$$Var(e) = Eee^T (1)$$

$$= M_2 I_n \tag{2}$$

$$Cov(\mu^T e, e^T e) = \mu^T E e e^T e$$

$$= \mu^T M_3 1_n$$
(3)

$$= \mu^T M_3 1_n \tag{4}$$

$$Var(e^T e) = Ee^T ee^T e - (Ee^T e)^2$$
 (5)

$$= nM_4 - nM_2^2 (6)$$

$$Var(X^{T}X) = Var(2\mu^{T}e + e^{T}e)$$

$$= 4\mu^{T}Var(e)\mu + 4Cov(\mu^{T}e, e^{T}e) + Var(e^{T}e)$$

$$= 4M_{2}\mu^{T}\mu + 4M_{3}\mu^{T}1_{n} + nM_{4} - nM_{2}^{2}$$
(7)

$$Ee^T ee^T \Phi^T \Phi e = E(\sum_{k=0}^n e_k^2) (\sum_{i,j} \Lambda_{i,j} e_i e_j)$$
(8)

$$= E(\sum_{k=0}^{n} e_k^2) (\sum_{k=0}^{n} \Lambda_{k,k} e_k^2)$$
 (9)

$$= E(\sum_{k=0}^{n} \Lambda_{k,k} e_k^2 (\sum_{i=0}^{n} e_i^2))$$
 (10)

$$= (M_4 + (n-1)M_2^2) \sum_{k=0}^{n} \Lambda_{k,k}$$
 (11)

$$= (M_4 + (n-1)M_2^2)(n-m)\sum_{k=0}^{m} \phi_k^2$$
 (12)

$$Cov(X^{T}X, e^{T}\Phi^{T}\Phi e) = Cov(2\mu^{T}e + e^{T}e, e^{T}\Phi^{T}\Phi e)$$
(13)

$$= 2\mu^{T}Eee^{T}\Phi^{T}\Phi e + Ee^{T}ee^{T}\Phi^{T}\Phi e - (Ee^{T}e)(Ee^{T}\Phi^{T}(\Phi e))$$

$$= 2M_{3}\mu^{T}diag(\Lambda) + (M_{4} + (n-1)M_{2}^{2})(n-m)\sum_{k=0}^{m}\phi_{k}^{2}$$
(15)

$$-n(n-m)M_{2}^{2}\sum_{k=0}^{m}\phi_{m}^{2}$$
(16)

$$= 2M_{3}\mu^{T}diag(\Lambda) + (M_{4} - M_{2}^{2})(n-m)\sum_{k=0}^{m}\phi_{k}^{2}$$
(17)