

TFE4152 - Lecture 4

MOSFET's

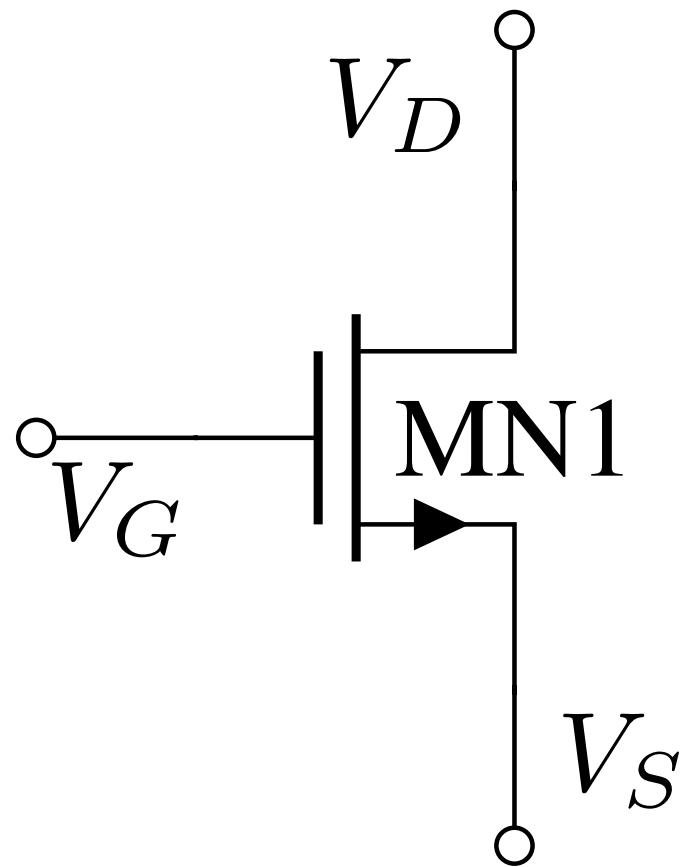
Source

Goal for today

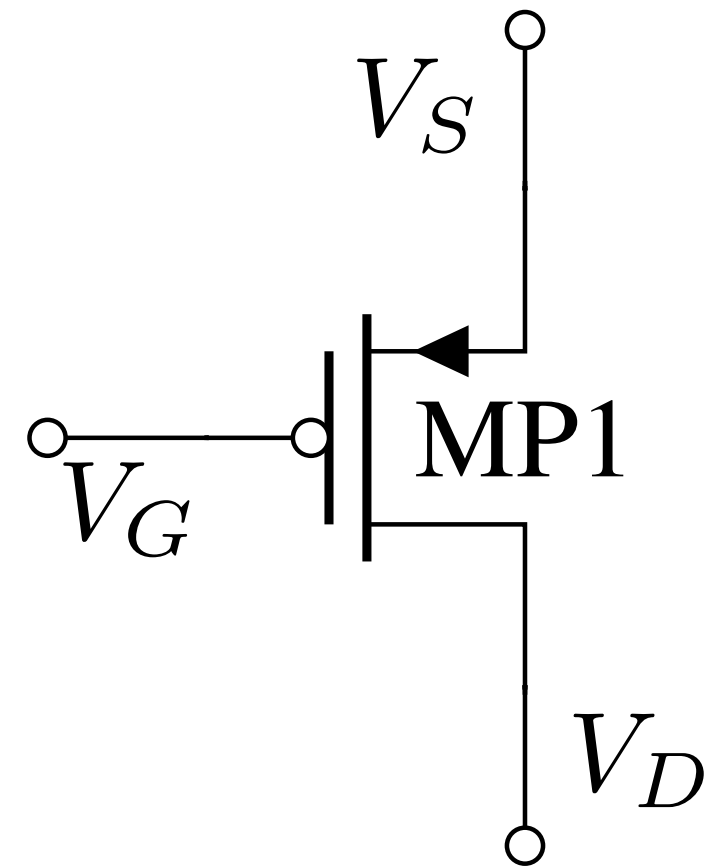
- Symbols
- Current characteristics
- Operating regions
- The square-law model
- Channel length modulation
- The small signal model (low frequency)
- Bulk Effect

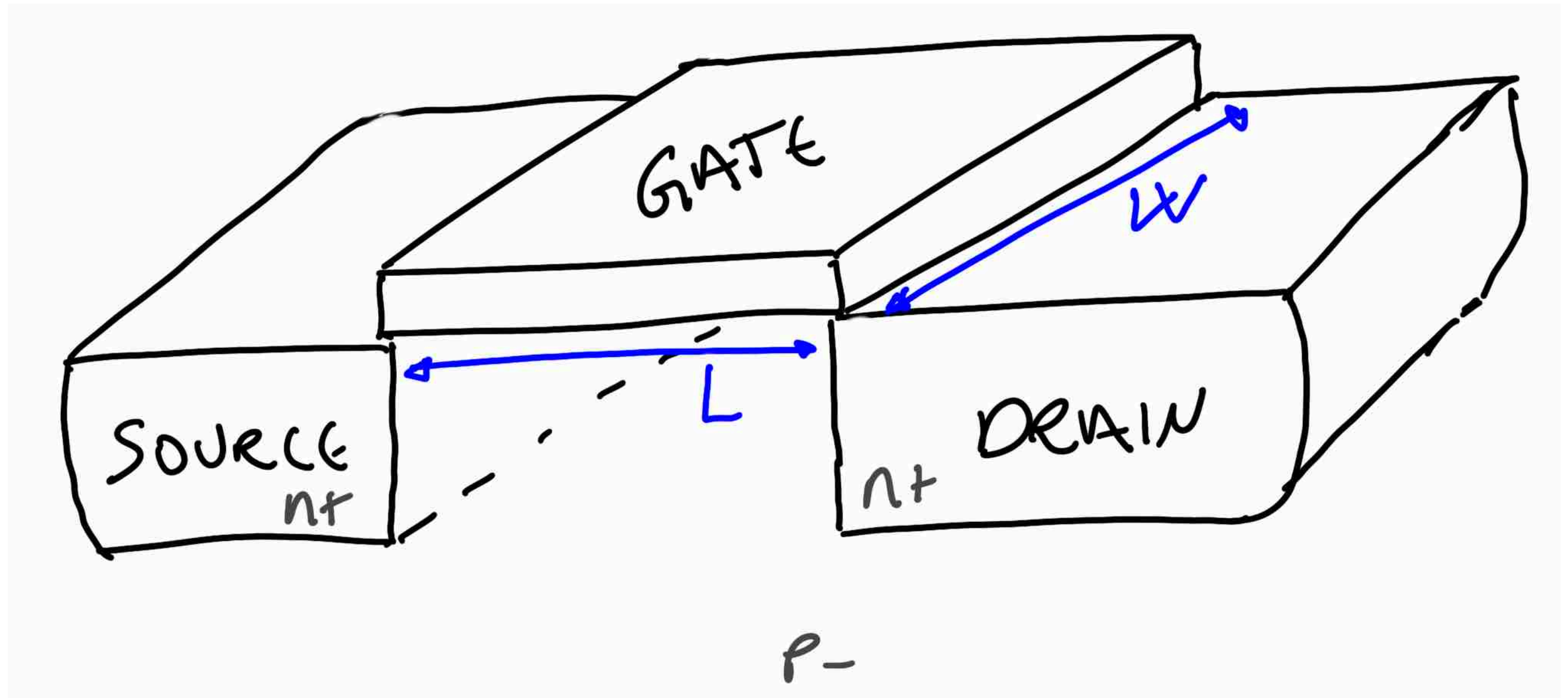
Metal-Oxide-Semiconductor (MOS) Transistors

NMOS conduct for positive gate-to-source voltage



PMOS conduct for negative gate-to-source voltage



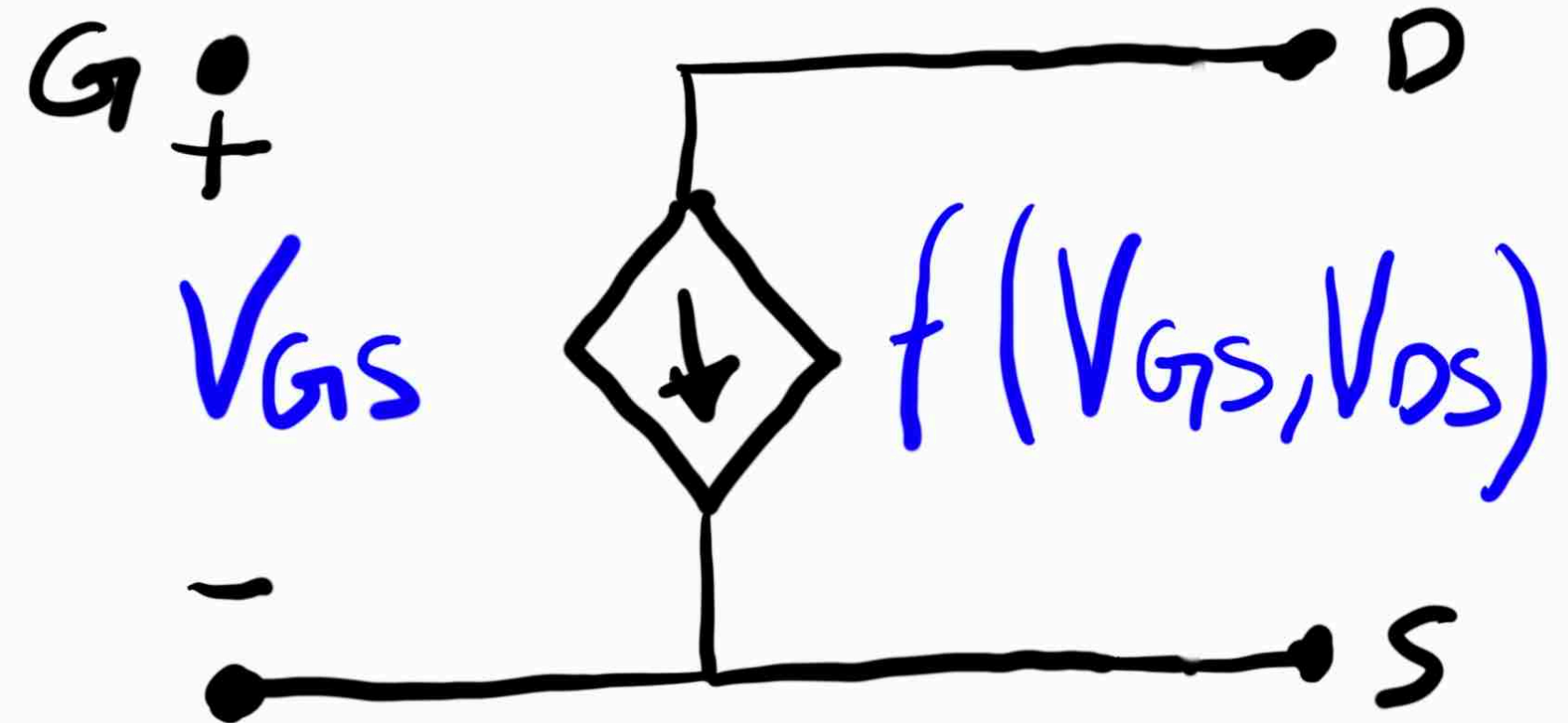


Drain Source Current (I_{DS})

`dicex/sim/spice/NCHIO`

Large signal model

$$I_{DS} = f(V_{GS}, V_{DS}, \dots)$$



Gate Source Voltage (V_{GS})

dicex/sim/spice/vgate.cir:

```
.include ../../../../lib/SUN_TRIO_GF130N.spi
.include ../../../../models/ptm_130.spi
```

```
vdrain D 0 dc 1
vgate G 0 dc 0.5
```

```
vbulk B 0 dc 0
vcur S 0 dc 0
```

```
X1 D G S B NCHIO
```

```
.dc vgate 0 1.8 0.01
```

```
.plot I(vcur)
```

dicex/lib/SUN_TRIO_GF13N.spi:

```
.SUBCKT NCHIO D G S B
M1 D G S B nmos w=1.08u l=0.6u
.ENDS
```

dicex/models/ptm_130.spi

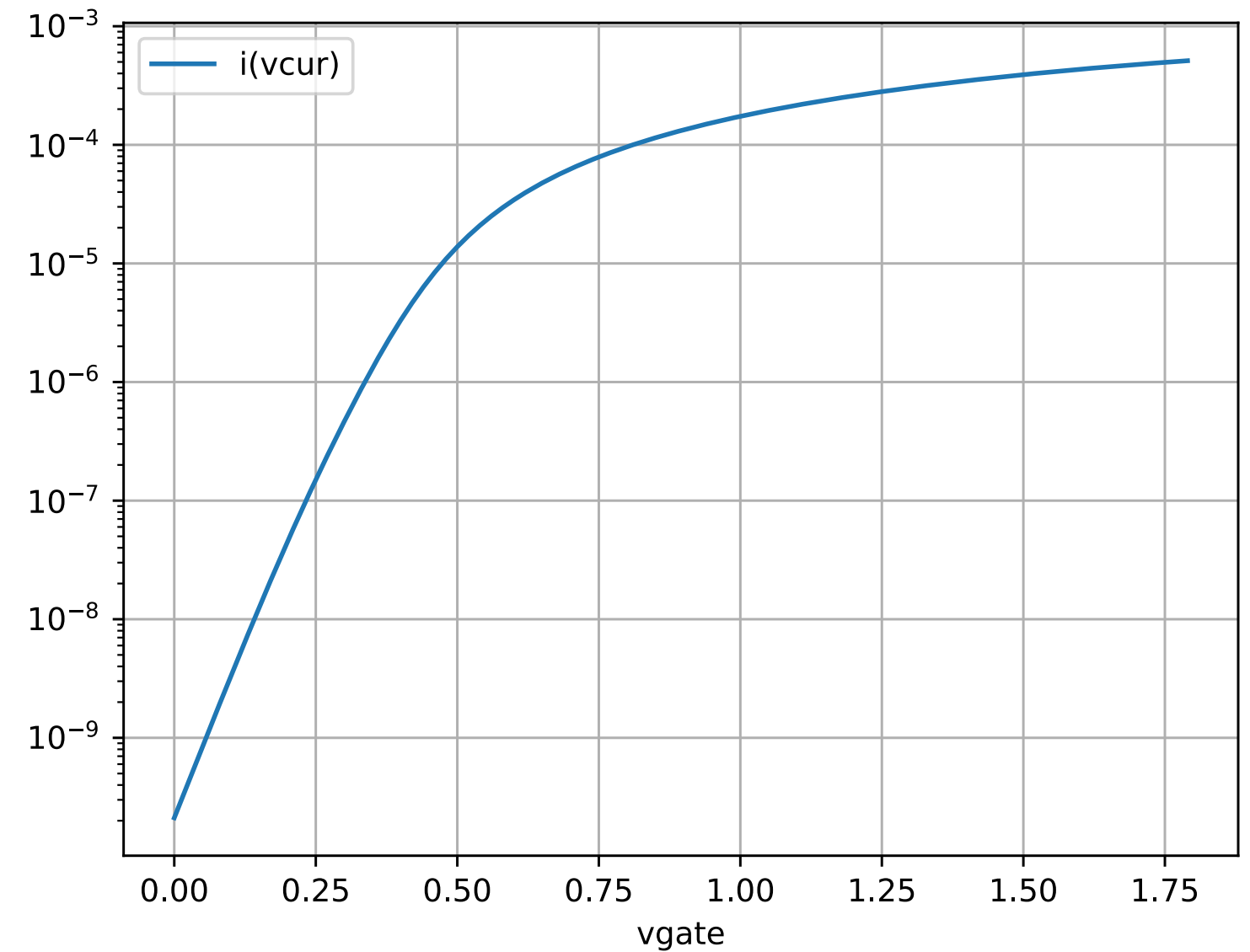
```
.model nmos nmos level = 21
+version = 4.0          binunit = 1          paramchk= 1          mobmod = 0
+capmod = 2             igcmmod = 1          igbmod = 1          geomod = 1
+diomod = 1             rdsmod = 0           rbodmod= 1          rgatemod= 1
+permod = 1             acnqsmod= 0          trnqsmod= 0

+tnom = 27              toxex = 2.25e-9      toxp = 1.6e-9      toxm = 2.25e-9
+dtox = 0.65e-9         epsrox = 3.9         wint = 5e-009      lint = 10.5e-009
...(about 60 more lines)
```


Gate-source voltage

Param	Voltage [V]
V_{GS}	0 to 1.8
V_{DS}	1.0
V_S	0
V_B	0

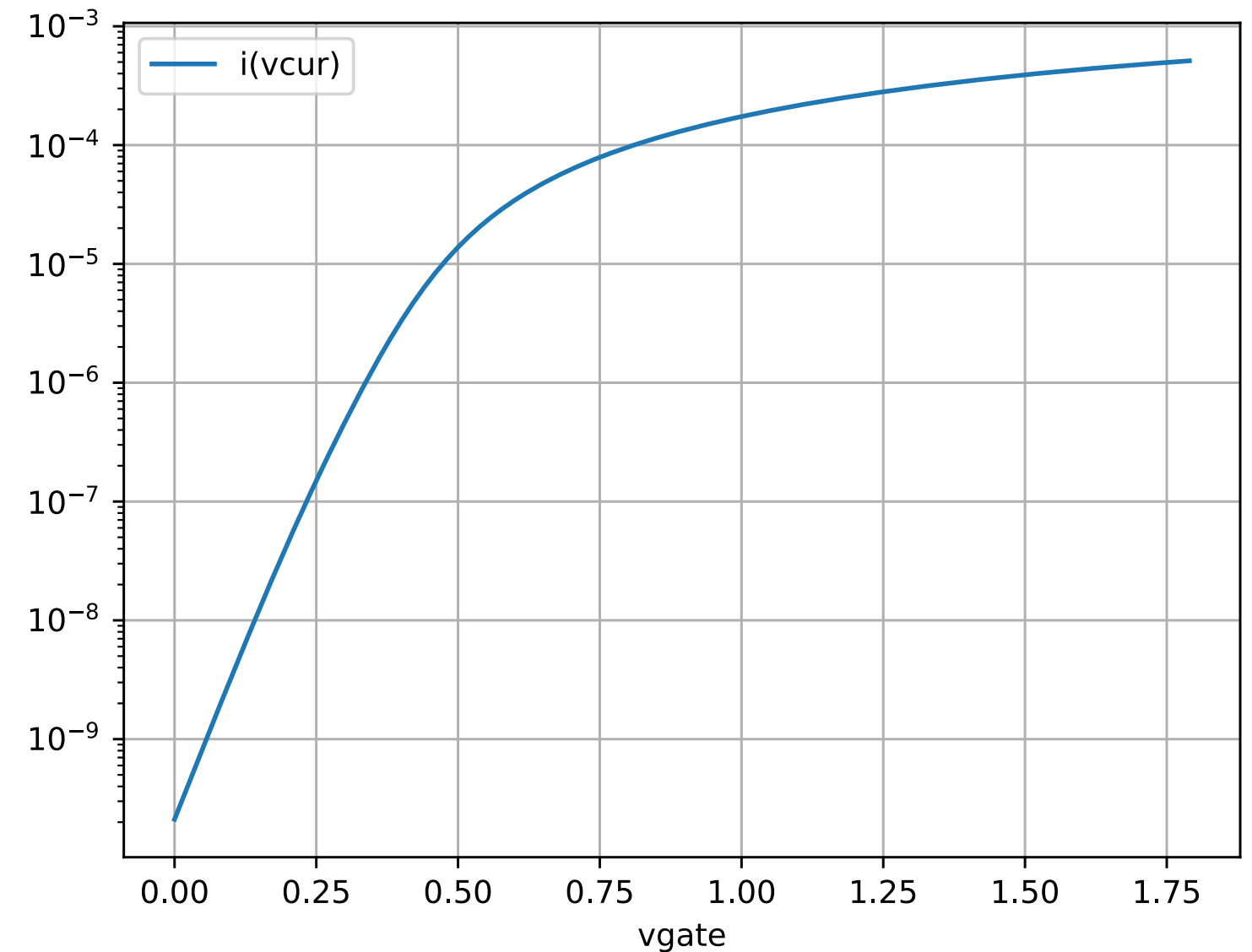
$$i(vcur) = I_{DS}$$



Inversion level

Define $V_{eff} \equiv V_{GS} - V_{tn}$, where V_{tn} is the "threshold voltage"

V_{eff}	Inversion level
< 0	weak inversion or subthreshold
0	moderate inversion
$> 100 \text{ mV}$	strong inversion

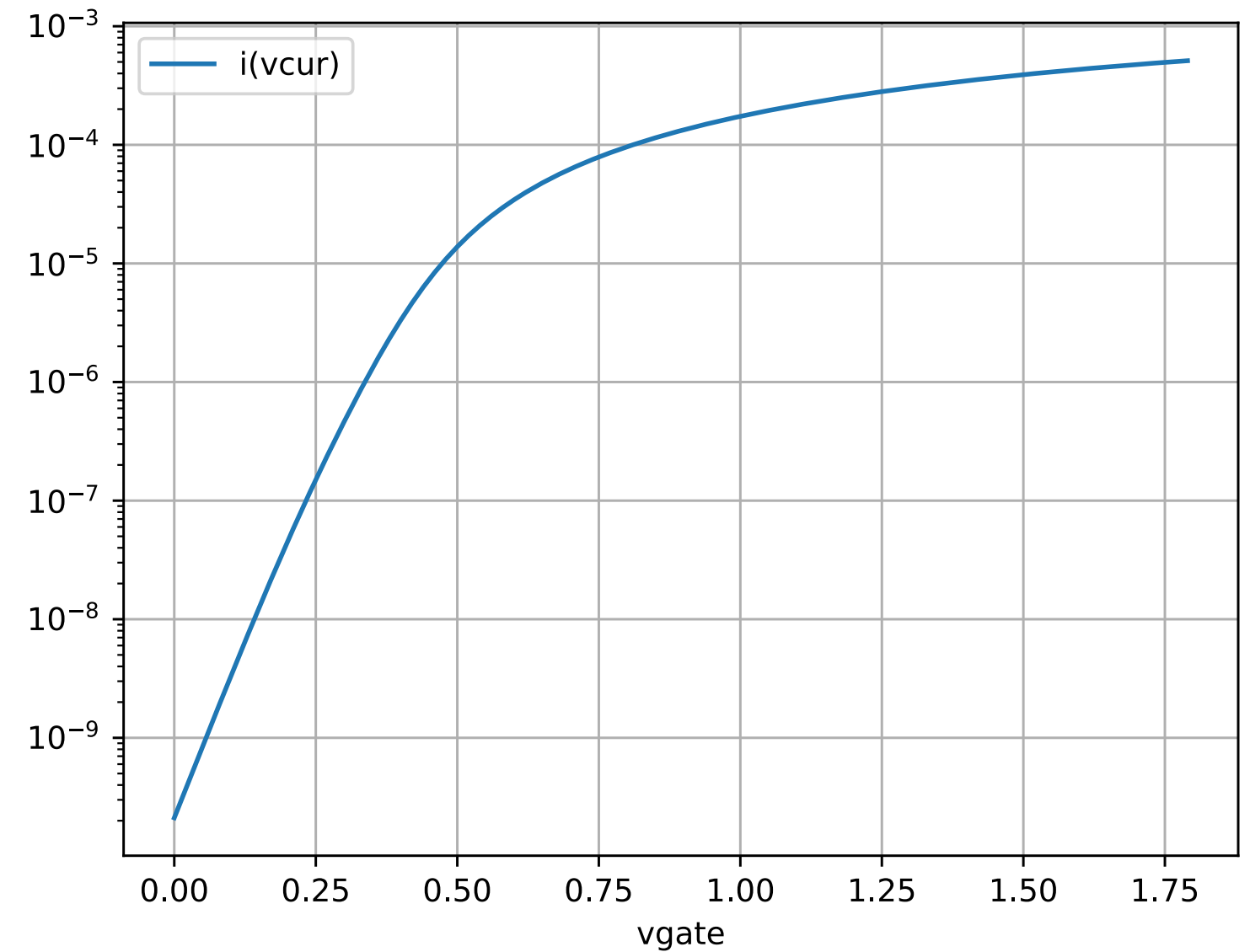


Weak inversion

The drain current is low, but not zero,
when $V_{eff} \ll 0$

$$I_{DS} \approx I_{D0} \frac{W}{L} e^{V_{eff}/nV_T} \text{ if } V_{DS} > 3V_T$$

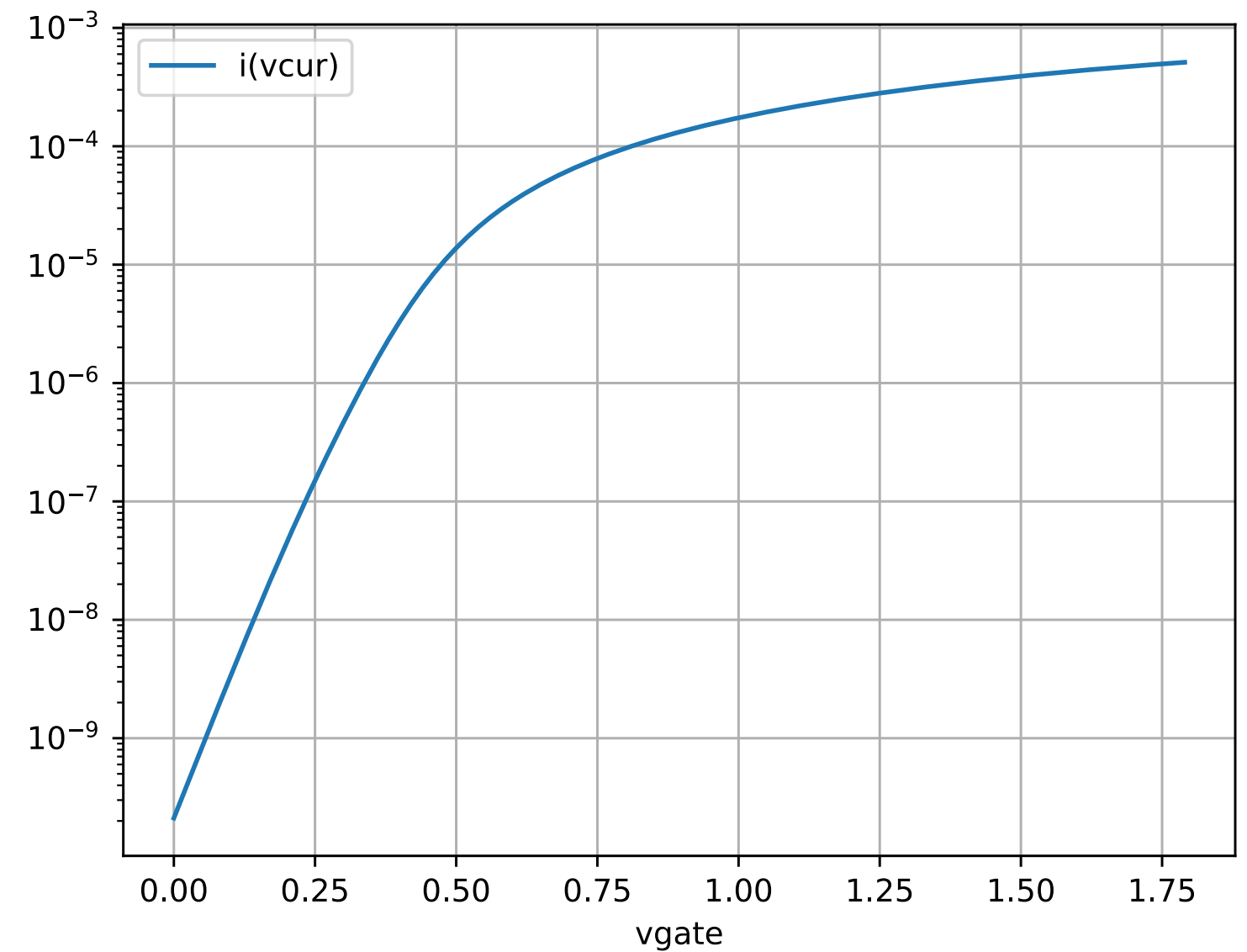
$$n \approx 1.5$$



Moderate inversion

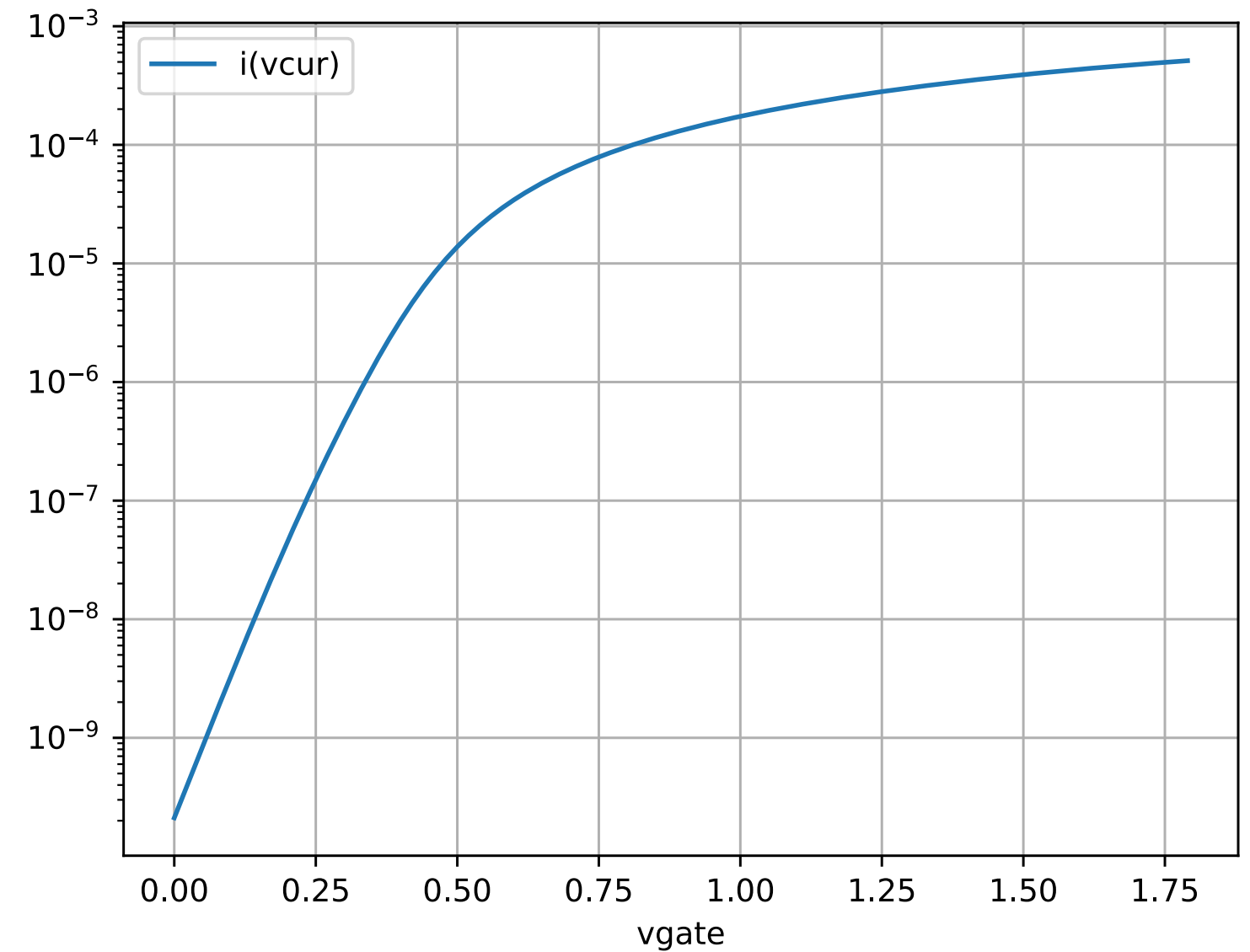
Stay away from moderate inversion for analog design.

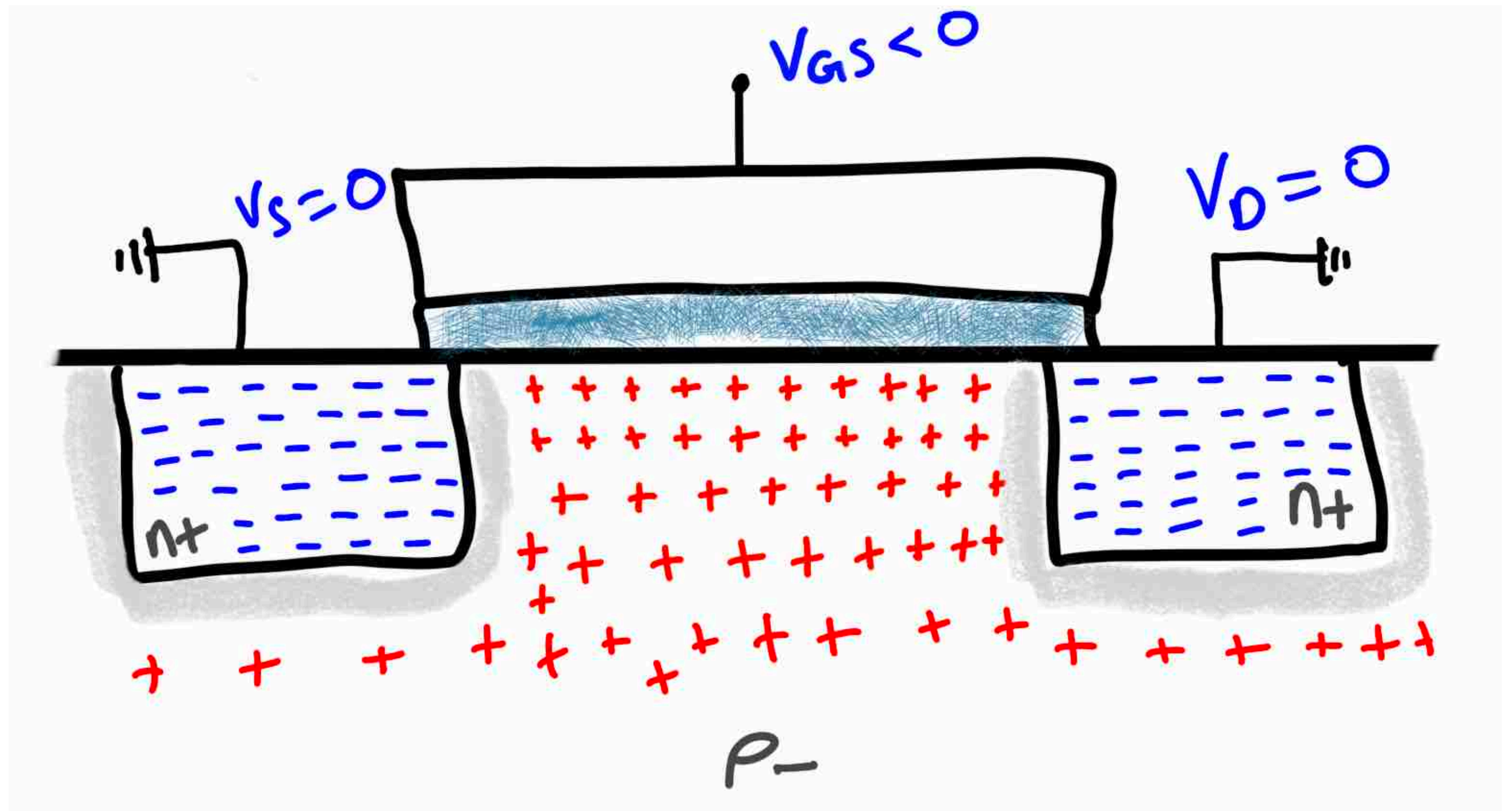
If you can't, then trust the model

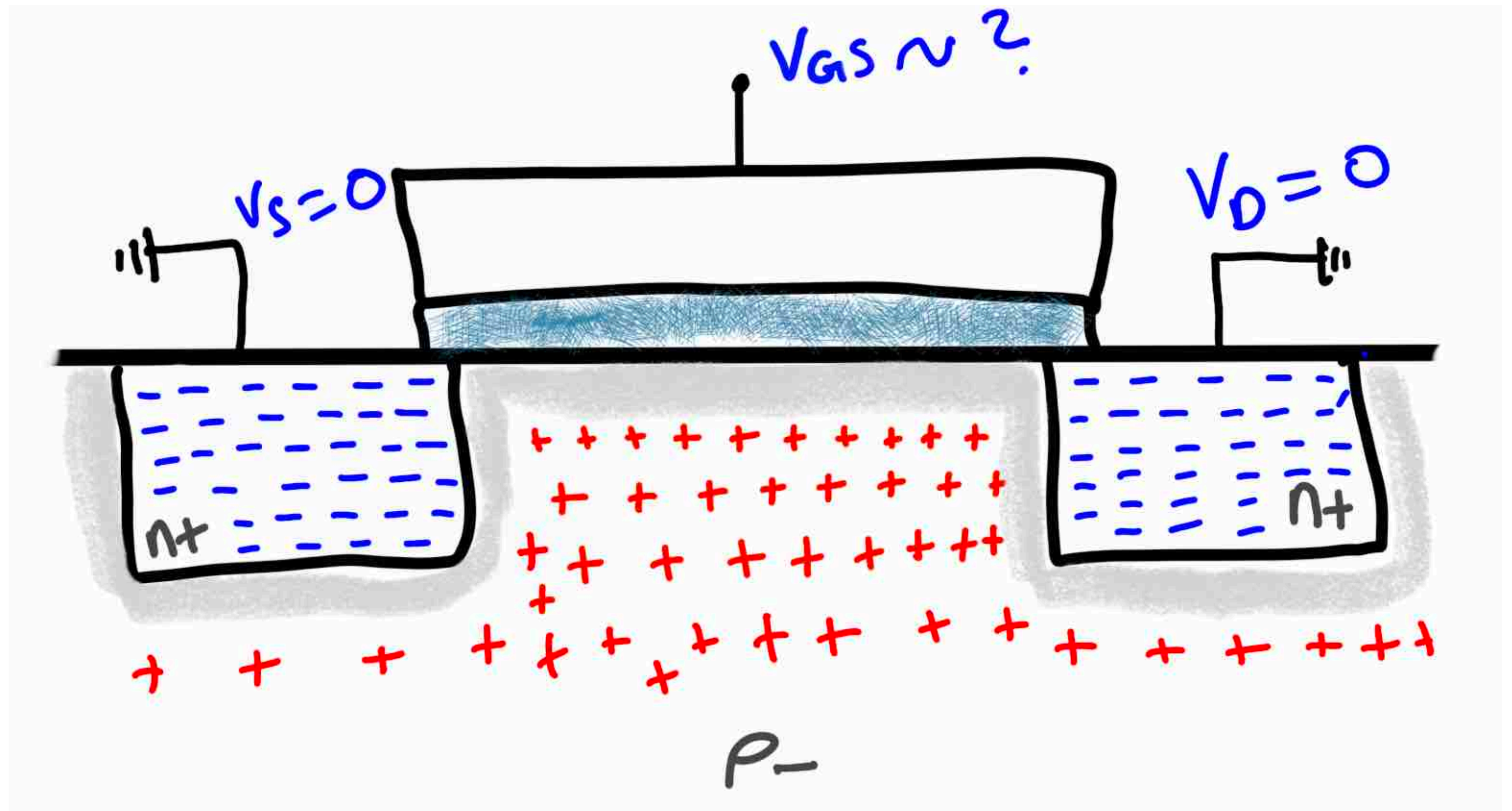


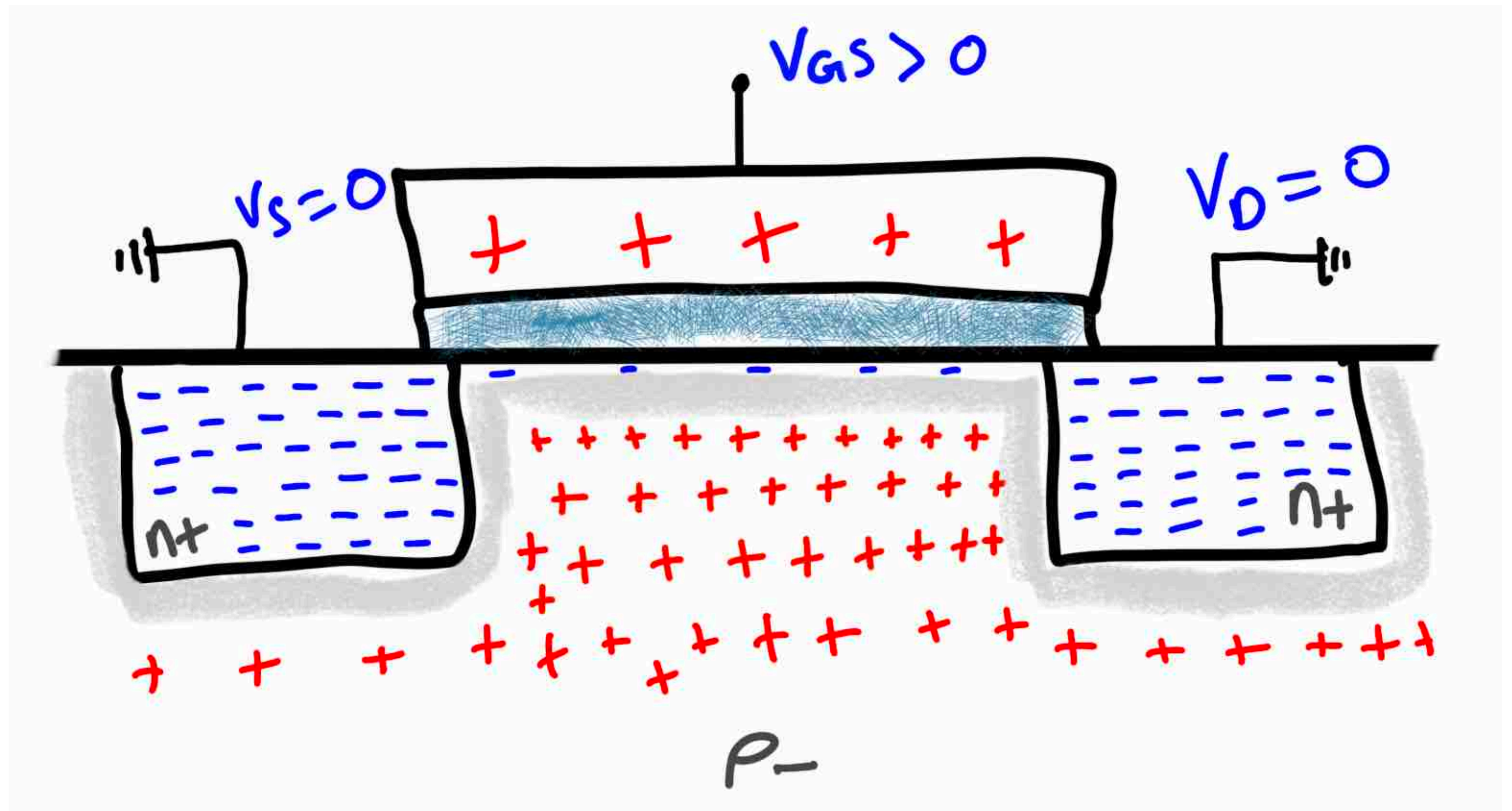
Strong inversion

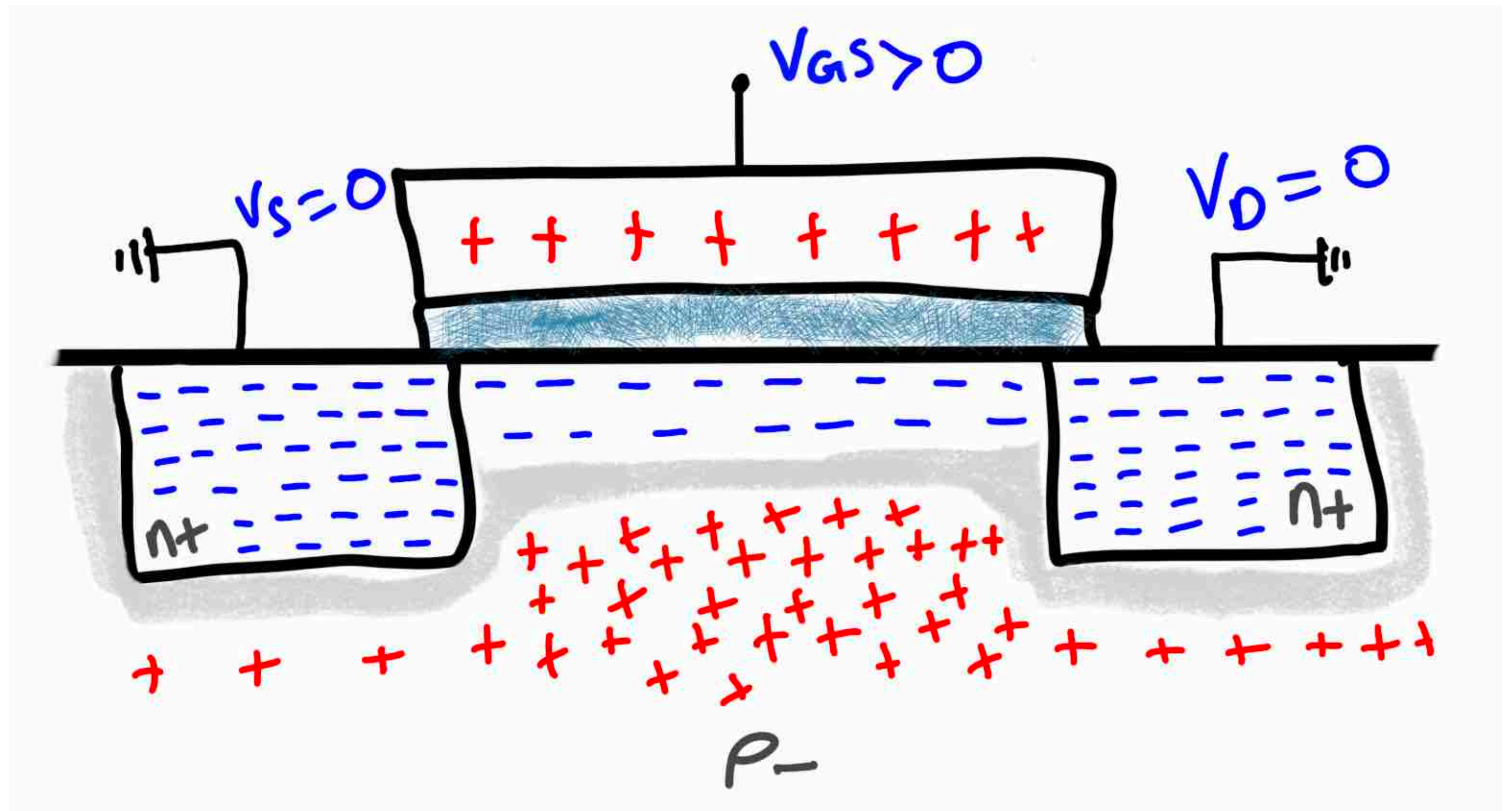
$$I_{DS} = \mu_n C_{ox} \frac{W}{L} \begin{cases} V_{eff} V_{DS} & \text{if } V_{DS} \ll V_{eff} \\ V_{eff} V_{DS} - V_{DS}^2/2 & \text{if } V_{DS} < V_{eff} \\ \frac{1}{2} V_{eff}^2 & \text{if } V_{DS} > V_{eff} \end{cases}$$











The threshold voltage (V_{tn}) is
defined as $p_p = n_{ch}$

Gate Source Capacitance (C_{GS})

C_{GS} for $V_{DS} = 0, V_S = 0$

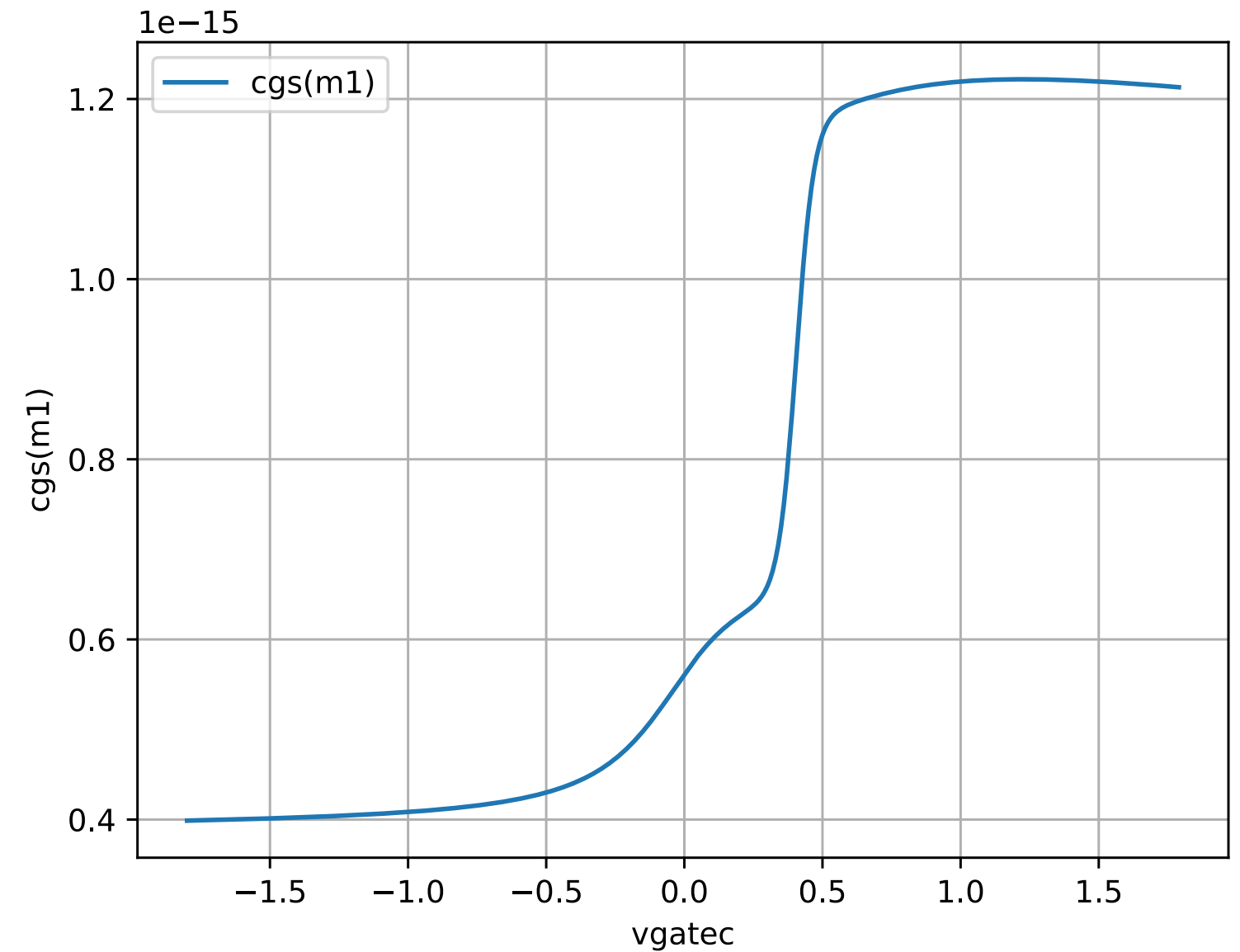
In strong inversion

$$C_{GS} = WLC_{ox}$$

where

$$C_{ox} = \frac{K_{ox}\epsilon_0}{t_{ox}}$$

$$Q_{ch} = WLC_{ox}V_{eff}$$

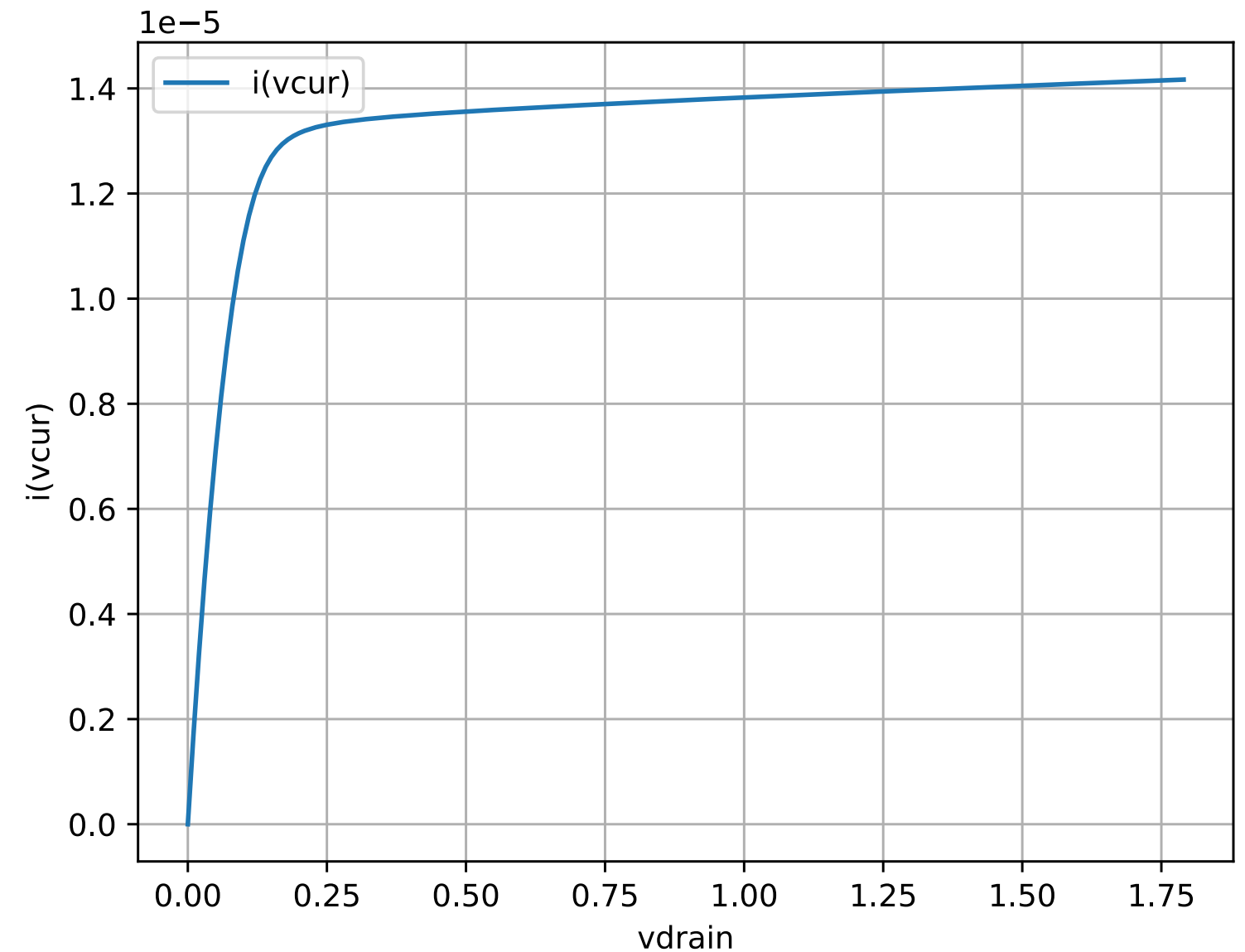


Drain Source Voltage (V_{DS})

Drain-source voltage

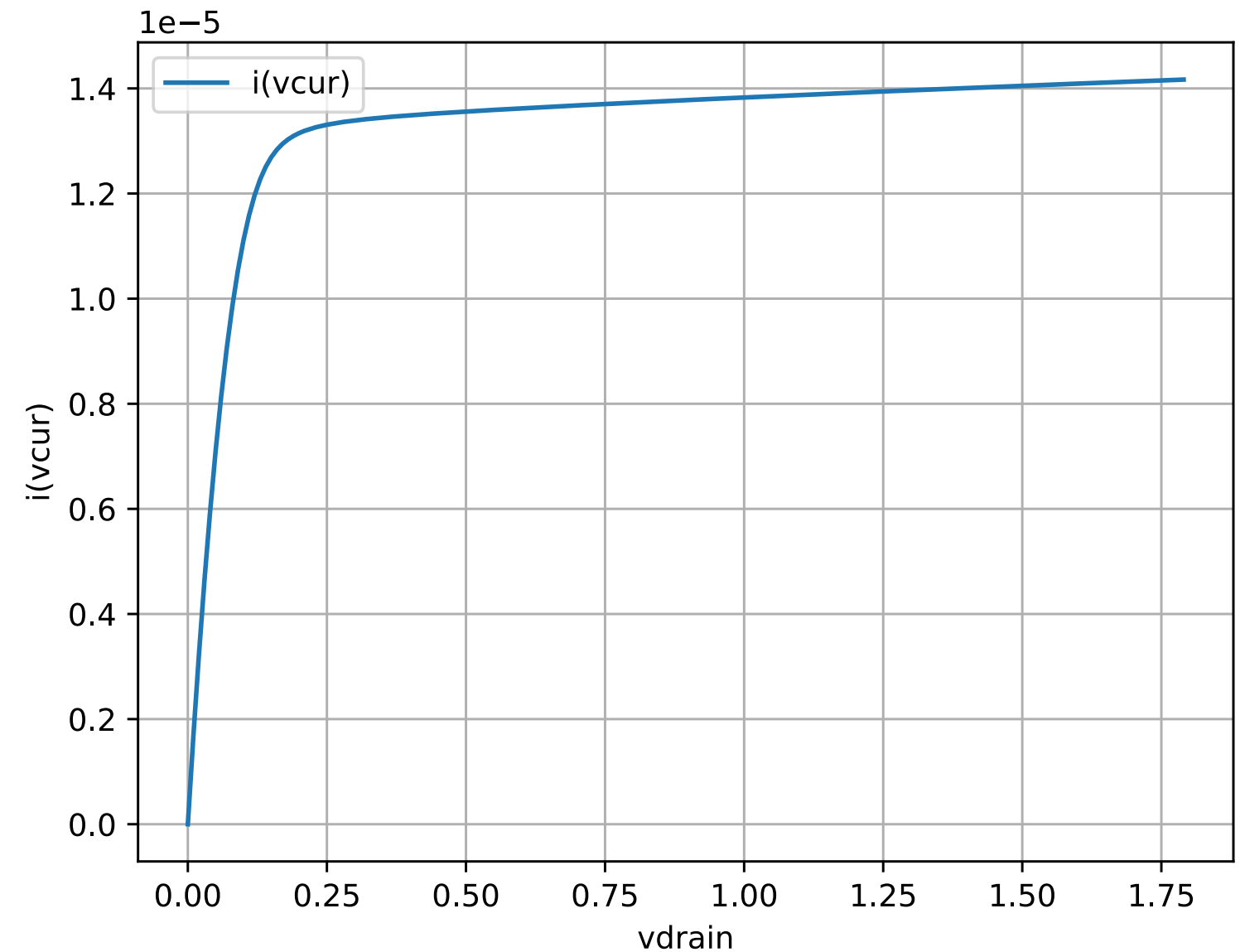
Param	Voltage [V]
V_{GS}	0.5
V_{DS}	0 to 1.8
V_S	0
V_B	0

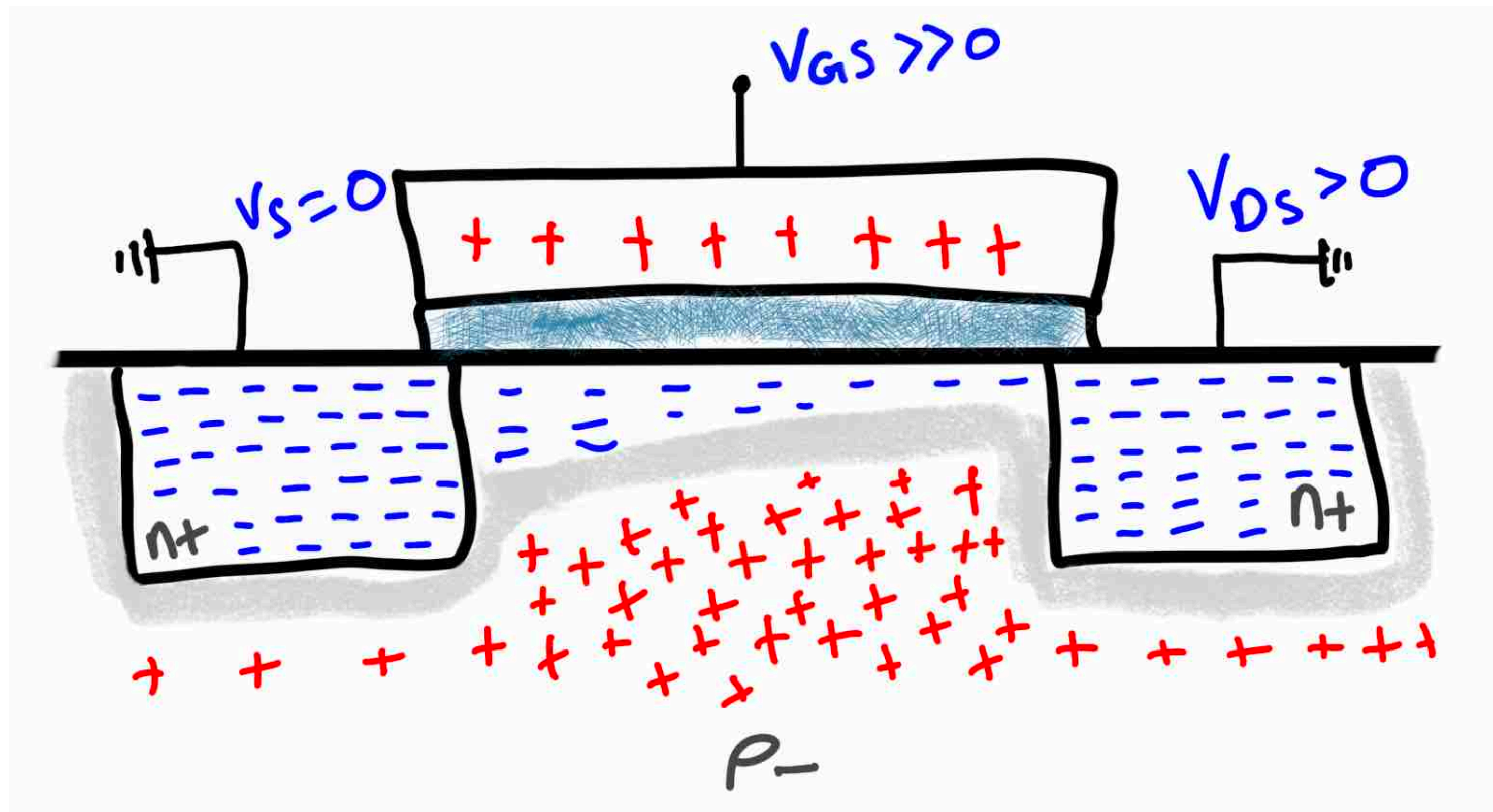
$$i(vcur) = I_{DS}$$

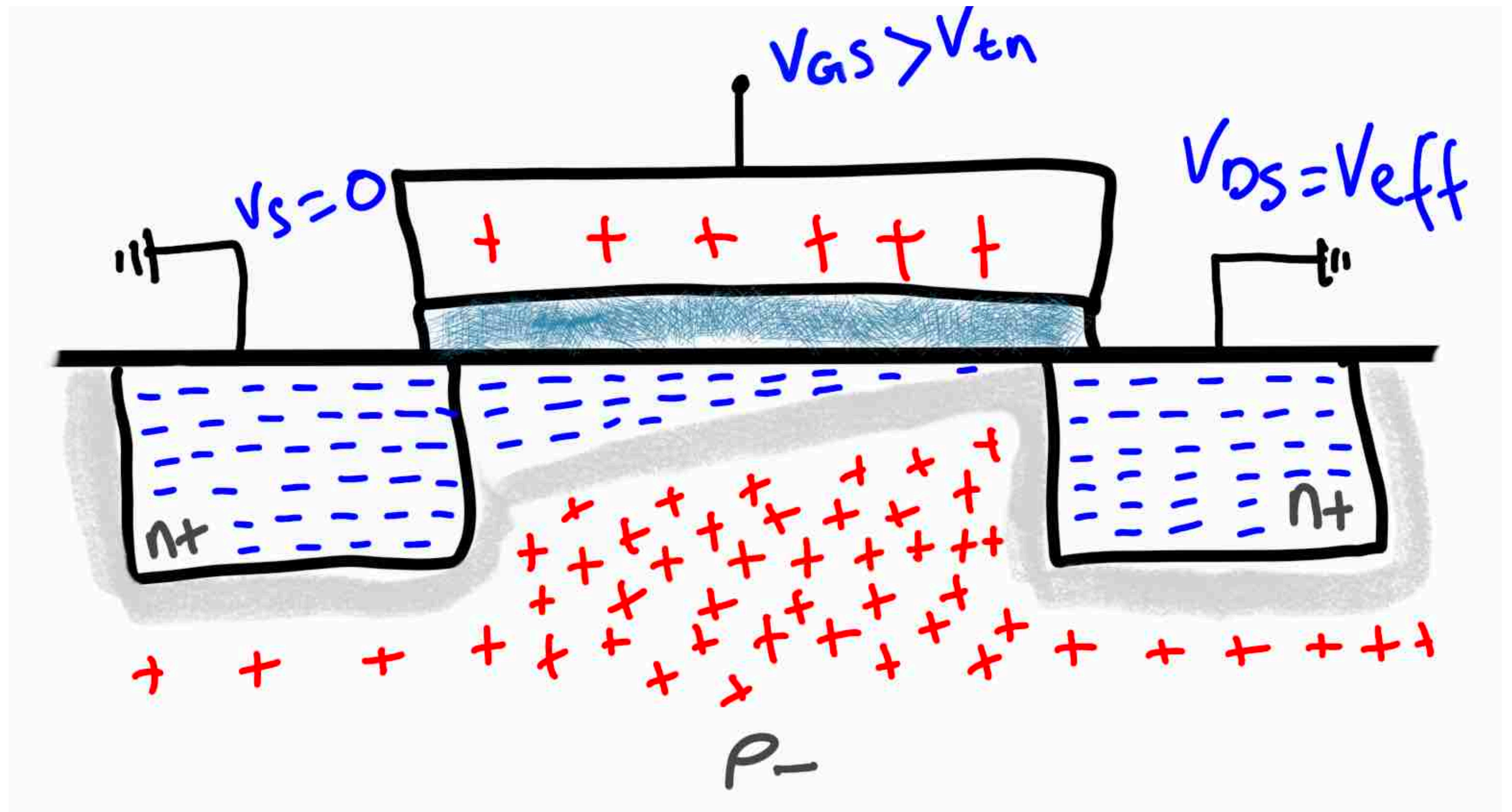


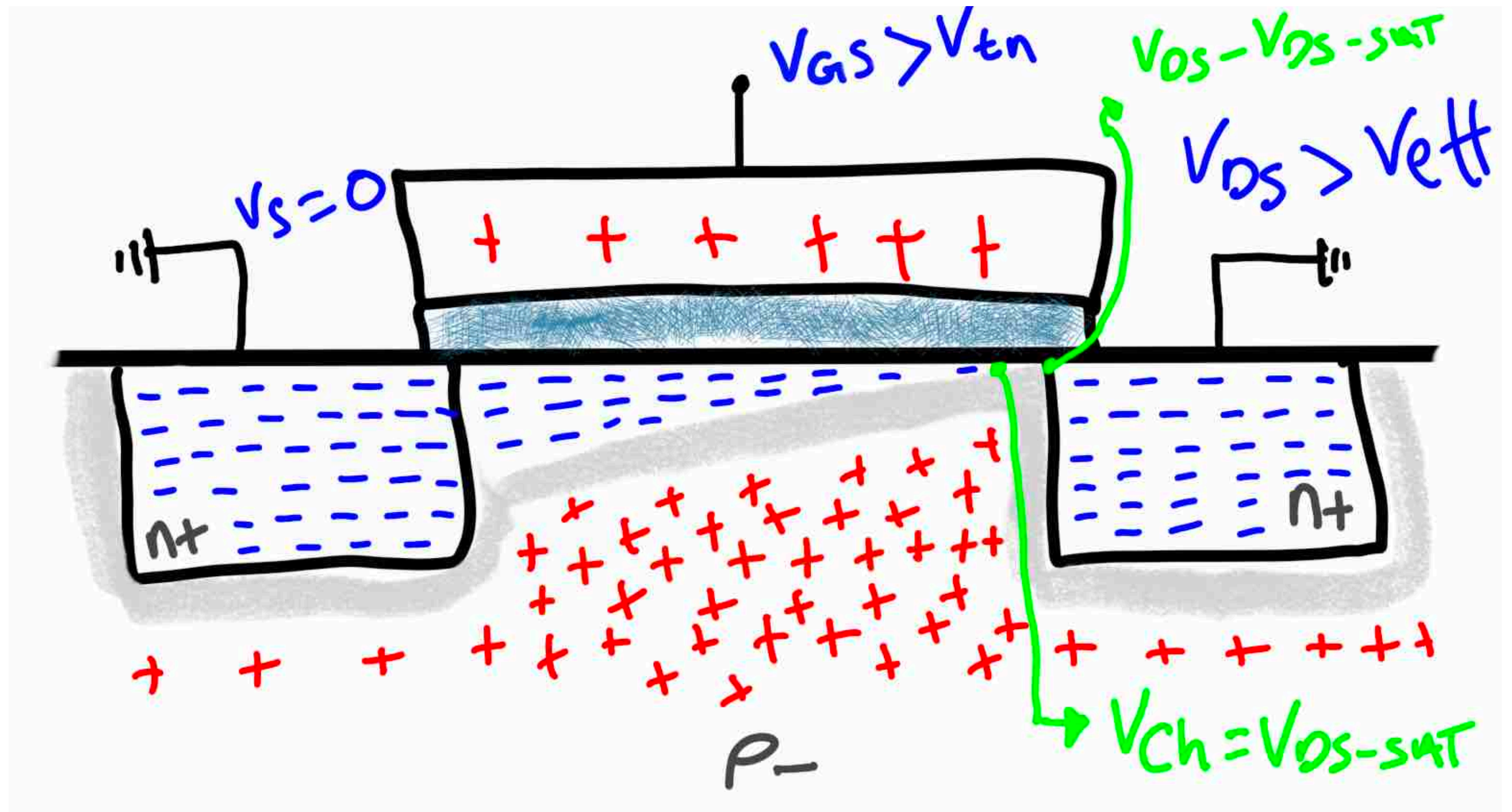
Strong inversion

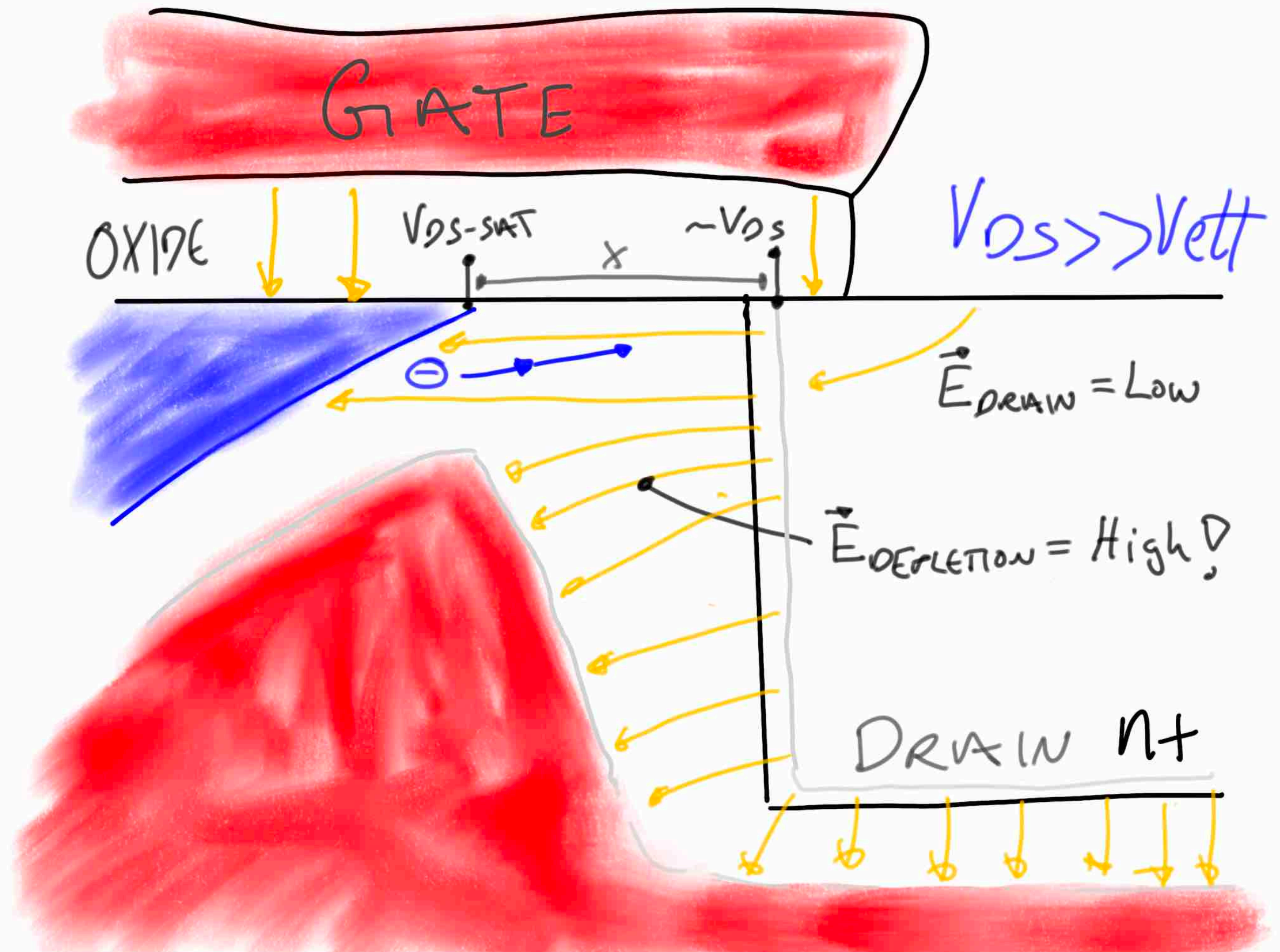
$$I_{DS} = \mu_n C_{ox} \frac{W}{L} \begin{cases} V_{eff} V_{DS} & \text{if } V_{DS} \ll V_{eff} \\ V_{eff} V_{DS} - V_{DS}^2/2 & \text{if } V_{DS} < V_{eff} \\ \frac{1}{2} V_{eff}^2 & \text{if } V_{DS} > V_{eff} \end{cases}$$

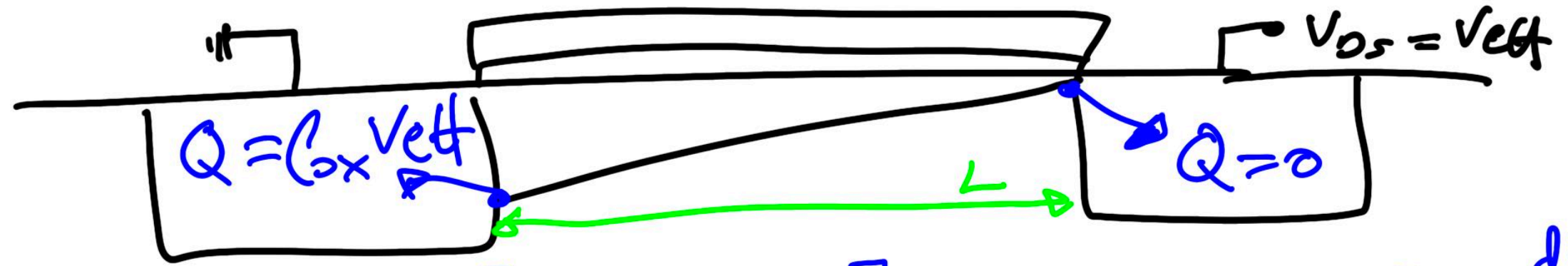












$$Q(x) = C_{ox} [V_{eff} - V(x)] \quad v = \text{speed} = \mu_n E = \mu_n \frac{dV}{dx}$$

$$I_D = W \cdot Q(x) \cdot v = \underbrace{\mu_n C_{ox} W}_l [V_{eff} - V(x)] \frac{dV}{dx}$$

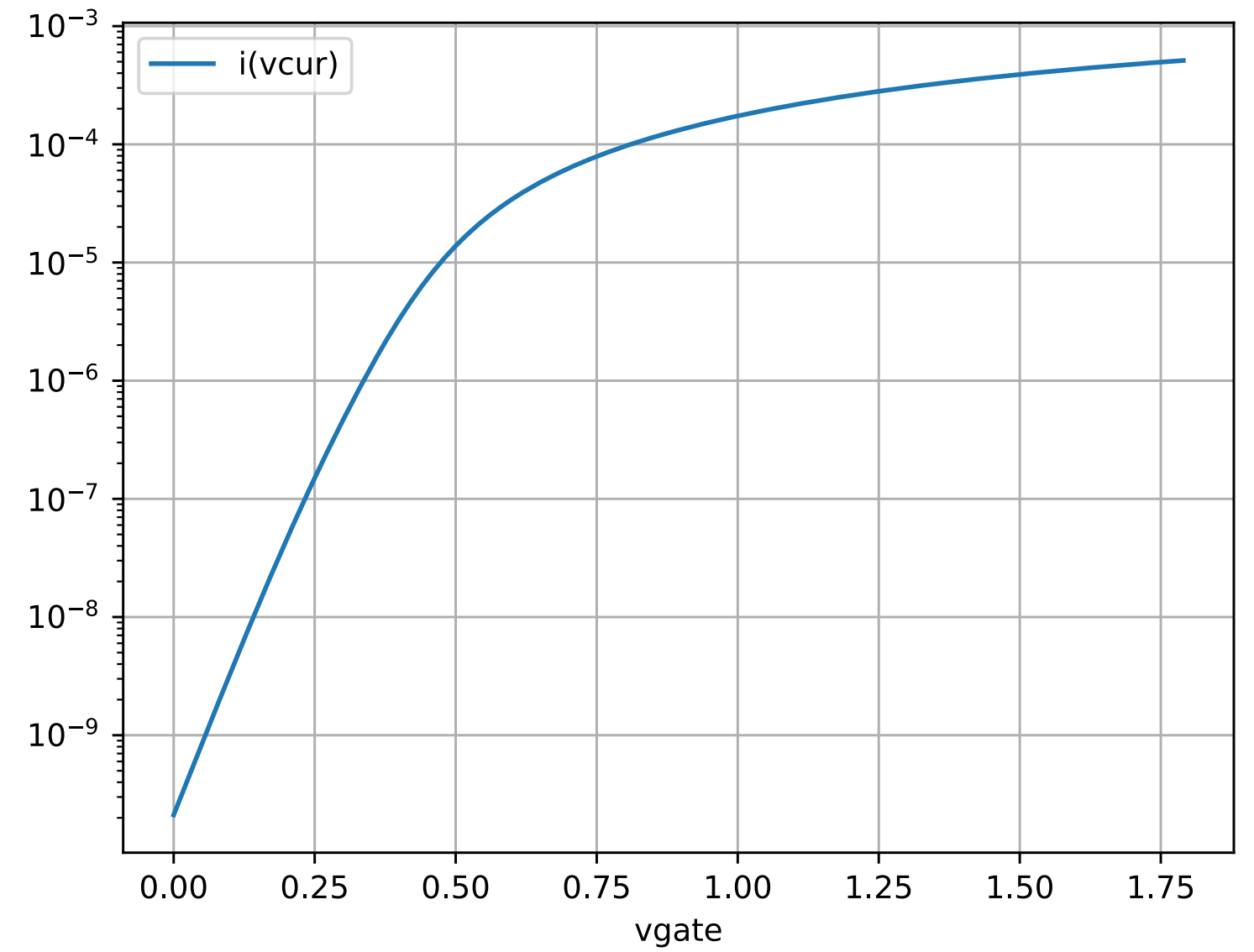
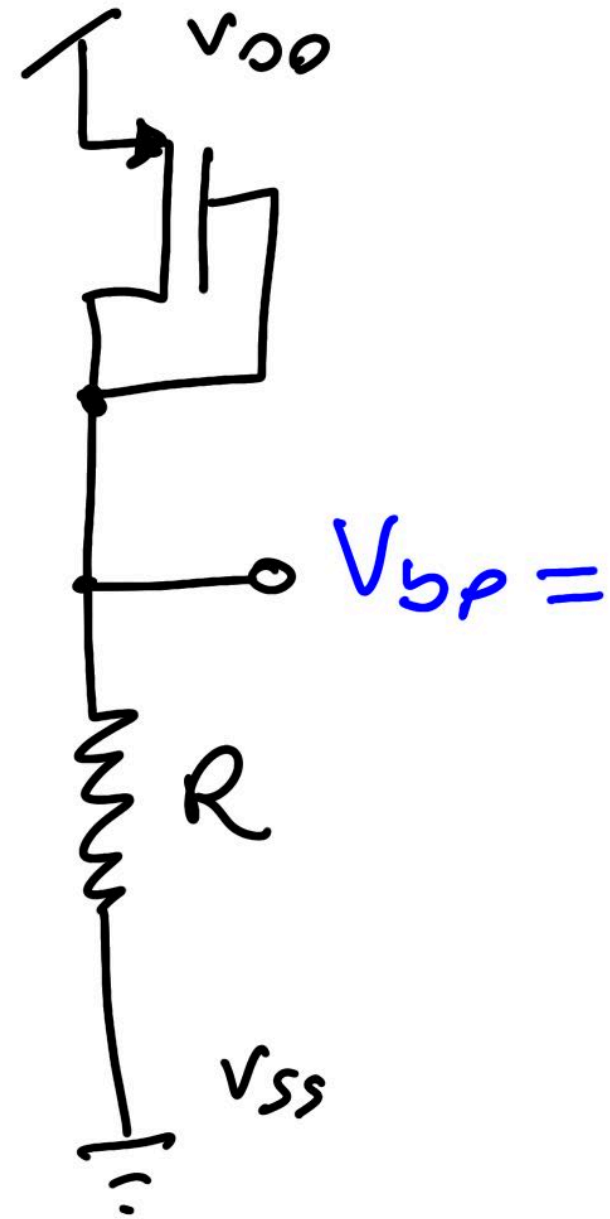
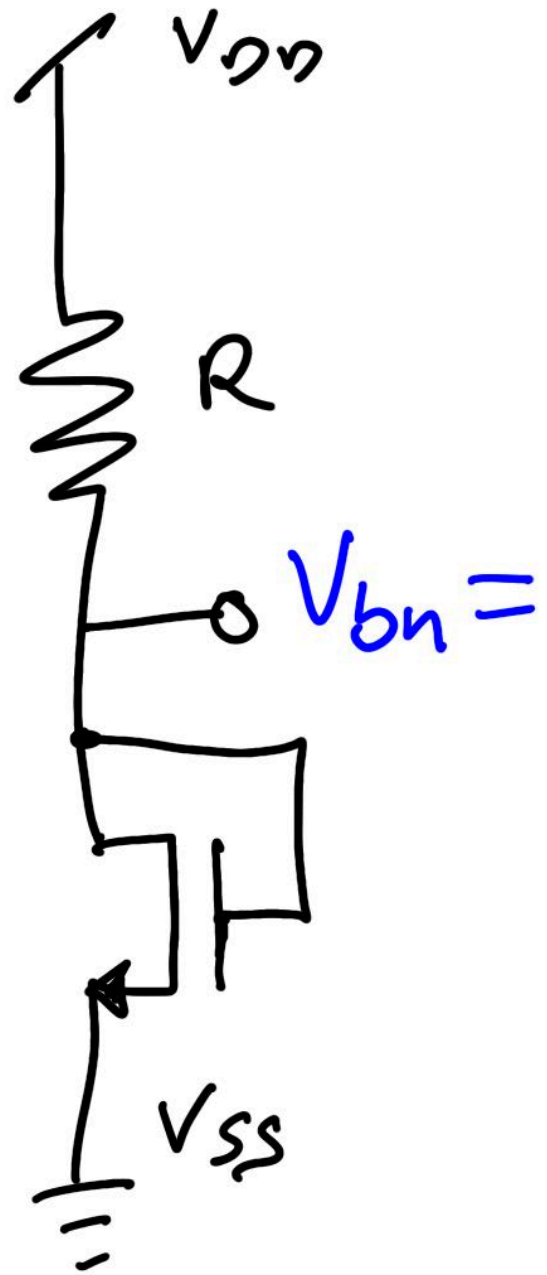
$$I_D dx = l [V_{eff} - V(x)] dV$$

$$I_D \int_0^L dx = l \int_0^{V_{ds}} [V_{eff} - V(x)] dV$$

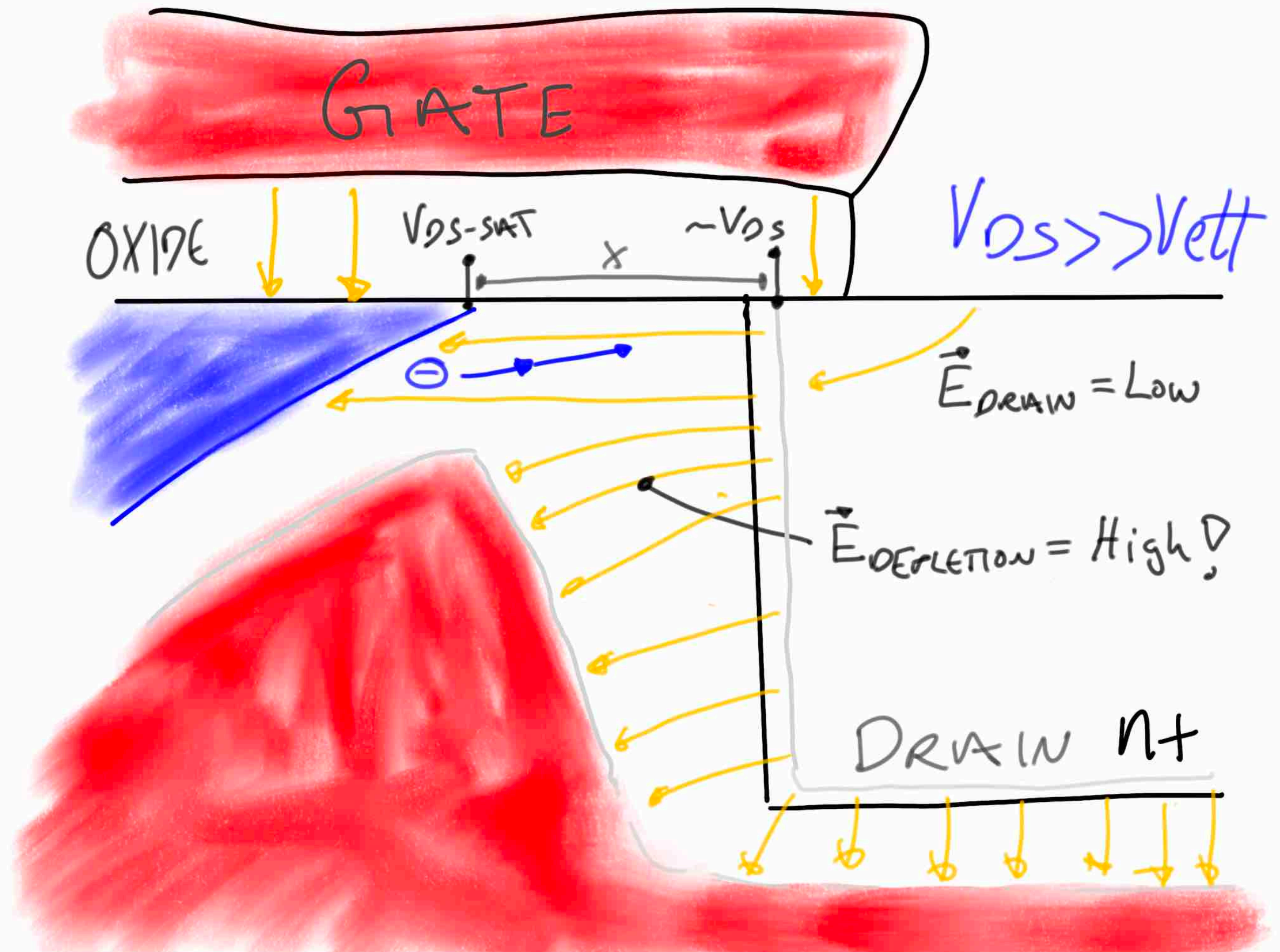
$$I_D L = \mu_n C_{ox} W \left[V_{eff} V_{ds} - \frac{V_{ds}^2}{2} \right]$$

Carsten Wulff 2021 @ $V_{ds} = V_{eff} \Rightarrow \underline{\underline{I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} V_{eff}^2}}$

Head simulation



Channel length modulation



$$I_{DS} = \mu_n C_{ox} \frac{W}{L} \begin{cases} V_{eff} V_{DS} & \text{if } V_{DS} \ll V_{eff} \\ V_{eff} V_{DS} - V_{DS}^2/2 & \text{if } V_{DS} < V_{eff} \\ \frac{1}{2} V_{eff}^2 [1 + \lambda(V_{DS} - V_{eff})] & \text{if } V_{DS} > V_{eff} \end{cases}$$

$$\lambda = \frac{k_{ds}}{2L\sqrt{V_{DS} - V_{eff} + \Phi_0}}, \text{ where } k_{ds} = \sqrt{\frac{2K_s\epsilon_0}{qN_A}}$$

Thanks!