

Prob2,

FASTER-ALL-PAIRS-SHORTEST-PATHS(W):

$n = W.rows$

$L^1 = W$

$m = 1$

while $m < n - 1$:

 let L^{2^m} be a new $n \times n$ matrix

$L^{2^m} = \text{EXTEND-SHORTEST-PATHS}(L^m, L^m)$

$m = 2m$

$L^{check} = \text{EXTEND-SHORTEST-PATHS}(L^m, L^m)$

For $i = 1$ to n

 If $L^{check}_{ii} < 0$:

 Print: "the graph contains a negative-weight cycle"

return L^m

We can detect the existence of negative cycles simply by checking whether there are negative values on the diagonal (which is L_{ii}) of the matrix $L^{(n)}$. Since the shortest weight circle might need to n edges, so we should calculate the matrix up to a least L^n which is L^{check} .