

date: 2025-01-30

TFE4188 - Lecture 3

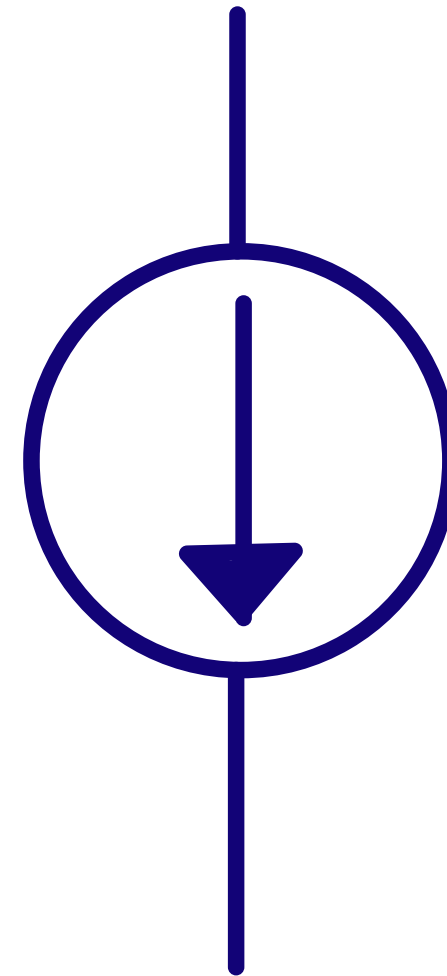
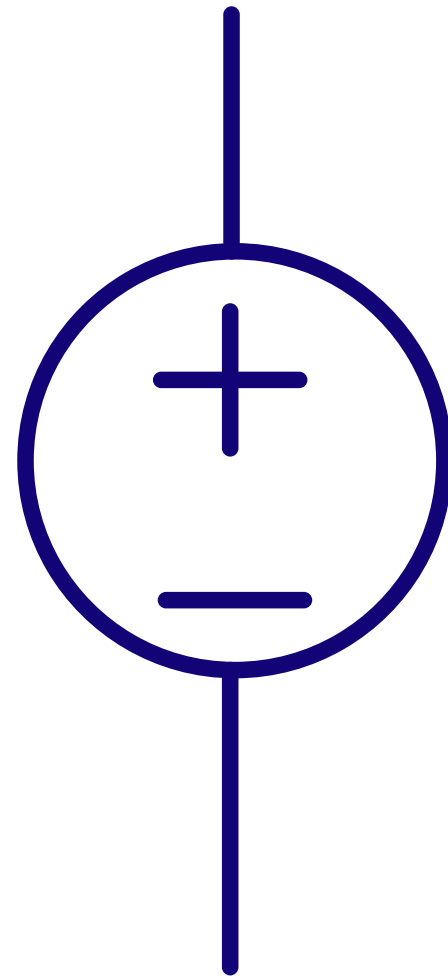
Reference and bias

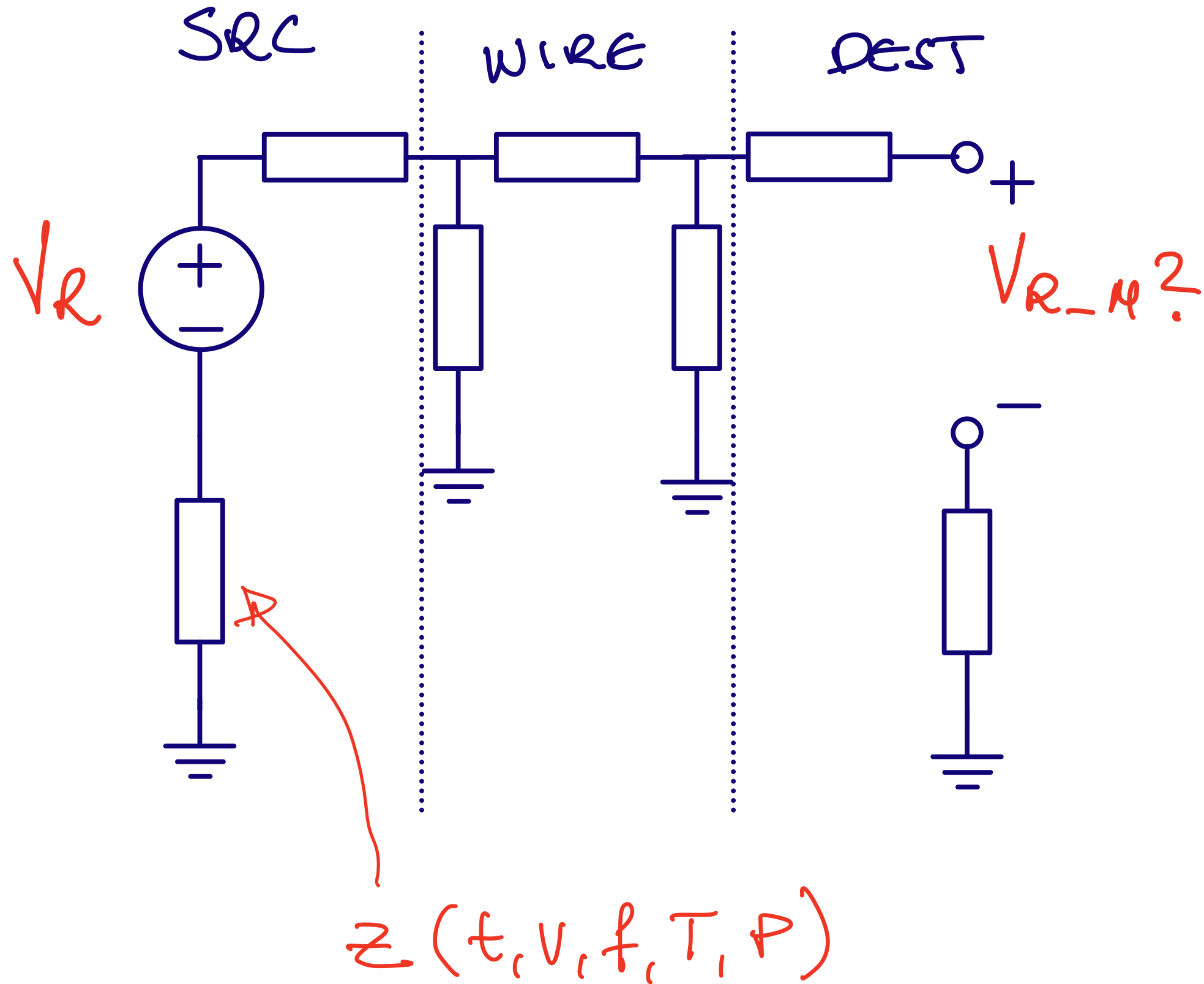
Goal for today

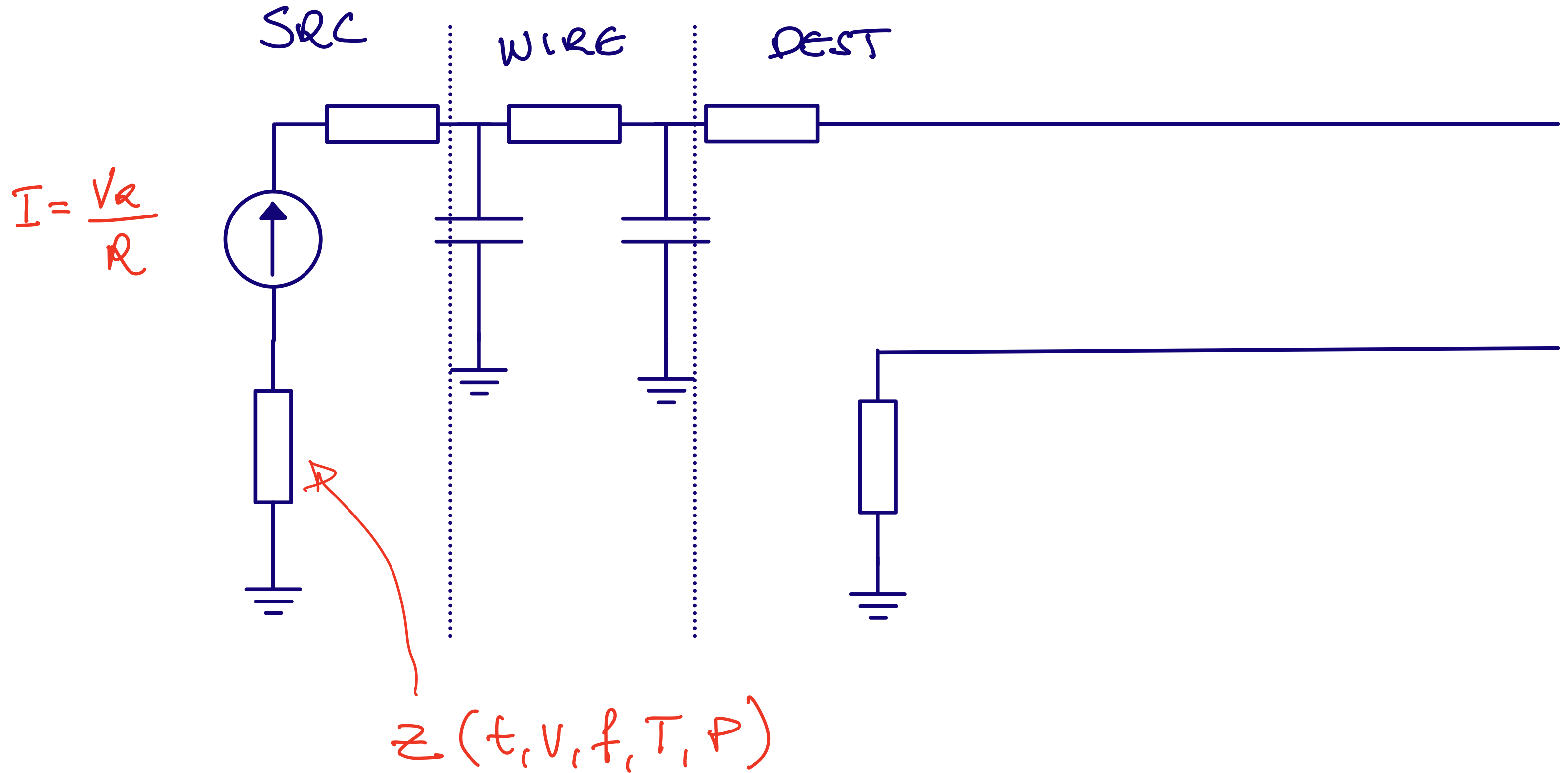
Understand **why** we need reference and bias circuits

Introduction to **circuit architectures**

Why

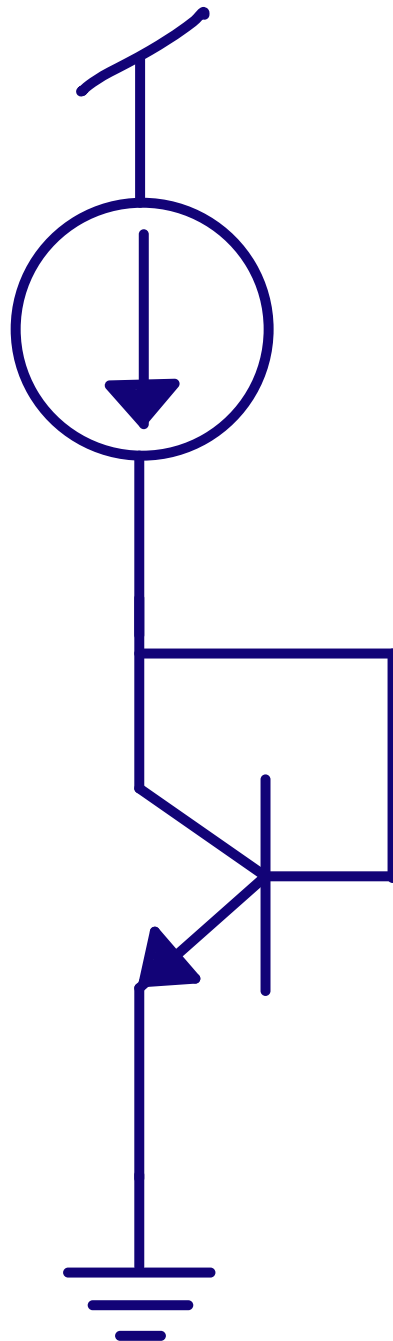






Bandgap voltage reference

A voltage complementary to temperature (CTAT)



$$I_D = I_S \left(e^{\frac{V_{BE}}{V_T}} - 1 \right) + I_B \approx I_S e^{\frac{V_{BE}}{V_T}}$$

$$V_T = \frac{kT}{q}$$

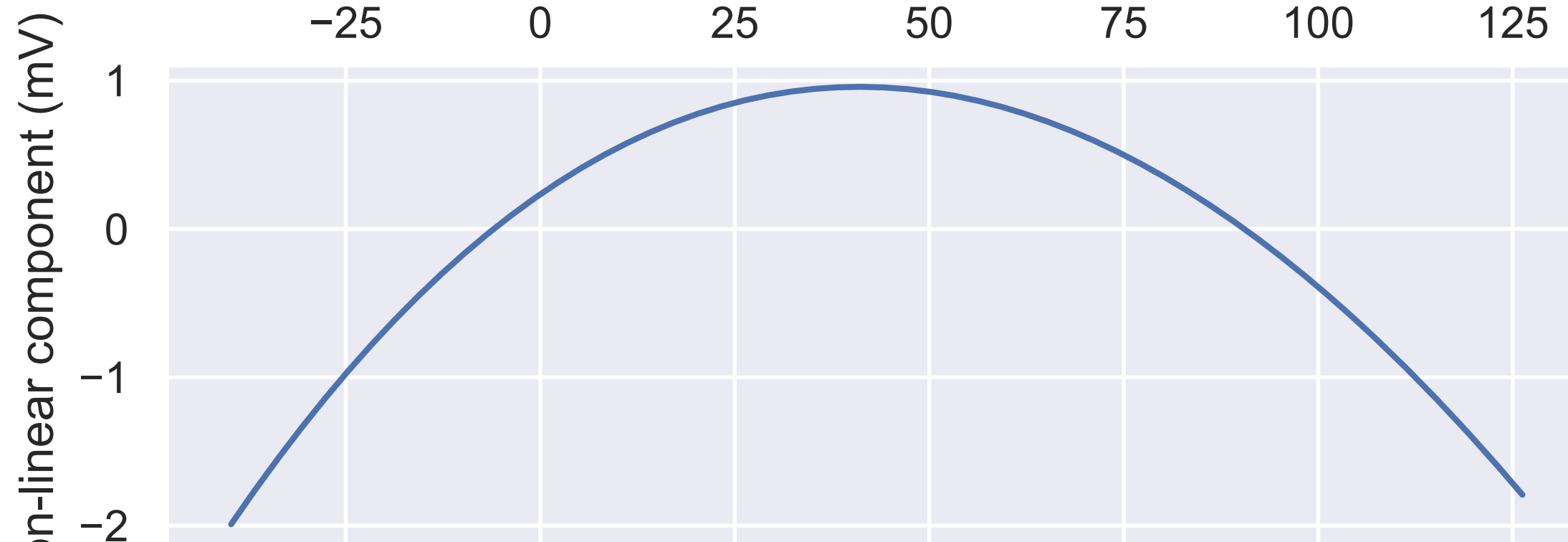
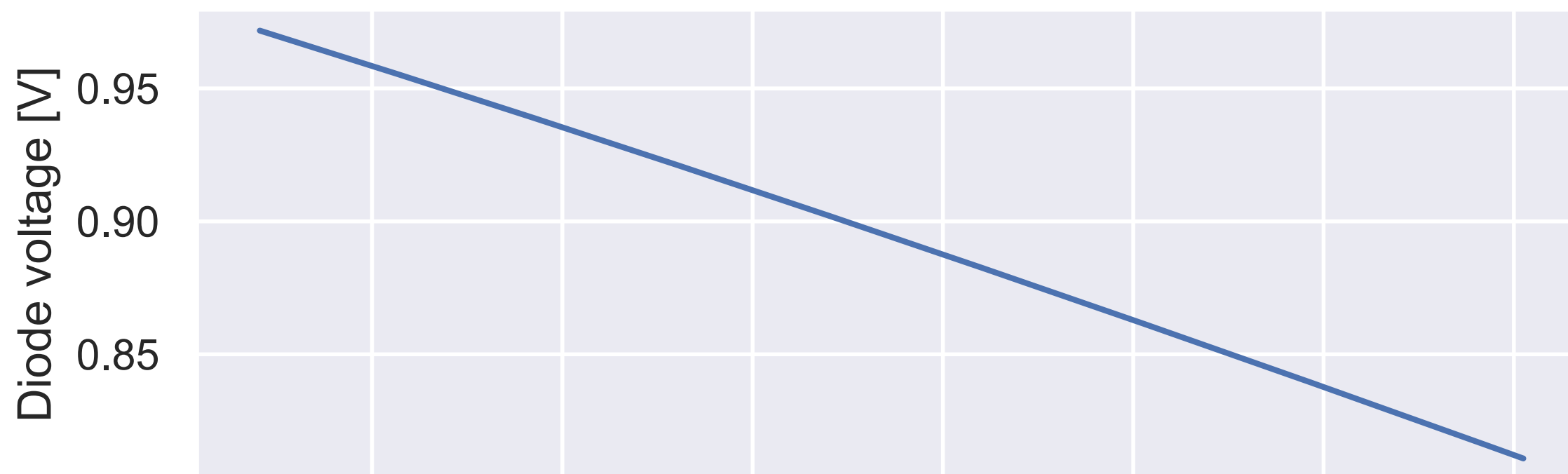
$$V_{BE} = \frac{kT}{q} \ln \frac{I_C}{I_S}$$

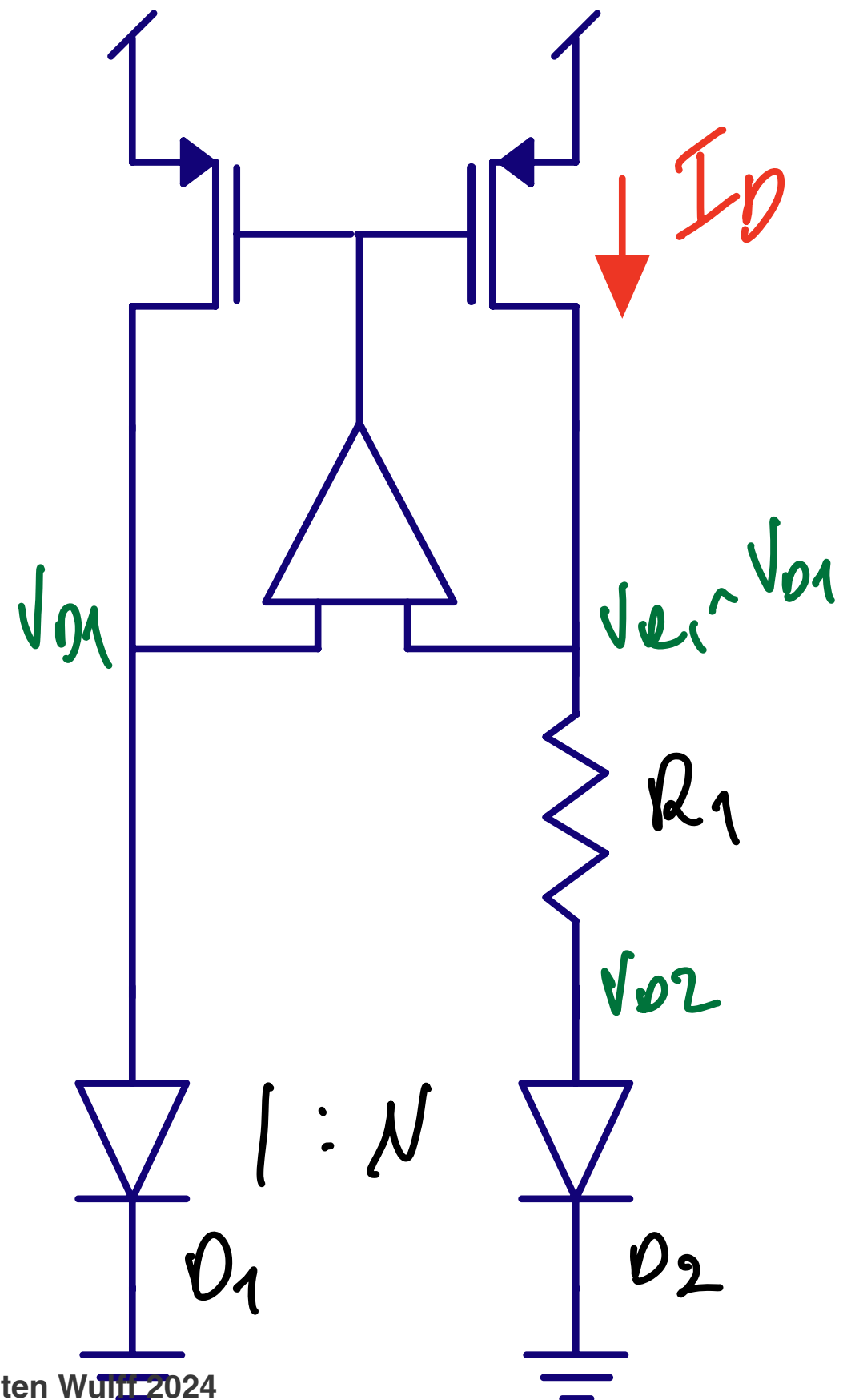
$$I_S = qA n_i^2 \left[\frac{D_n}{L_n N_A} + \frac{D_p}{L_p N_D} \right]$$

Some algebra (see [Diodes](#))

$$V_{BE} = \frac{kT}{q}(\ell - 3 \ln T) + V_G$$

$$\ell = \ln I_C - \ln qA - \ln \left[\frac{D_n}{L_n N_A} + \frac{D_p}{L_p N_D} \right] - 2 \ln 2 - \frac{3}{2} \ln m_n^* - \frac{3}{2} \ln m_p^* - 3 \ln \frac{2\pi k}{h^2}$$

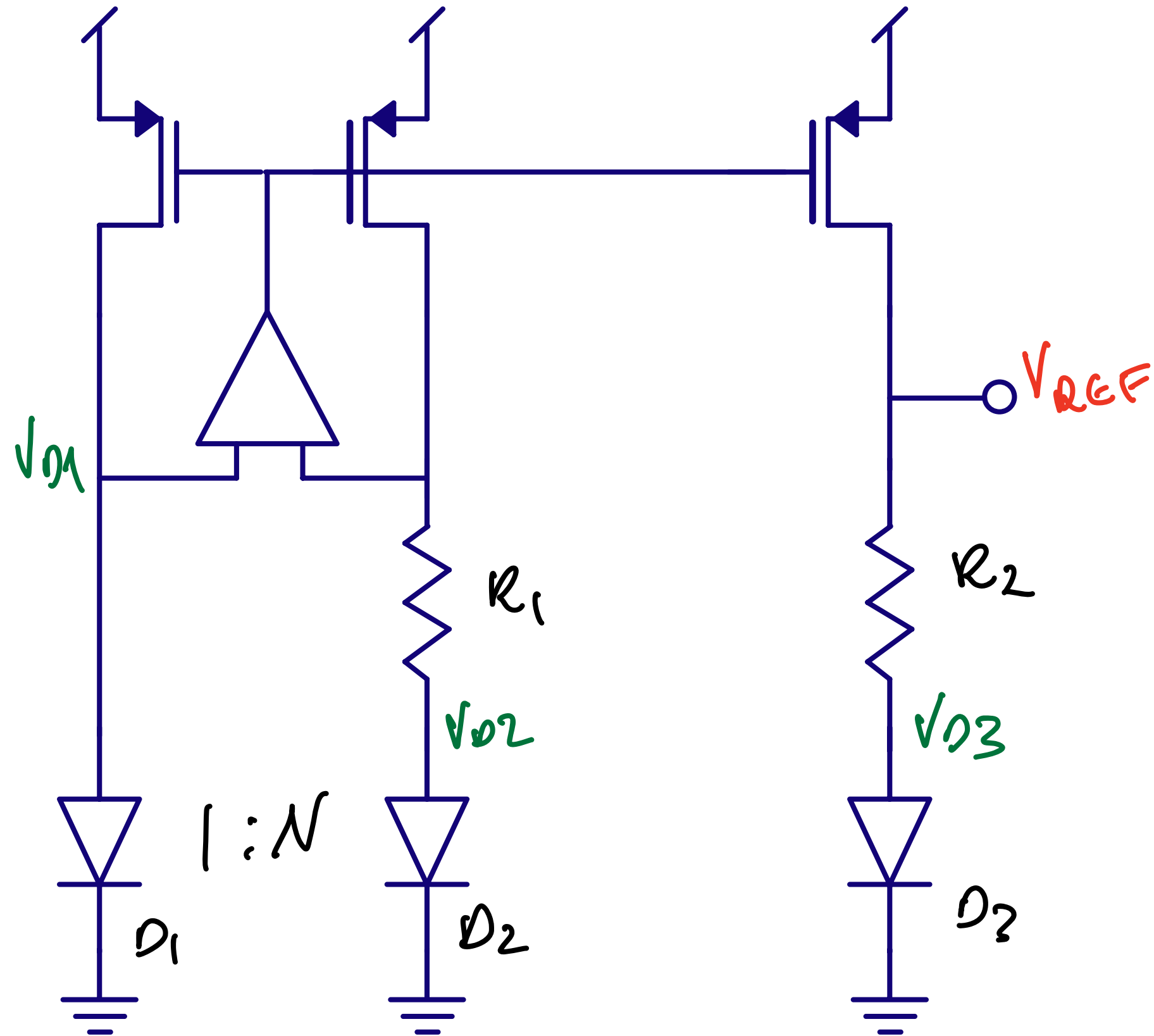


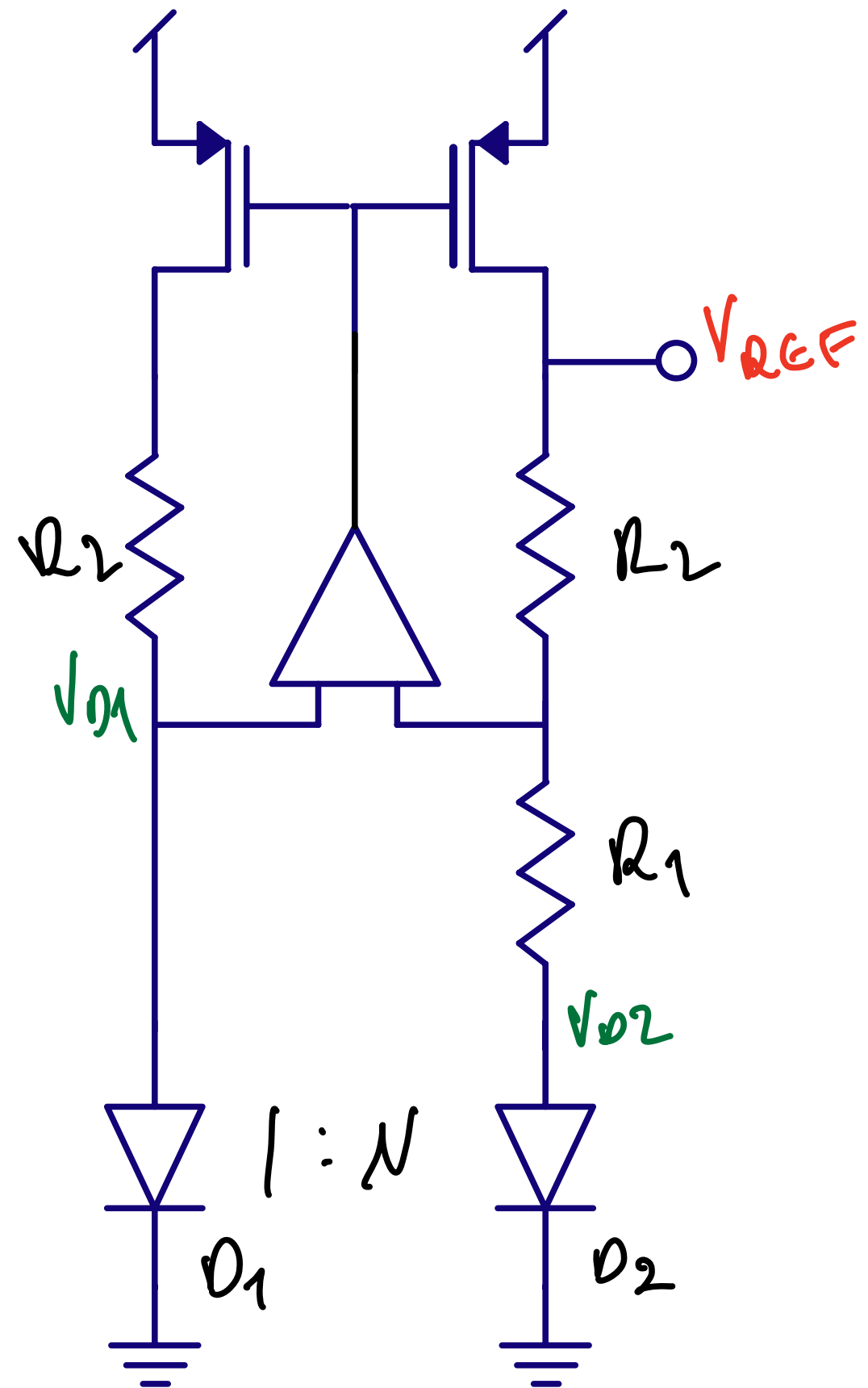


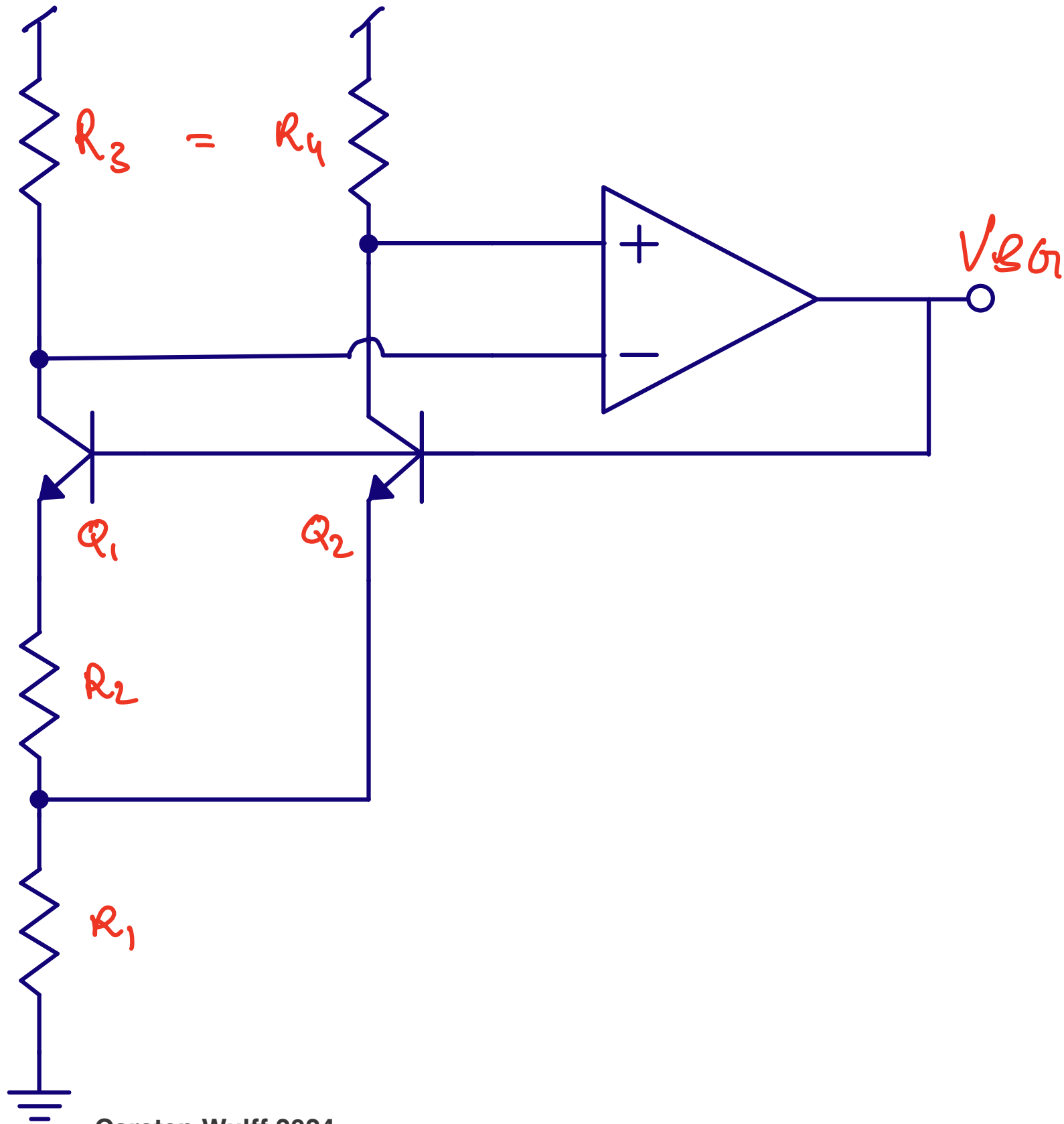
A current proportional to temperature (PTAT)

$$V_{D1} - V_{D2} = V_T \ln \frac{I_D}{I_{S1}} - V_T \ln \frac{I_D}{I_{S2}} = V_T \ln \frac{I_{S2}}{I_{S1}} = V_T \ln N$$

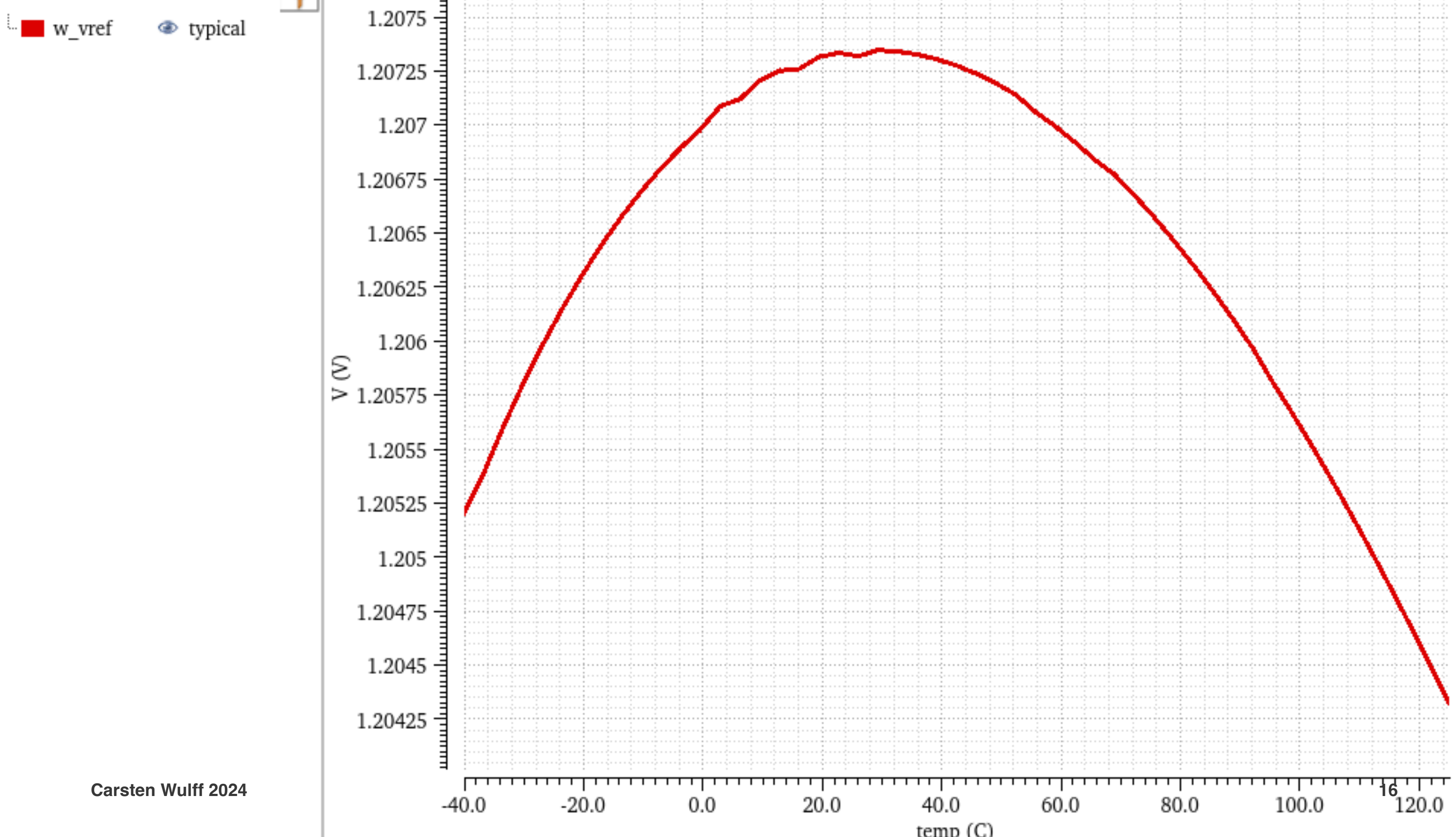
How to combine a CTAT with a PTAT ?

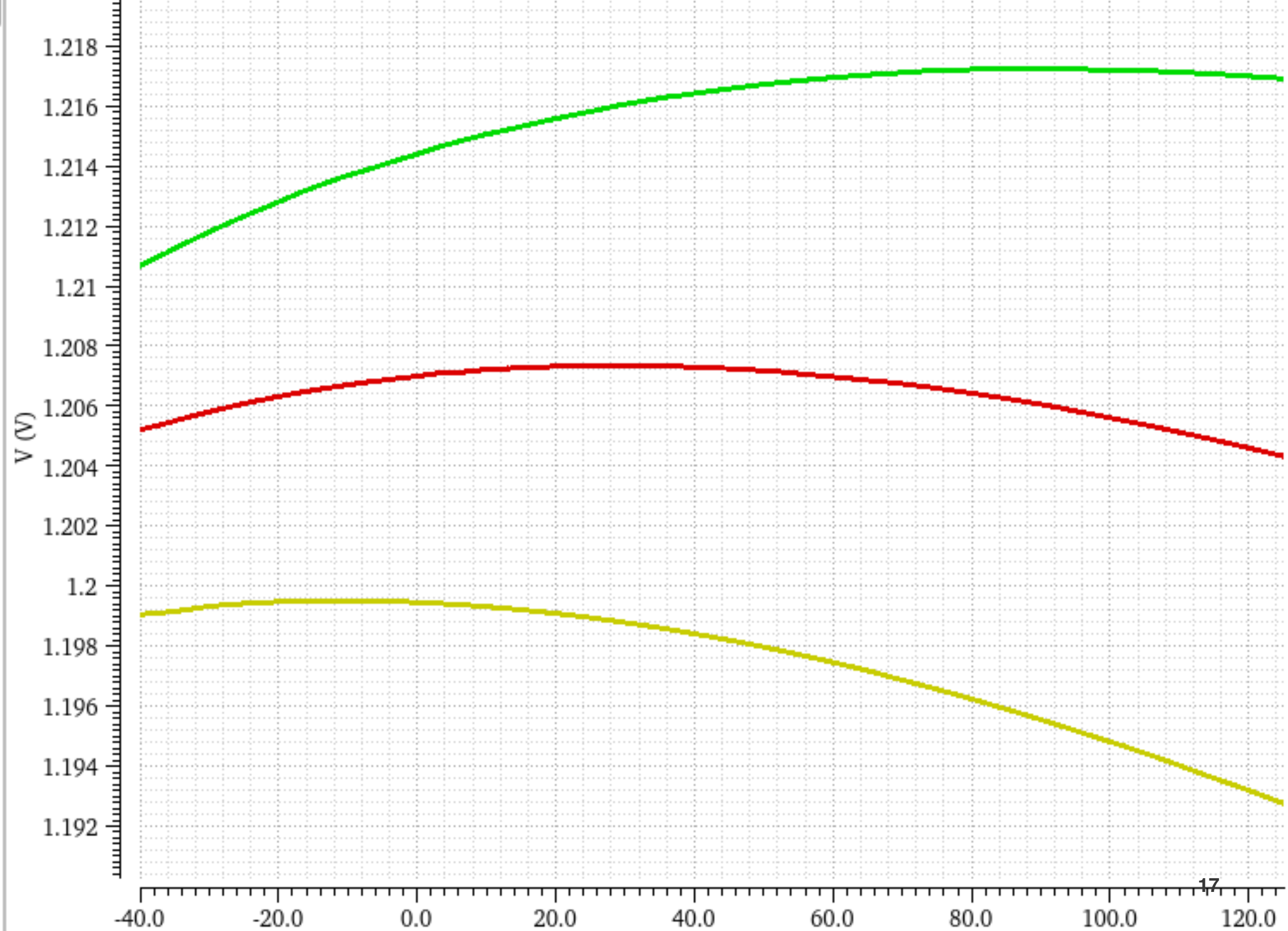
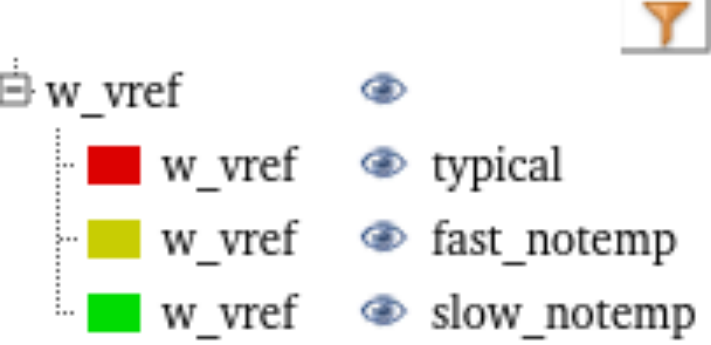




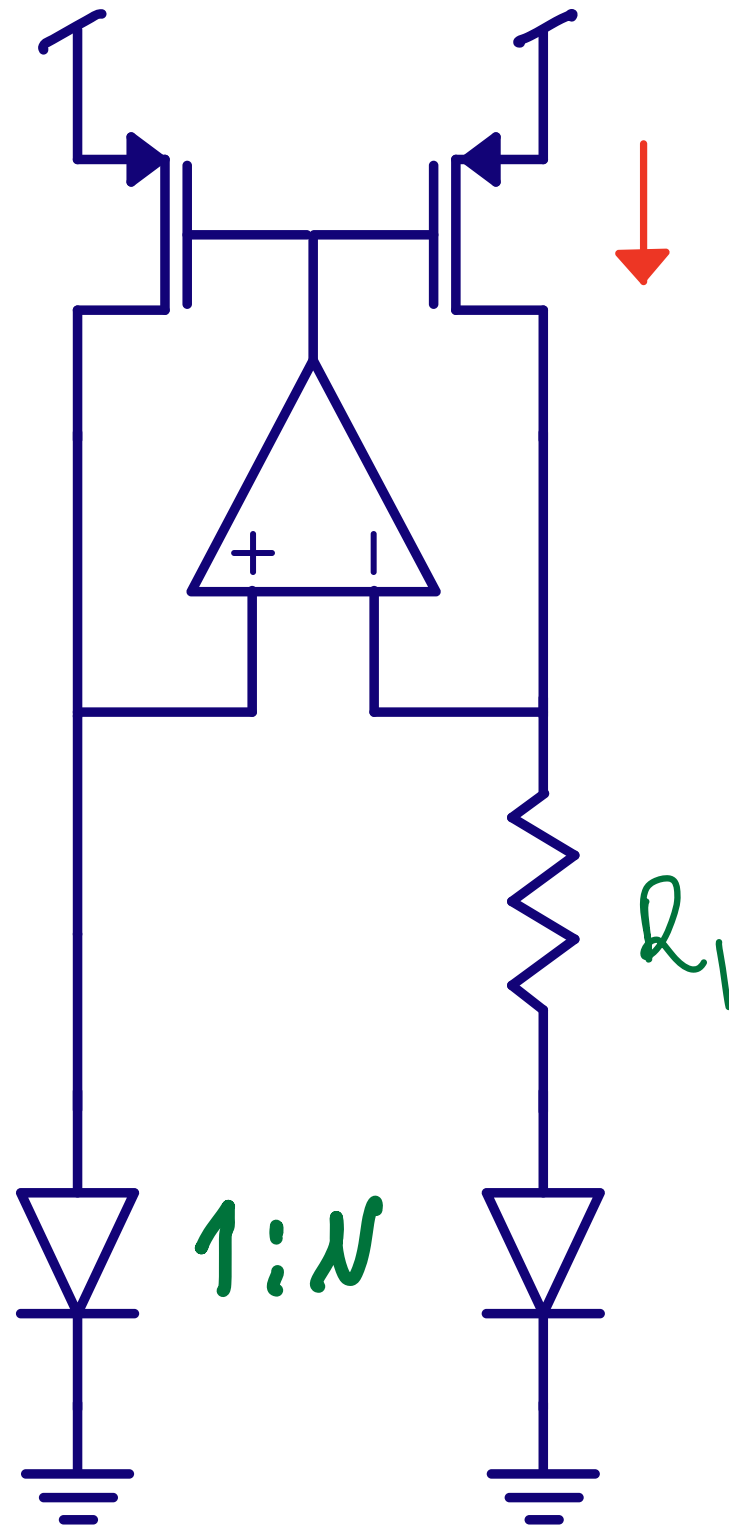


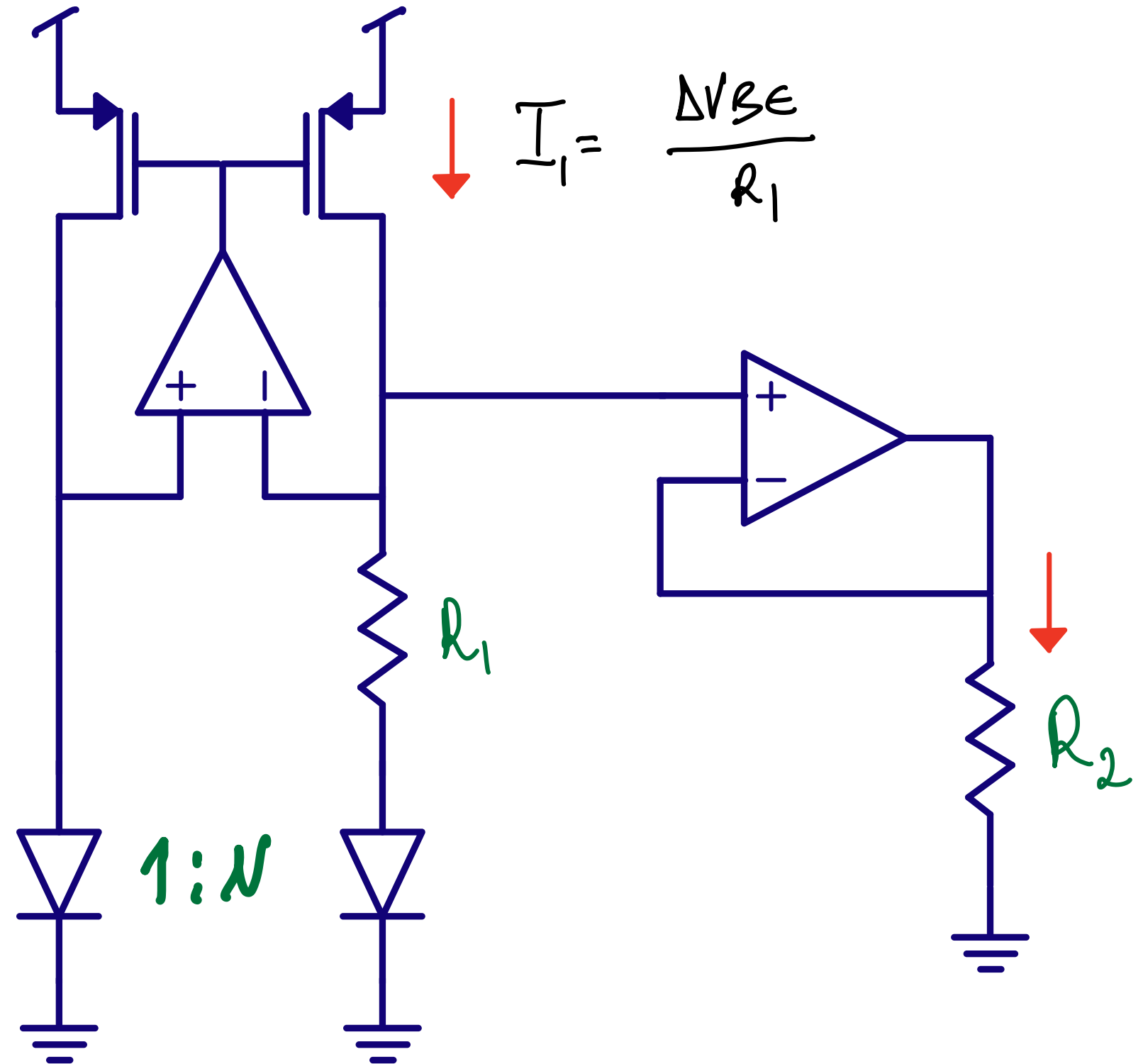
$$V_{BG} = V_{G0} + (m - 1) \frac{kT}{q} \ln \frac{T_0}{T} + T \left[\frac{k}{q} \ln \frac{J_2}{J_1} \frac{2R_2}{R_1} - \frac{V_{G0} - V_{be0}}{T_0} \right]$$



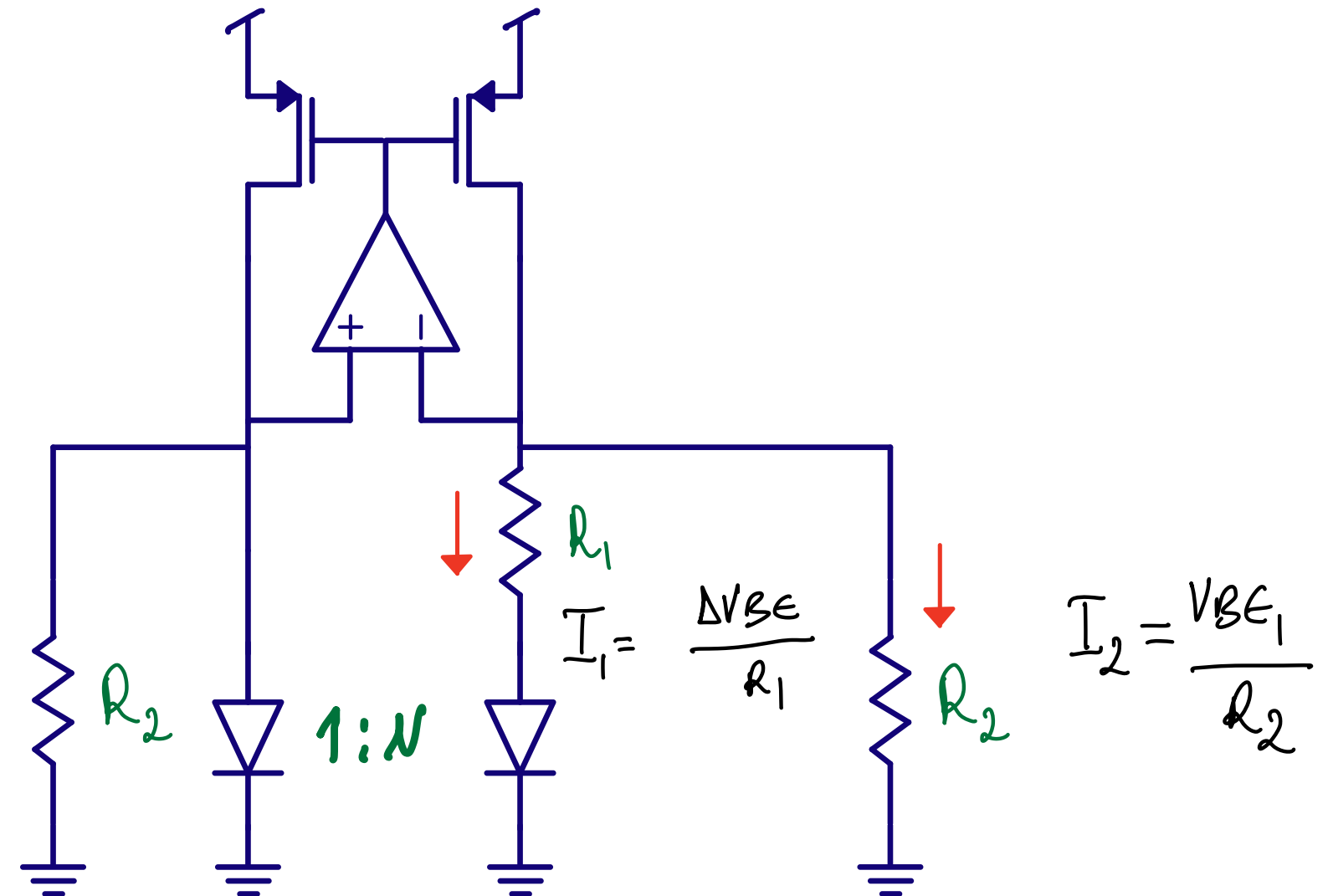


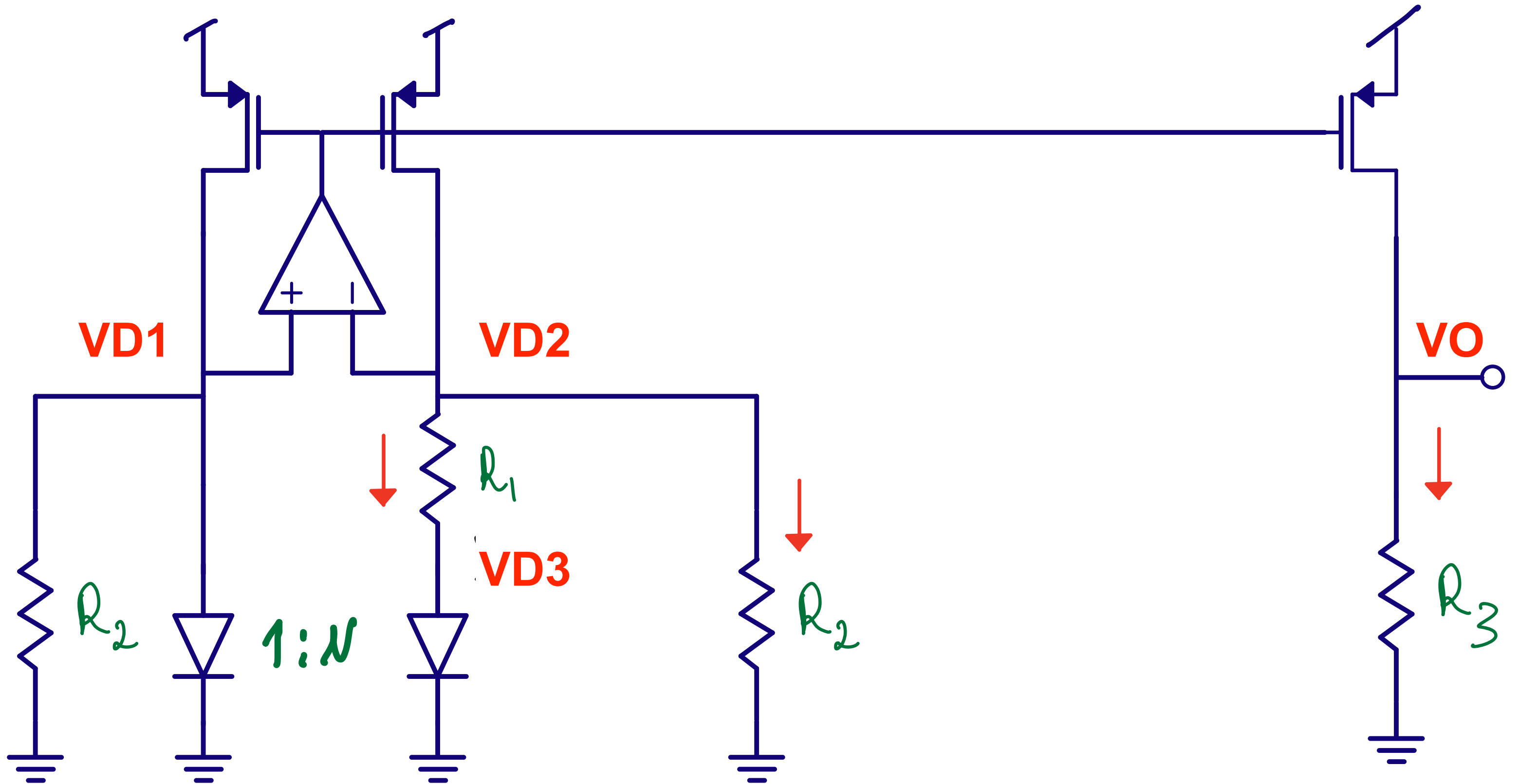
Low voltage bandgap





$$I_{PMOS} = \frac{V_D}{R_2} + \frac{\Delta V_D}{R_1}$$

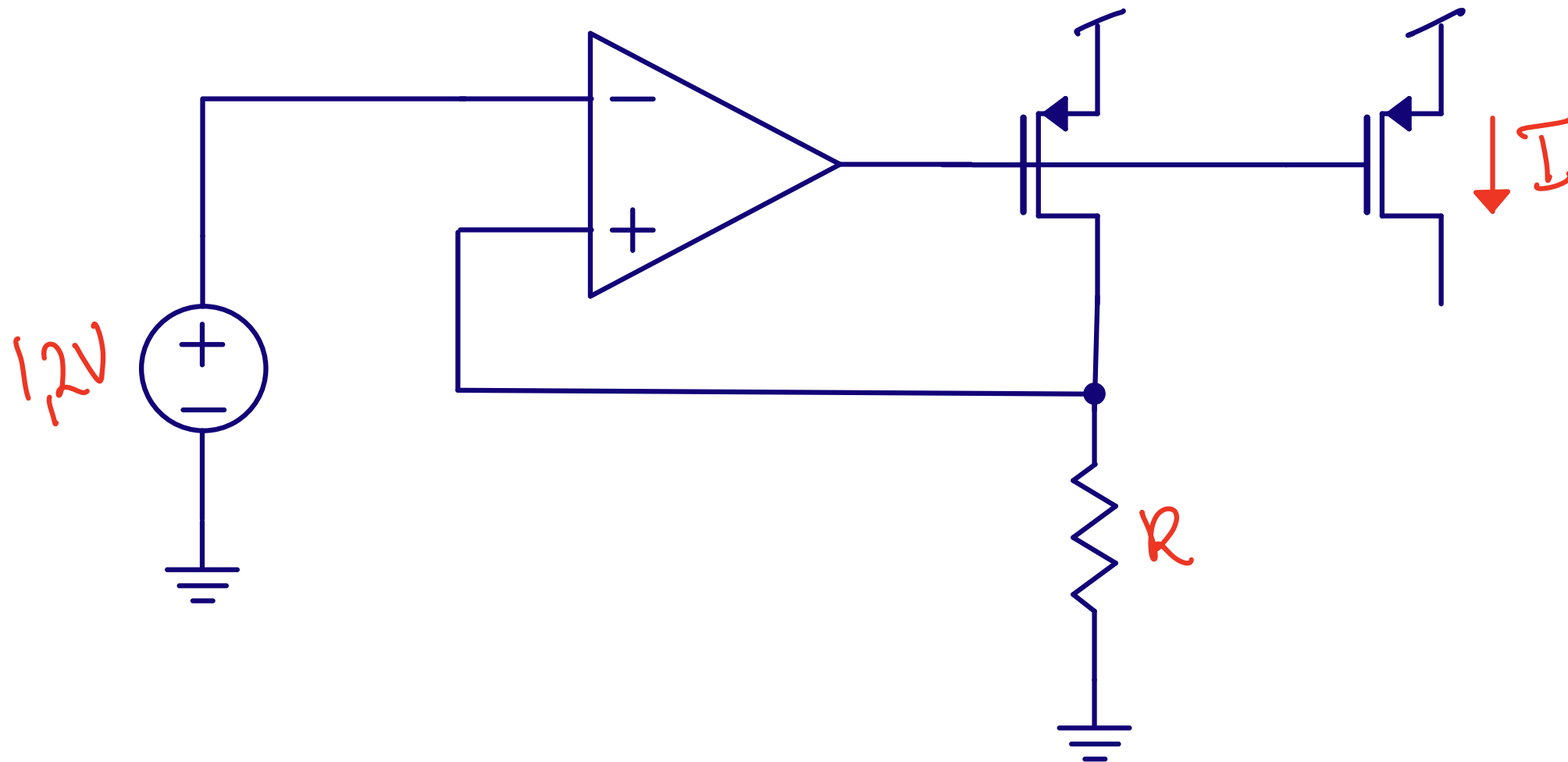




Bias

Sometimes we just need a current

Voltage to current conversion



GM Cell

$$V_o = V_{GS1} - V_{GS2} = V_{eff1} + V_{tn} - V_{eff2} - V_{tn} = V_{eff1} - V_{eff2}$$

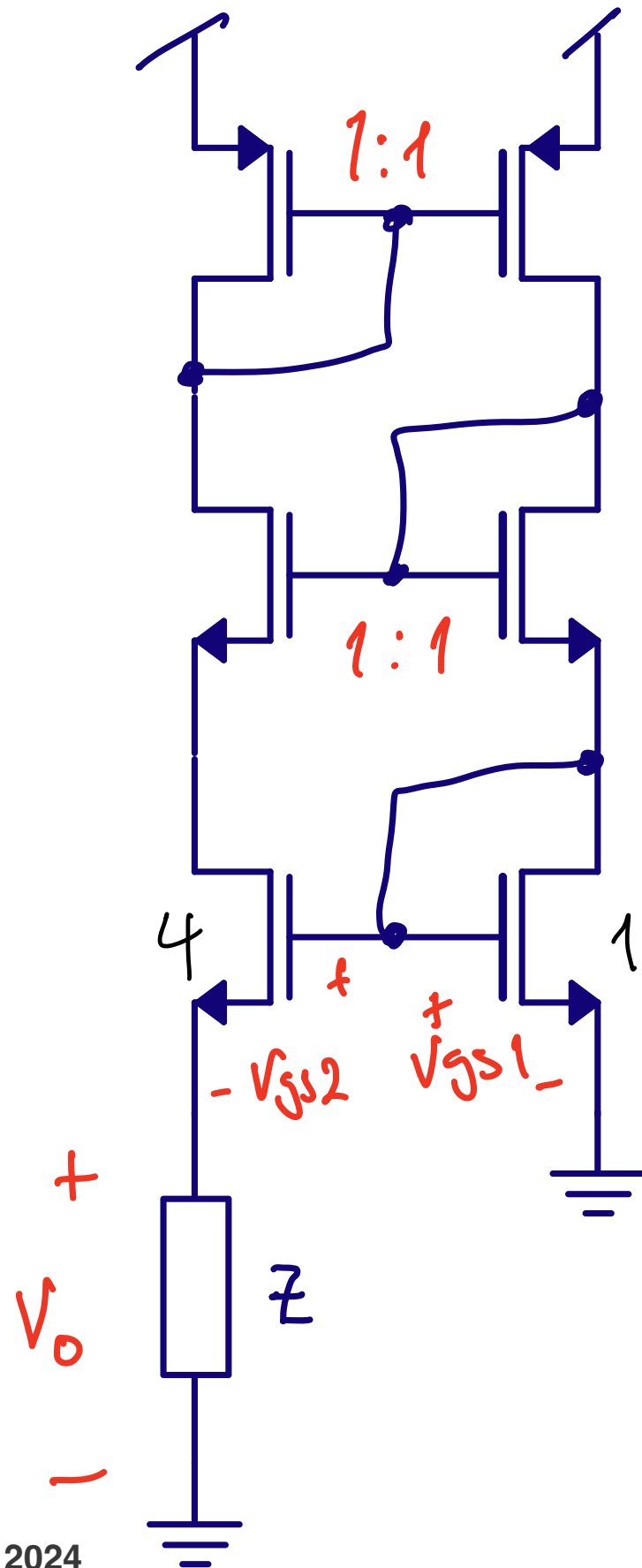
$$\frac{1}{2} \mu_n C_{ox} \frac{W_1}{L_1} V_{eff1}^2 = \frac{1}{2} \mu_n C_{ox} 4 \frac{W_1}{L_1} V_{eff2}^2$$

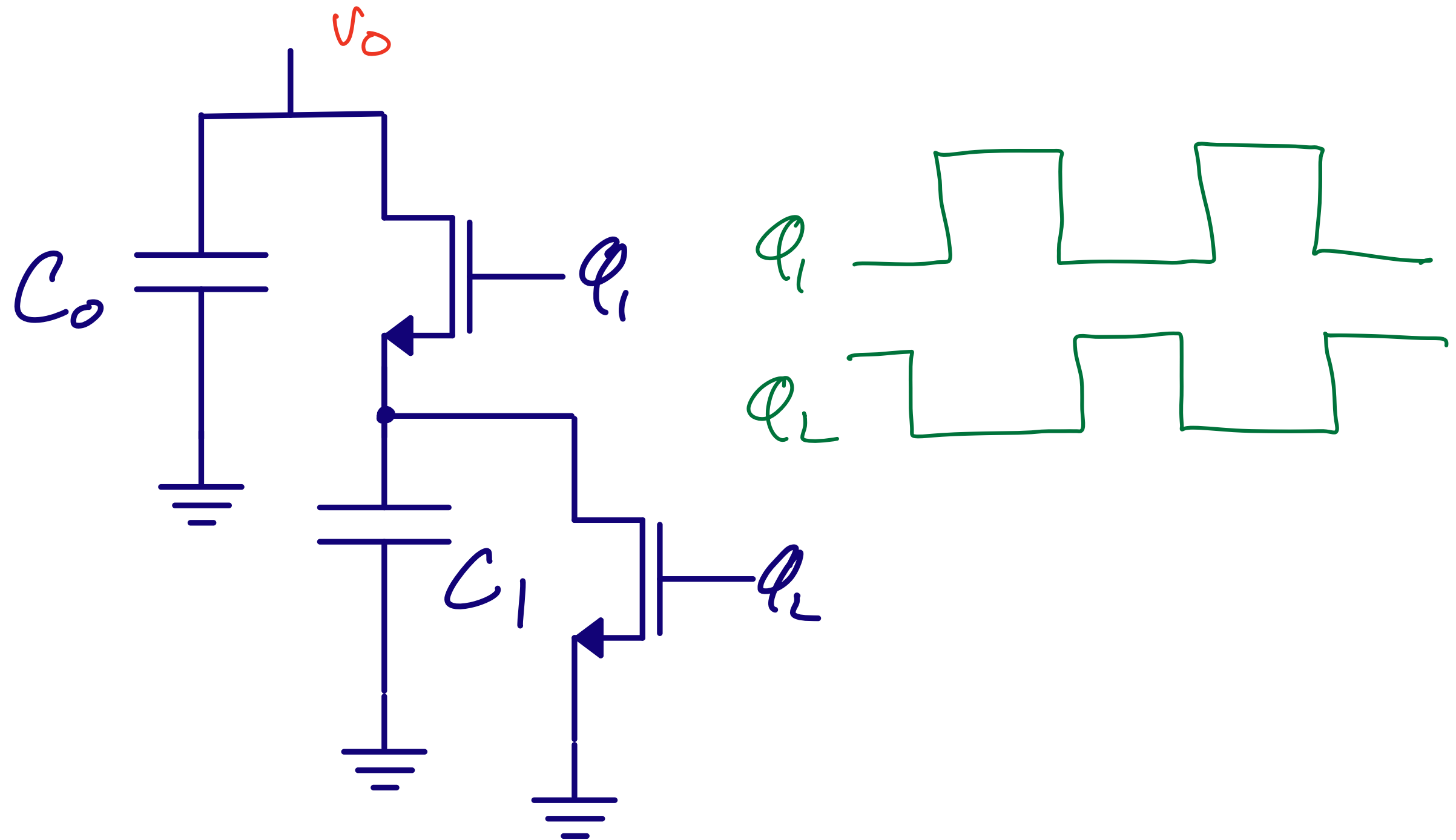
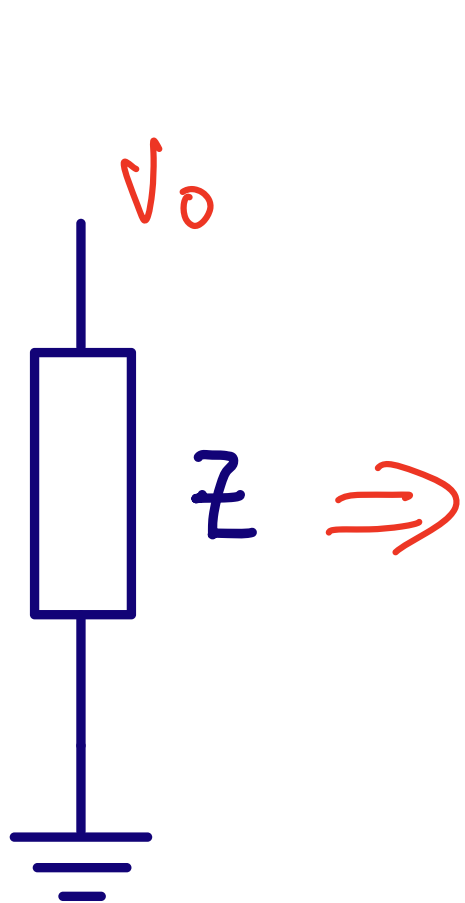
$$V_{eff1} = 2V_{eff2}$$

$$g_m = \frac{2I_d}{V_{eff}}$$

$$I = \frac{V_{eff1}}{2Z}$$

$$Z \Rightarrow \frac{1}{g_m}$$





Want to learn more?

A simple three-terminal IC bandgap reference

A CMOS bandgap reference circuit with sub-1-V operation

A sub-1-V 15-ppm//spl deg/C CMOS bandgap voltage reference without requiring low threshold voltage device

The Bandgap Reference

The Design of a Low-Voltage Bandgap Reference

Thanks!

