# CS5401 FS2018 Assignment 1d

### William Lorey wwlytc@mst.edu

#### Contents

Introduction	1
MOEA Overview	1
Impact of Initialization on MOEA Performance	2
Comparison of Parent Selection, Survival Strategy, and Survival Selection Strategies	2
BONUS #1: Impact of Increasing Number of Objectives on Number of Non- Domination and MOEA Performance	2

## Introduction

Assignment 1d involved implementing a Multi-Objective Evolutionary Algorithm (MOEA) to more effectively solve Light Up puzzles by balancing the fulfillment of three objectives:

- 1. maximize the number of cells lit up (represented in this implementation as a ratio of lit cells to the total number of white cells)
- 2. minimize the number of bulbs shining on each other
- 3. minimize the number of black cell adjacency constraint violations

For BONUS #1, a fourth objective was added, namely minimizing the number of bulbs placed on the board.

This report outlines this solution's particular implementation of a MOEA, the impact of initialization strategies on the MOEA's performance, a comparison between parent selection, survival strategy, and survival selection strategies on MOEA performance, as well as the impact of increasing the number of objectives on non-domination and MOEA performance (BONUS #1).

#### **MOEA Overview**

The MOEA implemented in this assignment is based on the NSGA-II algorithm. It begins, similar to a standard evolutionary algorithm, by creating an initial population using either uniform random or validity enforced plus uniform random initialization, the settings for which

are specified in the algorithm configuration file. That population is evaluated and the subfitnesses are determined and assigned to each individual in the population.

The population is then evaluated on the basis of non-domination. A list of Pareto fronts is created from the initial population where all genotypes in a given front are not dominated by any other genotypes in that front while genotypes in higher level fronts are dominated by genotypes in lower level fronts. The 'best' genotypes, those in the best level of non-domination, are assigned to level number one. Subsequent levels increase in increments of one for other levels of non-domination.

The fitness of each genotype is then set to its level in the list of Pareto fronts, with individuals exhibiting a smaller fitness (level number) are more fit. A binary tournament selection is performed to choose breeding parents. Then offspring are created using an n-point crossover recombination (with n determined in the configuration file). Following that, mutation is performed, completing the child population.

For the standard NSGA-II configuration (exhibited in the deliverables configuration folder), the plus survival strategy is exhibited, combining the children and parent populations into one large population from which to choose the new population. Individuals are then selected for survival using a binary tournament selection and the process is repeated using the new population until the end of the experiment.

## Impact of Initialization on MOEA Performance

Comparison of Parent Selection, Survival Strategy, and Survival Selection Strategies

BONUS #1: Impact of Increasing Number of Objectives on Number of Non-Domination and MOEA Performance

TODO: need to create config files and run test for this

Table 1: Statistical Analysis performed on the Uniform Random and Validity Enforced Uniform Random Initialized, Randomly Generated Puzzle, EA configurations

	random_gen	random_gen_uniform_random_init
mean	1.1032528479567796	1.0764116503308312
variance	0.5771562510229628	0.5665987346326673
standard deviation	0.7597080037902475	0.7527275301413303
observations	90	90
df	89	89
F	1.018633145019535	
F critical	0.7042808002041888	
Unequal variances assumed		
observations	90	
df	91	
t Stat	0.23677202742177048	
P two-tail	0.8131059379632284	
t Critical two-tail	1.9864	
Nether random_gen_uniform_random_init		
nor random_gen is statistically better		

Table 2: Statistical Analysis performed on the Uniform Random and Validity Enforced Uniform Random Initialized, Provided Puzzle, EA configurations

	website_puzzle	website_puzzle_uniform_random_init
mean	0.8031737242867952	0.7959489651519913
variance	0.734732706694364	0.7417386264875153
standard deviation	0.8571655071772102	0.8612424899454946
observations	90	90
df	89	89
F	0.9905547324313853	
F critical	0.7042808002041888	
Unequal variances assumed		
observations	90	
df	91	
t Stat	0.05609263818405474	
P two-tail	0.9553309228197409	
t Critical two-tail	1.9864	
Nether website_puzzle_uniform_random_init		
nor website_puzzle is statistically better		

Table 3: Statistical Analysis performed on the Fitness Proportional Parent & Survival Selection Configuration vs Tournament Parent & Survival Selection Configuration, Randomly Generated Puzzle, Plus Survival Strategy

	random_genfitness_proportional_parentfitness_proportional_survivalplus	random_gentournament_parenttournament_survivalplus
mean	0.9712902683331007	1.1621500278718002
variance	0.6831692544628184	0.5788550823616683
standard deviation	0.8265405340712689	0.7608252640137999
observations	90	90
df	89	89
F	1.180207750229227	
F critical	0.7042808002041888	
Equal variances assumed		
observations	90	
df	100	
t Stat	-1.602785890738212	
P two-tail	0.11075495921868657	
t Critical two-tail	1.984	
Nether random_gentournament_parenttournament_survivalplus		
nor random_genfitness_proportional_parentfitness_proportional_survivalplus		
is statistically better		

Table 4: Statistical Analysis performed on the Fitness Proportional Parent & Survival Selection Configuration vs Tournament Parent & Survival Selection Configuration, Randomly Generated Puzzle, Comma Survival Strategy

$\mathcal{S}_{\mathcal{S}}$		
	random_gentournament_parenttournament_survivalcomma	
1.0292821828716079	1.0534509493717248	
0.5750797820091365	0.5246394448913503	
0.7583401492794223	0.724319987913733	
90	90	
89	89	
1.0961428607950592		
0.7042808002041888		
90		
100		
-0.21742455014656503		
0.8281265270658065		
1.984		
	random_gen_fitness_proportional_parent_fitness_proportional_survival_comma 1.0292821882741697 0.5750797820091365 0.7583401492794223 90 89 1.0961428607950592 0.7042808002041888	

Table 5: Statistical Analysis performed on the Fitness Proportional Parent Selection & Tournament Survival Selection Configuration vs Tournament Parent Selection & Fitness Proportional Survival Selection Configuration, Randomly Generated Puzzle, Plus Survival Strategy

(	J /	/
	$random\_gen\_fitness\_proportional\_parent\_tournament\_survival\_plus$	random_gentournament_parentfitness_proportional_survivalplus
mean	1.1900153275106076	0.9222749663618832
variance	0.56922309186753	0.6628975581945191
standard deviation	0.7544687481052678	0.814185211235453
observations	90	90
df	89	89
F	0.8586893779151596	
F critical	0.7042808002041888	
Unequal variances assumed		
observations	90	
df	91	
t Stat	2.275528242233756	
P two-tail	0.02407306500131702	
t Critical two-tail	1.9864	
random_genfitness_proportional_parenttournament_survivalplus		
is statistically better than		
random_gen_tournament_parent_fitness_proportional_survival_plus		

Table 6: Statistical Analysis performed on the Fitness Proportional Parent Selection & Tournament Survival Selection Configuration vs Tournament Parent Selection & Fitness Proportional Survival Selection, Randomly Generated Puzzle, Comma Survival Strategy

,	· /	0.0
	random_genfitness_proportional_parenttournament_survivalcomma	random_gentournament_parentfitness_proportional_survivalcomma
mean	1.1186544987668479	1.0557988630231474
variance	0.5311136965722282	0.5221373804886605
standard deviation	0.7287754774772737	0.7225907420446657
observations	90	90
df	89	89
F	1.0171914833509275	
F critical	0.7042808002041888	
Unequal variances assumed		
observations	90	
df	91	
t Stat	0.5777943233491296	
P two-tail	0.564133232652437	
t Critical two-tail	1.9864	
Nether random_gentournament_parentfitness_proportional_survivalcomma		
nor random_genfitness_proportional_parenttournament_survivalcomma		
is statistically better		

Table 7: Statistical Analysis performed on the Tournament Parent & Survival Selection (Comma Survival Strategy) vs Tournament Parent & Survival Selection (Plus Selection Strategy), Randomly Generated Puzzle

	random_gentournament_parenttournament_survivalcomma	random_gentournament_parenttournament_survivalplus
mean	1.0534509493717248	1.1621500278718002
variance	0.5246394448913503	0.5788550823616683
standard deviation	0.724319987913733	0.7608252640137999
observations	90	90
df	89	89
F	0.9063398782833109	
F critical	0.7042808002041888	
Equal variances assumed		
observations	90	
df	100	
t Stat	-0.9761931904577807	
P two-tail	0.33029355296868534	
t Critical two-tail	1.984	
Nether random_gentournament_parenttournament_survivalplus		
nor random_gentournament_parenttournament_survivalcomma		
is statistically better		