

STAT 425 HW#2

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Problem 4:

$$F = \frac{MS(\text{reg})}{MS(\text{err})} = \frac{FSS/(P-1)}{RSS/(n-P)} = \frac{(TSS-RSS)}{RSS} \cdot \frac{n-P}{P-1} \quad \textcircled{1}$$

$$R^2 = \frac{FSS}{TSS} = \frac{TSS-RSS}{TSS}$$

$$\frac{R^2}{1-R^2} = \frac{(TSS-RSS)/TSS}{RSS/TSS} = \frac{TSS-RSS}{RSS}$$

Plug in $\textcircled{1}$:

$$F = \frac{R^2}{1-R^2} \cdot \frac{n-P}{P-1} \quad \begin{array}{l} \text{where } n \text{ is \# of observations,} \\ P \text{ is \# of predictors.} \end{array}$$

Problem 6:

Since $\hat{Y} = HY$.

$$\text{Var}(\hat{Y}|X) = \text{Var}(HY|X)$$

$$= H^T H \text{Var}(Y|X)$$

Since H only depends on X .

$$= H \text{Var}(Y|X)$$

Since $H^T H = HH^T = H$

$$= H\sigma^2$$

Since $\text{Var}(Y|X) = \sigma^2 I$

