```
In [607]: import warnings
    warnings.filterwarnings("ignore")
    from sklearn.datasets import load_boston
    from random import seed
    from random import randrange
    from csv import reader
    from math import sqrt
    from sklearn import preprocessing
    import pandas as pd
    import numpy as np
    import matplotlib.pyplot as plt
    from prettytable import PrettyTable
    from sklearn.linear_model import SGDRegressor
    from sklearn import preprocessing
    from sklearn import preprocessing
    from sklearn.metrics import mean_squared_error
```

1. Boston Dataset Exploration

6/25/2019

weizhiwanghit@outlook.com_com6_Implement SGD

In [608]: df =load_boston()
 print(df.feature_names)
 print(df.DESCR)

```
['CRIM' 'ZN' 'INDUS' 'CHAS' NOX RM AGE DIS RAD' 'TAX' 'PTRATIO'
'B' 'LSTAT']
```

.. _boston_dataset:

Boston house prices dataset

Data Set Characteristics:

:Number of Instances: 506

:Number of Attributes: 13 numeric/categorical predictive. Median Value (attribute 14) is usually the target.

:Attribute Information (in order):

- CRIM per capita crime rate by town
- ZN proportion of residential land zoned for lots over 25,000 sq.

ft.

- INDUS proportion of non-retail business acres per town
- CHAS Charles River dummy variable (= 1 if tract bounds river; 0 ot

herwise)

- NOX nitric oxides concentration (parts per 10 million)
- RM average number of rooms per dwelling
- AGE proportion of owner-occupied units built prior to 1940
- DIS weighted distances to five Boston employment centres
- RAD index of accessibility to radial highways
- TAX full-value property-tax rate per \$10,000
- PTRATIO pupil-teacher ratio by town
- B 1000(Bk 0.63)² where Bk is the proportion of blacks by tow

n

- LSTAT % lower status of the population
- MEDV Median value of owner-occupied homes in \$1000's

:Missing Attribute Values: None

:Creator: Harrison, D. and Rubinfeld, D.L.

This is a copy of UCI ML housing dataset. https://archive.ics.uci.edu/ml/machine-learning-databases/housing/

This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.

The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic prices and the demand for clean air', J. Environ. Economics & Management, vol.5, 81-102, 1978. Used in Belsley, Kuh & Welsch, 'Regression diagnostics ...', Wiley, 1980. N.B. Various transformations are used in the table on pages 244-261 of the latter.

The Boston house-price data has been used in many machine learning papers that a ddress regression problems.

- .. topic:: References
- Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Dat a and Sources of Collinearity', Wiley, 1980. 244-261.
- $\ Quinlan, R. \ (1993). \ Combining \ Instance-Based \ and \ Model-Based \ Learning. \ In \ Pr \ localhost: 8888/nbconvert/html/Desktop/Assignment/NLP \ and \ ML \ Intro/weizhiwanghit% 40 outlook.com_com6_Implement \ SGD.ipynb?download=false \ 3/12$

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oceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.

```
In [609]: #data = pd.DataFrame(bostan.data, columns = bostan.feature_names)

X = load_boston().data
Y = load_boston().target

X= pd.DataFrame(X, columns = df.feature_names)
Y = pd.DataFrame(Y, columns = ['PRICE'])
```

```
6/25/2019
                                            weizhiwanghit@outlook.com_com6_Implement SGD
            print(X.shape)
In [610]:
            print(X.head(10))
            Y.head(10)
            (506, 13)
                   CRIM
                                         CHAS
                                                   NOX
                                                                             DIS
                                                                                   RAD
                                                                                           TAX
                                                                                                 \
                            zn
                                 INDUS
                                                            RM
                                                                   AGE
               0.00632
                          18.0
                                  2.31
                                           0.0
                                                0.538
                                                         6.575
                                                                  65.2
                                                                         4.0900
                                                                                   1.0
                                                                                         296.0
            1
               0.02731
                           0.0
                                  7.07
                                           0.0
                                                0.469
                                                         6.421
                                                                  78.9
                                                                         4.9671
                                                                                   2.0
                                                                                         242.0
            2
                                  7.07
               0.02729
                           0.0
                                           0.0
                                                 0.469
                                                         7.185
                                                                  61.1
                                                                          4.9671
                                                                                   2.0
                                                                                         242.0
            3
               0.03237
                           0.0
                                  2.18
                                           0.0
                                                0.458
                                                         6.998
                                                                  45.8
                                                                         6.0622
                                                                                   3.0
                                                                                         222.0
                                                                  54.2
               0.06905
                           0.0
                                  2.18
                                                0.458
                                                                         6.0622
                                                                                         222.0
                                           0.0
                                                         7.147
                                                                                   3.0
            5
               0.02985
                           0.0
                                  2.18
                                           0.0
                                                0.458
                                                                  58.7
                                                                         6.0622
                                                                                         222.0
                                                         6.430
                                                                                   3.0
            6
               0.08829
                          12.5
                                  7.87
                                           0.0
                                                0.524
                                                         6.012
                                                                  66.6
                                                                         5.5605
                                                                                   5.0
                                                                                         311.0
            7
               0.14455
                          12.5
                                  7.87
                                           0.0
                                                0.524
                                                         6.172
                                                                  96.1
                                                                         5.9505
                                                                                   5.0
                                                                                         311.0
               0.21124
                          12.5
                                  7.87
                                           0.0
                                                0.524
                                                         5.631
                                                                 100.0
                                                                         6.0821
                                                                                   5.0
                                                                                         311.0
               0.17004
                          12.5
                                  7.87
                                           0.0
                                                0.524
                                                         6.004
                                                                  85.9
                                                                         6.5921
                                                                                   5.0
                                                                                         311.0
               PTRATIO
                                   LSTAT
                                В
            0
                          396.90
                   15.3
                                     4.98
            1
                   17.8
                          396.90
                                     9.14
            2
                                     4.03
                   17.8
                          392.83
            3
                   18.7
                          394.63
                                     2.94
            4
                   18.7
                          396.90
                                     5.33
            5
                   18.7
                          394.12
                                     5.21
            6
                   15.2
                          395.60
                                   12.43
            7
                   15.2
                          396.90
                                   19.15
            8
                   15.2
                          386.63
                                   29.93
            9
                   15.2
                          386.71
                                   17.10
Out[610]:
               PRICE
             0
                 24.0
                 21.6
             1
                 34.7
             2
```

7 27.18 16.5

3

4 5

6

9

33.4

36.2

28.7

22.9

18.9

1.1 Split Training and test data

```
6/25/2019
```

```
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In [611]:
          # Split data into training and test dataset
           from sklearn.model_selection import train_test_split
          X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size = 0.33, rando
          m_state = 10)
           print(X_train.shape)
          print(X_test.shape)
          print(Y_train.shape)
           print(Y_test.shape)
```

```
(339, 13)
(167, 13)
(339, 1)
(167, 1)
```

```
6/25/2019
                                     weizhiwanghit@outlook.com_com6_Implement SGD
          print(Y train['PRICE'].sample(10))
In [629]:
          print(np.asmatrix(Y_train['PRICE']))
          print(type(X_train))
          print(type(Y_train))
          389
                 11.5
          405
                  5.0
          415
                  7.2
          407
                 27.9
          368
                 50.0
          501
                 22.4
          471
                 19.6
          393
                 13.8
          109
                 19.4
          238
                 23.7
          Name: PRICE, dtype: float64
          [[14.6 19.8 10.2 23.7 18.7 20.3 50. 25. 14.8 9.5 33.
                                                                    19.4 15.6 20.2
            21.7 24.7 19.5 7.2 31.7 22.4 14.1 21.4 21.7 23.
                                                              20.3 30.7 35.1 20.9
            27. 10.2 22.4 23.3 33.1 28.7 31.6 22.2 17.4 16.1 23.
                                                                    35.4 22.9 34.9
                      24.8 30.5 36.5 21.5 17.5 19.4 34.7 19.6 25.
                                                                    13.9 13.3 18.5
                      22. 13.6 14.9 32.
                                          22.5 23.9 50.
                                                          13.8 20.1 20.8 18.8 50.
            22.2 26.2 20.1 13.8 19.8 17.8 24.1 19.4 22.3 20.
                                                               13.3 21.
                                                                         29.1 22.7
            18.2 21.7 19.6 24.5 14.1 19.9 22.
                                               20.1 15.
                                                          23.
                                                               42.3
                                                                    6.3 34.9 34.6
            20.5 28.7 17.8 10.4 13.9 11.7 50.
                                                 7.4 19.6 22.6 16.2 19.4 20.6 27.5
             5.6 7. 24.8 23.2
                                7.5 5. 19.2 21.1 20.3 24.
                                                               16.2 35.4 23.1 13.5
            15.1 22.9 36.1 22.6 10.2 12.8 50. 22.5 20.
                                                          19.
                                                               50.
                                                                    22.5 19.7
                          17.1 13.8 16.4 33.3 39.8 18.9 30.1 13.2 17.2 31.
            21.4 17.2 36.
            19.3 30.8 18.4 25.
                               11.7 22.3 19.1 21.1 24.4 19.4 17.5 12.7 20.9 19.3
            28.1 17.4 13.4 13.4 23.8 20.1 31.5 44.8 19.1 12.7 50.
                                                                    18.3
            13.4 17.2 8.3 24.8 28.4 22. 20.4 21.4 15.2 21.9 17.6 23.2 21.7 23.3
            11.5 11.8 20. 17.7 5.
                                     22.6 26.6 48.3 18.5 13.3 19.
                                                                    21.9 23.4 29.9
            35.2 19.1 7.2 20.5 18.2 13.
                                          20.6 18.7 24.4 22.
                                                               33.4 14.5 18.
            24.1 19.3 15.2 30.1 24.
                                     14.1 31.5 25.3 41.7
                                                          8.4 20.3 29.6 14.6 26.7
                                     26.6 24.3 15.6 15.6 14.2 25.2 25.
            43.5 18.8 18.9 21.5 29.
                                                                         28.5 37.9
            21.9 33.4 20.8 9.6 8.7 36.2 18.4 21.2 18.6 24.4 24.8 32.2 48.5 18.1
            14.5 13.8 11.8 23.7 21.7 20.4 16.1 20.6 13.8 23.3 24.1 21.2 21.8 24.5
            20.6 27.9 11.9 19.9 25.
                                     20.2 50.
                                               27.9 21.6 14.5 23.1 14.
                                                                         28.7 24.3
            20.1 16.5 24.5 14.4 11.3 27.5 23.7 20.4 17.8 20.8 25.
                                                                    37.2 24.6 19.5
            21.2 32.9 13.1 22.2 20.5 16.8 31.2 18.9 13.1 23.3 17.8 23.1 50.
            34.9 8.1 44. 23.4 16.5 16.8 16.3 21.7 29.8 13.1 17.3 50.
            20.6 21.4 22.8]]
          <class 'pandas.core.frame.DataFrame'>
          <class 'pandas.core.frame.DataFrame'>
```

1.2 Preprocess Numerical Value

```
In [614]: print(X_train.shape)
    print(X_train.shape)
    print(X_test.shape)

(339, 13)
    (339, 13)
    (167, 13)
```

2. SGD in Python

```
In [674]: | def SGD_own (w0, b0, x, y, learning_rate,n_iter):
              grad_m = 0
              grad_b = 0
               for j in range(1, n_iter):
                   \#x = x.sample(160)
                   \#y= y.sample(160)
                   y = np.asmatrix(y)
                   x = np.asmatrix(x)
                   for i in range(len(x)):
                       \#grad_m += -2*x[i].T , (y[:,i] - np.dot(x[i] , w0) - b0)
                       grad_m += -2*x[i].T * (y[:,i] - np.dot(x[i] , w0) - b0)
                       grad_b += -2*(y[:,i] - (np.dot(x[i] , w0) + b0))
                   w1 = w0 - learning_rate * grad_m
                   b1 = b0 - learning_rate * grad_b
                   if (w0==w1).all():
                       break
                   else:
                       w0 = w1
                       b0 = b1
                       learning_rate = learning_rate/2
              return w0, b0
```

```
In [675]: print(type(X_train))
    print(type(Y_train))

<class 'pandas.core.frame.DataFrame'>
```

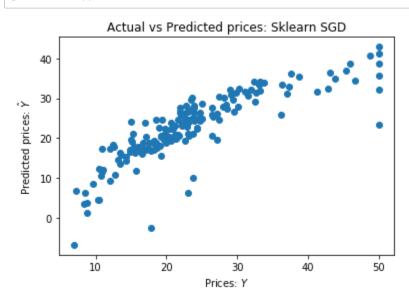
<class 'pandas.core.frame.DataFrame'>

```
In [723]: w0_random = np.random.rand(13)
          w0 = np.asmatrix(w0_random).T
          b0 = np.random.rand()
          optimal w , optimal b= SGD_own(w0, b0, X_train, Y_train['PRICE'],learning_rate =
          0.000485, n_iter = 10000)
          print(optimal_w,optimal_b)
          [[-0.4054812]
           [ 0.30596823]
           [-0.14248085]
           [ 1.06061206]
           [ 0.27256523]
           [ 3.44591036]
           [ 0.51097156]
           [-0.77915757]
           [ 0.37569295]
           [-0.14418825]
           [-1.59839591]
           [ 0.97176776]
           [-2.54343297]] [[21.42210946]]
In [724]: y_pred_own = np.dot(X_test,optimal_w)+optimal_b
          print(y pred own.shape)
          print(Y_test.shape)
          print(mean_squared_error(Y_test, y_pred_own))
          (167, 1)
          (167, 1)
          29.75498247935324
  In [ ]:
  In [ ]:
```

3. Compare with Python SGD

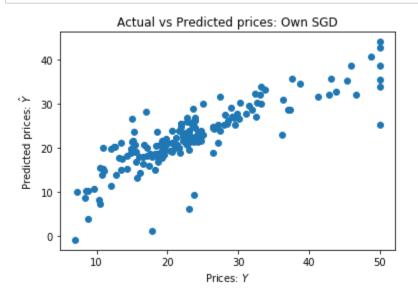
3.1 Sklearn results

```
In [725]: | clf = SGDRegressor()
          clf.fit(X_train, Y_train)
          Y_predict = clf.predict(X_test)
          print(clf)
          print("Coefficients: \n", clf.coef_)
          print("Y_intercept", clf.intercept_)
          SGDRegressor(alpha=0.0001, average=False, early_stopping=False, epsilon=0.1,
                 eta0=0.01, fit intercept=True, l1 ratio=0.15,
                 learning_rate='invscaling', loss='squared_loss', max_iter=None,
                 n_iter=None, n_iter_no_change=5, penalty='12', power_t=0.25,
                 random_state=None, shuffle=True, tol=None, validation_fraction=0.1,
                 verbose=0, warm start=False)
          Coefficients:
                         0.86104532 -0.4366005
                                                  0.5926068 -0.48103866 2.88662273
           [-0.8328814]
           -0.13853722 -1.84424267 0.61214727 -0.56195917 -1.62445177 1.27991093
           -3.46516903]
          Y_intercept [21.46480823]
In [726]: | print(mean_squared_error(Y_test, Y_predict))
          27.993673103581344
In [727]:
           #sklearn SGD actual vs predict
          plt.figure(1)
          plt.scatter(Y_test, Y_predict)
          plt.xlabel("Prices: $Y $")
          plt.ylabel("Predicted prices: $\hat{Y} $")
          plt.title("Actual vs Predicted prices: Sklearn SGD")
          plt.show()
```



3.2 Own SGD function results

In [728]: # Own SGD actual vs predict plt.scatter(Y_test,pd.DataFrame(y_pred_own)) plt.xlabel("Prices: \$Y \$") plt.ylabel("Predicted prices: \$\hat{Y} \$") plt.title("Actual vs Predicted prices: Own SGD") plt.show()



Out[729]:

	Sklearn_weights	Own_weights
0	-0.832881	-0.405481
1	0.861045	0.305968
2	-0.436600	-0.142481
3	0.592607	1.060612
4	-0.481039	0.272565
5	2.886623	3.445910
6	-0.138537	0.510972
7	-1.844243	-0.779158
8	0.612147	0.375693
9	-0.561959	-0.144188
10	-1.624452	-1.598396
11	1.279911	0.971768
12	-3.465169	-2.543433

In [730]:	print("-"*100)		
	<pre>print("The MSE Sklearn SGD is\n", mean_squared_error(Y_test, Y_predict)) print("The MSE own SGD is\n", mean_squared_error(Y_test, pd.DataFrame(y_pred_own)))</pre>		
	The MSE Sklearn SGD is		
	27.993673103581344		
	The MSE own SGD is 29.75498247935324		
In []:			