $\therefore \forall X \forall Y, brother(X, Y) \rightarrow \neg spouse(X, Y)$   
 $\therefore brother(Bill, Ellen) \rightarrow \neg spouse(Bill, Ellen)$  (全称实例化)  
 $\therefore brother(Bill, Ellen)$   
 $\therefore \neg spouse(Bill, Ellen)$  (假言推理)  
 这与  $spouse(Ellen, Bill)$  矛盾  
 $\therefore$  综上所述  $Ellen$  没有结婚

## 4

KB:

$$\begin{aligned}
 S_1 &\Rightarrow 1. (\neg P(x, y), P(y, x)) \\
 S_2 &\Rightarrow 2. (\neg P(m, n), \neg P(n, r), P(m, r)) \\
 S_3 &\Rightarrow 3. P(p, f(p))
 \end{aligned}$$

Q:

$$\forall x P(x, x) \Rightarrow 4. \neg P(q, q)$$

推导:

$$\begin{aligned}
 5. & R[2a, 3] m = p, n = f(p) \quad (\neg P(f(p), r), P(p, r)) \\
 6. & R[4, 5b] p = q, r = q \quad \neg P(f(q), q) \\
 7. & R[1b, 6] x = q, y = f(q) \quad \neg(q, f(q)) \\
 8. & R[3, 7] p = q \quad ()
 \end{aligned}$$

证毕。