Science Versus Magic

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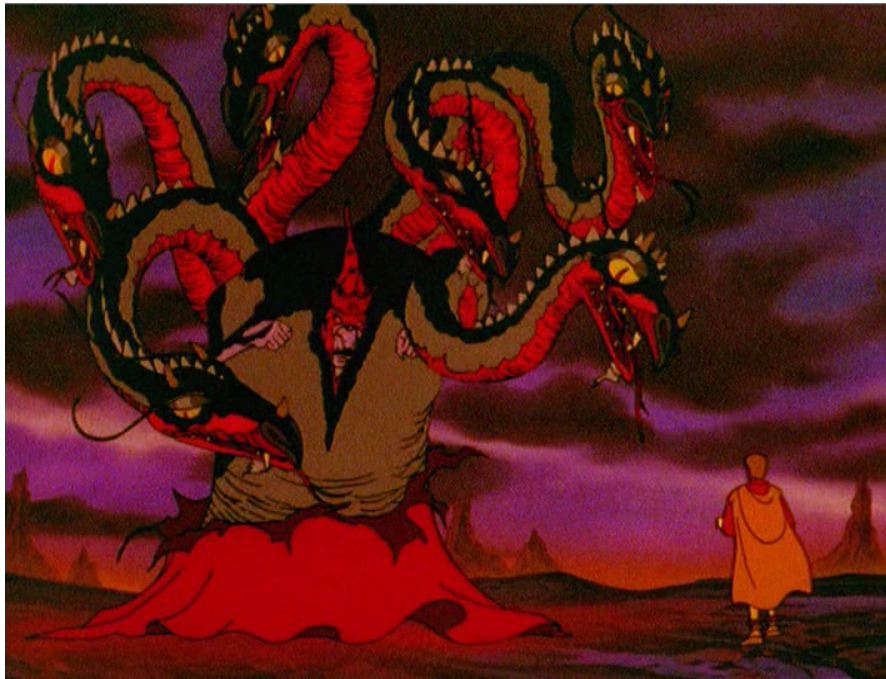
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1 The conflict

Figure 1: Maigc (on the left) versus science (on the right). *The final battle from The Flight of Dragons, a 1982 animated film produced by Jules Bass and Arthur Rankin, Jr.*

The dawn of 19'th century was the tipping point in the battle of logicians versus magicians. While logicians won, the battle isn't of the kind that wins the war. The war still rages on in each of the humans minds. But do we have to bow before our new overlords? What are the consequences of doing so? Or should we, perhaps, die fighting?

1.1 The history of the conflict

Even though the system of formal proof was known as early as Ancient Greece, due to the work of Euclid—who laid foundations of geometry and the modern day formal reasoning, it was not until Frege that formal reasoning become a requirement, first for logic and mathematics and later, with the help from philosophers such as Rudolf Carnap and Karl Popper, it become a requirement for natural sciences. These ideas were furthered by Jan Paul Sartr, who built upon Friedrich Nietzsche earlier works, which suggested that phenomenalism must be abandoned. The idea, which had a profound effect on human sciences. Combined with Piagetian approach to teaching and development of an individual it demystified the process of thinking. This, in turn, enabled Alan Turing to conceive of a *universal* theory of computation, that is to extend the thinking beyond

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Figure 2: "And I for one welcome our new insect overlords" *A statement made by Kent Brockman, a Channel 6 news anchor in the 1994 episode of The Simpsons, "Deep Space Homer"*

humanity, to level it with other natural events such as those which would be described by physcis or biology.

Of course, the magic didn't surrender its positions willingly! Occasionally its guerilla warfare gained enough strenght to overthrow the new regime, although so far, most such cases had been contained. Further in this pamphlet I'm going to speculate about what would happen, shall the magic win, what are the reasons to support either side, and finally, since I'm as biased as anyone is, I will lay out a plan of action for those honestly willing to serve our new overlords.

Formal languages used to be the prerogative of the few, at first only the logicics and mathematics, later natural and social sciences, and, finally with computers becoming a commodity it is gradually becoming a ubiquotous requirement for all kinds of education. This might have started with Alan Kay, his Croquet project, which later developed into http://www.opencobalt.org/. Initiatives like http://code.org are gaining momentum, and will continue to grow.

1.2 The tempation

Figure 3: A promo poster for the game Heroes of Might and Magic VI.

I admit that magic is cool.

Figure 4: The promo poster released for My Little Pony: Friendship is Magic series. *Second season, Episode 8.*

And some times even cooler.

Magic is the best possible solution to any kind of problem we might come up with. Even by the standards of science, there is no plausible reason not to choose magic, since it offers an easier solution. Doing things the scientific way is remarkably harder. But what makes magic so easy and appealing?

- We've inherited most of it. The will to believe in magic runs in our veings. It is the heirloom of our ancestors that we cherish and love so fondly that makes it a moral imperative to believe in magic.

- There seems to be a natural tendency in the way of how humans approach problem solving to prefer some algorithms over others. In particular, humans strongly discriminate against all algorithms which suggest more than added logarithmic time. We also favor myopic decisions, which seems to be due to the benefits of finding any being greater than the costs associated with search that will likely take a very long time.

- The very fact that anyone of us survived thus far ignites a belief that by doing what we did until this point we are guaranteed a greater chance of success than by following any other strategy.

- On top of that, there's the peer pressure. As long as we are convinced that our peers will accept our magical thinking as a valid approach to describing reality, we are safe in our beliefs. We don't require complete agreement to validate our belief system. A smiple acknowledgment of the method's validity is enough for magic to proliferate.

- Finally, magic is ubiquotous, it is forgiving, it is pervasive. Quantitatively, it occupies infinitely larger fraction of the solution space than the one left to the science. So, even if you don't choose sides, by the virtue of sheer chance alone, one would most likely end up doing magic.

Science, on the other hand, nags you, repremands you whenever you fall short of attaining its standards which seem to never stop getting higher. It pays no repsect to traditions or religions. It can't be bothered with the mood swings of your boss or the fact that you have a family to feed. It offers hard work and ever so rarely an elusive reward. It isn't something you can easily pass on to your heirs, in fact, it becomes more difficult with each generation to even preserve that what has been found. It is counterintuitive, it is rare and fragile. So why would you even consider choosing it?

1.3 Why magic is bad

$$\boxed{\text{VOLUME(R)} = (4/\text{INT(PI)}) * \text{PI} * R^{\wedge}\text{INT(PI)}}$$

PROGRAMMING TIP: THE NUMBER "3" IS CURSED. AVOID IT.

Figure 5: http://xkcd.com/1275/

You probably watched at least one movie urging you to believe in magic. Even the expression "believe in magic" itself is too catchy to have possibly escaped your attention. It is a far less known fact that the word "magic" has a negative or pejorative meaning, when used by programmers. In that later sense, "magic" means something that cannot be explained rationally. "Magic numbers" are numbers that appear in a program for no discernible reason. The same goes for strings. The reasons for dislike are simple: magic does not allow one to solve the problem mechanically. Mechancial solutions are based on the fact that the problem can be formulated logically, that is *formalized!* If there is a number in one's program without an explanation of how to produce it, that number is magical. What is meant by that is: that whoever will try to adapt the program to their need will have to answer the question *should this number be the same for me, or should I draw a different one?* Given the infinite nature of numbers, the question may not be answered through guessing (magic).

1.4 Inventor paradox

Figure 6: Bernard Turpin as a mad scientist

In a nutshell, inventor paradox is the observation that, despite what you might expect, once the subject of one's research is more constrained it becomes easier to proceed to finding solution. A way of understanding why this happens is to think that the unconstrained parts of the problem are *magical* in the same sense, in which numbers or strings can be (as discussed in 1.3.) Once the search space becomes infinitely large, it becomes impossible to make any progress. We've invented formalization as a response to the problem posed by infinity. In fact, despite all the hardship, there is no better way to combat it. No matter what Soren Kierkegaard has to say.

1.5 Magical thinking

Figure 7: The evil queen consulting the magic mirror. *A scene from Walt Disney 1937 film Snow White and the Seven Dwarfs*

Magical thinking is the extension of magical numbers and strings. Magical thinking is understood as reliance on superstition, religious belief or exercise of some religious rite, witnessing a revelation, being in a transe, or by observing a taboo. But some times it's not easy to recognize it as such. Quasi-religious practices are not in themselves a source of magical thinking, they are a fertile ground for one. It flourishes due to all the same reasons descirbed in 1.2.

Unfortunately, we already know, that to follow this route is to sink in the abyss of infinite choices, the despair of uncertain, meaningless existence.

Nevertheless, there is hope. Generations after generations, despite eventual defeats, periods of stagnation and highly unreliable infrastructre, it seems like the determination of the few had preserved and even improved the scientific knowledge. The next chapter of this pamphlet is an attempt to pass some of it onward.

2 The solution

In order to convince you of the practical benefits of formalization over magic I hereby present you the model of the PowToon player UI. I've spent about an hour constructing it, verifying its correctness and putting down related notes.

First, lets commit to the memory these vocabulary words:

- *symbol* or *term* is the basic unit of the Prolog program. By convention symbols start with a lowercase letter, but you can go against the convention, if you so want, in which case you will have to wrap them in single quotes.

- Prolog can define a *fact*. A fact is either a symbol, a relation (note that symbols are nullary relations too), or a recurrence (a complex kind of relation). The later two are also refered to as *rules* or *clauses*.

- All facts of a *program* constitute a *database*.

- Therefore, your program can add facts to the database, or *query* the database to derive new facts. Queries start with ?- symbol.

2.1 Database

Now, define some facts about what we know to be true for the player:

```prolog
playback(playing).
playback(stopped).
```

The player can either play or pause.

```prolog
position(beginning).
position(middle).
position(end).
```

The playhead can be positioned at the beginning of the timeline, at the end or somewhere in the middle.

```prolog
content(slide).
content(video).
```

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At any given moment the contents of the player are either video, or anything else, which I choose to describe as slide.

```prolog
mode(auto).
mode(manual).
```

Finally, the player can be either in auto-play or manual modes.

Now, lets sum it all up:

```prolog
modifiers(Playback, Position, Content, Mode):-
    playback(Playback),
    position(Position),
    content(Content),
    mode(Mode).
```

The state of the player is a combination of its playback, its position, its content and its mode.

2.2 Constraints

Now, lets put some constraints in place. This is the interesting part. Here we define what things we don't want to happen in the player. Specifically, we are interested in that certain buttons will not be visible in certain states.

```prolog
first_button(modifiers(_, Position, _, _), Button):-
    ( Position = beginning -> Button = none ; Button = rewind ).

second_button(modifiers(Playback, Position, Content, _), Button):-
    ( Position = end -> Button = replay ;
      ( Playback = stopped ->
        ( Content = video -> Button = play_video ; Button = play_slide ) ;
        ( Content = video -> Button = stop_video ; Button = stop_slide ) ) ).

third_button(modifiers(_, Position, _, _), Button):-
    ( Position = end -> Button = none ; Button = fast_forward ).

fourth_button(modifiers(_, _, _, Mode), Button):-
    ( Mode = auto -> Button = auto ; Button = manual ).
```

Whoa, this was a lot of code for one time, let's see what it does!

This code assumes there are four slots for buttons we are interested in. First slot can be either empty or occupied by rewind *button. Second slot can be occupied by a whole*

five different buttons. Third slot is very similar to the first one, and the last one is never empty, but switches between `auto` *and* `manual` *buttons.*

Note the constructions (`condition -> goal1 ; goal2`). Also note new vocabulary word *goal*. Goals are *propositions* that we *prove* by executing the program. Effectively, our program is a mechanical tool for proving formal statements made about the *universe of discourse* (or a *structure*) defined in the program. The sentence above could be thus read as follows:

If it is possible to prove `condition` *then prove* `goal1`, *otherwise prove* `goal2`.

2.3   Larger example

```
if_pressed(Button, modifiers(Playback, Position, Content, Mode), NextState):-
    ( Button = none ->
      NextState = modifiers(Playback, Position, Content, Mode) ;
      Button = rewind ->
      ( Position = middle ->
        NextState = modifiers(Playback, beginning, Content, Mode) ;
        NextState = modifiers(Playback, middle, Content, Mode) ) ;
      Button = fast_forward ->
      ( Position = middle ->
        NextState = modifiers(Playback, end, Content, Mode) ;
        NextState = modifiers(Playback, middle, Content, Mode) ) ;
      Button = play_video ->
      ( Content = video ,
        Playback = stopped ,
        ( Position = middle ; Position = beginning ) ,
        NextState = modifiers(playing, Position, Content, Mode) ) ;
      Button = stop_video ->
      ( Content = video , Playback = playing ,
        ( Position = middle ; Position = beginning ) ,
        NextState = modifiers(stopped, Position, Content, Mode) ) ;
      Button = play_slide ->
      ( Content = slide , Playback = stopped ,
        ( Position = middle ; Position = beginning ) ,
        NextState = modifiers(playing, Position, Content, Mode) ) ;
      Button = stop_slide ->
      ( Content = slide , Playback = playing ,
        ( Position = middle ; Position = beginning ) ,
        NextState = modifiers(playing, Position, Content, Mode) ) ;
      Button = replay ->
      ( Position = end ,
        NextState = modifiers(stopped, beginning, Content, Mode) ) ;
      Button = auto ->
      ( Mode = auto ,
        NextState = modifiers(Playback, Position, Content, manual) ) ;
      Button = manual ->
      ( Mode = manual ,
        NextState = modifiers(Playback, Position, Content, auto) ) ).
```

Even though we've defined the behavior of the buttons, we are still nowhere near

making our program useful. Below is a first attempt at putting it all together:

Whoa, this was a lot of code! But, to tell you the truth, this code could have been condenced to a fraction of the above by use of recursion. Recursion is universally acknowledged to be a hard topic for beginners, and this is one of the reasons why the code is presented as a list of rules rather than a more condence and mathematically appealing form. If you examine it closely you will see that the code is largerly repetitive, thus doesn't require as much effort understanding it as was the case with the previous snippets.

All this rule does it encodes the behavior of buttons, when they are pressed in various states. Now, this is what we were after! Finally, this is a really useful program. This program can unambiguously answer questions such as:

What should the UI look like, given its previous state and the fact that the `fast_forward` *button was clicked?*

Compare this to the existing document. Which one is longer? Which one can be reliably said to capture all possible cases? Which one can be used mechanically to develop a program and to verify that the program meets the requirements? Know that it is only the beginning. It is possible to do much, much more than this, if only you apply some effort!

2.4 Queries

Below are some examples of the queries one can execute against the database defined above:

```
?- if_pressed(fast_forward, modifiers(stopped, middle, slide, manual), X).
X = modifiers(stopped, end, slide, manual).
```

Reading:

What must be the state of the player UI, given that the previous state was such that the player didn't play, the playhead was in the middle of the timeline, the currently displayed content was a slide and the playback mode was manual.

The answer given seems to be self-explanatory.

Even more, you can refine the question by asking specifically about the change in position:

```
?- if_pressed(fast_forward,
              modifiers(stopped, middle, slide, manual),
              modifiers(_, X, _, _)).
X = end.
```

Or, you could omit some detail of specification, to obtain more possible answers:

```
?- if_pressed(play_video,
              modifiers(stopped, From, video, auto),
              modifiers(playing, To, video, auto)).
From = To, To = middle ;
From = To, To = beginning.
```

The interpretation of the above:

The effect of pressing `play_video` *button, given it is at all possible is such that if the player was in the* `middle` *state, it will remain in the same state, and the same is true for* `beginning` *state.*

From above you can also indirectly derive that this operation is not defined for the `end` state, since this state doesn't allow us to press `play_video` button.

2.5   Homework

But we aren't done yet! The program can be augmented with the notion of player's state, which also includes the state of the buttons:

```
buttons(State, [A, B, C, D]):-
    first_button(State, A),
    second_button(State, B),
    third_button(State, C),
    fourth_button(State, D).

state(Modifiers, Buttons):-
    modifiers(Modifiers), buttons(Modifiers, Buttons).
```

Given this as a start, and usign the example from 2.3, you can come up with a program, which can answer questions like:

Given the player is in a particular state, and such-and-such buttons are visible what are the possible actions that can be taken to transition to the next state?

Which I leave as an exercise for the reader.