

A	B	S_H	C_{in}	C_{out}	S_F
0	0	0	0	0	0
0	0	0	1	0	1
0	1	1	0	0	1
0	1	1	1	1	0
1	0	1	0	0	1
1	0	1	1	1	0
1	1	0	0	1	0
1	1	0	1	1	1

$$S = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C}$$

$$+ ABC$$

XNOR

$$= (\bar{A}B + \bar{B}A)\bar{C} + C(\bar{A}\bar{B} + AB)$$

XOR

$$XOR = D\bar{E} + E\bar{D}$$

$$S = A \oplus B \oplus C$$

$$C_{out} = \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C$$

$$+ ABC$$

$$= (\bar{A}B + A\bar{B})C + AB(C + \bar{C})$$

$$= (A \oplus B)C + AB \Rightarrow \text{Majority gate}$$