



# Functional Random Generators

Principles of Functional Programming

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## Other Uses of For-Expressions

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*Question:* Are for-expressions tied to collection-like things such as lists, sets, or databases?

*Answer:* No! All that is required is some interpretation of `map`, `flatMap` and `withFilter`.

There are many domains outside collections that afford such an interpretation.

*Example:* random value generators.

# Random Values

You know about random numbers:

```
val rand = java.util.Random()  
rand.nextInt()
```

*Question:* What is a systematic way to get random values for other domains, such as

► booleans, strings, pairs and tuples, lists, sets, trees

?

# Generators

Let's define a trait `Generator[T]` that generates random values of type `T`:

```
trait Generator[+T]:  
  def generate(): T
```

Some instances:

```
val integers = new Generator[Int]:  
  val rand = java.util.Random()  
  def generate() = rand.nextInt()
```

# Generators

Let's define a trait `Generator[T]` that generates random values of type `T`:

```
trait Generator[+T]:  
  def generate(): T
```

Some instances:

```
val booleans = new Generator[Boolean]:  
  def generate() = integers.generate() > 0
```

# Generators

Let's define a trait `Generator[T]` that generates random values of type `T`:

```
trait Generator[+T]:  
  def generate(): T
```

Some instances:

```
val pairs = new Generator[(Int, Int]):  
  def generate() = (integers.generate(), integers.generate())
```

## Streamlining It

Can we avoid the new Generator ... boilerplate?

Ideally, we would like to write:

```
val booleans = for x <- integers yield x > 0
```

```
def pairs[T, U](t: Generator[T], u: Generator[U]) =  
  for x <- t; y <- u yield (x, y)
```

What does this expand to?



## Streamlining It

Can we avoid the new Generator ... boilerplate?

Ideally, we would like to write:

```
val booleans = integers.map(x => x > 0)
```

```
def pairs[T, U](t: Generator[T], u: Generator[U]) =  
  t.flatMap(x => u.map(y => (x, y)))
```

Need map and flatMap for that!

## Generator with map and flatMap

Here's a more convenient version of Generator:

```
trait Generator[+T]:  
  def generate(): T  
  
extension [T, S](g: Generator[T])  
  def map(f: T => S) = new Generator[S]:  
    def generate() = f(g.generate())
```

## Generator with map and flatMap

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```
trait Generator[+T]:
```

```
  def generate(): T
```

```
extension [T, S](g: Generator[T])
```

```
  def map(f: T => S) = new Generator[S]:
```

```
    def generate() = f(g.generate())
```

```
  def flatMap(f: T => Generator[S]) = new Generator[S]:
```

```
    def generate() = f(g.generate()).generate()
```

## Generator with map and flatMap (2)

We can also implement map and flatMap as methods of class Generator:

```
trait Generator[+T]:  
  def generate(): T  
  
  def map[S](f: T => S) = new Generator[S]:  
    def generate() = f(Generator.this.generate())  
  def flatMap[S](f: T => Generator[S]) = new Generator[S]:  
    def generate() = f(Generator.this.generate()).generate()
```

Note the use of `Generator.this` to refer to the `this` of the “outer” object of class `Generator`.

## The booleans Generator

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```
val booleans = new Generator[Boolean]:  
  def generate() = ((x: Int) => x > 0)(integers.generate())
```

## The booleans Generator

What does this definition resolve to?

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val booleans = for x <- integers yield x > 0
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val booleans = integers.map(x => x > 0)
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val booleans = new Generator[Boolean]:  
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val booleans = new Generator[Boolean]:  
  def generate() = integers.generate() > 0
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## The pairs Generator

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def pairs[T, U](t: Generator[T], u: Generator[U]) = t.flatMap(  
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```
def pairs[T, U](t: Generator[T], u: Generator[U]) = t.flatMap(  
  x => new Generator[(T, U)] { def generate() = (x, u.generate()) })
```

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def pairs[T, U](t: Generator[T], u: Generator[U]) = new Generator[(T, U)]:  
  def generate() = (new Generator[(T, U)]:  
    def generate() = (t.generate(), u.generate())  
  ).generate()
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def pairs[T, U](t: Generator[T], u: Generator[U]) = t.flatMap(  
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  def generate() = (new Generator[(T, U)]:  
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  ).generate()
```

```
def pairs[T, U](t: Generator[T], u: Generator[U]) = new Generator[(T, U)]:  
  def generate() = (t.generate(), u.generate())
```

## Generator Examples

```
def single[T](x: T): Generator[T] = new Generator[T]:  
  def generate() = x
```

```
def range(lo: Int, hi: Int): Generator[Int] =  
  for x <- integers yield lo + x.abs % (hi - lo)
```

```
def oneOf[T](xs: T*): Generator[T] =  
  for idx <- range(0, xs.length) yield xs[idx]
```

## A List Generator

A list is either an empty list or a non-empty list.

```
def lists: Generator[List[Int]] =  
  for  
    isEmpty <- booleans  
    list <- if isEmpty then emptyLists else nonEmptyLists  
  yield list
```

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def lists: Generator[List[Int]] =  
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  yield list  
  
def emptyLists = single(Nil)
```

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  for  
    isEmpty <- booleans  
    list <- if isEmpty then emptyLists else nonEmptyLists  
  yield list
```

```
def emptyLists = single(Nil)
```

```
def nonEmptyLists =  
  for  
    head <- integers  
    tail <- lists  
  yield head :: tail
```



## A Tree Generator

Can you implement a generator that creates random Tree objects?

```
enum Tree:  
  case Inner(left: Tree, right: Tree)  
  case Leaf(x: Int)
```



## Application: Random Testing

You know about unit tests:

- ▶ Come up with some test inputs to program functions and a *postcondition*.
- ▶ The postcondition is a property of the expected result.
- ▶ Verify that the program satisfies the postcondition.

*Question:* Can we do without the test inputs?

Yes, by generating *random test inputs*.

## Random Test Function

Using generators, we can write a random test function:

```
def test[T](g: Generator[T], numTimes: Int = 100)
    (test: T => Boolean): Unit =
  for i <- 0 until numTimes do
    val value = g.generate()
    assert(test(value), s"test failed for $value")
  println(s"passed $numTimes tests")
```

# Random Test Function

Example usage:

```
test(pairs(lists, lists)) {  
  (xs, ys) => (xs ++ ys).length > xs.length  
}
```

**Question:** Does the above property always hold?

☐ Yes

☐ No

# Random Test Function

Example usage:

```
test(pairs(lists, lists)) {  
  (xs, ys) => (xs ++ ys).length > xs.length  
}
```

**Question:** Does the above property always hold?

- ☐ Yes
- ☒ No

# ScalaCheck

Shift in viewpoint: Instead of writing tests, write *properties* that are assumed to hold.

This idea is implemented in the ScalaCheck tool.

```
forAll { (l1: List[Int], l2: List[Int]) =>  
  l1.size + l2.size == (l1 ++ l2).size  
}
```

It can be used either stand-alone or as part of ScalaTest.