# Simulation\_summary

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6/16/2020

### Objective.

To effectively analyze different variable selection methods for high dimensional data, dataset that contains a combination of **strong**, **WAI**, **WBC**, and **NuII** predictors had to be generated. The signals were created using the following criterias:

#### 1. Strong signals

$$S_{strong} = j: |\beta_j| > c\sqrt{\frac{log(p)}{n}}$$
, for some c  $> 0, 1 \le j \le p$ 

#### 2. Weak-and-independent (WAI)

$$S_{WBC} = j : |\beta_j| \le c\sqrt{\frac{\log{(p)}}{n}}$$
, for some  $c > 0$ ,  $corr(X_j, X_j') \ne 0$ 

#### 3. Weak-and-correlated (WBC)

$$S_{WBC} = j : |\beta_j| \le c \sqrt{\frac{\log(p)}{n}}$$
, for some  $c > 0$ ,  $corr(X_j, X_j') = 0$ 

#### 4. Null signals

$$S_{null} = j : \beta_j = 0, 1 \le j \le p$$

## The general idea of generating data

- 1. Create a 50x50 positive-definite variance-covariance matrix with WBC variables being correlated to the first strong predictor with  $corr(X_j, X_j') = 0.3$
- 2. Generate a multivariate normal distribution with mean 0 and sigma equal to the variance-covariance matrix generated in step one.
- 3. The matrix of true coefficient values was created with the strong signals set to 5 and the weak predictors (WAI and WBC) set to the threshold value defined by the changing c value.
- 4. Finally, get the linear response Y values:

$$Y = 1 + X\beta + \epsilon$$

```
# generate_data function
                                                                                         ## generate data from multivariate normal
penerate_data = function(n = 1000, c =1, correlation = 0.3,
                                                                                         X = mvrnorm(n = n, mu = rep(0, num_p), Siama = matrix, empirical = F, tol = 0.1)
                       strong coeff - strong coeff.
                     strong_num = st_weak_num[k,1],
                      wai_num = st_weak_num[k,2],
                                                                                         ## set the coeffecient beta
                      wbc_num = st_weak_num[k,3],
                                                                                         b.true = c(
                                                                                           rep(strong coeff, strong num).
                                                                                            rep(threshold, wai num).
 null_num = num_p - wbc_num - wai_num - strong_num
                                                                                            rep(threshold, wbc_num),
 ## the coeff for wai and wbc
                                                                                            rep(0, null_num)
 threshold = c * (log(num_p)/n)/0.5
 ## the condition that cor(Xi,Xi')=correlation for i' belongs to strong signals
                                                                                         ## get response Y
                                                                                         Y = 1 + X %*% b.true + rnorm(n)
 matrix[1, (strong_num + wai_num + 1):(strong_num + wai_num + wai_num)] = correlation
                                                                                         data = as tibble(data.frame(cbind(X, Y)))
 matrix[(strong_num + wai_num + 1):(strong_num + wai_num + wai_num), 1] = correlation
```