#### Meaning of prefixes

S - REAL D - DOUBLE PRECISION C - COMPLEX Z - COMPLEX\*16

(this may not be supported by all machines)

For the Level 2 BLAS a set of extended-precision routines with the prefixes ES, ED, EC, EZ may also be available.

#### Level 1 BLAS

In addition to the listed routines there are two further extended-precision dot product routines DQDOTI and DQDOTA.

#### Level 2 and Level 3 BLAS

Matrix types:

GE - GEneral GB - General Band

SY - SYmmetric SB - Sym. Band SP - Sum. Packed HE - HErmitian HB - Herm. Band HP - Herm. Packed TR - TRiangular TB - Triang. Band TP - Triang. Packed

### Level 2 and Level 3 BLAS Options

Dummy options arguments are declared as CHARACTER\*1 and may be passed as character strings.

TRANx = 'No transpose', 'Transpose',

'Conjugate transpose'  $(X,X^T,X^H)$ 

UPLO = 'Upper triangular', 'Lower triangular'
DIAG = 'Non-unit triangular', 'Unit triangular'
SIDE = 'Left', 'Right' (A or op(A) on the left,

or A or op(A) on the right)

For real matrices, TRANSx = 'T' and TRANSx = 'C' have the same meaning.

For Hermitian matrices, TRANSx = 'T' is not allowed. For complex symmetric matrices, TRANSx = 'H' is not allowed.

### References

C. Lawson, R. Hanson, D. Kincaid, and F. Krogh, "Basic Linear Algebra Subprograms for Fortran Usage," *ACM Trans. on Math. Soft.* 5 (1979) 308-325

J.J. Dongarra, J. DuCroz, S. Hammarling, and R. Hanson,
 "An Extended Set of Fortran Basic Linear Algebra Subprograms,"
 ACM Trans. on Math. Soft. 14,1 (1988) 1-32

J.J. Dongarra, I. Duff, J. DuCroz, and S. Hammarling, "A Set of Level 3 Basic Linear Algebra Subprograms," *ACM Trans. on Math. Soft.* (1989)

### Obtaining the Software via netlib@ornl.gov

To receive a copy of the single-precision software, type in a mail message:

send sblas from blas send sblas2 from blas

send sblas2 from blas

To receive a copy of the double-precision software,

type in a mail message:

send dblas from blas

 $\verb|send dblas2 from blas|\\$ 

send dblas3 from blas

To receive a copy of the complex single-precision software, type in a mail message:

send cblas from blas

send cblas2 from blas

send cblas3 from blas

To receive a copy of the complex double-precision software, type in a mail message:

sype in a mail message: send zblas from blas

send zblas2 from blas

send zblas3 from blas

Send comments and questions to lapack@cs.utk.edu .

## Basic

## Linear

# Algebra

# Subprograms

### A Quick Reference Guide

University of Tennessee Oak Ridge National Laboratory Numerical Algorithms Group Ltd.

May 11, 1997

### Level 1 BLAS

```
dim scalar vector vector
                                                                 scalars
                                                                                              5-element array
                                                                                                                                                                                                                 prefixes
                                                                                                                                                                                                                 S, D
                                                                                                                            Generate plane rotation
SUBROUTINE xROTG (
                                                                            A, B, C, S)
SUBROUTINE xROTMG(
                                                                 D1, D2, A, B,
                                                                                              PARAM )
                                                                                                                            Generate modified plane rotation
                                                                                                                                                                                                                S, D
                                                                                    C, S)
                                                                                                                                                                                                                S, D
SUBROUTINE xROT ( N.
                                         X, INCX, Y, INCY,
                                                                                                                            Apply plane rotation
SUBROUTINE *ROTM ( N
                                        X, INCX, Y, INCY,
                                                                                              PARAM )
                                                                                                                            Apply modified plane rotation
                                                                                                                                                                                                                S. D
                                                                                                                                                                                                                S. D. C. Z
SUBROUTINE xSWAP ( N.
                                        X, INCX, Y, INCY)
                                                                                                                            x \leftrightarrow u
                               ALPHA, X, INCX )
                                                                                                                                                                                                                S, D, C, Z, CS, ZD
SUBROUTINE xSCAL ( N,
                                                                                                                            x \leftarrow \alpha x
                                        X, INCX, Y, INCY)
                                                                                                                                                                                                                S. D. C. Z
SUBROUTINE xCOPY ( N.
                                                                                                                            y \leftarrow x
                               ALPHA. X. INCX. Y. INCY )
                                                                                                                                                                                                                S, D, C, Z
SUBROUTINE XAXPY ( N.
                                                                                                                            y \leftarrow \alpha x + y
                                                                                                                            dot \leftarrow x^T u
                                        X. INCX. Y. INCY )
                                                                                                                                                                                                                S, D, DS
FUNCTION
               xDOT ( N.
                                        X, INCX, Y, INCY)
                                                                                                                            dot \leftarrow x^T y
                                                                                                                                                                                                                 C, Z
FUNCTION
               xDOTU ( N,
                                        X, INCX, Y, INCY)
                                                                                                                            dot \leftarrow x^H y
FUNCTION
               xDOTC ( N,
                                                                                                                                                                                                                 C, Z
                                                                                                                            dot \leftarrow \alpha + x^T y
                                        X, INCX, Y, INCY)
                                                                                                                                                                                                                 SDS
FUNCTION
               xxDOT ( N,
                                        X, INCX)
                                                                                                                            nrm2 \leftarrow ||x||_2
                                                                                                                                                                                                                S, D, SC, DZ
FUNCTION
               xNRM2 ( N,
                                        X, INCX )
                                                                                                                                                                                                                S, D, SC, DZ
FUNCTION
               xASUM ( N,
                                                                                                                            asum \leftarrow ||re(x)||_1 + ||im(x)||_1
                                         X, INCX)
                                                                                                                            amax \leftarrow 1^{st}k \ni |re(x_k)| + |im(x_k)|
                                                                                                                                                                                                                S, D, C, Z
FUNCTION
               IXAMAX( N,
                                                                                                                                             = max(|re(x_i)| + |im(x_i)|)
Level 2 BLAS
           options
                                             b-width scalar matrix vector scalar vector
                                                                                                                            y \leftarrow \alpha A x + \beta y, y \leftarrow \alpha A^T x + \beta y, y \leftarrow \alpha A^H x + \beta y, A - m \times n
                                                                                                                                                                                                                S, D, C, Z
xGEMV (
                    TRANS
                                     M. N.
                                                        ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
                                                                                                                           y \leftarrow \alpha Ax + \beta y, y \leftarrow \alpha A^T x + \beta y, y \leftarrow \alpha A^H x + \beta y, A - m \times n
                                                                                                                                                                                                                 S, D, C, Z
xGBMV (
                    TRANS,
                                     M, N, KL, KU, ALPHA, A, LDA, X, INCX, BETA, Y, INCY )
                                                                                                                                                                                                                 C, Z
xHEMV ( UPLO,
                                                        ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
                                                                                                                            y \leftarrow \alpha Ax + \beta y
                                        N,
                                        N.K.
                                                        ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
                                                                                                                           y \leftarrow \alpha Ax + \beta y
                                                                                                                                                                                                                 C, Z
xHBMV ( UPLO,
                                                                                                                                                                                                                C, Z
                                         N,
                                                        ALPHA, AP, X, INCX, BETA, Y, INCY)
                                                                                                                           y \leftarrow \alpha Ax + \beta y
xHPMV ( UPLO,
                                                        ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
                                                                                                                            y \leftarrow \alpha Ax + \beta y
                                                                                                                                                                                                                 S, D
xSYMV ( UPLO,
                                        N,
                                                                                                                                                                                                                 S. D
                                        N.K.
                                                        ALPHA, A, LDA, X, INCX, BETA, Y, INCY)
                                                                                                                            y \leftarrow \alpha Ax + \beta y
xSBMV ( UPLO,
                                                        ALPHA, AP, X, INCX, BETA, Y, INCY)
                                                                                                                            y \leftarrow \alpha Ax + \beta y
                                                                                                                                                                                                                S, D
xSPMV ( UPLO,
                                        N,
                                                                                                                            x \leftarrow Ax, x \leftarrow A^Tx, x \leftarrow A^Hx
                                                                 A, LDA, X, INCX )
                                                                                                                                                                                                                S, D, C, Z
xTRMV ( UPLO, TRANS, DIAG,
                                        N,
                                                                                                                            x \leftarrow Ax, x \leftarrow A^Tx, x \leftarrow A^Hx
                                                                 A, LDA, X, INCX )
xTBMV ( UPLO, TRANS, DIAG,
                                         N, K,
                                                                                                                                                                                                                S, D, C, Z
                                                                                                                           \begin{array}{l} x \leftarrow Ax, x \leftarrow A^Tx, x \leftarrow A^Hx \\ x \leftarrow A^\Gamma x, x \leftarrow A^\Gamma Tx, x \leftarrow A^\Gamma Hx \\ x \leftarrow A^\Gamma 1x, x \leftarrow A^\Gamma Tx, x \leftarrow A^\Gamma Hx \\ x \leftarrow A^\Gamma 1x, x \leftarrow A^\Gamma Tx, x \leftarrow A^\Gamma Hx \\ x \leftarrow A^\Gamma 1x, x \leftarrow A^\Gamma Tx, x \leftarrow A^\Gamma Hx \end{array}
xTPMV ( UPLO, TRANS, DIAG,
                                         N,
                                                                 AP, X, INCX)
                                                                                                                                                                                                                S, D, C, Z
                                                                 A, LDA, X, INCX )
                                                                                                                                                                                                                S, D, C, Z
xTRSV ( UPLO, TRANS, DIAG,
                                         N,
xTBSV ( UPLO, TRANS, DIAG,
                                                                 A, LDA, X, INCX )
                                                                                                                                                                                                                S, D, C, Z
                                         N, K,
xTPSV ( UPLO, TRANS, DIAG,
                                        Ν,
                                                                 AP,
                                                                            X, INCX)
                                                                                                                                                                                                                S, D, C, Z
           options
                                     dim scalar vector vector matrix
                                                                                                                            A \leftarrow \alpha x y^T + A, A - m \times n
xGER (
                                     M, N, ALPHA, X, INCX, Y, INCY, A, LDA)
                                                                                                                                                                                                                S. D
                                                                                                                           A \leftarrow \alpha x y^T + A, A - m \times n
                                    M, N, ALPHA, X, INCX, Y, INCY, A, LDA)
                                                                                                                                                                                                                 C. Z
xGERU (
                                                                                                                            A \leftarrow \alpha x y^H + A, A - m \times n
xGERC (
                                     M, N, ALPHA, X, INCX, Y, INCY, A, LDA)
                                                                                                                                                                                                                 C. Z
                                                                                                                           A \leftarrow \alpha x x^H + A
                                                                               A. LDA )
                                                                                                                                                                                                                 C, Z
xHER (UPLO,
                                        N, ALPHA, X, INCX,
                                                                                                                            A \leftarrow \alpha x x^H + A
                                        N, ALPHA, X, INCX,
                                                                               AP )
                                                                                                                                                                                                                 C, Z
xHPR (UPLO,
                                                                                                                           A \leftarrow \alpha x y^H + y(\alpha x)^H + A
                                                                                                                                                                                                                 C, Z
xHER2 ( UPLO,
                                        N, ALPHA, X, INCX, Y, INCY, A, LDA)
                                                                                                                           A \leftarrow \alpha x y^H + y(\alpha x)^H + A
                                                                                                                                                                                                                 C. Z
xHPR2 (UPLO,
                                        N, ALPHA, X, INCX, Y, INCY, AP)
                                                                                                                            A \leftarrow \alpha x x^T + A
xSYR ( UPLO,
                                        N, ALPHA, X, INCX,
                                                                               A, LDA)
                                                                                                                                                                                                                 S, D
                                                                                                                            A \leftarrow \alpha x x^T + A
                                                                                                                                                                                                                 S. D
xSPR (UPLO.
                                        N. ALPHA. X. INCX.
                                                                               AP )
                                                                                                                           A \leftarrow \alpha x y^T + \alpha y x^T + AA \leftarrow \alpha x y^T + \alpha y x^T + A
                                                                                                                                                                                                                 S. D
xSYR2 (UPLO.
                                        N, ALPHA, X, INCX, Y, INCY, A, LDA)
xSPR2 ( UPLO.
                                        N. ALPHA, X. INCX, Y. INCY, AP)
                                                                                                                                                                                                                 S. D
Level 3 BLAS
           options
                                                                     scalar matrix matrix scalar matrix
                                                                                                                            C \leftarrow \alpha o p(A) o p(B) + \beta C, o p(X) = X, X^T, X^H, C - m \times n
xGEMM (
                            TRANSA, TRANSB.
                                                        M. N. K. ALPHA, A. LDA, B. LDB, BETA, C. LDC )
                                                                                                                                                                                                                 S. D. C. Z
                                                                                                                            C \leftarrow \alpha AB + \beta C, C \leftarrow \alpha BA + \beta C, C - m \times n, A = A^T
                                                        M. N.
                                                                    ALPHA, A, LDA, B, LDB, BETA, C, LDC)
                                                                                                                                                                                                                S. D. C. Z
xSYMM ( SIDE, UPLO,
                                                        M. N.
                                                                    ALPHA, A, LDA, B, LDB, BETA, C, LDC)
                                                                                                                            C \leftarrow \alpha AB + \beta C, C \leftarrow \alpha BA + \beta C, C - m \times n, A = A^H
                                                                                                                                                                                                                 C, Z
xHEMM ( SIDE, UPLO,
                                                                                                                            C \leftarrow \alpha A A^T + \beta C, C \leftarrow \alpha A^T A + \beta C, C - n \times n
                                                            N, K, ALPHA, A, LDA,
                                                                                                   BETA, C. LDC )
                                                                                                                                                                                                                S. D. C. Z
xSYRK (
                   UPLO, TRANS,
                                                                                                                            C \leftarrow \alpha A A^H + \beta C. C \leftarrow \alpha A^H A + \beta C. C - n \times n
                                                                                                                                                                                                                 C. Z
                                                                                                   BETA. C. LDC )
xHERK (
                   UPLO, TRANS,
                                                            N, K, ALPHA, A, LDA,
                                                                                                                           C \leftarrow \alpha A B^T + \bar{\alpha} B A^T + \beta C, C \leftarrow \alpha A^T B + \bar{\alpha} B^T A + \beta C, C - n \times n
                                                                                                                                                                                                                S, D, C, Z
xSYR2K(
                   UPLO, TRANS,
                                                            N, K, ALPHA, A, LDA, B, LDB, BETA, C, LDC)
                                                                                                                           C \leftarrow \alpha A B^H + \bar{\alpha} B A^H + \beta C, C \leftarrow \alpha A^H B + \bar{\alpha} B^H A + \beta C, C - n \times n
                                                            N. K. ALPHA, A. LDA, B. LDB, BETA, C. LDC)
                                                                                                                                                                                                                C. Z
xHER2K(
                   UPLO. TRANS.
                                                                                                                            B \leftarrow \alpha op(A)B, B \leftarrow \alpha Bop(A), op(A) = A, A^T, A^H, B - m \times n
                                               DIAG, M, N.
                                                                                                                                                                                                                S, D, C, Z
xTRMM ( SIDE, UPLO, TRANSA.
                                                                    ALPHA, A. LDA, B. LDB )
                                                                                                                            B \leftarrow \alpha op(A^{\Gamma 1})B, B \leftarrow \alpha Bop(A^{\Gamma 1}), op(A) = A, A^T, A^H, B - m \times n
xTRSM ( SIDE, UPLO, TRANSA,
                                               DIAG. M. N.
                                                                    ALPHA, A, LDA, B, LDB)
                                                                                                                                                                                                                S. D. C. Z
```