

# 000 ACTION-CONSTRAINED IMITATION LEARNING

001  
002  
003 **Anonymous authors**

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## 005 006 ABSTRACT

007 Policy learning under action constraints plays a central role in ensuring safe be-  
 008 haviors in various robot control and resource allocation applications. In this paper,  
 009 we study a new problem setting termed Action-Constrained Imitation Learning  
 010 (ACIL), where an action-constrained imitator aims to learn from a demonstrative  
 011 expert with larger action space. The fundamental challenge of ACIL lies in the  
 012 unavoidable mismatch of occupancy measure between the expert and the imita-  
 013 tor caused by the action constraints. We tackle this mismatch through *trajectory*  
 014 *alignment* and propose DTWIL, which replaces the original expert demon-  
 015 strations with a surrogate dataset that follows similar state trajectories while adhering  
 016 to the action constraints. Specifically, we recast trajectory alignment as a planning  
 017 problem and solve it via Model Predictive Control, which aligns the surrogate tra-  
 018 jectories with the expert trajectories based on the Dynamic Time Warping (DTW)  
 019 distance. Through extensive experiments, we demonstrate that learning from the  
 020 dataset generated by DTWIL significantly enhances performance across multiple  
 021 robot control tasks and outperforms various benchmark imitation learning algo-  
 022 rithms in terms of sample efficiency.

## 023 1 INTRODUCTION

024 Reinforcement learning (RL) is commonly used to solve tasks by finding a policy that maximizes  
 025 cumulative rewards through interactions with the environment. However, in many real-world appli-  
 026 cations, designing an effective reward function that consistently encourages the desired behavior in  
 027 all situations is a significant challenge. In such cases, imitation learning (IL) offers a compelling  
 028 alternative. Rather than relying on a reward function, IL learns a policy directly from a set of  
 029 pre-collected expert demonstrations, which are transition data logged from a near-optimal policy  
 030 (Pomerleau & A, 1991; Ho & Ermon, 2016).

031 In many real-world tasks, ensuring the safe and proper functioning of agents is crucial. To achieve  
 032 this, we can impose constraints that define the feasible set of actions for the agents. Classic examples  
 033 include optimally allocating network resources under capacity constraints (Xu et al., 2018; Gu et al.,  
 034 2019; Zhang et al., 2020) and robot control under kinematic limitations that prevent damage to the  
 035 robot’s physical structure (Pham et al., 2018b; Gu et al., 2017; Jaillet & Porta, 2012; Tsounis et al.,  
 036 2020). Additionally, in many IL scenarios, the performance gap between the expert and the imitator  
 037 must be considered. **For example, if data is collected using a human to perform tasks, the imitator,**  
 038 **which may be a robot with hardware limitations, is likely to be unable to replicate the large-scale**  
 039 **human actions. In this case, action constraints are essential to ensure the imitator can safely perform**  
 040 **tasks within its own capabilities while still learning from the expert’s behavior.** While there has been  
 041 substantial research on action-constrained reinforcement learning (ACRL) (Kasaura et al., 2023; Lin  
 042 et al., 2021; Brahmane et al., 2023; Chen et al., 2024), surprisingly, little attention has been given  
 043 to action-constrained imitation learning (ACIL).

044 To ensure that the actions generated by the policy adhere to specific constraints during both training  
 045 and evaluation, most existing ACRL methods incorporate a projection layer on top of the policy  
 046 network (Chow et al., 2018; Liu et al., 2020; Gu et al., 2017). However, such an approach can  
 047 cause issues in IL. Most IL approaches aim to minimize the discrepancy between the occupancy  
 048 measure of the expert demonstrations and that of the imitator (Pomerleau & A, 1991; Ho & Ermon,  
 049 2016). When expert actions lie outside the feasible action set, the projection layer can prevent the  
 050 imitator from accurately matching the occupancy measure of the expert, especially in cases with  
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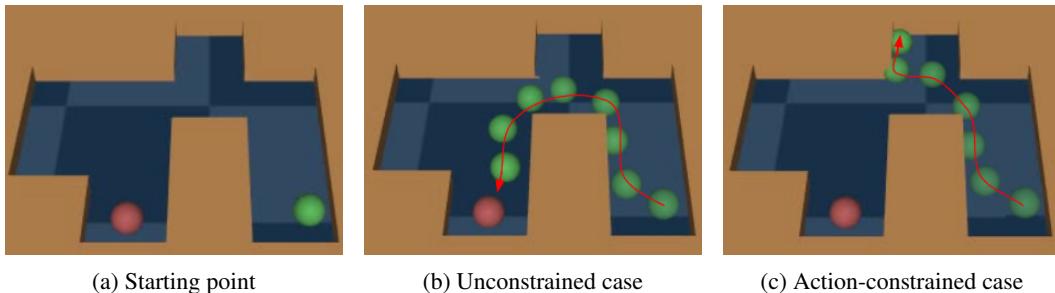


Figure 1: (a) The green sphere starts in the bottom-right corner and navigates toward the red sphere (goal). (b) A policy trained via BC successfully executes a U-turn to reach the target. (c) However, when the box constraint is applied by projection, the sphere struggles to make the sharp U-turn and ends up colliding with the wall.

more restrictive action sets. This issue leads to ambiguity in distribution matching for IL methods under action constraints, a problem we term “occupancy measure distortion.”

To better illustrate the issue of occupancy measure distortion, let's consider a simple example of a Maze2d goal-reaching task, as shown in Fig 1. (a). In this task, the green sphere (agent) needs to navigate towards the red sphere (goal), using a two-dimensional action space that controls the force applied along the x- and y-axes. An unconstrained policy trained by behavior cloning (BC)(Pomerleau & A, 1991), based on five expert trajectories, can successfully turn left, avoid colliding with the walls, and reach the goal (Fig 1. (b)). Now, consider a weaker agent with a smaller feasible action set, where a projection layer is applied to its policy network. This weaker agent lacks the force to turn as quickly as the unconstrained agent, resulting in a collision with the wall of the space we carved out (Fig 1. (c)) and getting stuck. This example demonstrates how occupancy measure distortion prevents the agent from accurately replicating the expert's trajectory. Without following the expert's path, the action-constrained agent suffers from the distribution shift, and even encounters unexpected dangers in the environment.

Another approach to preventing learning infeasible actions is to focus on matching the state distribution rather than the state-action distribution of expert demonstrations, a scenario known as Learning from observation (LfO). However, they cannot fully avoid issues related to mismatched state distributions, especially with constrained actions, and they typically require a substantial amount of interaction data with the environment.

The most effective way to eliminate occupancy measure distortion is to ensure that both the expert demonstrations and the learner share the same feasible action set, as this would prevent any distortion from occurring. To accomplish this, we recast trajectory alignment as a planning problem, aiming to generate trajectories that closely resemble the original expert trajectories but consist of constrained actions as surrogate expert demonstrations. We leverage Model Predictive Control (MPC) (Richalet et al., 1978) due to its flexibility in defining objective functions and its compatibility with various constraints. Unlike existing MPC approaches, which primarily focus on optimizing short-horizon returns during planning, we optimize for the similarity between the rollout trajectories and the expert trajectories. To quantify this similarity, we employ Dynamic Time Warping (DTW) (Hiroaki & Chiba, 1978), which allows us to compare trajectories that have different pacing of behaviors. In this paper, we introduce Dynamic Time Warping Imitation Learning (DTWIL), an algorithm designed to generate surrogate action-constrained demonstrations and learn the corresponding policy. Our experiments demonstrate that DTWIL outperforms a range of benchmark IL algorithms in navigation and locomotion tasks, particularly in terms of sample efficiency, while being less susceptible to the challenges posed by occupancy measure distortion.

## 2 RELATED WORK

**Action constrained Reinforcement Learning** To the best of our knowledge, no prior work has specifically addressed the problem of [ACIL](#), which tackles the capability gap between the expert and the learner agent. Therefore, we refer to [ACRL](#) methods to define the problem setting in this paper.

108 Kasaura et al. (2023) provides a benchmark for evaluating existing ACRL approaches. Some works,  
 109 such as Pham et al. (2018a); Bhatia et al. (2019); Dalal et al. (2018), ensure safe and compliant  
 110 behavior by incorporating a differentiable projection layer at the end of the policy network to meet  
 111 action constraints. However, Lin et al. (2021); Brahmanage et al. (2023) highlight issues with this  
 112 approach, particularly the zero gradient and longer training times, and propose alternative methods.  
 113 Notably, Brahmanage et al. (2023); Chen et al. (2024) employ normalizing flows to directly generate  
 114 actions that comply with the constraints, thereby circumventing the drawbacks associated with  
 115 projection layers.

116 **Learning from Demonstration** IL focuses on deriving a policy using only the information from  
 117 expert demonstrations, which also termed Learning from Demonstration (LfD). BC (Pomerleau &  
 118 A, 1991) approaches this by treating policy as a state-action mapping, learning it in a supervised  
 119 manner. Adversarial Imitation Learning (AIL), on the other hand, focuses on matching the state-  
 120 action distribution between expert and learner through adversarial training. GAIL (Ho & Ermon,  
 121 2016) is a foundational method in this domain, using a discriminator to distinguish between expert  
 122 and learner transitions, and providing rewards based on this discrimination. Various AIL extensions  
 123 (Kostrikov et al., 2019a;b) improve on GAIL, tailoring the method to different environments and  
 124 goals. A comprehensive review of IL techniques can be found in Zare et al. (2024), but ACIL  
 125 remains unexplored in these surveys.

126 **Learning from Observation** An alternative approach to avoid the undesirable effects of projected  
 127 policy outputs after imitating expert actions is to learn from expert observation data only, which falls  
 128 under the scenario of Learning from Observation (LfO). Methods like GAIfO and IDDM (Torabi  
 129 et al., 2018b; Yang et al., 2019) follow the principles of GAIL by training a state-only discriminator.  
 130 OPOLO (Zhu et al., 2020) further improves on this by relaxing the on-policy requirement, speeding  
 131 up the learning process. BCO (Torabi et al., 2018a) takes a different approach by learning an inverse  
 132 dynamics model to infer the expert’s missing actions from observations, and then applying BC to  
 133 train the policy. CFIL (Freund et al., 2023), using a flow-based model to capture state or state-action  
 134 distributions, sets a new benchmark for LfO scenario. However, despite relying solely on expert  
 135 state information, these methods still overlook the capability gap between the expert and the learner  
 136 agent, and many of them depend on a large amount of environment interaction data.

137 **Cross-Embodiment Imitation Learning** Cross-Embodiment Imitation Learning focuses on  
 138 transferring knowledge or skills between agents with different physical structures, such as robots  
 139 with varying morphologies or dynamics. This field addresses the challenges of aligning state and  
 140 action spaces across embodiments to enable effective knowledge transfer. Approaches in this do-  
 141 main often leverage shared latent spaces, domain adaptation techniques, or hierarchical reinforce-  
 142 ment learning to bridge embodiment-specific differences. For example, modular policy frameworks  
 143 (Huang et al., 2020) and domain randomization strategies (Tobin et al., 2017) have been employed  
 144 to achieve generalization across multiple embodiments. While ACIL also seeks to address the chal-  
 145 lenge of transferring knowledge across different agents, it does not consider differences in physical  
 146 structures. Instead, ACIL focuses on a unique problem setting where agents share action spaces of  
 147 the same dimension but differ in the scale or magnitude of their actions.

### 149 3 PRELIMINARIES

151 **Problem Formulation** We consider a Markov decision process (MDP) defined as a tuple  $\mathcal{M} =$   
 152  $\langle \mathcal{S}, \mathcal{A}, T, r, p_0, \gamma \rangle$ , where  $\mathcal{S}$  and  $\mathcal{A}$  are the sets of feasible state and action respectively;  $T$  describes  
 153 the dynamics of the environments, with  $T(s_{t+1}|s_t, a_t)$  indicating the transition probability to next  
 154 state  $s_{t+1}$  from the current state  $s_t$  if the agent takes action  $a_t$ ;  $p_0$  is the initial state distribution;  
 155  $R : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$  is the reward function; and  $\gamma \in [0, 1]$  is the discount factor. An agent follows  
 156 its policy  $\pi : \mathcal{S} \rightarrow \mathcal{A}$  to interact with the environment of MDP with an objective of maximizing  
 157 long-term expected cumulative reward. In this paper, we consider action-constrained MDPs where  
 158 for each state  $s \in \mathcal{S}$  there is a feasible action set  $\mathcal{C}(s) \subseteq \mathcal{A}$  determined by explicit action constraints  
 159 incorporated. That is, the agent can only take actions from  $\mathcal{C}(s)$  at each time step.

160 **Model Predictive Control** In actor-critic RL, solving an MDP is to find the optimal policy  $\pi^*$   
 161 maximizing cumulative reward. In control, the optimal policy is formulated by maximizing a spe-

162 specific performance measure. MPC achieves this by utilizing a forward dynamics model  $f(s_t, a_t)$  of  
 163 the environment to explore various action sequences. This allows MPC to evaluate potential future  
 164 trajectories and select the one that best meets the defined objective  $J$ . A local solution to the trajec-  
 165 tory optimization at each step  $t$  can be acquired by estimating the optimal action sequence  $a_{t:t+H}$   
 166 over a finite horizon  $H$ :

$$\pi_{\text{MPC}}(s_t) = \arg \min_{a_{t:t+H}} \mathbb{E} \left[ \sum_{i=t}^H J(s_i, a_i) \right], \quad (1)$$

170 The agent will execute the first action of the resulting action sequence, and repeat the procedure  
 171 again at the next time step. To improve action sampling, we can utilize the Cross-Entropy Method  
 172 (CEM) optimizer, which iteratively refines the mean ( $\mu$ ) and standard deviation ( $\sigma$ ) of a multivariate  
 173 Gaussian distribution by sampling actions, evaluating them, and updating the distribution based on  
 174 the best samples over a finite horizon. In this work, we employ an MPC implementation based on  
 175 Probabilistic Ensembles with Trajectory Sampling (PETS) as proposed by Chua et al. (2018). PETS  
 176 integrates probabilistic neural networks to model the dynamics of the environment, utilizing an en-  
 177 semble of learned models to estimate uncertainty in predictions. This ensemble approach allows for  
 178 more robust decision-making by accounting for variability in the system. In practice, PETS inter-  
 179 acts with the environment by iteratively predicting future states based on the current state, choosing  
 180 actions that maximize a given reward function while considering uncertainty, and then updating its  
 181 models as new data is collected. This method significantly reduces the sample complexity, allowing  
 182 the agent to perform well after a limited number of interactions with the environment.

183 **Dynamic Time Warping** DTW (Hiroaki & Chiba, 1978) is an algorithm designed to measure the  
 184 similarity between two temporal series data that may not align perfectly in time. It is particularly  
 185 useful in scenarios where trajectories, such as those generated by agents with different action con-  
 186 straints, differ in speed or timing but represent the same underlying behavior. The core of DTW lies  
 187 in the calculation of the optimal warping path  $\rho^*$  and the resulting DTW distance, which quantifies  
 188 the alignment cost. Specifically, let  $\mathbf{x} = \{x_1, x_2, \dots, x_n\}$  and  $\mathbf{y} = \{y_1, y_2, \dots, y_m\}$  denote two  
 189 sequences of length  $n$  and  $m$ , respectively, then the DTW distance between  $\mathbf{x}$  and  $\mathbf{y}$  is given by

$$\text{DTW Distance}(\mathbf{x}, \mathbf{y}) = \sum_{(i,j) \in \rho^*} \|x_i - y_j\|^2 = \min_{\rho} \sum_{(i,j) \in \rho} \|x_i - y_j\|^2,$$

190 where  $\rho = \{(i_k, j_k)\}_{k=1}^K$  is a warping path such that:

1.  $i_1 = 1$  and  $j_1 = 1$ ,
2.  $i_K = n$  and  $j_K = m$ ,
3.  $i_k \leq i_{k+1}$  and  $j_k \leq j_{k+1}$  for all  $k$ ,
4.  $|i_{k+1} - i_k| \leq 1$  and  $|j_{k+1} - j_k| \leq 1$  for all  $k$ .

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## Algorithm 1 Dynamic Time Warping Imitation Learning (DTWIL)

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203 1: **Input:** Expert demos  $\tau = \{\tau^i\}_{i=1}^N$ , planning horizon  $H$ , ERC horizon  $h_{\text{erc}}$ , number of particles  
 204  $P$ , dynamics model ensembles  $f$ , training dataset  $\mathcal{D} = \{\tau^i\}_{i=1}^N$ , the number of episodes to run  
 205  $K$   
 206 2: BC dataset  $\mathcal{D}_{\text{BC}} \leftarrow \{\}$   
 207 3: **for** Iteration  $k = 1$  to  $K$  **do**  
 208 4:     Select an expert trajectory  $\tau^i$   
 209 5:     Train  $f$  with  $\mathcal{D}$   
 210 6:      $\tau^{c_i} \leftarrow \text{Trajectory Alignment}(\tau^i)$   
 211 7:      $\mathcal{D} \leftarrow \mathcal{D} \cup \tau^{c_i}$   
 212 8:     **if** no alignment of  $\tau^i$  in  $\mathcal{D}_{\text{BC}}$  **or**  $\text{DTWDistance}(\tau^{c_i}, \tau^i) < \text{DTWDistance}(\mathcal{D}_{\text{BC}}[i], \tau^i)$  **then**  
 213 9:          $\mathcal{D}_{\text{BC}}[i] \leftarrow \tau^{c_i}$   
 214 10:      **end if**  
 215 11: **end for**  
 12: Train a BC policy with  $\mathcal{D}_{\text{BC}}$

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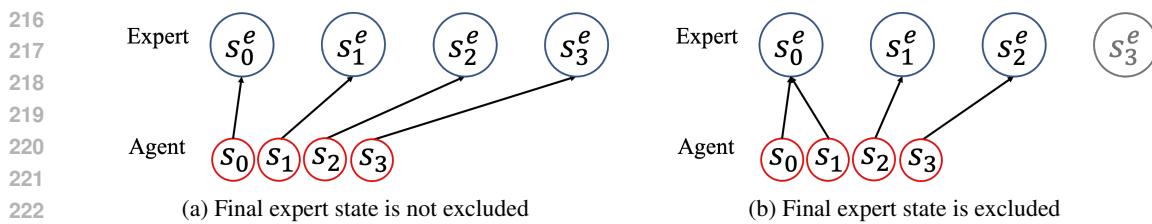


Figure 2: Effect of excluding the final expert state on the DTW warping path. Including the final expert state Figure 2a leads to a 1-to-1 alignment since both trajectories have the same number of states. Excluding it Figure 2b prevents state from advancing, yielding a more desirable matching. The total arrow length represents the DTW distance.

#### 4 METHODOLOGY

Our motivation is to generate a surrogate demonstration dataset that aligns with expert trajectories while operating within constrained action spaces , and later utilize this surrogate data set to train a BC policy for generalization. To this end, we recast the alignment issue as a trajectory planning task, where a trajectory of the agent is designed to follow the expert demonstration. As mentioned in Section 3, we leverage the PETS framework (Chua et al., 2018) to optimize the expected outcomes of sampled actions. In this process, we replace the environment reward with DTW (Hiroaki & Chiba, 1978) distance as our key criterion for selecting actions, ensuring better alignment with the expert trajectory. Additionally, to handle the complexities of environments requiring precise movements, we introduce Expert Regularized Control (ERC), inspired by Actor Regularized Control (ARC) (Sikchi et al., 2021), into the trajectory sampling process, improving the alignment’s effectiveness.

In the following sections, we detail our implementation of DTW distance as the action selection criterion in Section 4.1, highlighting its role in aligning the agent’s trajectory with that of the expert. Section 4.2 introduces ERC and its integration into the trajectory sampling process. The comprehensive pseudo code for DTWIL can be found in Algorithm 1, and the pseudo code for trajectory alignment is presented in Algorithm 2, and

#### 4.1 TRAJECTORY ALIGNMENT

Due to the asynchronous nature of the rollout pacing between the expert demonstration and the constrained agent, step-by-step alignment is not feasible. To address this, we incorporate DTW to evaluate the alignment and select the most appropriate planning trajectory that corresponds to the expert demonstration. In the following sections, we explain how DTW distance is utilized as a criterion for the MPC controller in PETS framework in Section 4.1.1 and how we determine the expert demonstration segment to be aligned at each step in Section 4.1.2.

### 4.1.1 DTW CRITERIA

To utilize DTW as a reference, we first introduce a progression parameter,  $t_{\text{pg}}$ , which indicates the timestep of the expert state with which the constrained agent is currently aligned. For instance, if the current progress is at  $t_{\text{pg}}$ , and the planning horizon is set to  $H$ , the targeted segment of the expert trajectory for alignment would be  $s_{t_{\text{pg}}:(t_{\text{pg}}+H)}^e$ , where  $s_t^e$  denotes the  $t$ -th expert state.

Let the current timestep be  $t$ , the current progress be  $t_{\text{pg}}$ , and the  $H$ -step planning trajectory rolled out by the action sequence  $A$  and a dynamics model  $f_\theta$  be  $s_{t:(t+H)}$ . The optimal planning action sequence  $A^*$  is then defined as:

$$A^* = \arg \min_A \mathbb{E} \left[ \text{DTWDistance}(s_{t_{\text{pg}}:(t_{\text{pg}}+H)}^{\text{e}}, s_{t:(t+H)}) \right]. \quad (2)$$

We approximate the solution to the optimization problem by employing a CEM optimizer, which samples 500 candidate action sequences and selects the one with the smallest DTW distance to the expert trajectory. To address variations in scale across different dimensions, we normalize both

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270   **Algorithm 2** Trajectory Alignment

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271   1: **Input:** Planning horizon  $H$ , ERC horizon  $h_{\text{erc}}$ , number of particles  $P$ , dynamics model ensembles  $f$ ,  $i$ -th expert trajectory  $\tau^i = \{(s^{e_i}, a^{e_i})\}_{t=0}^l$ , constrained action space  $\mathcal{C}(s)$ .

272   2: **Output:**  $\tau^{c_i}$

273   3: Agent's initial state  $s_0 \leftarrow s_0^{e_i}$ , progression  $t_{\text{pg}} \leftarrow 0$ , time step  $t \leftarrow 0$ , alignment  $\tau^{c_i} \leftarrow \{\}$

274   4: Action projection function  $\text{Proj}()$

275   5: **while**  $t < \text{max\_episode\_steps}$  **and**  $t_{\text{pg}} < l$  **do**

276   6:   **if**  $t_{\text{pg}} + H > l$  **then**

277   7:     Pad the target expert segment to length=  $H$  with  $s_l^{e_i}$ .

278   8:   **end if**

279   9:   **for** Particle  $p = 1$  to  $P$  **do**

280   10:   **for** Action sampled  $a_{t+h}^p$  from CEM,  $h = 0$  to  $H$  **do**

281   11:     **if**  $h \leq h_{\text{erc}}$  **then**

282   12:        $a_{t+h}^p \leftarrow \beta \text{Proj}(a_{\min(t_{\text{pg}}+h, l)}^{e_i} | \mathcal{C}(s_{\min(t+h, l)}^p)) + (1 - \beta) a_{t+h}^p$

283   13:     **end if**

284   14:      $s_{t+h+1}^p = f(s_{t+h}^p | a_{t+h}^p)$

285   15:   **end for**

286   16:      $\|p\|_{\text{DTW}} \leftarrow \text{DTWDistance}(s_{t:t+H}^p, s_{(t_{\text{pg}}):(t_{\text{pg}}+H)}^{e_i})$

287   17:   **end for**

288   18:      $p^* \leftarrow \arg \min_p \|p\|_{\text{DTW}}$

289   19:     Update CEM distribution

290   20:     Execute  $a_t^{p^*}$  and get  $s_{t+1}$

291   21:      $\tau^{c_i} \leftarrow \tau^{c_i} \cup (s_t, a_t^{p^*})$

292   22:     **if** Progression has advanced in the warping path **then**

293   23:        $t_{\text{pg}} \leftarrow t_{\text{pg}} + 1$

294   24:     **end if**

295   25: **end while**

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296

297

298   the planned trajectory and the corresponding expert trajectory segment prior to computing the DTW  
 299   distance. Specifically, each dimension is linearly scaled such that the minimum and maximum values  
 300   of the expert trajectories are mapped to 0 and 1, respectively. To ensure compatibility with the action-  
 301   constrained setting, we adapt the CEM optimizer through rejection sampling, strictly enforcing that  
 302   all sampled actions satisfy the imposed constraints. Subsequently, the MPC controller executes the  
 303   first action of  $A^*$ .

#### 304   4.1.2 PROGRESSION MANAGEMENT

305   The progression parameter,  $t_{\text{pg}}$ , is initialized to 0 at the start of every trajectory alignment. After  
 306   each action, we update  $t_{\text{pg}}$  by analyzing the warping map to determine how many expert states the  
 307   agent's action has advanced. Notably, when constructing the warping path, the final expert state in  
 308   the segment is excluded from the matching calculation to prevent unintended progression when the  
 309   agent exhibits minimal movement across consecutive actions. Specifically, when two trajectories  
 310   have an equal number of states, DTW often tends to align states in a strictly 1-to-1 manner, which  
 311   can mislead progression. By excluding the final expert state, the DTW algorithm is encouraged  
 312   to create a 2-to-1 alignment during the matching process. Given the constrained actions, which  
 313   naturally take smaller steps than expert actions, this 2-to-1 alignment often occurs in the initial few  
 314   states. Consequently, if the agent's first planning state,  $s_1$ , is not sufficiently close to the next expert  
 315   state,  $s_1^e$ , it is more likely to be matched with the current expert state,  $s_0^e$ . This concept is illustrated  
 316   in Figure 2.

317   Figure 3 shows how this advancement value is determined. The advancement value is then added to  
 318    $t_{\text{pg}}$  after every MPC step.

#### 321   4.2 EXPERT REGULARIZED CONTROL

322   In environments that demand precise movements, even small errors can lead to significant disruptions.  
 323   To mitigate this, we incorporate expert actions into the sampled actions as guidance , termed

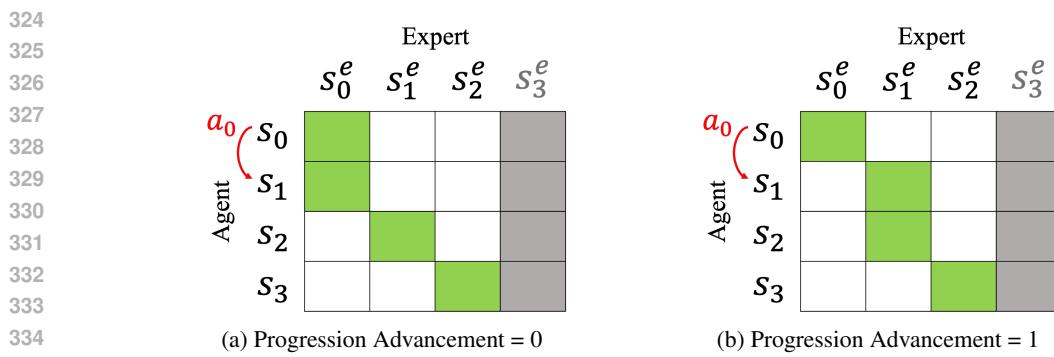


Figure 3: Since the MPC controller executes only the first planning step per iteration, we focus on the number of expert states the agent advances after the initial action  $a_0$ . The figure shows two DTW warping path cases (green patches). In Figure 3a, the agent transitions from  $s_0$  to  $s_1$  while staying aligned with  $s_0^e$  causing no progression ( $t_{pg}$  unchanged). In Figure 3b, the agent advances to the next expert state, updating  $t_{pg}$  to  $t_{pg} + 1$ .

ERC. Specifically, the actions used to rollout the planning trajectories in the MPC controller become the weighted average of the sampled actions and a corresponding segment of the expert demonstration. To implement this, we first extract a specific segment  $a_{t_{pg},(t_{pg}+h_{erc})}^e$ , from the expert actions  $a^e$ , where  $h_{erc}$  is the horizon over which expert actions are blended. Then, given the dynamics model ensembles  $f(s, a)$ , a specific weight  $\beta \in [0, 1]$ , and the projection function  $\text{Proj}(a | \mathcal{C}(s))$ , which projects an action  $a$  onto a specific constrained action space  $\mathcal{C}(s)$ , ERC guide the trajectory generation with the following functions:

For  $h = 0, 1, \dots, H$  :

$$a_h = \begin{cases} \beta \text{Proj}(a_{t_{pg},(t_{pg}+h_{erc})}^e | s_h) + (1 - \beta) a_h^{\text{sampled}}, & \text{if } h \leq h_{erc}, \\ a_h^{\text{sampled}}, & \text{if } h > h_{erc}, \end{cases} \quad (3)$$

$$s_{h+1} = f(s_h, a_h),$$

where  $a_h$  is the  $h^{\text{th}}$  action step in an  $H$ -step planning trajectory,  $a_h^{\text{sampled}}$  is the  $h^{\text{th}}$  action directly sampled from a CEM optimizer, and  $s_h$  is the  $h^{\text{th}}$  state of the planning trajectory.

The performance of our algorithm in environments where agents are highly susceptible to deviations—such as Hopper, where falling results in early termination—is significantly enhanced by incorporating ERC. A detailed analysis of this improvement is presented in Section 5.6.

## 5 EXPERIMENTS

In this chapter, we assess DTWIL across a range of randomly initialized continuous control tasks in navigation and locomotion environments, each subject to different constraints. We compare our results against both offline baselines and online baselines. For a fair comparison, we allocate the same number of environment steps to the online baselines as we do to DTWIL.

Two types of constraints are applied: box constraints and state-dependent constraints. A box constraint, denoted as  $\text{Box}(c_{\text{box}})$ , restricts each action dimension to the range  $[-c_{\text{box}}, c_{\text{box}}]$ , where  $c_{\text{box}}$  is a positive constant. In contrast, a state-dependent constraint varies based on the agent's current state. To ensure that these baseline methods adhere to the constrained action domains, we project their generated actions onto the nearest feasible actions based on the  $L_2$  norm.

### 5.1 CONSTRAINED ENVIRONMENTS

**Maze2d (Fu et al., 2020)** To evaluate our method on a navigation task, we selected the Maze2d-Medium-v1 environment. This task involves a point-mass agent navigating a 2D maze from a randomly chosen start location to a goal. The original action set is a 2-dimensional vector  $(v_1, v_2)$  with

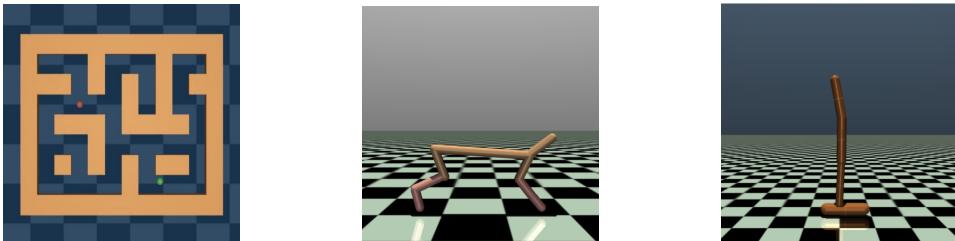


Figure 4: We evaluate the impact of action constraints on DTWIL and baseline methods across three environments : Maze2d-Medium-v1, HalfCheetah-v3, and Hopper-v2.

each element in the range  $[-1.0, 1.0]$ . We impose an  $\text{Box}(0.1)$  constraint and a state-dependent constraint **M+O** defined as  $\sum_{i=1}^2 |v_i w_i| \leq 0.5$  on agent actions, where  $(w_1, w_2)$  represent the velocities in the x and y directions, respectively. For this task, we collected 100 demonstrations, resulting in a total of 18,525 state-action pairs for training.

**HalfCheetah (Brockman et al., 2016)** The task involves controlling a bipedal cheetah agent to run forward by applying torque to its joints. The action space consists of a 6-dimensional vector  $(v_1, v_2, \dots, v_6)$ , where each component is bounded by  $[-1, 1]$ . We introduce a  $\text{Box}(0.5)$  constraint and a state-dependent constraint **HC+O** defined as  $\sum_{i=1}^6 |v_i w_i| \leq 10$ , where  $w_i$  denotes the angular velocity of the  $i$ -th joint, a component of the agent’s state. We rely on five 1000-step expert demonstrations for training.

**Hopper (Brockman et al., 2016)** The task requires controlling a robot to hop forward by applying torques to its hinges. The action is represented by a 3-dimensional vector  $(v_1, v_2, v_3)$ , with each value constrained between  $[-1.0, 1.0]$ . We also impose two separate constraints on this task. The first one is a  $\text{Box}(0.9)$  constraint, while the second introduces a state-dependent constraint **H+M**:  $\sum_{i=1}^3 |v_i w_i| \leq 10$ , where  $w_i$  denotes the angular velocity of the  $i$ -th joint, which is part of the robot’s state. For training, we use five expert demonstrations, each consisting of 1000 state-action pairs.

## 5.2 BASELINES

To ensure that the action outputs of various baseline methods meet specific constraints, we incorporate a projection layer into each method’s policy, allowing the action outputs to remain within the feasible set. We append “+P” to the names of each baseline method to denote the versions of the algorithms that include a projection layer.

- **BC+P (Pomerleau & A, 1991):** BC formulates policy learning as a supervised problem, treating the policy as a mapping between states and actions.
- **BCO+P (Torabi et al., 2018a):** BCO is a LfO method, learning an inverse dynamics model to infer action from state-only data and applying BC to learn a policy.
- **GAIL+P (Ho & Ermon, 2016):** GAIL is an online LfD method that utilize a generative adversarial network (GAN) to infer the underlying reward function.
- **GAIfO+P (Torabi et al., 2018b):** Similar to GAIL but only learning from observations, GAIfO is an AIL-based online LfO algorithm.
- **OPOLO+P (Zhu et al., 2020):** OPOLO is an online LfO method. Leveraging off-policy learning, OPOLO ranks among the most effective LfO techniques.
- **CFIL-s+P/ CFIL-sa+P (Freund et al., 2023):** CFIL utilize a flow-based model to capture state or state-action distributions, sets a new benchmark for LfO scenario. The LfD version of CFIL is denoted as CFIL-sa, and LfO version of CFIL is denoted as CFIL-s.

432    **5.3 PERFORMANCE COMPARISON**  
 433

434    In all tasks, DTWIL only interacts with the environment using MPC for no more than 50K steps.  
 435    To ensure a fair comparison, we limit the interaction for all online IL methods to 50K environment  
 436    steps during training. **All results are evaluated with randomly initialized starting states.**

437    Following this, the best-performing model from each algorithm during these interactions was se-  
 438    lected for final evaluation. This ensures that the results reflect the effectiveness of each method  
 439    within a limited sample regime, providing a fair comparison across environments while emphasiz-  
 440    ing sample efficiency.

441

Task	Maze2d box	Maze2d M+O	HalfCheetah Box	HalfCheetah HC+O	Hopper Box	Hopper H+M
BC+P	$0.61 \pm 0.05$	$0.81 \pm 0.05$	$1815.51 \pm 303.89$	<b><math>2753.86 \pm 27.34</math></b>	$2204.83 \pm 753.32$	$1233.96 \pm 211.87$
GAIL+P	$0.22 \pm 0.0$	$0.14 \pm 0.05$	$-163.63 \pm 47.47$	$-185.53 \pm 66.11$	$360.97 \pm 59.19$	$261.83 \pm 81.41$
BCO+P	$0.14 \pm 0.05$	<b><math>0.88 \pm 0.06</math></b>	$-4.05 \pm 4.07$	$6.23 \pm 31.85$	$219.46 \pm 20.33$	$224.25 \pm 32.81$
GAfO+P	$0.07 \pm 0.02$	$0.19 \pm 0.08$	$-74.77 \pm 32.98$	$-163.84 \pm 33.79$	$197.36 \pm 30.12$	$206.37 \pm 19.19$
OPOLO+P	$0.2 \pm 0.06$	$0.64 \pm 0.13$	$-605.84 \pm 390.21$	$-9.12 \pm 80.47$	$1068.3 \pm 952.96$	$228.28 \pm 33.10$
CFIL-sa+P	$0.23 \pm 0.21$	$0.47 \pm 0.10$	$-95.67 \pm 515.43$	$1674.75 \pm 1316.81$	$1485.74 \pm 677.37$	$1553.86 \pm 1096.28$
CFIL-s+P	$0.23 \pm 0.06$	$0.45 \pm 0.12$	$-172.56 \pm 738.44$	$1422.98 \pm 1830.51$	$866.27 \pm 249.20$	$1443.06 \pm 547.59$
<b>DTWIL</b>	<b><math>0.77 \pm 0.04</math></b>	$0.87 \pm 0.04$	<b><math>2669.41 \pm 4.56</math></b>	$2637.34 \pm 26.82$	<b><math>2844.68 \pm 57.77</math></b>	<b><math>2873.88 \pm 240.46</math></b>

450    Table 1: Evaluation performance of the proposed method and baseline algorithms across various  
 451    tasks, with results expressed as the mean and standard deviation calculated from three seeds.

452

453    Based on the experimental results, the BC+P algorithm maintains basic functionality across all tasks  
 454    but is still affected by action constraints, which hinders its ability to replicate expert-level perfor-  
 455    mance. This limitation is particularly noticeable in the Hopper environment, where a single fall  
 456    results in the episode ending prematurely, further hindering its performance. The rigid constraints  
 457    imposed on the actions make it challenging for BC+P to generalize well in tasks requiring smooth  
 458    and dynamic control.

459

460    Moreover, the other online algorithms such as GAIL+P and OPOLO+P face dual challenges. Not  
 461    only are they affected by the same action constraints, but they also suffer from poor sample ef-  
 462    ficiency, which leads to subpar performance across all tasks. These methods, despite interacting  
 463    with the environment, cannot recover expert-like behavior within the limited number of interaction  
 464    steps, contributing to their consistently low scores. **While BCO+P show competitive performance in**  
**simpler tasks like Maze2d M+O, they fall short in more complex environments.**

465

466    In contrast, DTWIL, which learns from surrogate expert data and adopts a **BC** approach to learn  
 467    the policy, perform well across all tasks. By learning from the surrogate data to match the expert  
 468    trajectories and using **BC** for policy learning, DTWIL manages to replicate expert performance  
 469    while maintaining sample efficiency. As a result, it successfully reproduces expert-like trajectories  
 470    across tasks, without being adversely affected by the constraints that cripple other methods. **The**  
**results of training the various baseline methods for sufficient steps are included in Appendix A.3.**

471

472    **5.4 PREVENTION FROM UNINTENDED PROGRESSION**  
 473

474

475    To mitigate unintended progression of the parameter  $t_{pg}$ , as detailed in 4.1.2, we exclude the termi-  
 476    nal state of the alignment target during com-  
 477    putation. As demonstrated in Table 2, this ad-  
 478    justment significantly enhances performance in  
 479    the Maze2d-Medium environment under box con-  
 480    straints. Specifically, excluding the final expert  
 481    state when determining the DTW warping path im-  
 482    proves the returns obtained during both the trajec-  
 483    tory alignment phase and the subsequent behavioral  
 484    cloning (BC) phase. These results validate the ef-  
 485    fectiveness of the proposed modification in stabiliz-  
 ing and optimizing the alignment process.

	Excluded	Not Excluded
DTW-S	$2.99 \pm 0.75$	$2.99 \pm 0.82$
Return-S	<b><math>0.76 \pm 0.0</math></b>	$0.69 \pm 0.0$
Return-BC	<b><math>0.77 \pm 0.04</math></b>	$0.72 \pm 0.03$

476    Table 2: Results comparison of whether the  
 477    final expert state is excluded when calculat-  
 478    ing the warping path in Maze2d-Medium un-  
 479    der the box constraint.

Task	HalfCheetah Box	HalfCheetah Box-Sync	Hopper Box	Hopper Box-Sync
DTW-S	$15.17 \pm 0.24$	<b><math>15.06 \pm 0.12</math></b>	<b><math>11.70 \pm 6.02</math></b>	$27.68 \pm 0.26$
Return-S	$2576.20 \pm 61.62$	<b><math>2590.31 \pm 24.07</math></b>	<b><math>2527.63 \pm 572.53</math></b>	$418.73 \pm 89.35$
Return-BC	<b><math>2669.41 \pm 4.56</math></b>	$2594.28 \pm 29.80$	<b><math>2844.68 \pm 57.77</math></b>	$153.52 \pm 1.20$

Table 3: Comparison of results between asynchronous and synchronous progression methods. DTW-S denotes the DTW distance between the generated surrogate trajectories and the expert trajectories, Return-S indicates the average return of the surrogate expert data, and Return-BC represents the average return of BC policy trained on this surrogate expert data.

### 5.5 ASYNCHRONOUS PROGRESSION UPDATE

In this section, we compare two approaches to progression management. The first is asynchronous progression, where the parameter  $t_{pg}$  is updated in tandem with the warping path. This method is primarily used in our algorithm. The second is synchronous progression, where  $t_{pg}$  increases by 1 with each step, matching the expert’s pace. Given that agents with constrained actions typically take longer to replicate expert behavior, asynchronous progression is more sensible. Table 3 presents the full experimental results for both methods. While the differences on HalfCheetah are minimal, asynchronous progression significantly outperforms on Hopper.

### 5.6 EXPERT REGULARIZED CONTROL

We evaluate the effectiveness of our ERC design in the Hopper environment. Table 4 demonstrate a clear performance difference: without ERC, the agent frequently falls, leading to significantly lower rewards and shorter trajectories. In contrast, incorporating ERC stabilizes the agent’s behavior, allowing it to generate surrogate trajectories of appropriate length and maintain consistent performance throughout the task. This highlights the importance of ERC in enabling robust and reliable imitation under action-constrained settings. Refer to Appendix A.5 for detailed hyperparameter tuning.

	Without ERC	With ERC
Return-S	$820.7 \pm 84.8$	<b><math>2527.6 \pm 572.5</math></b>
Return-BC	$889.7 \pm 5.4$	<b><math>2844.7 \pm 57.8</math></b>

Table 4: Comparison of results with and without ERC applied during action sampling in Hopper.

## 6 CONCLUSION

ACIL has the potential to greatly influence real-world robot training, as real robots often operate under constrained action spaces due to limited power, mechanical imperfections, or restricted capabilities resulting from wear and tear. These limitations present challenges that previous methods have not effectively addressed. In this paper, we highlight that directly learning from expert demonstrations using agents with constrained action spaces introduces several issues, including occupancy measure distortion and asynchronous progression. These challenges cannot be resolved by traditional RL and IL methods because of the inevitable progression gap between expert and agent trajectories. To address this, we propose the first-ever ACIL method, DTWIL, which effectively bridges the gap caused by asynchronous time series alignment. DTWIL leverages DTW distance as a reference to select optimal actions in a MPC framework, and incorporates Actor Regularized Critic (ARC) to stabilize the sampled actions. As a result, our approach outperforms methods heavily reliant on projection in multiple environments, demonstrating that a dedicated algorithm for the ACIL problem is both effective and necessary. Our results indicate that as long as the computational cost of DTW is manageable, DTWIL achieves exceptional performance on ACIL tasks. As the first contribution to the ACIL research field, we hope our work inspires further research. Future efforts could focus on developing ACIL algorithms that handle more complex environments with greater efficiency.

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648    **A APPENDIX**

649

650    **A.1 CEM OPTIMIZER**

651

652    Our implementation of the CEM optimizer closely follows the approach used in PETS (Chua et al.,  
 653    2018), where a momentum term is added into the update calculations, and bounds are imposed on  
 654    the standard deviations in addition to the standard CEM optimization.

655    Specifically, if a distribution at CEM iteration  $i$ ,  $\mathcal{N}(\mu_i, \sigma_i^2)$ , is updated toward a target distribution  
 656     $\mathcal{N}(\mu_{\text{target}}, \sigma_{\text{target}}^2)$ , the resulting updated distribution at iteration  $i + 1$ ,  $\mathcal{N}(\mu_{i+1}, \sigma_{i+1}^2)$ , will be given  
 657    by:

658

659

$$660 \quad \mathcal{N}(\mu_{i+1}, \sigma_{i+1}^2) = \mathcal{N}(\alpha\mu_i + (1 - \alpha)\mu_{\text{target}}, \alpha\sigma_i^2 + (1 - \alpha)\sigma_{\text{target}}^2), \alpha \in [0, 1], \quad (4)$$

661

662    and the value of  $\sigma_i^2$  is further constrained by  $\frac{1}{2}w$ , where  $w$  represents the minimum distance from  $\mu_i$   
 663    to the bounds of the feasible action space.

664    Moreover, to adapt the CEM optimizer for our action-constrained setting, we employ rejection sam-  
 665    pling to ensure that all sampled actions strictly adhere to the predefined constraints.

666

667    **A.2 DYNAMICS MODEL**

668

669    In this work, we train an ensemble of probabilistic neural networks to model the system’s dynamics.  
 670    Specifically, we utilize ensembles of five dynamics models, where the  $b^{th}$  model,  $f_{\theta_b}$ , is parameter-  
 671    ized by  $\theta_b$ . Each network in the ensemble is trained to minimize the negative log-likelihood of the  
 672    predicted outcomes, optimizing the following objective:

673

674

$$675 \quad \mathcal{L}(\theta_b) = - \sum_{n=1}^N \log f_{\theta_b}(s_{n+1}|s_n, a_n). \quad (5)$$

676

677    Referring to the ensembles used in PETS (Chua et al., 2018), we define our network to output a  
 678    Gaussian distribution with diagonal covariance parameterized by  $\theta$  and conditioned on  $s_n$  and  $a_n$ ,  
 679    i.e.:  $f = Pr(s_{t+1}|s_t, a_t) = \mathcal{N}(\mu_\theta(s_t, a_t), \Sigma_\theta(s_t, a_t))$ . In this specific case, Eq. (5) becomes:

680

681

$$682 \quad \mathcal{L}_G(\theta_b) = \sum_{n=1}^N [\mu_{\theta_b}(s_n, a_n) - s_{n+1}]^\top \Sigma_{\theta_b}^{-1}(s_n, a_n) [\mu_{\theta_b}(s_n, a_n) - s_{n+1}] + \log \det \Sigma_{\theta_b}(s_n, a_n), \quad (6)$$

683

684    The next states are obtained in the same manner as **TS**∞ described in PETS.

685

686    Additionally, to mitigate the risk of over-fitting that can occur when a dynamics model is trained  
 687    solely on expert trajectories, we augment the training data with online agent experiences and itera-  
 688    tively retrain the dynamics models.

689

690    **A.3 TRAINING CURVES FOR BASELINE METHODS WITH ADDITIONAL STEPS**

691

692    In Section 5.3, we presented the performance of DTWIL and various baseline methods when inter-  
 693    acting with the environment for up to 50K steps, focusing on sample efficiency. In Figure 5, we  
 694    showcase the training curves of baseline methods over 500 thousand steps, which is 10 times the  
 695    original limit. These results reveal that methods like CFIL and OPOLO can train effective poli-  
 696    cies on multiple tasks when granted sufficient interaction steps. However, compared to DTWIL,  
 697    which requires only the training of an MPC dynamics model to generate surrogate expert demon-  
 698    strations, these online LfO methods demand significantly more interaction steps, highlighting their  
 699    inefficiency relative to DTWIL.

700

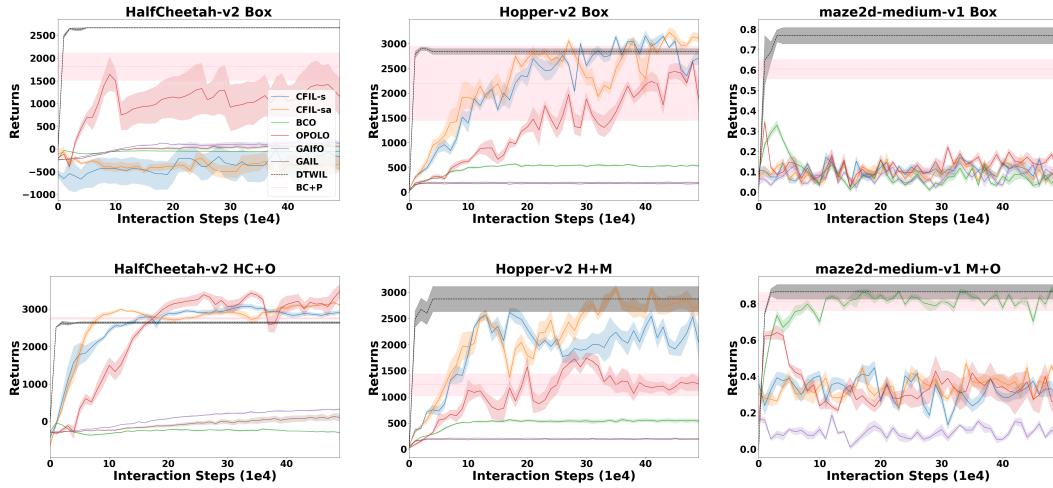


Figure 5: Training curves for baseline methods over 1 million interaction steps across multiple tasks.

#### A.4 DTW INPUT NORMALIZATION

Typically, trajectories are normalized before being fed into the DTW calculation, as described in 4.1.1. In this section, we analyze the impact of this normalization. Table 5 shows an ablation study on HalfCheetah and Hopper with their respective box constraints. We observe a performance drop in both environments when this normalization step is omitted from DTWIL. This is because, without normalization, DTW becomes disproportionately influenced by dimensions with larger scales, leading to poor generalization. Conversely, when the states are normalized in advance, DTW treats each dimension equally, resulting in more effective warping.

Task	HalfCheetah Box	HalfCheetah Box w/o N	Hopper Box	Hopper Box w/o N
Return-S	<b>2576.2 ± 61.62</b>	1667.46 ± 51.13	<b>2527.63 ± 572.53</b>	608.18 ± 208.20
Return-BC	<b>2669.41 ± 4.56</b>	1893.9 ± 71.56	<b>2844.68 ± 57.77</b>	281.13 ± 31.88

Table 5: Impact of DTW input normalization on performance. Return-S represent the average return of surrogate expert data, while Return-BC denotes the average evaluation return of the BC policy trained on this surrogate data. “W/o N” indicates results obtained without applying DTW input normalization.

	$\beta = 0$	$\beta = 0.02$	$\beta = 0.05$	$\beta = 0.1$	$\beta = 0.2$
Return-S	820.71 ± 84.78	1492.97 ± 144.35	<b>2527.63 ± 572.53</b>	1657.47 ± 286.44	670.72 ± 328.28
Return-BC	889.65 ± 5.39	1138.85 ± 56.35	<b>2844.68 ± 57.77</b>	2167.3 ± 360.73	723.95 ± 345.70
	$h_{erc} = 0$	$h_{erc} = 5$	$h_{erc} = 10$	$h_{erc} = 20$	
Return-S	820.71 ± 84.78	<b>2527.63 ± 572.53</b>	2425.25 ± 370.40	2166.99 ± 351.04	
Return-BC	889.65 ± 5.39	<b>2844.68 ± 57.77</b>	2686.85 ± 135.64	2616.09 ± 102.90	

Table 6: Impact of varying  $\beta$  and  $h_{erc}$  values on performance in the Hopper task with H+M constraints. The table highlights the optimal balance between expert actions and MPC sampling, showing the best-performing configurations for stability and action guidance.

#### A.5 HYPERPARAMETERS IN ERC

We explore the influence of the hyperparameter  $\beta$ , which regulates the balance between expert actions and MPC-sampled actions in the ERC method. Additionally, we examine the effect of the

horizon length  $h_{erc}$ , which determines how many steps to blend MPC-sampled actions with expert actions. We conducted experiments on the Hopper with H+M constraints, varying  $\beta$  from 0 to 0.2 and  $h_{erc}$  from 0 to 30, while keeping all other hyperparameters fixed at their optimal values identified in prior tuning. As shown in Table 6, setting  $\beta$  to 0.05 resulted in the highest performance. A lower  $\beta$  led to instability in the sampled actions, while higher values negatively impacted the MPC optimization process. Regarding  $h_{erc}$ , a value of 5 provided the best results. Extending the horizon did not improve performance, as expert actions taken too far in the future became less informative due to the action constraints.

## A.6 COMPUTATIONAL TIME

In this section, we present the computational time of various baselines and DTWIL during inference. Table 7 reports the average computational time (in seconds) required to generate a single action during inference in HalfCheetah, averaged over 5000 generations. As shown, methods with state-dependent constraints require significantly more time due to the use of the projection function implemented with Gurobi, whereas box constraints, which allow actions to be directly clipped, are much faster.

	DTWIL	BC+P	GAIL+P	BCO+P	GAIFO+P	OPOLO+P	CFIL-sa+P	CFIL-s+P
HalfCheetah Box	0.0002092	0.0002164	0.0004068	0.0003413	0.0003860	0.0002955	0.0010342	0.0010611
HalfCheetah HC+O	0.0337372	0.0334898	0.0091491	0.0104184	0.0093199	0.0091958	0.0099135	0.0098245

Table 7: Average computation time required to generate a single action during inference, averaged over 5000 trials.