

**Logistic Regression with Regularizer** $L_2$  regularizer

Regularization strength $\lambda$	Classification error on test data	Number of 0's in learned weight vector
0.001	0.1172	0
0.01	0.1241	0
0.05	0.1241	0
0.1	0.1172	0

 $L_1$  regularizer

Regularization strength $\lambda$	Classification error on test data	Number of 0's in learned weight vector
0.001	0.1241	0
0.01	0.1241	0
0.05	0.1241	1
0.1	0.1655	3

For  $L_1$  regularizer, in our experiment, when  $\lambda = 0.001, 0.01$ , and  $0.05$ , the classification errors on the test data are the same. When  $\lambda = 0.1$ , the classification error increases. Therefore, when  $\lambda$  reaches a certain threshold, our performance becomes worse (we impose a too strong regularization and are underfitting). When  $\lambda = 0.001, 0.01$ , number of zeros in the learned weight vector is 0. When  $\lambda$  increases, number of zeros in the learned weight vector increases, because we are imposing a stronger regularization, that is, more truncation happens, because  $w'(t+1)$  and  $w(t+1)$  have more chance to have different signs.