

For translation

$$\hat{r}_L = k_{EX} R_T \left(\frac{mRNA^*}{z_T K_T + (z_T + 1) mRNA^*} \right)$$

$$k_{EX} = K_P \left(\frac{v_T}{L_P} \right)$$

$$= \left(\frac{16.5 \text{ aa/s} \times 3600 \text{ s/h}}{308 \text{ aa}} \right) = 192.86 \text{ h}^{-1}$$

$$mRNA^* = \frac{v_x}{\lambda} = \frac{5.88 \mu\text{M/s} \times 3600 \text{ s/h}}{8.35 \text{ h}} = 2535.1 \mu\text{M}$$

$$\begin{aligned} 0 \leq v_5 \leq \hat{r}_L &= 192.86 \text{ h}^{-1} \cdot 1.6 \mu\text{M} \left(\frac{2535.1 \mu\text{M}}{0.8 \times 57 \mu\text{M} + (0.8 + 1) \cdot 2535.1 \mu\text{M}} \right) \\ &= 169.7 \mu\text{M/h} \\ &= 0.047 \mu\text{M/s} \end{aligned}$$

c). In linear programming problems, the shadow price of a constraint is the difference between the optimised value of the objective function and the value of object function, evaluated at the optional basis, when the right hand side of a constraint is increased by a unit. In our problem, we can observe that by increasing the metabolite by one unit, the flux b shows how much more protein can be produced.