

Write Yourself a Scheme in 48 Hours

An Introduction to Haskell through Example

by Wikibooks contributors

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Overview

Most Haskell tutorials on the web seem to take a language-reference-manual approach to teaching. They show you the syntax of the language, a few language constructs, and then have you construct a few simple functions at the interactive prompt. The “hard stuff” of how to write a functioning, useful program is left to the end, or sometimes omitted entirely.

This tutorial takes a different tack. You’ll start off with command-line arguments and parsing, and progress to writing a fully-functional Scheme interpreter that implements a good-sized subset of [R5RS Scheme](#). Along the way, you’ll learn Haskell’s I/O, mutable state, dynamic typing, error handling, and parsing features. By the time you finish, you should be fairly fluent in both Haskell and Scheme.

There’re two main audiences targetted by this tutorial:

1. People who already know [Lisp](#) or [Scheme](#) and want to learn [Haskell](#)
2. People who don’t know any programming language, but have a strong quantitative background and are familiar with computers

The second group will likely find this challenging, as I gloss over several Scheme and general programming concepts to stay focused on the Haskell. A good textbook like *Structure and Interpretation of Computer Programs* or *The Little Schemer* may help a lot here.

Users of a procedural or object-oriented language like C, Java, or Python should beware, however: You’ll have to forget most of what you already know about programming. Haskell is completely different from those languages, and requires a different way of thinking about programming. It’s best to go into this tutorial with a blank slate and try not to compare Haskell to imperative languages, because many concepts in them (classes, functions, ‘return’) have a significantly different meaning in Haskell.

Since each lesson builds on the code written for the previous one, it’s probably best to go through the lessons in order.

This tutorial assumes that you’ll be using [GHC](#) as your Haskell compiler. It may work with eg. [Hugs](#), but it hasn’t been tested at all, and you may need to download additional libraries.

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Chapter 1

First Steps: Compiling and Running

First, you'll need to install GHC. On Linux, it's often pre-installed or available via apt-get or yum. It's also downloadable from <http://www.haskell.org/ghc/>. A binary package is probably easiest, unless you really know what you're doing. It should download and install like any other software package. This tutorial was developed on Linux, but everything should also work on Windows as long as you know how to use the DOS command line.

For UNIX (or [Windows Emacs](#)) users, there is a pretty good [Emacs mode](#), including syntax highlighting and automatic indentation. Windows users can use Notepad or any other text editor: Haskell syntax is fairly Notepad-friendly, though you have to be careful with the indentation. [Eclipse](#) users might want to try the [Function Programming](#) plug-in. Finally, there's also a [Haskell plugin for Visual Studio](#) using the GHC compiler.

Now, it's time for your first Haskell program. This program will read a name off the command line and then print a greeting. Create a file ending in `.hs` and type the following text:

Listing 1.1: Your first Haskell program (hello.hs)

```
module Main where
import System.Environment

main :: IO ()
5 main = do args <- getArgs
          putStrLn ("Hello, " ++ args !! 0)
```

Let's go through this code. The first two lines specify that we'll be creating a module named `Main` that imports the `System` module. Every Haskell program begins with an action called `main` in a module named `Main`. That module may import others, but it must be present for the compiler to generate an executable file. Haskell is case-sensitive: module names are always capitalized, declarations always uncapitalized.

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The line `main :: IO ()` is a type declaration: it says that the action `main` has type `IO ()`. Type declarations in Haskell are optional: the compiler figures them out automatically, and only complains if they differ from what you’ve specified. In this tutorial, I specify the types of all declarations explicitly, for clarity. If you’re following along at home, you may want to omit them, because it’s less to change as we build our program.

The `IO` type is an instance of something called a monad, which is a scary name for a not-so-scary concept. Basically, a monad is a way of saying “there’s some extra information attached to this value, which most functions don’t need to worry about.” In this example, the “extra information” is the fact that this action performs IO, and the basic value is nothing, represented as `()`. Monadic values are often called “actions,” because the easiest way to think about the `IO` monad is a sequencing of actions that each might affect the outside world.

Haskell is a declarative language: instead of giving the computer a sequence of instructions to carry out, you give it a collection of definitions that tell it how to perform every function it might need. These definitions use various compositions of actions and functions. The compiler figures out an execution path that puts everything together.

To write one of these definitions, you set it up as an equation. The left hand side defines a name, and optionally one or more patterns (explained later) that will bind variables. The right hand side defines some composition of other definitions that tells the computer what to do when it encounters the name. These equations behave just like ordinary equations in algebra: you can always substitute the right hand side for the left within the text of the program, and it’ll evaluate to the same value. Called *referential transparency*, this property makes it significantly easier to reason about Haskell programs than other languages.

How will we define our `main` action? We know that it must be an `IO` action, and that we want it to read the command line args and print some output. There are two ways to create an `IO` action:

1. Lift an ordinary value into the `IO` monad, using the `return` function.
2. Combine two existing `IO` actions.

Since we want to do two things, we’ll take the second approach. The built-in action `getArgs` reads the command-line arguments and stores them in a list of strings. The built-in function `putStrLn` takes a string and writes it to the console.

To combine them, we use a `do`-block. A `do`-block consists of a series of lines, all lined up with the first non-whitespace character after the `do`. Each line can have one of two forms:

1. `name <- action`
2. `action`

The first form takes the result of the `action` and binds it to `name`. For example, if the type of the action is `IO [String]` (an `IO` action returning a list

of strings, as with `getArgs`), then `name` will be bound to the list of strings returned. The second form just executes the action, sequencing it with the previous line through the `>>` (pronounced “bind”) operator. This operator has different semantics for each monad: in the case of the IO monad, it executes the actions sequentially, performing whatever external side-effects that result. Because the semantics of this composition depends upon the particular monad used, you cannot mix actions of different monad types in the same `do`-block.

Of course, these actions may themselves be the result of functions or complicated expressions. In this example, we first take index 0 of the argument list (`args !! 0`), concatenate it onto the end of the string “Hello, ” (`"Hello, "++`), and finally pass that to `putStrLn` for IO sequencing. `Strings` are lists of characters in Haskell, so you can use any of the list functions and operators on them. A full table of the standard operators and their precedences follows:

Table 1.1: Operators and their precedence

Operator(s)	Precedence	Associativity	Description
.	9	Right	Function composition
!!	9	Left	List indexing
[^] , ^{^^} , **	8	Right	Exponentiation (integer, fractional, and floating-point)
*, /	7	Left	Multiplication, Division
+, −	6	Left	Addition, Subtraction
:	5	Right	Cons (list construction)
++	5	Right	List Concatenation
<code>'elem'</code> , <code>'notElem'</code>	4	Left	List Membership
<code>==</code> , <code>/=</code> , <code><</code> , <code><=</code> , <code>>=</code> , <code>></code>	4	Left	Equals, Not-equals, and other relation operators
<code>&&</code>	3	Right	Logical And
<code> </code>	2	Right	Logical Or
<code>>></code> , <code>>>=</code>	1	Left	Monadic Bind, Monadic Bind (piping value to next function)
<code>=<<</code>	1	Right	Reverse Monadic Bind (same as above, but arguments reversed)
<code>\$</code>	0	Right	Infix Function Application (same as <code>f x</code> , but right-associative instead of left)

To compile and run the program, try something like this:

```
user>> ghc -o hello_you hello.hs
user>> ./hello_you Jonathan
Hello , Jonathan
```

The `-o` option specifies the name of the executable you want to create, and then you just specify the name of the Haskell source file.

Exercises

1. Change the program so it reads two arguments from the command line, and prints out a message using both of them.
2. Change the program so it performs a simple arithmetic operation on the two arguments and prints out the result. You can use **read** to convert a string to a number, and **show** to convert a number back into a string. Play around with different operations.
3. **getLine** is an IO action that reads a line from the console and returns it as a string. Change the program so it prompts for a name, reads the name, and then prints that instead of the command line value.

Chapter 2

Parsing

Writing a Simple Parser

Now, let's try writing a very simple parser. We'll be using the [Parsec](#) library, which comes with [GHC](#) but may need to be downloaded separately if you're using another compiler.

Start by adding this line to the import section:

```
3 import Text.ParserCombinators.Parsec hiding (spaces)
```

This makes the Parsec library functions available to us, except the `spaces` function, whose name conflicts with a function that we'll be defining later.

Now, we'll define a parser that recognizes one of the symbols allowed in Scheme identifiers:

```
9 symbol :: Parser Char
10 symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ~ # "
```

This is another example of a monad: in this case, the “extra information” that is being hidden is all the info about position in the input stream, backtracking record, first and follow sets, etc. Parsec takes care of all of that for us. We need only use the Parsec library function `oneOf`, and it'll recognize a single one of any of the characters in the string passed to it. Parsec provides a number of pre-built parsers: for example, `letter` and `digit` are library functions. And as you're about to see, you can compose primitive parsers into more sophisticated productions.

Let's define a function to call our parser and handle any possible errors:

```
12 readExpr :: String -> String
13 readExpr input = case parse symbol "lisp" input of
14     Left err -> "No match: " ++ show err
15     Right val -> "Found value"
```

As you can see from the type signature, `readExpr` is a function `(->)` from a `String` to a `String`. We name the parameter `input`, and pass it, along with

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the symbol action we defined above and the name of the parser (“lisp”), to the Parsec function `parse`.

`parse` can return either the parsed value or an error, so we need to handle the error case. Following typical Haskell convention, Parsec returns an `Either` data type, using the `Left` constructor to indicate an error and the `Right` one for a normal value.

We use a `case...of` construction to match the result of `parse` against these alternatives. If we get a `Left` value (error), then we bind the error itself to `err` and return “No match” with the string representation of the error. If we get a `Right` value, we bind it to `val`, ignore it, and return the string “Found value”.

The `case...of` construction is an example of pattern matching, which we will see in much greater detail later on.

Finally, we need to change our main function to call `readExpr` and print out the result:

```
5 main :: IO ()
6 main = do args <- getArgs
7         putStrLn (readExpr (args !! 0))
```

The complete code is therefore:

Listing 2.1: A simple parsing program (simpleparser1.hs)

```
module Main where
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)

5 main :: IO ()
  main = do args <- getArgs
           putStrLn (readExpr (args !! 0))

symbol :: Parser Char
10 symbol = oneOf " ! % & | * + - / : < = ? > @ ^ _ ~ # "

readExpr :: String -> String
readExpr input = case parse symbol "lisp" input of
  Left err -> "No match: " ++ show err
15  Right val -> "Found value"
```

To compile and run this, you need to specify `-package parsec` on the command line, or else there will be link errors. For example:

```
user>> ghc -package parsec -o simple-parser simpleparser1.hs
user>> ./simple_parser $
Found value
user>> ./simple_parser a
No match: "lisp" (line 1, column 1):
unexpected "a"
```

Whitespace

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Next, we’ll add a series of improvements to our parser that’ll let it recognize progressively more complicated expressions. The current parser chokes if there’s whitespace preceding our symbol:

```
user>> ./simple_parser " %"
No match: "lisp" (line 1, column 1):
unexpected " "
```

Let's fix that, so that we ignore whitespace.

First, let's define a parser that recognizes any number of whitespace characters. Incidentally, this is why we included the `hiding` (spaces) clause when we imported Parsec: there's already a function `spaces` in that library, but it doesn't quite do what we want it to. (For that matter, there's also a parser called `lexeme` that does exactly what we want, but we'll ignore that for pedagogical purposes.)

```
16 spaces :: Parser ()
17 spaces = skipMany1 space
```

Just as functions can be passed to functions, so can actions. Here we pass the Parser action `space` to the Parser action `skipMany1`, to get a Parser that will recognize one or more spaces.

Now, let's edit our parse function so that it uses this new parser. Changes are highlighted:

```
1 readExpr input = case parse (spaces >> symbol) "lisp" input of
2     Left err -> "No match: " ++ show err
3     Right val -> "Found value"
```

We touched briefly on the `>>` (“bind”) operator in lesson 2, where we mentioned that it was used behind the scenes to combine the lines of a `do`-block. Here, we use it explicitly to combine our whitespace and symbol parsers. However, `bind` has completely different semantics in the Parser and IO monads. In the Parser monad, `bind` means “Attempt to match the first parser, then attempt to match the second with the remaining input, and fail if either fails.” In general, `bind` will have wildly different effects in different monads; it's intended as a general way to structure computations, and so needs to be general enough to accommodate all the different types of computations. Read the documentation for the monad to figure out precisely what it does.

Listing 2.2: A simple parsing program, now ignoring whitespace (`simpleparser2.hs`)

```
module Main where
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)

5 main :: IO ()
  main = do args <- getArgs
           putStrLn (readExpr (args !! 0))

symbol :: Parser Char
10 symbol = oneOf " ! % & | * + - / : < = ? > @ ^ _ ~ # "

readExpr input = case parse (spaces >> symbol) "lisp" input of
    Left err -> "No match: " ++ show err
    Right val -> "Found value"

15 spaces :: Parser ()
  spaces = skipMany1 space
```

Compile and run this code. Note that since we defined `spaces` in terms of `skipMany1`, it will no longer recognize a plain old single character. Instead you have to precede a symbol with some whitespace. We'll see how this is useful shortly:

```
user>> ghc -package parsec -o simple_parser simpleparser2.hs
user>> ./simple_parser " %" Found value
user>> ./simple_parser %
No match: "lisp" (line 1, column 1):
unexpected "%"
expecting space
user>> ./simple_parser " abc"
No match: "lisp" (line 1, column 4):
unexpected "a"
expecting space
```

Return Values

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Right now, the parser doesn't do much of anything—it just tells us whether a given string can be recognized or not. Generally, we want something more out of our parsers: we want them to convert the input into a data structure that we can traverse easily. In this section, we learn how to define a data type, and how to modify our parser so that it returns this data type.

First, we need to define a data type that can hold any Lisp value:

```
21 data LispVal = Atom String
22             | List [LispVal]
23             | DottedList [LispVal] LispVal
24             | Number Integer
25             | String String
26             | Bool Bool
```

This is an example of an algebraic data type: it defines a set of possible values that a variable of type `LispVal` can hold. Each alternative (called a constructor and separated by `|`) contains a tag for the constructor along with the type of data that that constructor can hold. In this example, a `LispVal` can be:

1. An `Atom`, which stores a `String` naming the atom
2. A `List`, which stores a list of other `LispVals` (Haskell lists are denoted by brackets); also called a proper list
3. A `DottedList`, representing the Scheme form `(a b . c)`; also called an improper list. This stores a list of all elements but the last, and then stores the last element as another field
4. A `Number`, containing a Haskell `Integer`

5. A `String`, containing a Haskell `String`

6. A `Bool`, containing a Haskell boolean value

Constructors and types have different namespaces, so you can have both a constructor named `String` and a type named `String`. Both types and constructor tags always begin with capital letters.

Next, let's add a few more parsing functions to create values of these types. A string is a double quote mark, followed by any number of non-quote characters, followed by a closing quote mark:

```

28 parseString :: Parser LispVal
29 parseString = do char '"'
30                 x <- many (noneOf "\"")
31                 char '"'
32                 return $ String x

```

We're back to using the do-notation instead of the `>>` operator. This is because we'll be retrieving the value of our parse (returned by `many (noneOf "\"")`) and manipulating it, interleaving some other parse operations in the meantime. In general, use `>>` if the actions don't return a value, `>>=` if you'll be immediately passing that value into the next action, and do-notation otherwise.

Once we've finished the parse and have the Haskell `String` returned from `many`, we apply the `String` constructor (from our `LispVal` data type) to turn it into a `LispVal`. Every constructor in an algebraic data type also acts like a function that turns its arguments into a value of its type. It also serves as a pattern that can be used in the left-hand side of a pattern-matching expression.

We then apply the built-in function `return` to lift our `LispVal` into the `Parser` monad. Remember, each line of a do-block must have the same type, but the result of our `String` constructor is just a plain old `LispVal`. `Return` lets us wrap that up in a `Parser` action that consumes no input but returns it as the inner value. Thus, the whole `parseString` action will have type `Parser LispVal`.

The `$` operator is infix function application: it's the same as if we'd written `return (String x)`, but `$` is right-associative, letting us eliminate some parentheses. Since `$` is an operator, you can do anything with it that you'd normally do to a function: pass it around, partially apply it, etc. In this respect, it functions like the `Lisp` function `apply`.

Now let's move on to Scheme variables. An `atom` is a letter or symbol, followed by any number of letters, digits, or symbols:

```

34 parseAtom :: Parser LispVal
35 parseAtom = do first <- letter <|> symbol
36               rest <- many (letter <|> digit <|> symbol)
37               let atom = [first] ++ rest
38               return $ case atom of
39                   "#t" -> Bool True
40                   "#f" -> Bool False
41                   otherwise -> Atom atom

```

Here, we introduce another Parsec combinator, the choice operator `<|>`. This tries the first parser, then if it fails, tries the second. If either succeeds, then it returns the value returned by that parser. The first parser must fail before it consumes any input: we'll see later how to implement backtracking.

Once we've read the first character and the rest of the atom, we need to put them together. The `let` statement defines a new variable `atom`. We use the list concatenation operator `++` for this. Recall that `first` is just a single character, so we convert it into a singleton list by putting brackets around it. If we'd wanted to create a list containing many elements, we need only separate them by commas.

Then we use a case statement to determine which `LispVal` to create and return, matching against the literal strings for `true` and `false`. The otherwise alternative is a readability trick: it binds a variable named `otherwise`, whose value we ignore, and then always returns the value of `atom`.

Finally, we create one more parser, for numbers. This shows one more way of dealing with monadic values:

```
43 parseNumber :: Parser LispVal
44 parseNumber = liftM (Number . read) $ many1 digit
```

It's easiest to read this backwards, since both function application (`$`) and function composition (`.`) associate to the right. The parsec combinator `many1` matches one or more of its argument, so here we're matching one or more digits. We'd like to construct a number `LispVal` from the resulting string, but we have a few type mismatches. First, we use the built-in function `read` to convert that string into a number. Then we pass the result to `Number` to get a `LispVal`. The function composition operator `.` creates a function that applies its right argument and then passes the result to the left argument, so we use that to combine the two function applications.

Unfortunately, the result of `many1 digit` is actually a `Parser String`, so our combined `Number . read` still can't operate on it. We need a way to tell it to just operate on the value inside the monad, giving us back a `Parser LispVal`. The standard function `liftM` does exactly that, so we apply `liftM` to our `Number . read` function, and then apply the result of that to our parser.

We also have to import the `Monad` module up at the top of our program to get access to `liftM`:

```
2 import Monad
```

This style of programming—relying heavily on function composition, function application, and passing functions to functions—is very common in Haskell code. It often lets you express very complicated algorithms in a single line, breaking down intermediate steps into other functions that can be combined in various ways. Unfortunately, it means that you often have to read Haskell code from right-to-left and keep careful track of the types. We'll be seeing many more examples throughout the rest of the tutorial, so hopefully you'll get pretty comfortable with it.

Let's create a parser that accepts either a string, a number, or an atom:

```

45
46 parseExpr :: Parser LispVal
47 parseExpr = parseAtom
48     <|> parseString

```

And edit readExpr so it calls our new parser:

```

1 readExpr :: String -> String
2 readExpr input = case parse parseExpr "lisp" input of
3     Left err -> "No match: " ++ show err
4     Right _ -> "Found value"

```

The complete code is therefore:

Listing 2.3: A parser able to handle data types (datatypeparser.hs)

```

module Main where
import Monad
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)
5
main :: IO ()
main = do args <- getArgs
        putStrLn (readExpr (args !! 0))

10 symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ~ # "

readExpr :: String -> String
readExpr input = case parse parseExpr "lisp" input of
15     Left err -> "No match: " ++ show err
        Right val -> "Found value"

spaces :: Parser ()
spaces = skipMany1 space
20
data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
              | Number Integer
25     | String String
              | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
30     x <- many (noneOf "\"")
        char '"'
        return $ String x

parseAtom :: Parser LispVal
35 parseAtom = do first <- letter <|> symbol
        rest <- many (letter <|> digit <|> symbol)
        let atom = [first] ++ rest
        return $ case atom of
40             "#t" -> Bool True
             "#f" -> Bool False
             otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit
45
parseExpr :: Parser LispVal
parseExpr = parseAtom
        <|> parseString
        <|> parseNumber

```

Compile and run this code, and you'll notice that it accepts any number, string, or symbol, but not other strings:

```

user>> ghc -package parsec -o simple-parser datatypeparser.hs
user>> ./simple-parser "\"this is a string\""
Found value
user>> ./simple-parser 25
Found value
user>> ./simple-parser symbol
Found value
user>> ./simple-parser (symbol)
bash: syntax error near unexpected token `symbol'
user>> ./simple-parser "(symbol)"
No match: "lisp" (line 1, column 1):
unexpected "("
expecting letter, "\"" or digit

```

Exercises

1. Rewrite `parseNumber` using
 - (a) do-notation.
 - (b) explicit sequencing with the `>>=` operator.
2. Our strings aren't quite [R5RS compliant](#), because they don't support escaping of internal quotes within the string. Change `parseString` so that `\` gives a literal quote character instead of terminating the string. You may want to replace `noneOf "\""` with a new parser action that accepts either a non-quote character or a backslash followed by a quote mark.
3. Modify the previous exercise to support `\n`, `\r`, `\t`, `\\`, and any other desired escape characters.
4. Change `parseNumber` to support the [Scheme standard for different bases](#). You may find the [readOct](#) and [readHex](#) functions useful.
5. Add a `Character` constructor to `LispVal`, and create a parser for [character literals](#) as described in R5RS.
6. Add a `Float` constructor to `LispVal`, and support R5RS syntax for [decimals](#). The Haskell function [readFloat](#) may be useful.
7. Add data types and parsers to support the [full numeric tower](#) of Scheme numeric types. Haskell has built-in types to represent many of these; check the Prelude. For the others, you can define compound types that represent eg. a Rational as a numerator and denominator, or a Complex as a real and imaginary part (each itself a Real number).

Recursive Parsers: Adding lists, dotted lists, and quoted datums

[\[edit section\]](#)

Next, we add a few more parser actions to our interpreter. Start with the parenthesized lists that make Lisp famous:

```
46 parseList :: Parser LispVal
47 parseList = liftM List $ sepBy parseExpr spaces
```

This works analogously to `parseNumber`, first parsing a series of expressions separated by whitespace (`sepBy parseExpr spaces`) and then apply the `List` constructor to it within the Parser monad. Note too that we can pass `parseExpr` to `sepBy`, even though it's an action we wrote ourselves.

The dotted-list parser is somewhat more complex, but still uses only concepts that we're already familiar with:

```
49 parseDottedList :: Parser LispVal
50 parseDottedList = do
51   head <- endBy parseExpr spaces
52   tail <- char '.' >> spaces >> parseExpr
53   return $ DottedList head tail
```

Note how we can sequence together a series of Parser actions with `>>` and then use the whole sequence on the right hand side of a `do`-statement. The expression `char '.' >> spaces` returns a `Parser ()`, then combining that with `parseExpr` gives a `Parser LispVal`, exactly the type we need for the `do`-block.

Next, let's add support for the single-quote syntactic sugar of Scheme:

```
55 parseQuoted :: Parser LispVal
56 parseQuoted = do
57   char '\''
58   x <- parseExpr
59   return $ List [Atom "quote", x]
```

Most of this is fairly familiar stuff: it reads a single quote character, reads an expression and binds it to `x`, and then returns `(quote x)`, to use Scheme notation. The `Atom` constructor works like an ordinary function: you pass it the String you're encapsulating, and it gives you back a `LispVal`. You can do anything with this `LispVal` that you normally could, like put it in a list.

Finally, edit our definition of `parseExpr` to include our new parsers:

```
1  parseExpr :: Parser LispVal
2  parseExpr = parseAtom
3           <|> parseString
4           <|> parseNumber
5           <|> parseQuoted
6           <|> do char '('
7                x <- (try parseList) <|> parseDottedList
8                char ')'
9                return x
```

This illustrates one last feature of Parsec: backtracking. `parseList` and `parseDottedList` recognize identical strings up to the dot; this breaks the requirement that a choice alternative may not consume any input before failing. The `try` combinator attempts to run the specified parser, but if it fails, it backs up to the previous state. This lets you use it in a choice alternative without interfering with the other alternative.

The complete code is therefore:

Listing 2.4: A simple parser, now with Lisp list, dotted list and quoted datum parsing (recursiveparser.hs)

```

module Main where
import Monad
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)
5
main :: IO ()
main = do args <- getArgs
        putStrLn (readExpr (args !! 0))

10 symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ~ # "

readExpr input = case parse parseExpr "lisp" input of
    Left err -> "No match: " ++ show err
15    Right val -> "Found val"

spaces :: Parser ()
spaces = skipMany1 space

20 data LispVal = Atom String
                | List [LispVal]
                | DottedList [LispVal] LispVal
                | Number Integer
                | String String
25                | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
30                x <- many (noneOf "\"")
                char '"'
                return $ String x

parseAtom :: Parser LispVal
35 parseAtom = do first <- letter <|> symbol
                rest <- many (letter <|> digit <|> symbol)
                let atom = [first] ++ rest
                return $ case atom of
40                    "#t" -> Bool True
                    "#f" -> Bool False
                    otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit
45

parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
50 parseDottedList = do
    head <- endBy parseExpr spaces
    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

```

```

55 parseQuoted :: Parser LispVal
   parseQuoted = do
       char '\'',
       x <- parseExpr
       return $ List [Atom "quote", x]
60
   parseExpr :: Parser LispVal
   parseExpr = parseAtom
       <|> parseString
       <|> parseNumber
65       <|> parseQuoted
       <|> do char '('
           x <- (try parseList) <|> parseDottedList
           char ')'
           return x

```

Compile and run this code:

```

user>> ghc -package parsec -o simple_parser recursiveparser.hs
user>> ./simple_parser "(a test)"
Found value
user>> ./simple_parser "(a (nested) test)"
Found value
user>> ./simple_parser "(a (dotted . list) test)"
Found value
user>> ./simple_parser "(a '(quoted (dotted . list)) test)"
Found value
user>> ./simple_parser "(a '(imbalanced parens)"
No match: "lisp" (line 1, column 24):
unexpected end of input
expecting space or ")"

```

Note that by referring to `parseExpr` within our parsers, we can nest them arbitrarily deep. Thus, we get a full Lisp reader with only a few definitions. That's the power of recursion.

Exercises

1. Add support for the `backquote` syntactic sugar: the Scheme standard details what it should expand into (`quasiquote/unquote`).
2. Add support for `vectors`. The Haskell representation is up to you: GHC does have an `Array` data type, but it can be difficult to use. Strictly speaking, a vector should have constant-time indexing and updating, but destructive update in a purely functional language is difficult. You may have a better idea how to do this after the section on `set!`, later in this tutorial.
3. Instead of using the `try` combinator, left-factor the grammar so that the common subsequence is its own parser. You should end up with a parser that matches a string of expressions, and one that matches either nothing or a dot and a single expressions. Combining the return values of these into either a `List` or a `DottedList` is left as a (somewhat tricky) exercise for the reader: you may want to break it out into another helper function.

Chapter 3

Evaluation, Part 1

Beginning the Evaluator

Currently, we've just been printing out whether or not we recognize the given program fragment. We're about to take the first steps towards a working Scheme interpreter: assigning values to program fragments. We'll be starting with baby steps, but fairly soon you'll be progressing to doing working computations.

Let's start by telling Haskell how to print out a string representation of the various possible `LispVals`:

```
70 showVal :: LispVal -> String
71 showVal (String contents) = "\"" ++ contents ++ "\""
72 showVal (Atom name) = name
73 showVal (Number contents) = show contents
74 showVal (Bool True) = "#t"
75 showVal (Bool False) = "#f"
```

This is our first real introduction to pattern matching. Pattern matching is a way of destructuring an algebraic data type, selecting a code clause based on its constructor and then binding the components to variables. Any constructor can appear in a pattern; that pattern matches a value if the tag is the same as the value's tag and all subpatterns match their corresponding components. Patterns can be nested arbitrarily deep, with matching proceeding in an inside \rightarrow outside, left \rightarrow right order. The clauses of a function definition are tried in textual order, until one of the patterns matches. If this is confusing, you'll see some examples of deeply-nested patterns when we get further into the evaluator.

For now, you only need to know that each clause of the above definition matches one of the constructors of `LispVal`, and the right-hand side tells what to do for a value of that constructor.

The `List` and `DottedList` clauses work similarly, but we need to define a helper function `unwordsList` to convert the contained list into a string:

```
76 showVal (List contents) = "(" ++ unwordsList contents ++ ")"
```

- [live version](#)
- [discussion](#)
- [edit](#)
- [comment](#)
- [report an error](#)

[\[edit section\]](#)

```

77 showVal (DottedList head tail) = "(" ++ unwordsList head ++ "
    . " ++ showVal tail ++ ")"

```

The `unwordsList` function works like the Haskell Prelude’s `unwords` function, which glues together a list of words with spaces. Since we’re dealing with a list of `LispVals` instead of words, we define a function that first converts the `LispVals` into their string representations and then applies `unwords` to it:

```

79 unwordsList :: [LispVal] -> String
80 unwordsList = unwords . map showVal

```

Our definition of `unwordsList` doesn’t include any arguments. This is an example of point-free style: writing definitions purely in terms of function composition and partial application, without regard to individual values or “points.” Instead, we define it as the composition of a couple built-in functions. First, we partially-apply `map` to `showVal`, which creates a function that takes a list of `LispVals` and returns a list of their string representations. Haskell functions are curried: this means that a function of two arguments, like `map`, is really a function that returns a function of one argument. As a result, if you supply only a single argument, you get back a function one argument that you can pass around, compose, and apply later. In this case, we compose it with `unwords`: `map showVal` converts a list of `LispVals` to a list of their `String` representations, and then `unwords` joins the result together with spaces.

We used the function `show` above. This standard Haskell function lets you convert any type that’s an instance of the class `Show` into a string. We’d like to be able to do the same with `LispVal`, so we make it into a member of the class `Show`, defining its `show` method as `showVal`:

```

82 instance Show LispVal where show = showVal

```

A full treatment of typeclasses is beyond the scope of this tutorial; you can find more information in [other tutorials](#) and the [Haskell 98 report](#).

Let’s try things out by changing our `readExpr` function so it returns the string representation of the value actually parsed, instead of just `"Found value"`:

```

13 readExpr input = case parse parseExpr "lisp" input of
14     Left err -> "No match: " ++ show err
15     Right val -> "Found " ++ show val

```

The complete code is therefore:

Listing 3.1: A parser using pattern matching (evaluator1.hs)

```

module Main where
import Monad
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)
5
main :: IO ()
main = do args <- getArgs
        putStrLn (readExpr (args !! 0))
10
symbol :: Parser Char

```

```

symbol = oneOf "!$%&|*+~/<=>@^_~#"

readExpr input = case parse parseExpr "lisp" input of
    Left err -> "No match: " ++ show err
    Right val -> "Found " ++ show val
15
spaces :: Parser ()
spaces = skipMany1 space

20 data LispVal = Atom String
                | List [LispVal]
                | DottedList [LispVal] LispVal
                | Number Integer
                | String String
25                | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
                x <- many (noneOf "\"")
30                char '"'
                return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
                rest <- many (letter <|> digit <|> symbol)
35                let atom = [first] ++ rest
                return $ case atom of
                    "#t" -> Bool True
                    "#f" -> Bool False
40                    otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

45 parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
50     head <- endBy parseExpr spaces
     tail <- char '.' >> spaces >> parseExpr
     return $ DottedList head tail

parseQuoted :: Parser LispVal
55 parseQuoted = do
     char '\''
     x <- parseExpr
     return $ List [Atom "quote", x]

60 parseExpr :: Parser LispVal
parseExpr = parseAtom
        <|> parseString
        <|> parseNumber
        <|> parseQuoted
65        <|> do char '('
                x <- (try parseList) <|> parseDottedList
                char ')'
                return x

70 showVal :: LispVal -> String
showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
showVal (Bool True) = "#t"
75 showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"

```

```

unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal

instance Show LispVal where show = showVal

```

And compile and run...

```

user>> ghc -package parsec -o parser evaluator1.hs
user>> ./parser "(1 2 2)"
Found (1 2 2)
user>> ./parser "'(1 3 (\\"this\\" \\"one\\"))'"
Found (quote (1 3 ("this" "one")))

```

Beginnings of an Evaluator: Primitives

[\[edit section\]](#)

Now, we start with the beginnings of an evaluator. The purpose of an evaluator is to map some “code” data type into some “data” data type, the result of the evaluation. In Lisp, the data types for both code and data are the same, so our evaluator will return a `LispVal`. Other languages often have more complicated code structures, with a variety of syntactic forms.

Evaluating numbers, strings, booleans, and quoted lists is fairly simple: return the datum itself.

```

85 eval :: LispVal -> LispVal
86 eval val@(String _) = val
87 eval val@(Number _) = val
88 eval val@(Bool _) = val
89 eval (List [Atom "quote", val]) = val

```

This introduces a new type of pattern. The notation `val@(String _)` matches against any `LispVal` that’s a string and then binds `val` to the whole `LispVal`, and not just the contents of the `String` constructor. The result has type `LispVal` instead of type `String`. The underbar is the “don’t care” variable, matching any value yet not binding it to a variable. It can be used in any pattern, but is most useful with `@`-patterns (where you bind the variable to the whole pattern) and with simple constructor-tests where you’re just interested in the tag of the constructor.

The last clause is our first introduction to nested patterns. The type of data contained by `List` is `[LispVal]`, a list of `LispVals`. We match that against the specific two-element list `[Atom "quote", val]`, a list where the first element is the symbol `"quote"` and the second element can be anything. Then we return that second element.

Let’s integrate `eval` into our existing code. Start by changing `readExpr` back so it returns the expression instead of a string representation of the expression:

```

12 readExpr :: String -> LispVal
13 readExpr input = case parse parseExpr "lisp" input of
14     Left err -> String $ "No match: " ++ show err
15     Right val -> val

```

And then change our `main` function to read an expression, evaluate it, convert it to a string, and print it out. Now that we know about the `>>=` monad sequencing operator and the function composition operator, let's use them to make this a bit more concise:

```
6 main :: IO ()
7 main = getArgs >>= putStrLn . show . eval . readExpr . (!! 0)
```

Here, we take the result of the `getArgs` action (a list of `strings`) and pass it into the composition of:

1. Take the first value (`(!! 0)`). This notation is known as an operator section: it's telling the compiler to partially-apply the list indexing operator to 0, giving you back a function that takes the first element of whatever list it's passed.
2. Parse it (`readExpr`)
3. Evaluate it (`eval`)
4. Convert it to a string (`show`)
5. Print it (`putStrLn`)

The complete code is therefore:

Listing 3.2: The evaluator skeleton (evaluator2.hs)

```
module Main where
import Monad
import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)

5 main :: IO ()
  main = getArgs >>= putStrLn . show . eval . readExpr . (!! 0)

symbol :: Parser Char
10 symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ` # "

readExpr :: String -> LispVal
readExpr input = case parse parseExpr "lisp" input of
    Left err -> String $ "No match: " ++ show err
15    Right val -> val

spaces :: Parser ()
spaces = skipMany1 space

20 data LispVal = Atom String
                | List [LispVal]
                | DottedList [LispVal] LispVal
                | Number Integer
25                | String String
                | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
30                x <- many (noneOf "\"")
                char '"'
                return $ String x
```

```

35 parseAtom :: Parser LispVal
   parseAtom = do first <- letter <|> symbol
                  rest <- many (letter <|> digit <|> symbol)
                  let atom = [first] ++ rest
                  return $ case atom of
40                     "#t" -> Bool True
                     "#f" -> Bool False
                     otherwise -> Atom atom

   parseNumber :: Parser LispVal
   parseNumber = liftM (Number . read) $ many1 digit

45   parseList :: Parser LispVal
   parseList = liftM List $ sepBy parseExpr spaces

   parseDottedList :: Parser LispVal
50   parseDottedList = do
       head <- endBy parseExpr spaces
       tail <- char '.' >> spaces >> parseExpr
       return $ DottedList head tail

55   parseQuoted :: Parser LispVal
   parseQuoted = do
       char '\''
       x <- parseExpr
       return $ List [Atom "quote", x]

60   parseExpr :: Parser LispVal
   parseExpr = parseAtom
              <|> parseString
              <|> parseNumber
              <|> parseQuoted
65   <|> do char '('
           x <- (try parseList) <|> parseDottedList
           char ')'
           return x

70   showVal :: LispVal -> String
   showVal (String contents) = "\"" ++ contents ++ "\""
   showVal (Atom name) = name
   showVal (Number contents) = show contents
75   showVal (Bool True) = "#t"
   showVal (Bool False) = "#f"
   showVal (List contents) = "(" ++ unwordsList contents ++ ")"
   showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
       showVal tail ++ ")"

80   unwordsList :: [LispVal] -> String
   unwordsList = unwords . map showVal

   instance Show LispVal where show = showVal

85   eval :: LispVal -> LispVal
   eval val@(String _) = val
   eval val@(Number _) = val
   eval val@(Bool _) = val
   eval (List [Atom "quote", val]) = val

```

Compile and run the code the normal way:

```

user>> ghc -package parsec -o eval evaluator2.hs
user>> ./eval "'atom"
atom
user>> ./eval 2
2
user>> ./eval "\"a string\""

```

```
"a string"
user>> ./eval "(+ 2 2)"
```

```
Fail: eval.hs:83: Non-exhaustive patterns in function eval
```

We still can't do all that much useful with the program (witness the failed `(+ 2 2)` call), but the basic skeleton is in place. Soon, we'll be extending it with some functions to make it useful.

Adding Basic Primitives

[\[edit section\]](#)

Next, we'll improve our Scheme so we can use it as a simple calculator. It's still not yet a "programming language", but it's getting close.

Begin by adding a clause to `eval` to handle function application. Remember that all clauses of a function definition must be placed together and are evaluated in textual order, so this should go after the other `eval` clauses:

```
89 eval (List (Atom func : args)) = apply func $ map eval args
```

This is another nested pattern, but this time we match against the `cons` operator `:` instead of a literal list. Lists in Haskell are really syntactic sugar for a change of `cons` applications and the empty list: `[1, 2, 3, 4] = 1:(2:(3:(4:[])))`. By pattern-matching against `cons` itself instead of a literal list, we're saying "give me the rest of the list" instead of "give me the second element of the list." For example, if we passed `(+ 2 2)` to `eval`, `func` would be bound to `+` and `args` would be bound to `[Number 2, Number 2]`.

The rest of the clause consists of a couple functions we've seen before and one we haven't defined yet. We have to recursively evaluate each argument, so we map `eval` over the `args`. This is what lets us write compound expressions like `(+ 2 (- 3 1) (* 5 4))`. Then we take the resulting list of evaluated arguments, and pass it and the original function to `apply`:

```
91 apply :: String -> [LispVal] -> LispVal
92 apply func args = maybe (Bool False) ($ args) $ lookup func
    primitives
```

The built-in function `lookup` looks up a key (its first argument) in a list of pairs. However, `lookup` will fail if no pair in the list contains the matching key. To express this, it returns an instance of the built-in type `Maybe`. We use the function `maybe` to specify what to do in case of either success or failure. If the function isn't found, we return a `Bool False` value, equivalent to `#f` (we'll add more robust error-checking later). If it is found, we apply it to the arguments using `($ args)`, an operator section of the function application operator.

Next, we define the list of primitives that we support:

```
94 primitives :: [(String, [LispVal] -> LispVal)]
95 primitives = [( "+", numericBinop (+)),
96               ("-", numericBinop (-)),
97               ("*", numericBinop (*)),
```

```

98         ("/", numericBinop div) ,
99         ("mod", numericBinop mod) ,
100        ("quotient", numericBinop quot) ,
101        ("remainder", numericBinop rem)]

```

Look at the type of primitives. It is a list of pairs, just like lookup expects, but the values of the pairs are functions from `[LispVal]` to `LispVal`. In Haskell, you can easily store functions in other data structures, though the functions must all have the same type.

Also, the functions that we store are themselves the result of a function, `numericBinop`, which we haven't defined yet. This takes a primitive Haskell function (often an operator section) and wraps it with code to unpack an argument list, apply the function to it, and wrap the result up in our `Number` constructor.

```

103 numericBinop :: (Integer -> Integer -> Integer) -> [LispVal]
104               -> LispVal
105
106 numericBinop op params = Number $ foldl1 op $ map unpackNum
107                               params
108
109 unpackNum :: LispVal -> Integer
110 unpackNum (Number n) = n
111 unpackNum (String n) = let parsed = reads n in
112                           if null parsed
113                             then 0
114                             else fst $ parsed !! 0
115
116 unpackNum (List [n]) = unpackNum n
117 unpackNum _ = 0

```

As with R5RS Scheme, we don't limit ourselves to only two arguments. Our numeric operations can work on a list of any length, so $(+ 2 3 4) = 2 + 3 + 4$, and $(- 15 5 3 2) = 15 - 5 - 3 - 2$. We use the built-in function `foldl1` to do this. It essentially changes every cons operator in the list to the binary function we supply, `op`.

Unlike R5RS Scheme, we're implementing a form of weak typing. That means that if a value can be interpreted as a number (like the string "2"), we'll use it as one, even if it's tagged as a string. We do this by adding a couple extra clauses to `unpackNum`. If we're unpacking a string, attempt to parse it with Haskell's built-in `reads` function, which returns a list of pairs of (parsed value, original value).

For lists, we pattern-match against the one-element list and try to unpack that. Anything else falls through to the next case.

If we can't parse the number, for any reason, we'll return 0 for now. We'll fix this shortly so that it signals an error.

The complete code is therefore:

Listing 3.3: A basic evaluator (evaluator3.hs)

```

module Main where
import Monad

```



```

import System.Environment
import Text.ParserCombinators.Parsec hiding (spaces)

5
main :: IO ()
main = getArgs >=> putStrLn . show . eval . readExpr . (!! 0)

symbol :: Parser Char
10 symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ~ "

readExpr :: String -> LispVal
readExpr input = case parse parseExpr "lisp" input of
    Left err -> String $ "No match: " ++ show err
15    Right val -> val

spaces :: Parser ()
spaces = skipMany1 space

20 data LispVal = Atom String
                | List [LispVal]
                | DottedList [LispVal] LispVal
                | Number Integer
                | String String
25    | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
                x <- many (noneOf "\"")
                char '"'
30    return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
                rest <- many (letter <|> digit <|> symbol)
35    let atom = [first] ++ rest
    return $ case atom of
        "#t" -> Bool True
        "#f" -> Bool False
40    otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

45 parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
50    head <- endBy parseExpr spaces
    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

parseQuoted :: Parser LispVal
55 parseQuoted = do
    char '\''
    x <- parseExpr
    return $ List [Atom "quote", x]

60 parseExpr :: Parser LispVal
parseExpr = parseAtom
    <|> parseString
    <|> parseNumber
    <|> parseQuoted
65    <|> do char '('
            x <- (try parseList) <|> parseDottedList
            char ')'
            return x

70 showVal :: LispVal -> String

```

```

showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
showVal (Bool True) = "#t"
75 showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"

unwordsList :: [LispVal] -> String
80 unwordsList = unwords . map showVal

instance Show LispVal where show = showVal

eval :: LispVal -> LispVal
85 eval val@(String _) = val
eval val@(Number _) = val
eval val@(Bool _) = val
eval (List [Atom "quote", val]) = val
eval (List (Atom func : args)) = apply func $ map eval args
90
apply :: String -> [LispVal] -> LispVal
apply func args = maybe (Bool False) ($ args) $ lookup func primitives

primitives :: [(String, [LispVal] -> LispVal)]
95 primitives = [( "+", numericBinop (+)),
                  ("-", numericBinop (-)),
                  ("*", numericBinop (*)),
                  ("/", numericBinop div),
                  ("mod", numericBinop mod),
100                  ("quotient", numericBinop quot),
                  ("remainder", numericBinop rem)]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] -> LispVal
numericBinop op params = Number $ foldl1 op $ map unpackNum params
105
unpackNum :: LispVal -> Integer
unpackNum (Number n) = n
unpackNum (String n) = let parsed = reads n in
110                        if null parsed
                        then 0
                        else fst $ parsed !! 0
unpackNum (List [n]) = unpackNum n
unpackNum _ = 0

```

Compile and run this the normal way. Note how we get nested expressions “for free” because we call `eval` on each of the arguments of a function:

```

user>> ghc -package parsec -o eval neweval.hs
user>> ./eval "(+ 2 2)"
4
user>> ./eval "(+ 2 (-4 1))"
2
user>> ./eval "(+ 2 (- 4 1))"
5
user>> ./eval "(- (+ 4 6 3) 3 5 2)"
3

```

Exercises

1. Add primitives to perform the various [type-testing](#) functions of R5RS: `symbol?`, `string?`, `number?`, etc.
2. Change `unpackNum` so that it always returns 0 if the value is not a number, even if it's a string or list that could be parsed as a number.
3. Add the [symbol-handling functions](#) from R5RS. A symbol is what we've been calling an `Atom` in our data constructors.

Chapter 4

Error Checking and Exceptions

Currently, there are a variety of places within the code where we either ignore errors or silently assign “default” values like `\#f` or `0` that make no sense. Some languages - like Perl and PHP - get along fine with this approach. However, it often means that errors pass silently throughout the program until they become big problems, which means rather inconvenient debugging sessions for the programmer. We’d like to signal errors as soon as they happen and immediately break out of execution.

First, we need to `import Control.Monad.Error` to get access to Haskell’s built-in error functions:

```
4 import Control.Monad.Error
```

Then, we should define a data type to represent an error:

```
123 data LispError = NumArgs Integer [LispVal]
124                | TypeMismatch String LispVal
125                | Parser ParseError
126                | BadSpecialForm String LispVal
127                | NotFunction String String
128                | UnboundVar String String
129                | Default String
```

This is a few more constructors than we need at the moment, but we might as well foresee all the other things that can go wrong in the interpreter later. Next, we define how to print out the various types of errors and make `LispError` an instance of `Show`:

```
131 showError :: LispError -> String
132 showError (UnboundVar message varname) = message ++ ": " ++
    varname
133 showError (BadSpecialForm message form) = message ++ ": " ++
    show form
```

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```

134 showError (NotFunction message func) = message ++ ": " ++ show
    func
135 showError (NumArgs expected found) = "Expected " ++ show
    expected
136                                     ++ " args: found values " ++
    unwordsList found
137 showError (TypeMismatch expected found) = "Invalid type:
    expected " ++ expected
138                                     ++ ", found " ++ show
    found
139 showError (Parser parseErr) = "Parse error at " ++ show
    parseErr
140
141 instance Show LispError where show = showError

```

Our next step is to make our error type into an instance of `Error`. This is necessary for it to work with GHC's built-in error handling functions. Being an instance of `error` just means that it must provide functions to create an instance either from a previous error message or by itself:

```

143 instance Error LispError where
144     noMsg = Default "An error has occurred"
145     strMsg = Default

```

Then we define a type to represent functions that may throw a `LispError` or return a value. Remember how `parse` used an `Either` data type to represent exceptions? We take the same approach here:

```

147 type ThrowsError = Either LispError

```

Type constructors are curried just like functions, and can also be partially applied. A full type would be `Either LispError Integer` or `Either LispError LispVal`, but we want to say `ThrowsError LispVal` and so on. We only partially apply `Either` to `LispError`, creating a type constructor `ThrowsError` that we can use on any data type.

`Either` is yet another instance of a monad. In this case, the “extra information” being passed between `Either` actions is whether or not an error occurred. `Bind` applies its function if the `Either` action holds a normal value, or passes an error straight through without computation. This is how exceptions work in other languages, but because Haskell is lazily-evaluated, there's no need for a separate control-flow construct. If `bind` determines that a value is already an error, the function is never called.

The `Either` monad also provides two other functions besides the standard monadic ones:

1. `throwError`, which takes an `Error` value and lifts it into the `Left` (error) constructor of an `Either`
2. `catchError`, which takes an `Either` action and a function that turns an error into another `Either` action. If the action represents an error, it

applies the function, which you can use to eg. turn the error value into a normal one via return or re-throw as a different error.

In our program, we'll be converting all of our errors to their string representations and returning that as a normal value. Let's create a helper function to do that for us:

```
149 trapError action = catchError action (return . show)
```

The result of calling `trapError` is another `Either` action which will always have valid (`Right`) data. We still need to extract that data from the `Either` monad so it can be passed around to other functions:

```
151 extractValue :: ThrowsError a -> a
152 extractValue (Right val) = val
```

We purposely leave `extractValue` undefined for a `Left` constructor, because that represents a programmer error. We intend to use `extractValue` only after a `catchError`, so it's better to fail fast than to inject bad values into the rest of the program.

Now that we have all the basic infrastructure, it's time to start using our error-handling functions. Remember how our parser had previously just return a string saying `"No match"` on an error? Let's change it so that it wraps and throws the original `ParseError`:

```
16 readExpr :: String -> ThrowsError LispVal
17 readExpr input = case parse parseExpr "lisp" input of
18     Left err -> throwError $ Parser err
19     Right val -> return val
```

Here, we first wrap the original `ParseError` with the `LispError` constructor `Parser`, and then use the built-in function `throwError` to return that in our `ThrowsError` monad. Since `readExpr` now returns a monadic value, we also need to wrap the other case in a return function.

Next, we change the type signature of `eval` to return a monadic value, adjust the return values accordingly, and add a clause to throw an error if we encounter a pattern that we don't recognize:

```
88 eval :: LispVal -> ThrowsError LispVal
89 eval val@(String _) = return val
90 eval val@(Number _) = return val
91 eval val@(Bool _) = return val
92 eval (List [Atom "quote", val]) = return val
93 eval (List (Atom func : args)) = mapM eval args >>= apply func
94 eval badForm = throwError $ BadSpecialForm "Unrecognized
    special form" badForm
```

Since the function application clause calls `eval` (which now returns a monadic value) recursively, we need to change that clause. First, we had to change `map` to `mapM`, which maps a monadic function over a list of values, sequences the resulting actions together with `bind`, and then returns a list of the inner results.

Inside the `Error` monad, this sequencing performs all computations sequentially but throws an error value if any one of them fails—giving you `Right [results]` on success, or `Left error` on failure. Then, we used the monadic `bind` operation to pass the result into the partially applied `apply func`, again returning an error if either operation failed.

Next, we change `apply` itself so that it throws an error if it doesn't recognize the function:

```

96 apply :: String -> [LispVal] -> ThrowsError LispVal
97 apply func args = maybe (throwError $ NotFunction "
    Unrecognized primitive function args" func)
98                        ($ args)
99                        (lookup func primitives)

```

We didn't add a `return` statement to the function application `($ args)`. We're about to change the type of our primitives, so that the function returned from the lookup itself returns a `ThrowsError` action:

```

101 primitives :: [(String, [LispVal] -> ThrowsError LispVal)]

```

And, of course, we need to change the `numericBinop` function that implements these primitives so it throws an error if there's only one argument:

```

110 numericBinop :: (Integer -> Integer -> Integer) -> [LispVal]
    -> ThrowsError LispVal
111 numericBinop op singleVal@[_] = throwError $ NumArgs 2
    singleVal
112 numericBinop op params = mapM unpackNum params >>= return .
    Number . foldl1 op

```

We use an `at`-pattern to capture the single-value case because we want to include the actual value passed in for error-reporting purposes. Here, we're looking for a list of exactly one element, and we don't care what that element is. We also need to use `mapM` to sequence the results of `unpackNum`, because each individual call to `unpackNum` may fail with a `TypeMismatch`:

```

114 unpackNum :: LispVal -> ThrowsError Integer
115 unpackNum (Number n) = return n
116 unpackNum (String n) = let parsed = reads n in
117                        if null parsed
118                        then throwError $ TypeMismatch "
                            number" $ String n
119                        else return $ fst $ parsed !! 0
120 unpackNum (List [n]) = unpackNum n
121 unpackNum notNum = throwError $ TypeMismatch "number" notNum

```

Finally, we need to change our `main` function to use this whole big error monad. This can get a little complicated, because now we're dealing with two monads (`Error` and `IO`). As a result, we go back to `do`-notation, because it's nearly impossible to use point-free style when the result of one monad is nested inside another:


```

7  main :: IO ()
8  main = do
9      args <- getArgs
10     evaled <- return $ liftM show $ readExpr (args !! 0) >>=
        eval
11     putStrLn $ extractValue $ trapError evaled

```

Here's what this new function is doing:

1. args is the list of command-line arguments
2. evaled is the result of:
 - (a) taking first argument (`args !! 0`)
 - (b) parsing it (`readExpr`)
 - (c) passing it to `eval` (`>>= eval`; the bind operation has higher precedence than function application)
 - (d) calling `show` on it within the `Error` monad. Note also that the whole action has type `IO (Either LispError String)`, giving `evaled` type `Either LispError String`. It has to be, because our `trapError` function can only convert errors to strings, and that type must match the type of normal values
3. caught is the result of
 - (a) calling `trapError` on `evaled`, converting errors to their string representation.
 - (b) calling `extractValue` to get a `String` out of this `Either LispError String` action
 - (c) printing the results through `putStrLn`

The complete code is therefore:

Listing 4.1: Lisp parser with basic error-checking functionality (errorcheck.hs)

```

module Main where
import Monad
import System.Environment
import Control.Monad.Error
5 import Text.ParserCombinators.Parsec hiding (spaces)

main :: IO ()
main = do
    args <- getArgs
10    evaled <- return $ liftM show $ readExpr (args !! 0) >>= eval
        putStrLn $ extractValue $ trapError evaled

symbol :: Parser Char
symbol = oneOf " ! % & | * + - / : < = ? > @ ^ _ ` # "

15 readExpr :: String -> ThrowsError LispVal
readExpr input = case parse parseExpr "lisp" input of
    Left err -> throwError $ Parser err
    Right val -> return val

```

```

20 spaces :: Parser ()
   spaces = skipMany1 space

data LispVal = Atom String
25           | List [LispVal]
           | DottedList [LispVal] LispVal
           | Number Integer
           | String String
           | Bool Bool

30 parseString :: Parser LispVal
   parseString = do char '"'
                   x <- many (noneOf "\"")
                   char '"'
35                   return $ String x

   parseAtom :: Parser LispVal
   parseAtom = do first <- letter <|> symbol
                  rest <- many (letter <|> digit <|> symbol)
40                  let atom = [first] ++ rest
                  return $ case atom of
                           "#t" -> Bool True
                           "#f" -> Bool False
                           otherwise -> Atom atom

45   parseNumber :: Parser LispVal
   parseNumber = liftM (Number . read) $ many1 digit

   parseList :: Parser LispVal
50   parseList = liftM List $ sepBy parseExpr spaces

   parseDottedList :: Parser LispVal
   parseDottedList = do
75       head <- endBy parseExpr spaces
       tail <- char '.' >> spaces >> parseExpr
       return $ DottedList head tail

   parseQuoted :: Parser LispVal
   parseQuoted = do
60       char '\''
       x <- parseExpr
       return $ List [Atom "quote", x]

   parseExpr :: Parser LispVal
65   parseExpr = parseAtom
               <|> parseString
               <|> parseNumber
               <|> parseQuoted
               <|> do char '('
70                   x <- (try parseList) <|> parseDottedList
                   char ')'
                   return x

   showVal :: LispVal -> String
75   showVal (String contents) = "\"" ++ contents ++ "\""
   showVal (Atom name) = name
   showVal (Number contents) = show contents
   showVal (Bool True) = "#t"
   showVal (Bool False) = "#f"
80   showVal (List contents) = "(" ++ unwordsList contents ++ ")"
   showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
                                     showVal tail ++ ")"

   unwordsList :: [LispVal] -> String
   unwordsList = unwords . map showVal

85   instance Show LispVal where show = showVal

```

```

eval :: LispVal -> ThrowsError LispVal
eval val@(String _) = return val
90 eval val@(Number _) = return val
eval val@(Bool _) = return val
eval (List [Atom "quote", val]) = return val
eval (List (Atom func : args)) = mapM eval args >>= apply func
eval badForm = throwError $ BadSpecialForm "Unrecognized special form"
badForm

95
apply :: String -> [LispVal] -> ThrowsError LispVal
apply func args = maybe (throwError $ NotFunction "Unrecognized
    primitive function args" func)
    ($ args)
    (lookup func primitives)

100
primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [(("+", numericBinop (+)),
    ("-", numericBinop (-)),
    ("*", numericBinop (*)),
105    ("/", numericBinop div),
    ("mod", numericBinop mod),
    ("quotient", numericBinop quot),
    ("remainder", numericBinop rem)]

110 numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
    ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
numericBinop op params = mapM unpackNum params >>= return . Number .
    foldl1 op

unpackNum :: LispVal -> ThrowsError Integer
115 unpackNum (Number n) = return n
unpackNum (String n) = let parsed = reads n in
    if null parsed
    then throwError $ TypeMismatch "number" $
        String n
    else return $ fst $ parsed !! 0

120 unpackNum (List [n]) = unpackNum n
unpackNum notNum = throwError $ TypeMismatch "number" notNum

data LispError = NumArgs Integer [LispVal]
    | TypeMismatch String LispVal
125 | Parser ParseError
    | BadSpecialForm String LispVal
    | NotFunction String String
    | UnboundVar String String
    | Default String

130
showError :: LispError -> String
showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
showError (NotFunction message func) = message ++ ": " ++ show func
135 showError (NumArgs expected found) = "Expected " ++ show expected
    ++ " args: found values " ++
        unwordsList found
showError (TypeMismatch expected found) = "Invalid type: expected " ++
    expected
    ++ ", found " ++ show found
showError (Parser parseErr) = "Parse error at " ++ show parseErr

140
instance Show LispError where show = showError

instance Error LispError where
    noMsg = Default "An error has occurred"
145 strMsg = Default

type ThrowsError = Either LispError

```

```
150 trapError action = catchError action (return . show)
    extractValue :: ThrowsError a -> a
    extractValue (Right val) = val
```

Compile and run the new code, and try throwing it a couple errors:

```
user>> ghc -package parsec -o errorcheck errorcheck.hs
user>> ./errorcheck "(+ 2 \"two\")"
Invalid type: expected number, found "two"
user>> ./errorcheck "(+ 2)"
Expected 2 args: found values 2
Unrecognized primitive function args: "what?"
```

Some readers have reported that you need to add a `--make` flag to build this example, and presumably all further listings. This tells GHC to build a complete executable, searching out all dependencies listed in the import statements. The command above works on my system, but if it fails on yours, give `--make` a try.

Chapter 5

Evaluation, Part 2

Additional Primitives: Partial Application

Now that we can deal with type errors, bad arguments, and so on, we'll flesh out our primitive list so that it does something more than calculate. We'll add boolean operators, conditionals, and some basic string operations.

Start by adding the following into the list of primitives:

```
109         ("=", numBoolBinop (==)) ,
110         ("<", numBoolBinop (<)) ,
111         (">", numBoolBinop (>)) ,
112         ("/=", numBoolBinop (/=)) ,
113         (">=", numBoolBinop (>=)) ,
114         ("<=", numBoolBinop (<=)) ,
115         ("&&", boolBoolBinop (&&)) ,
116         ("||", boolBoolBinop (||)) ,
117         ("string=?", strBoolBinop (==)) ,
118         ("string?", strBoolBinop (>)) ,
119         ("string<=?", strBoolBinop (<=)) ,
120         ("string>=?", strBoolBinop (>=)) ]
```

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These depend on helper functions that we haven't written yet: `numBoolBinop` and `strBoolBinop`. Instead of taking a variable number of arguments and returning an integer, these both take exactly 2 arguments and return a boolean. They differ from each other only in the type of argument they expect, so let's factor the duplication into a generic `boolBinop` function that's parameterized by the `unpacker` function it applies to its arguments:

```
126 boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) ->
    [LispVal] -> ThrowsError LispVal
127 boolBinop unpacker op args = if length args /= 2
128                             then throwError $ NumArgs 2 args
129                             else do left <- unpacker $ args
    !! 0
```

```

130         right <- unpacker $ args
           !! 1
131     return $ Bool $ left 'op'
           right

```

Because each arg may throw a type mismatch, we have to unpack them sequentially, in a `do`-block (for the `Error` monad). We then apply the operation to the two arguments and wrap the result in the `Bool` constructor. Any function can be turned into an infix operator by wrapping it in backticks (`'op'`).

Also, take a look at the type signature. `boolBinop` takes two functions as its first two arguments: the first is used to unpack the arguments from `LispVals` to native Haskell types, and the second is the actual operation to perform. By parameterizing different parts of the behavior, you make the function more reusable.

Now we define three functions that specialize `boolBinop` with different unpackers:

```

133 numBoolBinop = boolBinop unpackNum
134 strBoolBinop = boolBinop unpackStr
135 boolBoolBinop = boolBinop unpackBool

```

We haven't told Haskell how to unpack strings from `LispVals` yet. This works similarly to `unpackNum`, pattern matching against the value and either returning it or throwing an error. Again, if passed a primitive value that could be interpreted as a string (such as a number or boolean), it will silently convert it to the string representation.

```

146 unpackStr :: LispVal -> ThrowsError String
147 unpackStr (String s) = return s
148 unpackStr (Number s) = return $ show s
149 unpackStr (Bool s) = return $ show s
150 unpackStr notString = throwError $ TypeMismatch "string"
    notString

```

And we use similar code to unpack booleans:

```

152 unpackBool :: LispVal -> ThrowsError Bool
153 unpackBool (Bool b) = return b
154 unpackBool notBool = throwError $ TypeMismatch "boolean"
    notBool

```

The complete code is therefore:

Listing 5.1: A simple parser, now with several primitive operators (operator-parser.hs)

```

module Main where
import Monad
import System.Environment
import Control.Monad.Error
5  import Text.ParserCombinators.Parsec hiding (spaces)

main :: IO ()
main = do

```

```

10     args <- getArgs
    evaled <- return $ liftM show $ readExpr (args !! 0) >>= eval
    putStrLn $ extractValue $ trapError evaled

symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ~ # "

15 readExpr :: String -> ThrowsError LispVal
readExpr input = case parse parseExpr "lisp" input of
    Left err -> throwError $ Parser err
    Right val -> return val

20 spaces :: Parser ()
spaces = skipMany1 space

data LispVal = Atom String
25             | List [LispVal]
             | DottedList [LispVal] LispVal
             | Number Integer
             | String String
             | Bool Bool

30 parseString :: Parser LispVal
parseString = do char '"'
    x <- many (noneOf "\"")
    char '"'
35     return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
    rest <- many (letter <|> digit <|> symbol)
40     let atom = [first] ++ rest
    return $ case atom of
        "#t" -> Bool True
        "#f" -> Bool False
        otherwise -> Atom atom

45 parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

parseList :: Parser LispVal
50 parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
    head <- endBy parseExpr spaces
55     tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

parseQuoted :: Parser LispVal
parseQuoted = do
60     char '\''
    x <- parseExpr
    return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
65 parseExpr = parseAtom
    <|> parseString
    <|> parseNumber
    <|> parseQuoted
    <|> do char '('
70         x <- (try parseList) <|> parseDottedList
        char ')'
        return x

showVal :: LispVal -> String
75 showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name

```

```

showVal (Number contents) = show contents
showVal (Bool True) = "#t"
showVal (Bool False) = "#f"
80 showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"

unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal
85
instance Show LispVal where show = showVal

eval :: LispVal -> ThrowsError LispVal
eval val@(String _) = return val
90 eval val@(Number _) = return val
eval val@(Bool _) = return val
eval (List [Atom "quote", val]) = return val
eval (List (Atom func : args)) = mapM eval args >>= apply func
eval badForm = throwError $ BadSpecialForm "Unrecognized special form"
    badForm
95
apply :: String -> [LispVal] -> ThrowsError LispVal
apply func args = maybe (throwError $ NotFunction "Unrecognized
    primitive function args" func)
    ($ args)
    (lookup func primitives)
100
primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [( "+", numericBinop (+)),
    ("-", numericBinop (-)),
    ("*", numericBinop (*)),
    105 ("/", numericBinop div),
    ("mod", numericBinop mod),
    ("quotient", numericBinop quot),
    ("remainder", numericBinop rem),
    ("=", numBoolBinop (==)),
    110("<", numBoolBinop (<)),
    (">", numBoolBinop (>)),
    ("/=", numBoolBinop (/=)),
    (">=", numBoolBinop (>=)),
    ("<=", numBoolBinop (<=)),
    115("&&", boolBoolBinop (&&)),
    ("||", boolBoolBinop (||)),
    ("string=?", strBoolBinop (==)),
    ("string?", strBoolBinop (>)),
    ("string<=?", strBoolBinop (<=)),
    120("string>=?", strBoolBinop (>=))]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
    ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
numericBinop op params = mapM unpackNum params >>= return . Number .
    foldl1 op
125
boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
    -> ThrowsError LispVal
boolBinop unpacker op args = if length args /= 2
    then throwError $ NumArgs 2 args
    else do left <- unpacker $ args !! 0
    right <- unpacker $ args !! 1
    return $ Bool $ left 'op' right
130

numBoolBinop = boolBinop unpackNum
strBoolBinop = boolBinop unpackStr
135 boolBoolBinop = boolBinop unpackBool

unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n

```



```

unpackNum (String n) = let parsed = reads n in
140   if null parsed
       then throwError $ TypeMismatch "number" $
           String n
       else return $ fst $ parsed !! 0
unpackNum (List [n]) = unpackNum n
unpackNum notNum = throwError $ TypeMismatch "number" notNum
145
unpackStr :: LispVal -> ThrowsError String
unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
unpackStr (Bool s) = return $ show s
150 unpackStr notString = throwError $ TypeMismatch "string" notString

unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
unpackBool notBool = throwError $ TypeMismatch "boolean" notBool
155
data LispError = NumArgs Integer [LispVal]
                | TypeMismatch String LispVal
                | Parser ParseError
                | BadSpecialForm String LispVal
160   | NotFunction String String
                | UnboundVar String String
                | Default String

showError :: LispError -> String
165 showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
showError (NotFunction message func) = message ++ ": " ++ show func
showError (NumArgs expected found) = "Expected " ++ show expected
                                     ++ " args: found values " ++
                                     unwordsList found
170 showError (TypeMismatch expected found) = "Invalid type: expected " ++
                                     expected
                                     ++ ", found " ++ show found
showError (Parser parseErr) = "Parse error at " ++ show parseErr

instance Show LispError where show = showError
175
instance Error LispError where
    noMsg = Default "An error has occurred"
    strMsg = Default

180 type ThrowsError = Either LispError

trapError action = catchError action (return . show)

extractValue :: ThrowsError a -> a
185 extractValue (Right val) = val

```

Let's compile and test this to make sure it's working, before we proceed to the next feature:

```

user>> ghc -package parsec -o simple-parser operatorparser.hs
user>> ./simple-parser "< 2 3"
#t
user>> ./simple-parser "> 2 3"
#f
user>> ./simple-parser ">= 3 3"
#t
user>> ./simple-parser "(string=? \"test\" \"test\")"
#t
user>> ./simple-parser "(string<? \"abc\" \"bba\")"

```

#t

Conditionals: Pattern Matching 2

[\[edit section\]](#)

Now, we'll proceed to adding an if-clause to our evaluator. As with standard Scheme, our evaluator considers `#f` to be false and any other value to be true:

```

93 eval (List [Atom "if", pred, conseq, alt]) =
94     do result <- eval pred
95     case result of
96         Bool False -> eval alt
97         otherwise -> eval conseq

```

This is another example of nested pattern-matching. Here, we're looking for a 4-element list. The first element must be the atom `if`. The others can be any Scheme forms. We take the first element, evaluate, and if it's false, evaluate the alternative. Otherwise, we evaluate the consequent.

Compile and run this, and you'll be able to play around with conditionals:

```

user>> ghc -package parsec -o simple_parser conditionalparser.
        hs
user>> ./simple_parser "(if (> 2 3) \"no\" \"yes\")"
"yes"
user>> ./simple_parser "(if (= 3 3) (+ 2 3 (- 5 1)) \"unequal
        \")"
9

```

List Primitives: car, cdr, and cons

[\[edit section\]](#)

For good measure, let's also add in the basic list-handling primitives. Because we've chosen to represent our lists as Haskell algebraic data types instead of pairs, these are somewhat more complicated than their definitions in many Lisps. It's easiest to think of them in terms of their effect on printed S-expressions:

1. $(\text{car } (a \ b \ c)) = a$
2. $(\text{car } (a)) = a$
3. $(\text{car } (a \ b \ . \ c)) = a$
4. $(\text{car } a) = \text{error (not a list)}$
5. $(\text{car } a \ b) = \text{error (car takes only one argument)}$

We can translate these fairly straightforwardly into pattern clauses, recalling that $(x : xs)$ divides a list into the first element and the rest:

```

167 car :: [LispVal] -> ThrowsError LispVal
168 car [List (x : xs)] = return x
169 car [DottedList (x : xs) _] = return x
170 car [badArg] = throwError $ TypeMismatch "pair" badArg
171 car badArgList = throwError $ NumArgs 1 badArgList

```

Let's do the same with `cdr`:

1. $(\text{cdr } (a \ b \ c)) = (b \ c)$
2. $(\text{cdr } (a \ b)) = (b)$
3. $(\text{cdr } (a)) = \text{NIL}$
4. $(\text{cdr } (a \ b \ . \ c)) = (b \ . \ c)$
5. $(\text{cdr } (a \ . \ b)) = b$
6. $(\text{cdr } a) = \text{error (not list)}$
7. $(\text{cdr } a \ b) = \text{error (too many args)}$

We can represent the first 3 cases with a single clause. Our parser represents `()` as `List []`, and when you pattern-match $(x : xs)$ against `[x]`, `xs` is bound to `[]`. The other ones translate to separate clauses:

```

173 cdr :: [LispVal] -> ThrowsError LispVal
174 cdr [List (x : xs)] = return $ List xs
175 cdr [DottedList (_ : xs) x] = return $ DottedList xs x
176 cdr [DottedList [xs] x] = return x
177 cdr [badArg] = throwError $ TypeMismatch "pair" badArg
178 cdr badArgList = throwError $ NumArgs 1 badArgList

```

`Cons` is a little tricky, enough that we should go through each clause case-by-case. If you cons together anything with `Nil`, you end up with a one-item list, the `Nil` serving as a terminator:

```

180 cons :: [LispVal] -> ThrowsError LispVal
181 cons [x1, List []] = return $ List [x1]

```

If you cons together anything and a list, it's like tacking that anything onto the front of the list:

```

182 cons [x, List xs] = return $ List $ [x] ++ xs

```

However, if the list is a `DottedList`, then it should stay a `DottedList`, taking into account the improper tail:

```

183 cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs
    ) xlast

```

If you cons together two non-lists, or put a list in front, you get a `DottedList`. This is because such a cons cell isn't terminated by the normal `Nil` that most lists are.

```
184 cons [x1, x2] = return $ DottedList [x1] x2
```

Finally, attempting to cons together more or less than 2 arguments is an error:

```
185 cons badArgList = throwError $ NumArgs 2 badArgList
```

Our last step is to implement `eqv?`. Scheme offers 3 levels of equivalence predicates: `eq?`, `eqv?`, and `equal?`. For our purposes, `eq?` and `eqv?` are basically the same: they recognize two items as the same if they print the same, and are fairly slow. So we can write one function for both of them and register it under `eq?` and `eqv?`.

```
187 eqv :: [LispVal] -> ThrowsError LispVal
188 eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
189 eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 ==
    arg2
190 eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 ==
    arg2
191 eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
192 eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++
    [x], List $ ys ++ [y]]
193 eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1
    == length arg2) &&
194                                     (and $ map
                                         eqvPair
                                         $ zip
                                         arg1
                                         arg2)

195     where eqvPair (x1, x2) = case eqv [x1, x2] of
196                               Left err -> False
197                               Right (Bool val) -> val
198 eqv [-, -] = return $ Bool False
199 eqv badArgList = throwError $ NumArgs 2 badArgList
```

Most of these clauses are self-explanatory, the exception being the one for two `Lists`. This, after checking to make sure the lists are the same length, zips the two lists of pairs, runs `eqvPair` on them to test if each corresponding pair is equal, and then uses the function `and` to return false if any of the resulting values is false. `eqvPair` is an example of a local definition: it is defined using the `where` keyword, just like a normal function, but is available only within that particular clause of `eqv`.

The complete code is therefore:

Listing 5.2: A parser able to handle lists (listparser.hs)

```
module Main where
import Monad
import System.Environment
import Control.Monad.Error
5 import Text.ParserCombinators.Parsec hiding (spaces)
```

```

main :: IO ()
main = do
  args <- getArgs
  10   evald <- return $ liftM show $ readExpr (args !! 0) >>= eval
      putStrLn $ extractValue $ trapError evald

symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ` # "

15
readExpr :: String -> ThrowsError LispVal
readExpr input = case parse parseExpr "lisp" input of
  Left err -> throwError $ Parser err
  Right val -> return val

20
spaces :: Parser ()
spaces = skipMany1 space

data LispVal = Atom String
25             | List [LispVal]
              | DottedList [LispVal] LispVal
              | Number Integer
              | String String
              | Bool Bool

30
parseString :: Parser LispVal
parseString = do char '"'
  x <- many (noneOf "\"")
  char '"'
  35   return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
  rest <- many (letter <|> digit <|> symbol)
  40   let atom = [first] ++ rest
      return $ case atom of
        "#t" -> Bool True
        "#f" -> Bool False
        otherwise -> Atom atom

45
parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

parseList :: Parser LispVal
50 parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
  head <- endBy parseExpr spaces
  55   tail <- char '.' >> spaces >> parseExpr
  return $ DottedList head tail

parseQuoted :: Parser LispVal
parseQuoted = do
  60   char '\''
  x <- parseExpr
  return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
65 parseExpr = parseAtom
  <|> parseString
  <|> parseNumber
  <|> parseQuoted
  <|> do char '('
  70       x <- (try parseList) <|> parseDottedList
       char ')'
       return x

showVal :: LispVal -> String

```

```

75 showVal (String contents) = "\"" ++ contents ++ "\""
   showVal (Atom name) = name
   showVal (Number contents) = show contents
   showVal (Bool True) = "#t"
   showVal (Bool False) = "#f"
80 showVal (List contents) = "(" ++ unwordsList contents ++ ")"
   showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
       showVal tail ++ ")"

unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal

85 instance Show LispVal where show = showVal

eval :: LispVal -> ThrowsError LispVal
eval val@(String _) = return val
90 eval val@(Number _) = return val
   eval val@(Bool _) = return val
   eval (List [Atom "quote", val]) = return val
   eval (List [Atom "if", pred, conseq, alt]) =
       do result <- eval pred
95         case result of
            Bool False -> eval alt
            otherwise -> eval conseq
   eval (List (Atom func : args)) = mapM eval args >>= apply func
   eval badForm = throwError $ BadSpecialForm "Unrecognized special form"
   badForm

100 apply :: String -> [LispVal] -> ThrowsError LispVal
   apply func args = maybe (throwError $ NotFunction "Unrecognized
       primitive function args" func)
       ($ args)
       (lookup func primitives)

105 primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
   primitives = [("+", numericBinop (+)),
       ("-", numericBinop (-)),
       ("*", numericBinop (*)),
       ("/", numericBinop div),
110       ("mod", numericBinop mod),
       ("quotient", numericBinop quot),
       ("remainder", numericBinop rem),
       ("=", numBoolBinop (==)),
      ("<", numBoolBinop (<)),
115      (">", numBoolBinop (>)),
       ("<=", numBoolBinop (<=)),
       (">=", numBoolBinop (>=)),
       ("<=", numBoolBinop (<=)),
       ("&&", boolBoolBinop (&&)),
120       ("||", boolBoolBinop (||)),
       ("string=?", strBoolBinop (==)),
       ("string?", strBoolBinop (>)),
       ("string<=?", strBoolBinop (<=)),
       ("string>=?", strBoolBinop (>=)),
125       ("car", car),
       ("cdr", cdr),
       ("cons", cons),
       ("eq?", eqv),
130       ("eqv?", eqv)]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
   ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
135 numericBinop op params = mapM unpackNum params >>= return . Number .
   foldl1 op

```

```

boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
            -> ThrowsError LispVal
boolBinop unpacker op args = if length args /= 2
                              then throwError $ NumArgs 2 args
140      else do left <- unpacker $ args !! 0
                right <- unpacker $ args !! 1
                return $ Bool $ left `op` right

numBoolBinop = boolBinop unpackNum
145 strBoolBinop = boolBinop unpackStr
    boolBoolBinop = boolBinop unpackBool

unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
150 unpackNum (String n) = let parsed = reads n in
                          if null parsed
                          then throwError $ TypeMismatch "number" $
                              String n
                          else return $ fst $ parsed !! 0

unpackNum (List [n]) = unpackNum n
155 unpackNum notNum = throwError $ TypeMismatch "number" notNum

unpackStr :: LispVal -> ThrowsError String
unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
160 unpackStr (Bool s) = return $ show s
    unpackStr notString = throwError $ TypeMismatch "string" notString

unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
165 unpackBool notBool = throwError $ TypeMismatch "boolean" notBool

car :: [LispVal] -> ThrowsError LispVal
car [List (x : xs)] = return x
car [DottedList (x : xs) _] = return x
170 car [badArg] = throwError $ TypeMismatch "pair" badArg
    car badArgList = throwError $ NumArgs 1 badArgList

cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
175 cdr [DottedList (_ : xs) x] = return $ DottedList xs x
    cdr [DottedList [xs] x] = return x
    cdr [badArg] = throwError $ TypeMismatch "pair" badArg
    cdr badArgList = throwError $ NumArgs 1 badArgList

180 cons :: [LispVal] -> ThrowsError LispVal
cons [x1, List []] = return $ List [x1]
cons [x, List xs] = return $ List $ [x] ++ xs
cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs) xlast
cons [x1, x2] = return $ DottedList [x1] x2
185 cons badArgList = throwError $ NumArgs 2 badArgList

eqv :: [LispVal] -> ThrowsError LispVal
eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 == arg2
190 eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 == arg2
eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++ [x], List
    $ ys ++ [y]]
eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1 == length
    arg2) &&
                                (and $ map eqvPair $
                                    zip arg1 arg2)
195 where eqvPair (x1, x2) = case eqv [x1, x2] of
                                Left err -> False
                                Right (Bool val) -> val

eqv [-, _] = return $ Bool False
eqv badArgList = throwError $ NumArgs 2 badArgList

```

```

200 data LispError = NumArgs Integer [LispVal]
                | TypeMismatch String LispVal
                | Parser ParseError
                | BadSpecialForm String LispVal
205 | NotFunction String String
                | UnboundVar String String
                | Default String

showError :: LispError -> String
210 showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
showError (NotFunction message func) = message ++ ": " ++ show func
showError (NumArgs expected found) = "Expected " ++ show expected
                                   ++ " args: found values " ++
                                   unwordsList found
215 showError (TypeMismatch expected found) = "Invalid type: expected " ++
expected
                                   ++ ", found " ++ show found
showError (Parser parseErr) = "Parse error at " ++ show parseErr

instance Show LispError where show = showError
220 instance Error LispError where
    noMsg = Default "An error has occurred"
    strMsg = Default

225 type ThrowsError = Either LispError

trapError action = catchError action (return . show)

extractValue :: ThrowsError a -> a
230 extractValue (Right val) = val

```

Compile and run to try out the new list functions:

```

user>> ghc -package parsec -o eqv listparser.hs
user>> ./eqv "(car '(2 3 4))"
2
user>> ./eqv "(cdr '(2 3 4))"
(3 4)
user>> ./eqv "(car (cdr (cons 2 '(3 4))))"
3

```

Equal? and Weak Typing: Heterogenous Lists

[\[edit section\]](#)

Since we introduced weak typing above, we'd also like to introduce an `equal?` function that ignores differences in the type tags and only tests if two values can be interpreted the same. For example, `(eqv? 2 "2") = #f`, yet we'd like `(equal? 2 "2") = #t`. Basically, we want to try all of our unpack functions, and if any of them result in Haskell values that are equal, return true.

The obvious way to approach this is to store the unpacking functions in a list and use `mapM` to execute them in turn. Unfortunately, this doesn't work, because standard Haskell only lets you put objects in a list if they're the same type. The various unpacker functions return different types, so you can't store them in the same list.

We'll get around this by using a GHC extension—Existential Types—that lets us create a heterogenous list, subject to typeclass constraints. Extensions are fairly common in the Haskell world: they're basically necessary to create any reasonably large program, and they're often compatible between implementations (existential types work in both Hugs and GHC and are a candidate for standardization).

The first thing we need to do is define a data type that can hold any function from a `LispVal` \rightarrow `something`, provided that that “something” supports equality:

```
201 data Unpacker = forall a. Eq a => AnyUnpacker (LispVal ->
    ThrowsError a)
```

This is like any normal algebraic datatype, except for the type constraint. It says, “For any type that is an instance of `Eq`, you can define an `Unpacker` that takes a function from `LispVal` to that type, and may throw an error.” We'll have to wrap our functions with the `AnyUnpacker` constructor, but then we can create a list of `Unpackers` that does just what we want it.

Rather than jump straight to the `equal?` function, let's first define a helper function that takes an `Unpacker` and then determines if two `LispVals` are equal when it unpacks them:

```
203 unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError
    Bool
204 unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
205     do unpacked1 <- unpacker arg1
206        unpacked2 <- unpacker arg2
207        return $ unpacked1 == unpacked2
208     'catchError' (const $ return False)
```

After pattern-matching to retrieve the actual function, we enter a `do`-block for the `ThrowsError` monad. This retrieves the Haskell values of the two `LispVals`, and then tests whether they're equal. If there is an error anywhere within the two unpackers, it returns false, using the `const` function because `catchError` expects a function to apply to the error value.

Finally, we can define `equal?` in terms of these helpers:

```
210 equal :: [LispVal] -> ThrowsError LispVal
211 equal [arg1, arg2] = do
212     primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2
213                                     )
214                                     [AnyUnpacker unpackNum, AnyUnpacker
215                                     unpackStr, AnyUnpacker unpackBool]
216     eqvEquals <- eqv [arg1, arg2]
217     return $ Bool $ (primitiveEquals || let (Bool x) =
218                                     eqvEquals in x)
219 equal badArgList = throwError $ NumArgs 2 badArgList
```

The first action makes a heterogenous list of `[unpackNum, unpackStr, unpackBool]`, and then maps the partially-applied `(unpackEquals arg1 arg2)` over it. This

gives a list of `Bools`, so we use the `Prelude` function `or` to return true if any single one of them is true.

The second action tests the two arguments with `eqv?`. Since we want `equal?` to be looser than `eqv?`, it should return true whenever `eqv?` does so. This also lets us avoid handling cases like the list or dotted-list (though this introduces a bug; see exercise #2 in this section).

Finally, `equal?` `ors` both of these values together and wraps the result in the `Bool` constructor, returning a `LispVal`. The `let (Bool x) = eqvEquals in x` is a quick way of extracting a value from an algebraic type: it pattern matches `Bool x` against the `eqvEquals` value, and then returns `x`. The result of a `let`-expression is the expression following the keyword `in`.

To use these functions, insert them into our primitives list:

```

126         ("car", car),
127         ("cdr", cdr),
128         ("cons", cons),
129         ("eq?", eqv),
130         ("eqv?", eqv),
131         ("equal?", equal)]

1         ("car", car),
2         ("cdr", cdr),
3         ("cons", cons),
4         ("eq?", eqv),
5         ("eqv?", eqv),
6         ("equal?", equal)

```

Listing 5.3: A parser able to compare values of different types (equalparser.hs)

```

module Main where
import Monad
import System.Environment
import Control.Monad.Error
5 import Text.ParserCombinators.Parsec hiding (spaces)

main :: IO ()
main = do
    args <- getArgs
10    evaled <- return $ liftM show $ readExpr (args !! 0) >>= eval
    putStrLn $ extractValue $ trapError evaled

symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = ? > @ ^ _ ` # "
15
readExpr :: String -> ThrowsError LispVal
readExpr input = case parse parseExpr "lisp" input of
    Left err -> throwError $ Parser err
    Right val -> return val
20
spaces :: Parser ()
spaces = skipMany1 space

data LispVal = Atom String
25         | List [LispVal]
        | DottedList [LispVal] LispVal
        | Number Integer
        | String String

```

```

| Bool Bool
30 parseString :: Parser LispVal
parseString = do char '"'
                x <- many (noneOf "\\")
                char '"'
35                return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
                rest <- many (letter <|> digit <|> symbol)
40                let atom = [first] ++ rest
                return $ case atom of
                    "#t" -> Bool True
                    "#f" -> Bool False
                    otherwise -> Atom atom
45
parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

parseList :: Parser LispVal
50 parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
    head <- endBy parseExpr spaces
55    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

parseQuoted :: Parser LispVal
parseQuoted = do
60    char '\''
    x <- parseExpr
    return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
65 parseExpr = parseAtom
                <|> parseString
                <|> parseNumber
                <|> parseQuoted
                <|> do char '('
70                    x <- (try parseList) <|> parseDottedList
                    char ')'
                    return x

showVal :: LispVal -> String
75 showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
showVal (Bool True) = "#t"
showVal (Bool False) = "#f"
80 showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"

unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal
85
instance Show LispVal where show = showVal

eval :: LispVal -> ThrowsError LispVal
eval val@(String _) = return val
90 eval val@(Number _) = return val
eval val@(Bool _) = return val
eval (List [Atom "quote", val]) = return val
eval (List [Atom "if", pred, consequ, alt]) =
    do result <- eval pred
95    case result of

```

```

    Bool False -> eval alt
    otherwise -> eval conseq
eval (List (Atom func : args)) = mapM eval args >>= apply func
eval badForm = throwError $ BadSpecialForm "Unrecognized special form"
    badForm
100
apply :: String -> [LispVal] -> ThrowsError LispVal
apply func args = maybe (throwError $ NotFunction "Unrecognized
    primitive function args" func)
    ($ args)
    (lookup func primitives)
105
primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [( "+", numericBinop (+)),
    ("-", numericBinop (-)),
    ("*", numericBinop (*)),
    ("/", numericBinop div),
110    ("mod", numericBinop mod),
    ("quotient", numericBinop quot),
    ("remainder", numericBinop rem),
    ("=", numBoolBinop (==)),
    ("<", numBoolBinop (<)),
115    (">", numBoolBinop (>)),
    ("/=", numBoolBinop (/=)),
    (">=", numBoolBinop (>=)),
    ("<=", numBoolBinop (<=)),
    ("&&", boolBoolBinop (&&)),
120    ("||", boolBoolBinop (||)),
    ("string=?", strBoolBinop (==)),
    ("string?", strBoolBinop (>)),
    ("string<=?", strBoolBinop (<=)),
125    ("string>=?", strBoolBinop (>=)),
    ("car", car),
    ("cdr", cdr),
    ("cons", cons),
    ("eq?", eqv),
130    ("eqv?", eqv),
    ("equal?", equal)]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
    ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
135 numericBinop op params = mapM unpackNum params >>= return . Number .
    foldl1 op

boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
    -> ThrowsError LispVal
boolBinop unpacker op args = if length args /= 2
    then throwError $ NumArgs 2 args
140    else do left <- unpacker $ args !! 0
        right <- unpacker $ args !! 1
        return $ Bool $ left `op` right

numBoolBinop = boolBinop unpackNum
strBoolBinop = boolBinop unpackStr
boolBoolBinop = boolBinop unpackBool

unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
150 unpackNum (String n) = let parsed = reads n in
    if null parsed
    then throwError $ TypeMismatch "number" $
        String n
    else return $ fst $ parsed !! 0
unpackNum (List [n]) = unpackNum n
155 unpackNum notNum = throwError $ TypeMismatch "number" notNum

unpackStr :: LispVal -> ThrowsError String

```

```

unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
160 unpackStr (Bool s) = return $ show s
    unpackStr notString = throwError $ TypeMismatch "string" notString

unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
165 unpackBool notBool = throwError $ TypeMismatch "boolean" notBool

car :: [LispVal] -> ThrowsError LispVal
car [List (x : xs)] = return x
car [DottedList (x : xs) -] = return x
170 car [badArg] = throwError $ TypeMismatch "pair" badArg
    car badArgList = throwError $ NumArgs 1 badArgList

cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
175 cdr [DottedList (- : xs) x] = return $ DottedList xs x
    cdr [DottedList [xs] x] = return x
    cdr [badArg] = throwError $ TypeMismatch "pair" badArg
    cdr badArgList = throwError $ NumArgs 1 badArgList

180 cons :: [LispVal] -> ThrowsError LispVal
    cons [x1, List []] = return $ List [x1]
    cons [x, List xs] = return $ List $ [x] ++ xs
    cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs) xlast
    cons [x1, x2] = return $ DottedList [x1] x2
185 cons badArgList = throwError $ NumArgs 2 badArgList

eqv :: [LispVal] -> ThrowsError LispVal
eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 == arg2
190 eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 == arg2
    eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
    eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++ [x], List
        $ ys ++ [y]]
    eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1 == length
        arg2) &&
        (and $ map eqvPair $ zip arg1 arg2)
195     where eqvPair (x1, x2) = case eqv [x1, x2] of
        Left err -> False
        Right (Bool val) -> val

eqv [-, -] = return $ Bool False
eqv badArgList = throwError $ NumArgs 2 badArgList
200
data Unpacker = forall a. Eq a => AnyUnpacker (LispVal -> ThrowsError a)

unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError Bool
unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
205     do unpacked1 <- unpacker arg1
        unpacked2 <- unpacker arg2
        return $ unpacked1 == unpacked2
    'catchError' (const $ return False)

210 equal :: [LispVal] -> ThrowsError LispVal
    equal [arg1, arg2] = do
        primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2)
            [AnyUnpacker unpackNum, AnyUnpacker unpackStr,
             AnyUnpacker unpackBool]
        eqvEquals <- eqv [arg1, arg2]
215     return $ Bool $ (primitiveEquals || let (Bool x) = eqvEquals in x)
    equal badArgList = throwError $ NumArgs 2 badArgList

data LispError = NumArgs Integer [LispVal]
    | TypeMismatch String LispVal
    | Parser ParseError
    | BadSpecialForm String LispVal
220

```

```

| NotFunction String String
| UnboundVar String String
| Default String
225
showError :: LispError -> String
showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
showError (NotFunction message func) = message ++ ": " ++ show func
230 showError (NumArgs expected found) = "Expected " ++ show expected
    ++ " args: found values " ++
        unwordsList found
showError (TypeMismatch expected found) = "Invalid type: expected " ++
    expected
    ++ ", found " ++ show found
showError (Parser parseErr) = "Parse error at " ++ show parseErr
235
instance Show LispError where show = showError

instance Error LispError where
    noMsg = Default "An error has occurred"
240    strMsg = Default

type ThrowsError = Either LispError

trapError action = catchError action (return . show)

245 extractValue :: ThrowsError a -> a
extractValue (Right val) = val

```

To compile this code, you need to enable GHC extensions with `-fglasgow-exts`:

```

user>> ghc -package parsec -fglasgow-exts -o parser
    equalparser.hs
user>> ./simple_parser "(cdr '(a simple test))"
    (simple test)
user>> ./simple_parser "(car (cdr '(a simple test)))"
    simple
user>> ./simple_parser "(car '((this is) a test))"
    (this is)
user>> ./simple_parser "(cons '(this is) 'test)"
    ((this is) . test)
user>> ./simple_parser "(cons '(this is) '())"
    ((this is))
user>> ./simple_parser "(eqv? 1 3)" #f
user>> ./simple_parser "(eqv? 3 3)"
    #t
user>> ./simple_parser "(eqv? 'atom 'atom)"
    #t

```

Exercises

1. Instead of treating any non-`false` value as true, change the definition of `if` so that the predicate accepts only `Bool` values and throws an error on any others.
2. `equal?` has a bug in that a list of values is compared using `eqv?` instead of `equal?`. For example, `(equal? '(1 "2") '(1 2)) = #f`, while you'd

expect it to be true. Change `equal?` so that it continues to ignore types as it recurses into list structures. You can either do this explicitly, following the example in `eqv?`, or factor the list clause into a separate helper function that is parameterized by the equality testing function.

3. Implement `cond` and `case` expressions.
4. Add the rest of the `string functions`. You don't yet know enough to do `string-set!`; this is difficult to implement in Haskell, but you'll have enough information after the next two sections.

Chapter 6

Building a REPL: Basic I/O

So far, we've been content to evaluate single expressions from the command line, printing the result and exiting afterwards. This is fine for a calculator, but isn't what most people think of as "programming." We'd like to be able to define new functions and variables, and refer to them later. But before we can do this, we need to build a system that can execute multiple statements without exiting the program.

Instead of executing a whole program at once, we're going to build a read-eval-print loop. This reads in expressions from the console one at a time and executes them interactively, printing the result after each expression. Later expressions can reference variables set by earlier ones (or will be able to, after the next section), letting you build up libraries of functions.

First, we need to import some additional [IO functions](#). Add the following to the top of the program:

```
6 import IO hiding (try)
```

We have to hide the `try` function (used in the `IO` module for exception handling) because we use Parsec's `try` function.

Next, we define a couple helper functions to simplify some of our IO tasks. We'll want a function that prints out a string and immediately flushes the stream; otherwise, output might sit in output buffers and the user will never see prompts or results.

```
251 flushStr :: String -> IO ()
252 flushStr str = putStr str >> hFlush stdout
```

Then, we create a function that prints out a prompt and reads in a line of input:

```
254 readPrompt :: String -> IO String
255 readPrompt prompt = flushStr prompt >> getLine
```

Pull the code to parse and evaluate a string and trap the errors out of main into its own function:

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```

257 evalString :: String -> IO String
258 evalString expr = return $ extractValue $ trapError (liftM
    show $ readExpr expr >=> eval)

```

And write a function that evaluates a string and prints the result:

```

260 evalAndPrint :: String -> IO ()
261 evalAndPrint expr = evalString expr >=> putStrLn

```

Now it's time to tie it all together. We want to read input, perform a function, and print the output, all in an infinite loop. The built-in function `interact` almost does what we want, but doesn't loop. If we used the combination sequence `. repeat . interact`, we'd get an infinite loop, but we wouldn't be able to break out of it. So we need to roll our own loop:

```

263 until_ :: Monad m => (a -> Bool) -> m a -> (a -> m ()) -> m ()
264 until_ pred prompt action = do
265     result <- prompt
266     if pred result
267         then return ()
268         else action result >> until_ pred prompt action

```

The underscore after the name is a typical naming convention in Haskell for monadic functions that repeat but do not return a value. `until_` takes a predicate that signals when to stop, an action to perform before the test, and a function-returning-an-action to do to the input. Each of the latter two is generalized over any monad, not just `IO`. That's why we write their types using the type variable `m`, and include the type constraint `Monad m =>`.

Note also that we can write recursive actions just as we write recursive functions.

Now that we have all the machinery in place, we can write our REPL easily:

```

270 runRepl :: IO ()
271 runRepl = until_ (== "quit") (readPrompt "Lisp>>> ")
    evalAndPrint

```

And change our main function so it either executes a single expression, or enters the REPL and continues evaluating expressions until we type `"quit"`:

```

8  main :: IO ()
9  main = do args <- getArgs
10         case length args of
11             0 -> runRepl
12             1 -> evalAndPrint $ args !! 0
13             otherwise -> putStrLn "Program takes only 0 or 1
    argument"

```

The complete code is therefore:

Listing 6.1: A parser implementing the REPL method (replparser.hs)

```

module Main where
import Monad
import System.Environment

```

```

import Control.Monad.Error
5 import Text.ParserCombinators.Parsec hiding (spaces)
import IO hiding (try)

main :: IO ()
main = do args <- getArgs
10     case length args of
        0 -> runRepl
        1 -> evalAndPrint $ args !! 0
        otherwise -> putStrLn "Program takes only 0 or 1 argument"

15 symbol :: Parser Char
symbol = oneOf "!$%&|*+-/:<=>@^_`#"

readExpr :: String -> ThrowsError LispVal
readExpr input = case parse parseExpr "lisp" input of
20     Left err -> throwError $ Parser err
     Right val -> return val

spaces :: Parser ()
spaces = skipMany1 space
25

data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
              | Number Integer
30              | String String
              | Bool Bool

parseString :: Parser LispVal
parseString = do char '"'
35             x <- many (noneOf "\"")
             char '"'
             return $ String x

parseAtom :: Parser LispVal
40 parseAtom = do first <- letter <|> symbol
                 rest <- many (letter <|> digit <|> symbol)
                 let atom = [first] ++ rest
                 return $ case atom of
45                     "#t" -> Bool True
                     "#f" -> Bool False
                     otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit
50

parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
55 parseDottedList = do
    head <- endBy parseExpr spaces
    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

60 parseQuoted :: Parser LispVal
parseQuoted = do
    char '\''
    x <- parseExpr
65     return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
parseExpr = parseAtom
    <|> parseString
    <|> parseNumber
    <|> parseQuoted
70     <|> do char '('

```

```

x <- (try parseList) <|> parseDottedList
char ')',
return x
75
showVal :: LispVal -> String
showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
80 showVal (Bool True) = "#t"
showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"

85 unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal

instance Show LispVal where show = showVal

90 eval :: LispVal -> ThrowsError LispVal
eval val@(String _) = return val
eval val@(Number _) = return val
eval val@(Bool _) = return val
eval (List [Atom "quote", val]) = return val
95 eval (List [Atom "if", pred, consequ, alt]) =
    do result <- eval pred
    case result of
        Bool False -> eval alt
        otherwise -> eval consequ
100 eval (List (Atom func : args)) = mapM eval args >>= apply func
eval badForm = throwError $ BadSpecialForm "Unrecognized special form"
    badForm

apply :: String -> [LispVal] -> ThrowsError LispVal
apply func args = maybe (throwError $ NotFunction "Unrecognized
    primitive function args" func)
105     ($ args)
    (lookup func primitives)

primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [( "+", numericBinop (+)),
110     ("-", numericBinop (-)),
    ("*", numericBinop (*)),
    ("/", numericBinop div),
    ("mod", numericBinop mod),
    ("quotient", numericBinop quot),
115     ("remainder", numericBinop rem),
    ("=", numBoolBinop (==)),
   ("<", numBoolBinop (<)),
   (">", numBoolBinop (>)),
    ("/=", numBoolBinop (/=)),
   (">=", numBoolBinop (>=)),
120    ("<=", numBoolBinop (<=)),
   ("&&", boolBoolBinop (&&)),
    ("||", boolBoolBinop (||)),
    ("string=?", strBoolBinop (==)),
    ("string?", strBoolBinop (>)),
125     ("string<=?", strBoolBinop (<=)),
    ("string>=?", strBoolBinop (>=)),
    ("car", car),
    ("cdr", cdr),
130     ("cons", cons),
    ("eq?", eqv),
    ("eqv?", eqv),
    ("equal?", equal)]

135 numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
    ThrowsError LispVal

```

```

numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
numericBinop op params = mapM unpackNum params >>= return . Number .
    foldl1 op

boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
    -> ThrowsError LispVal
140 boolBinop unpacker op args = if length args /= 2
    then throwError $ NumArgs 2 args
    else do left <- unpacker $ args !! 0
    right <- unpacker $ args !! 1
    return $ Bool $ left 'op' right

145
numBoolBinop = boolBinop unpackNum
strBoolBinop = boolBinop unpackStr
boolBoolBinop = boolBinop unpackBool

150 unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
unpackNum (String n) = let parsed = reads n in
    if null parsed
    then throwError $ TypeMismatch "number" $
        String n
    else return $ fst $ parsed !! 0
155
unpackNum (List [n]) = unpackNum n
unpackNum notNum = throwError $ TypeMismatch "number" notNum

unpackStr :: LispVal -> ThrowsError String
160 unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
unpackStr (Bool s) = return $ show s
unpackStr notString = throwError $ TypeMismatch "string" notString

165 unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
unpackBool notBool = throwError $ TypeMismatch "boolean" notBool

car :: [LispVal] -> ThrowsError LispVal
170 car [List (x : xs)] = return x
car [DottedList (x : xs) -] = return x
car [badArg] = throwError $ TypeMismatch "pair" badArg
car badArgList = throwError $ NumArgs 1 badArgList

175 cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
cdr [DottedList (- : xs) x] = return $ DottedList xs x
cdr [DottedList [xs] x] = return x
cdr [badArg] = throwError $ TypeMismatch "pair" badArg
180 cdr badArgList = throwError $ NumArgs 1 badArgList

cons :: [LispVal] -> ThrowsError LispVal
cons [x1, List []] = return $ List [x1]
cons [x, List xs] = return $ List $ [x] ++ xs
185 cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs) xlast
cons [x1, x2] = return $ DottedList [x1] x2
cons badArgList = throwError $ NumArgs 2 badArgList

eqv :: [LispVal] -> ThrowsError LispVal
190 eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 == arg2
eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 == arg2
eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++ [x], List
    $ ys ++ [y]]
195 eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1 == length
    arg2) &&
    (and $ map eqvPair $
        zip arg1 arg2)

where eqvPair (x1, x2) = case eqv [x1, x2] of

```

```

                                Left err -> False
                                Right (Bool val) -> val
200 eqv [-, -] = return $ Bool False
    eqv badArgList = throwError $ NumArgs 2 badArgList

    data Unpacker = forall a. Eq a => AnyUnpacker (LispVal -> ThrowsError a)

205 unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError Bool
    unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
        do unpacked1 <- unpacker arg1
           unpacked2 <- unpacker arg2
           return $ unpacked1 == unpacked2
210 'catchError' (const $ return False)

    equal :: [LispVal] -> ThrowsError LispVal
    equal [arg1, arg2] = do
        primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2)
215 [AnyUnpacker unpackNum, AnyUnpacker unpackStr,
        AnyUnpacker unpackBool]
        eqvEquals <- eqv [arg1, arg2]
        return $ Bool $ (primitiveEquals || let (Bool x) = eqvEquals in x)
    equal badArgList = throwError $ NumArgs 2 badArgList

220 data LispError = NumArgs Integer [LispVal]
                | TypeMismatch String LispVal
                | Parser ParseError
                | BadSpecialForm String LispVal
                | NotFunction String String
225 | UnboundVar String String
                | Default String

    showError :: LispError -> String
    showError (UnboundVar message varname) = message ++ ": " ++ varname
    showError (BadSpecialForm message form) = message ++ ": " ++ show form
230 showError (NotFunction message func) = message ++ ": " ++ show func
    showError (NumArgs expected found) = "Expected " ++ show expected
        ++ " args: found values " ++
            unwordsList found
    showError (TypeMismatch expected found) = "Invalid type: expected " ++
        expected
235 ++ ", found " ++ show found
    showError (Parser parseErr) = "Parse error at " ++ show parseErr

    instance Show LispError where show = showError

240 instance Error LispError where
    noMsg = Default "An error has occurred"
    strMsg = Default

    type ThrowsError = Either LispError

245 trapError action = catchError action (return . show)

    extractValue :: ThrowsError a -> a
    extractValue (Right val) = val

250 flushStr :: String -> IO ()
    flushStr str = putStr str >> hFlush stdout

    readPrompt :: String -> IO String
255 readPrompt prompt = flushStr prompt >> getLine

    evalString :: String -> IO String
    evalString expr = return $ extractValue $ trapError (liftM show $
        readExpr expr >=> eval)

260 evalAndPrint :: String -> IO ()
    evalAndPrint expr = evalString expr >=> putStrLn

```

```

until_ :: Monad m => (a -> Bool) -> m a -> (a -> m ()) -> m ()
until_ pred prompt action = do
265   result <- prompt
      if pred result
      then return ()
      else action result >> until_ pred prompt action
270 runRepl :: IO ()
runRepl = until_ (== "quit") (readPrompt "Lisp>>> ") evalAndPrint

```

Compile and run the program, and try it out:

```

user>> ghc -package parsec -fglasgow-exts -o lisp realparser.
hs
user>> ./lisp
Lisp>>> (+ 2 3)
5
Lisp>>> (cons this '())
Unrecognized special form: this
Lisp>>> (cons 2 3)
(2 . 3)
Lisp>>> (cons 'this '())
(this)
Lisp>>> quit
user>>

```


Chapter 7

Adding Variables and Assignment: Mutable State in Haskell

Finally, we get to the good stuff: variables. A variable lets us save the result of an expression and refer to it later. In Scheme, a variable can also be reset to new values, so that its value changes as the program executes. This presents a complication for Haskell, because the execution model is built upon functions that return values, but never change them.

Nevertheless, there are several ways to simulate state in Haskell, all involving monads. The simplest is probably the `State monad`, which lets you hide arbitrary state within the monad and pass it around behind the scenes. You specify the state type as a parameter to the monad (eg. if a function returns an integer but modifies a list of string pairs, it would have type `State [(String, String)] Integer`), and access it via the `get` and `put` functions, usually within a `do`-block. You'd specify the initial state via the `runState myStateAction initialState`, which returns a pair containing the return value and the final state.

Unfortunately, the `state` monad doesn't work well for us, because the type of data we need to store is fairly complex. For a simple top-level environment, we could get away with `[(String, LispVal)]`, storing mappings from variable names to values. However, when we start dealing with function calls, these mappings become a stack of nested environments, arbitrarily deep. And when we add closures, environments might get saved in an arbitrary `Function` value, and passed around throughout the program. In fact, they might be saved in a variable and passed out of the `runState` monad entirely, something we're not allowed to do.

Instead, we use a feature called state threads, letting Haskell manage the aggregate state for us. This lets us treat mutable variables as we would in any other programming language, using functions to get or set variables. There are two flavors of state threads: the `ST monad` creates a stateful computation that

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can be executed as a unit, without the state escaping to the rest of the program. The `IORef` module lets you use stateful variables within the `IO` monad. Since our state has to be interleaved with `IO` anyway (it persists between lines in the REPL, and we will eventually have `IO` functions within the language itself), we'll be using `IORefs`.

We can start out by importing `Data.IORef` and defining a type for our environments:

```
5  import Data.IORef
282 type Env = IORef [(String, IORef LispVal)]
```

This declares an `Env` as an `IORef` holding a list that maps `Strings` to mutable `LispVals`. We need `IORefs` for both the list itself and for individual values because there are two ways that the program can mutate the environment. It might use `set!` to change the value of an individual variable, a change visible to any function that shares that environment (Scheme allows nested scopes, so a variable in an outer scope is visible to all inner scopes). Or it might use `define` to add a new variable, which should be visible on all subsequent statements.

Since `IORefs` can only be used within the `IO` monad, we'll want a helper action to create an empty environment. We can't just use the empty list `[]` because all accesses to `IORefs` must be sequenced, and so the type of our null environment is `IO Env` instead of just plain `Env`:

```
284 nullEnv :: IO Env
285 nullEnv = newIORef []
```

From here, things get a bit more complicated, because we'll be simultaneously dealing with two monads. Remember, we also need an `Error` monad to handle things like unbound variables. The parts that need `IO` functionality and the parts that may throw exceptions are interleaved, so we can't just catch all the exceptions and return only normal values to the `IO` monad.

Haskell provides a mechanism known as monad transformers that lets you combine the functionality of multiple monads. We'll be using one of these—`ErrorT`—which lets us layer error-handling functionality on top of the `IO` monad. Our first step is create a type synonym for our combined monad:

```
287 type IOThrowsError = ErrorT LispError IO
```

Like `IOThrows`, `IOThrowsError` is really a type constructor: we've left off the last argument, the return type of the function. However, `ErrorT` takes one more argument than plain old `Either`: we have to specify the type of monad that we're layering our error-handling functionality over. We've created a monad that may contain `IO` actions that throw a `LispError`.

We have a mix of `IOThrows` and `IOThrowsError` functions, but actions of different types cannot be contained within the same `do`-block, even if they provide essentially the same functionality. Haskell already provides a mechanism—`lifting`—to bring values of the lower type (`IO`) into the combined monad. Unfortunately, there's no similar support to bring a value of the untransformed upper type into the combined monad, so we need to write it ourselves:

```

289 liftThrows :: ThrowsError a -> IOThrowsError a
290 liftThrows (Left err) = throwError err
291 liftThrows (Right val) = return val

```

This deconstructs the `Either` type and either re-throws the error type or returns the ordinary value. Methods in typeclasses resolve based on the type of the expression, so `throwError` and `return` (members of `MonadError` and `Monad`, respectively) take on their `IOThrowsError` definitions. Incidentally, the type signature provided here is not fully general: if we'd left it off, the compiler would have inferred `liftThrows :: MonadError m => Either e a -> m e`.

We'll also want a helper function to run the whole top-level `IOThrowsError` action, returning an `IO` action. We can't escape from the `IO` monad, because a function that performs IO has an effect on the outside world, and you don't want that in a lazily-evaluated pure function. But you can run the error computation and catch the errors.

```

293 runIOThrows :: IOThrowsError String -> IO String
294 runIOThrows action = runErrorT (trapError action) >>= return .
    extractValue

```

This uses our previously-defined `trapError` function to take any error values and convert them to their string representations, then runs the whole computation via `runErrorT`. The result is passed into `extractValue` and returned as a value in the `IO` monad.

Now we're ready to return to environment handling. We'll start with a function to determine if a given variable is already bound in the environment, necessary for proper handling of `define`:

```

296 isBound :: Env -> String -> IO Bool
297 isBound envRef var = readIORef envRef >>= return . maybe False
    (const True) . lookup var

```

This first extracts the actual environment value from its `IORef` via `readIORef`. Then we pass it to `lookup` to search for the particular variable we're interested in. `lookup` returns a `Maybe` value, so we return `False` if that value was `Nothing` and `True` otherwise (we need to use the `const` function because `maybe` expects a function to perform on the result and not just a value). Finally, we use `return` to lift that value into the `IO` monad. Since we're just interested in a true/false value, we don't need to deal with the actual `IORef` that `lookup` returns.

Next, we'll want to define a function to retrieve the current value of a variable:

```

299 getVar :: Env -> String -> IOThrowsError LispVal
300 getVar envRef var = do env <- liftIO $ readIORef envRef
301                      maybe (throwError $ UnboundVar "
302                          Getting an unbound variable" var)
303                          (liftIO . readIORef)
304                          (lookup var env)

```

Like the previous function, this begins by retrieving the actual environment from the `IORef`. However, `getVar` uses the `IOThrowsError` monad, because it

also needs to do some error handling. As a result, we need to use the `liftIO` function to lift the `readIORef` action into the combined monad. Similarly, when we return the value, we use `liftIO . readIORef` to generate an `IOThrowsError` action that reads the returned `IORef`. We don't need to use `liftIO` to throw an error, however, because `throwError` is defined for the `MonadError` typeclass, of which `ErrorT` is an instance.

Now we create a function to set values:

```

305 setVar :: Env -> String -> LispVal -> IOThrowsError LispVal
306 setVar envRef var value = do env <- liftIO $ readIORef envRef
307                             maybe (throwError $ UnboundVar "
                                Setting an unbound variable"
                                var)
308                             (liftIO . (flip writeIORef
                                value))
309                             (lookup var env)
310                             return value

```

Again, we first read the environment out of its `IORef` and run a lookup on it. This time, however, we want to change the variable instead of just reading it. The `writeIORef` action provides a means for this, but takes its arguments in the wrong order (`ref -> value` instead of `value -> ref`). So we use the built-in function `flip` to switch the arguments of `writeIORef` around, and then pass it the value. Finally, we return the value we just set, for convenience.

We'll want a function to handle the special behavior of `define`, which sets a variable if already bound or creates a new one if not. Since we've already defined a function to set values, we can use it in the former case:

```

312 defineVar :: Env -> String -> LispVal -> IOThrowsError LispVal
313 defineVar envRef var value = do
314     alreadyDefined <- liftIO $ isBound envRef var
315     if alreadyDefined
316     then setVar envRef var value >> return value
317     else liftIO $ do
318         valueRef <- newIORef value
319         env <- readIORef envRef
320         writeIORef envRef ((var, valueRef) : env)
321         return value

```

It's the latter case that's interesting, where the variable is unbound. We create an IO action (via `do`-notation) that creates a new `IORef` to hold the new variable, reads the current value of the environment, then writes a new list back to that variable consisting of the new (`key`, `variable`) pair added to the front of the list. Then we lift that whole `do`-block into the `IOThrowsError` monad with `liftIO`.

There's one more useful environment function: being able to bind a whole bunch of variables at once, like what would happen at function invocation. We might as well build that functionality now, though we won't be using it until the next section:

```

323 bindVars :: Env -> [(String, LispVal)] -> IO Env
324 bindVars envRef bindings = readIORef envRef >>= extendEnv
    bindings >>= newIORef
325     where extendEnv bindings env = liftM (++ env) (mapM
        addBinding bindings)
326         addBinding (var, value) = do ref <- newIORef value
327             return (var, ref)

```

This is perhaps more complicated than the other functions, since it uses a monadic pipeline (rather than `do`-notation) and a pair of helper functions to do the work. It's best to start with the helper functions. `addBinding` takes a variable name and value, creates an `IORef` to hold the new variable, and then returns the `(name, value)` pair. `extendEnv` calls `addBinding` on each member of `bindings` (`mapM`) to create a list of `(String, IORef LispVal)` pairs, and then appends the current environment to the end of that (`++ env`). Finally, the whole function wires these functions up in a pipeline, starting by reading the existing environment out of its `IORef`, then passing the result to `extendEnv`, then returning a new `IORef` with the extended environment.

Now that we have all our environment functions, we need to start using them in the evaluator. Since Haskell has no global variables, we'll have to thread the environment through the evaluator as a parameter. While we're at it, we might as well add the `set!` and `define` special forms.

```

91 eval :: Env -> LispVal -> IOThrowsError LispVal
92 eval env val@(String _) = return val
93 eval env val@(Number _) = return val
94 eval env val@(Bool _) = return val
95 eval env (Atom id) = getVar env id
96 eval env (List [Atom "quote", val]) = return val
97 eval env (List [Atom "if", pred, consequent, alt]) =
98     do result <- eval env pred
99     case result of
100         Bool False -> eval env alt
101         otherwise -> eval env consequent
102 eval env (List [Atom "set!", Atom var, form]) =
103     eval env form >>= setVar env var
104 eval env (List [Atom "define", Atom var, form]) =
105     eval env form >>= defineVar env var
106 eval env (List (Atom func : args)) = mapM (eval env) args >>=
    liftThrows . apply func
107 eval env badForm = throwError $ BadSpecialForm "Unrecognized
    special form" badForm

```

Since a single environment gets threaded through a whole interactive session, we need to change a few of our IO functions to take an environment.

```

263 evalAndPrint :: Env -> String -> IO ()
264 evalAndPrint env expr = evalString env expr >>= putStrLn
265
266 evalString :: Env -> String -> IO String

```

```
267 evalString env expr = runIOThrows $ liftM show $ (liftThrows $
    readExpr expr) >>= eval env
```

We need the `runIOThrows` in `evalString` because the type of the monad has changed from `ThrowError` to `IOThrowError`. Similarly, we need a `liftThrows` to bring `readExpr` into the `IOThrowError` monad.

Next, we initialize the environment with a null variable before starting the program:

```
276 runOne :: String -> IO ()
277 runOne expr = nullEnv >>= flip evalAndPrint expr
278
279 runRepl :: IO ()
280 runRepl = nullEnv >>= until_ (== "quit") (readPrompt "Lisp>>>
    ") . evalAndPrint
```

We've created an additional helper function `runOne` to handle the single-expression case, since it's now somewhat more involved than just running `evalAndPrint`. The changes to `runRepl` are a bit more subtle: notice how we added a function composition operator before `evalAndPrint`. That's because `evalAndPrint` now takes an additional `Env` parameter, fed from `nullEnv`. The function composition tells `until_` that instead of taking plain old `evalAndPrint` as an action, it ought to apply it first to whatever's coming down the monadic pipeline, in this case the result of `nullEnv`. Thus, the actual function that gets applied to each line of input is `(evalAndPrint env)`, just as we want it.

Finally, we need to change our main function to call `runOne` instead of evaluating `evalAndPrint` directly:

```
9  main :: IO ()
10  main = do args <- getArgs
11         case length args of
12             0 -> runRepl
13             1 -> runOne $ args !! 0
14             otherwise -> putStrLn "Program takes only 0 or 1
    argument"
```

The complete code is therefore:

Listing 7.1: A parser able to handle variables (variableparser.hs)

```
module Main where
import Monad
import System.Environment
import Control.Monad.Error
5  import Data.IORef
import Text.ParserCombinators.Parsec hiding (spaces)
import IO hiding (try)

main :: IO ()
10 main = do args <- getArgs
        case length args of
            0 -> runRepl
            1 -> runOne $ args !! 0
            otherwise -> putStrLn "Program takes only 0 or 1 argument"
15
symbol :: Parser Char
```

```

symbol = oneOf "!$%&|*+~/<=>@^_`~#"

readExpr :: String -> ThrowsError LispVal
20 readExpr input = case parse parseExpr "lisp" input of
    Left err -> throwError $ Parser err
    Right val -> return val

spaces :: Parser ()
25 spaces = skipMany1 space

data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
30              | Number Integer
              | String String
              | Bool Bool

parseString :: Parser LispVal
35 parseString = do char '"'
    x <- many (noneOf "\"")
    char '"'
    return $ String x

40 parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
    rest <- many (letter <|> digit <|> symbol)
    let atom = [first] ++ rest
    return $ case atom of
45         "#t" -> Bool True
         "#f" -> Bool False
         otherwise -> Atom atom

parseNumber :: Parser LispVal
50 parseNumber = liftM (Number . read) $ many1 digit

parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

55 parseDottedList :: Parser LispVal
parseDottedList = do
    head <- endBy parseExpr spaces
    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

60 parseQuoted :: Parser LispVal
parseQuoted = do
    char '\''
    x <- parseExpr
65    return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
parseExpr = parseAtom
    <|> parseString
70    <|> parseNumber
    <|> parseQuoted
    <|> do char '('
        x <- (try parseList) <|> parseDottedList
        char ')'
75        return x

showVal :: LispVal -> String
showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
showVal (Bool True) = "#t"
showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++

```

```

      showVal tail ++ ")"
85  unwordsList :: [LispVal] -> String
    unwordsList = unwords . map showVal

instance Show LispVal where show = showVal
90
eval :: Env -> LispVal -> IOThrowsError LispVal
eval env val@(String _) = return val
eval env val@(Number _) = return val
eval env val@(Bool _) = return val
95 eval env (Atom id) = getVar env id
eval env (List [Atom "quote", val]) = return val
eval env (List [Atom "if", pred, consequ, alt]) =
  do result <- eval env pred
  case result of
100    Bool False -> eval env alt
    otherwise -> eval env consequ
eval env (List [Atom "set!", Atom var, form]) =
  eval env form >>= setVar env var
eval env (List [Atom "define", Atom var, form]) =
105   eval env form >>= defineVar env var
eval env (List (Atom func : args)) = mapM (eval env) args >>= liftThrows
  . apply func
eval env badForm = throwError $ BadSpecialForm "Unrecognized special
  form" badForm

apply :: String -> [LispVal] -> ThrowsError LispVal
110 apply func args = maybe (throwError $ NotFunction "Unrecognized
  primitive function args" func)
  ($ args)
  (lookup func primitives)

primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
115 primitives = [(("+", numericBinop (+)),
  ("-", numericBinop (-)),
  ("*", numericBinop (*)),
  ("/", numericBinop div),
  ("mod", numericBinop mod),
120  ("quotient", numericBinop quot),
  ("remainder", numericBinop rem),
  ("=", numBoolBinop (==)),
 ("<", numBoolBinop (<)),
 (">", numBoolBinop (>)),
125  ("/=", numBoolBinop (/=)),
  (">=", numBoolBinop (>=)),
  ("<=", numBoolBinop (<=)),
  ("&&", boolBoolBinop (&&)),
  ("||", boolBoolBinop (||)),
130  ("string=?", strBoolBinop (==)),
  ("string?", strBoolBinop (>)),
  ("string<=?", strBoolBinop (<=)),
  ("string>=?", strBoolBinop (>=)),
  ("car", car),
135  ("cdr", cdr),
  ("cons", cons),
  ("eq?", eqv),
  ("eqv?", eqv),
  ("equal?", equal)]

140 numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
  ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
numericBinop op params = mapM unpackNum params >>= return . Number .
  foldl1 op

145 boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
  -> ThrowsError LispVal

```



```

boolBinop unpacker op args = if length args /= 2
                              then throwError $ NumArgs 2 args
                              else do left <- unpacker $ args !! 0
                                      right <- unpacker $ args !! 1
                                      return $ Bool $ left 'op' right
150
numBoolBinop = boolBinop unpackNum
strBoolBinop = boolBinop unpackStr
boolBoolBinop = boolBinop unpackBool
155
unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
unpackNum (String n) = let parsed = reads n in
                        if null parsed
160                          then throwError $ TypeMismatch "number" $
                               String n
                          else return $ fst $ parsed !! 0
unpackNum (List [n]) = unpackNum n
unpackNum notNum = throwError $ TypeMismatch "number" notNum
165
unpackStr :: LispVal -> ThrowsError String
unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
unpackStr (Bool s) = return $ show s
unpackStr notString = throwError $ TypeMismatch "string" notString
170
unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
unpackBool notBool = throwError $ TypeMismatch "boolean" notBool
175
car :: [LispVal] -> ThrowsError LispVal
car [List (x : xs)] = return x
car [DottedList (x : xs) -] = return x
car [badArg] = throwError $ TypeMismatch "pair" badArg
car badArgList = throwError $ NumArgs 1 badArgList
180
cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
cdr [DottedList (- : xs) x] = return $ DottedList xs x
cdr [DottedList [xs] x] = return x
185
cdr [badArg] = throwError $ TypeMismatch "pair" badArg
cdr badArgList = throwError $ NumArgs 1 badArgList
cons :: [LispVal] -> ThrowsError LispVal
cons [x1, List []] = return $ List [x1]
190
cons [x, List xs] = return $ List $ [x] ++ xs
cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs) xlast
cons [x1, x2] = return $ DottedList [x1] x2
cons badArgList = throwError $ NumArgs 2 badArgList
195
eqv :: [LispVal] -> ThrowsError LispVal
eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 == arg2
eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 == arg2
eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
200
eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++ [x], List
    $ ys ++ [y]]
eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1 == length
    arg2) &&
    (and $ map eqvPair $
        zip arg1 arg2)
    where eqvPair (x1, x2) = case eqv [x1, x2] of
        Left err -> False
        Right (Bool val) -> val
205
eqv [-, -] = return $ Bool False
eqv badArgList = throwError $ NumArgs 2 badArgList
data Unpacker = forall a. Eq a => AnyUnpacker (LispVal -> ThrowsError a)

```

```

210 unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError Bool
    unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
        do unpacked1 <- unpacker arg1
           unpacked2 <- unpacker arg2
           return $ unpacked1 == unpacked2
215 'catchError' (const $ return False)

equal :: [LispVal] -> ThrowsError LispVal
equal [arg1, arg2] = do
220   primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2)
                        [AnyUnpacker unpackNum, AnyUnpacker unpackStr,
                         AnyUnpacker unpackBool]
   eqvEquals <- eqv [arg1, arg2]
   return $ Bool $ (primitiveEquals || let (Bool x) = eqvEquals in x)
equal badArgList = throwError $ NumArgs 2 badArgList

225 data LispError = NumArgs Integer [LispVal]
                  | TypeMismatch String LispVal
                  | Parser ParseError
                  | BadSpecialForm String LispVal
230   | NotFunction String String
                  | UnboundVar String String
                  | Default String

showError :: LispError -> String
235 showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
showError (NotFunction message func) = message ++ ": " ++ show func
showError (NumArgs expected found) = "Expected " ++ show expected
                                     ++ " args: found values " ++
                                     unwordsList found
240 showError (TypeMismatch expected found) = "Invalid type: expected " ++
                                             expected
                                             ++ ", found " ++ show found
showError (Parser parseErr) = "Parse error at " ++ show parseErr

instance Show LispError where show = showError

245 instance Error LispError where
    noMsg = Default "An error has occurred"
    strMsg = Default

250 type ThrowsError = Either LispError

trapError action = catchError action (return . show)

extractValue :: ThrowsError a -> a
255 extractValue (Right val) = val

flushStr :: String -> IO ()
flushStr str = putStr str >> hFlush stdout

260 readPrompt :: String -> IO String
readPrompt prompt = flushStr prompt >> getLine

evalAndPrint :: Env -> String -> IO ()
evalAndPrint env expr = evalString env expr >=> putStrLn

265 evalString :: Env -> String -> IO String
evalString env expr = runIOThrows $ liftM show $ (liftThrows $ readExpr
    expr) >=> eval env

until_ :: Monad m => (a -> Bool) -> m a -> (a -> m ()) -> m ()
270 until_ pred prompt action = do
    result <- prompt
    if pred result
    then return ()

```

```

    else action result >> until_ pred prompt action
275 runOne :: String -> IO ()
    runOne expr = nullEnv >>= flip evalAndPrint expr

    runRepl :: IO ()
280 runRepl = nullEnv >>= until_ (== "quit") (readPrompt "Lisp>>> ") .
        evalAndPrint

    type Env = IORef [(String, IORef LispVal)]

    nullEnv :: IO Env
285 nullEnv = newIORef []

    type IOThrowsError = ErrorT LispError IO

    liftThrows :: ThrowsError a -> IOThrowsError a
290 liftThrows (Left err) = throwError err
    liftThrows (Right val) = return val

    runIOThrows :: IOThrowsError String -> IO String
    runIOThrows action = runErrorT (trapError action) >>= return .
        extractValue

295 isBound :: Env -> String -> IO Bool
    isBound envRef var = readIORef envRef >>= return . maybe False (const
        True) . lookup var

    getVar :: Env -> String -> IOThrowsError LispVal
300 getVar envRef var = do env <- liftIO $ readIORef envRef
        maybe (throwError $ UnboundVar "Getting an
            unbound variable" var)
            (liftIO . readIORef)
            (lookup var env)

305 setVar :: Env -> String -> LispVal -> IOThrowsError LispVal
    setVar envRef var value = do env <- liftIO $ readIORef envRef
        maybe (throwError $ UnboundVar "Setting an
            unbound variable" var)
            (liftIO . (flip writeIORef value))
            (lookup var env)
310 return value

    defineVar :: Env -> String -> LispVal -> IOThrowsError LispVal
    defineVar envRef var value = do
        alreadyDefined <- liftIO $ isBound envRef var
315 if alreadyDefined
        then setVar envRef var value >> return value
        else liftIO $ do
            valueRef <- newIORef value
            env <- readIORef envRef
            writeIORef envRef ((var, valueRef) : env)
320 return value

    bindVars :: Env -> [(String, LispVal)] -> IO Env
    bindVars envRef bindings = readIORef envRef >>= extendEnv bindings >>=
        newIORef
325 where extendEnv bindings env = liftM (++ env) (mapM addBinding
        bindings)
        addBinding (var, value) = do ref <- newIORef value
            return (var, ref)

```

And we can compile and test our program:

```

user>> ghc -package parsec -o lisp variableparser.hs
user>># ./lisp
Lisp>>> (define x 3)

```

```
3
Lisp>>> (+ x 2)
5
Lisp>>> (+ y 2)
Getting an unbound variable: y
Lisp>>> (define y 5)
5
Lisp>>> (+ x (- y 2))
6
Lisp>>> (define str "A string")
"A string"
Lisp>>> (< str "The string")
Invalid type: expected number, found "A string"
Lisp>>> (string<? str "The string")
#t
```

Chapter 8

Defining Scheme Functions: Closures and Environments

Now that we can define variables, we might as well extend it to functions. After this section, you'll be able to define your own functions within Scheme and use them from other functions. Our implementation is nearly finished.

Let's start by defining new `LispVal` constructors:

```
33         | PrimitiveFunc ([LispVal] -> ThrowsError LispVal
34         | Func {params :: [String], vararg :: (Maybe
35               String),
               body :: [LispVal], closure :: Env}
```

We've added a separate constructor for primitives, because we'd like to be able to store `+`, `eqv?`, etc. in variables and pass them to functions. The `PrimitiveFunc` constructor stores a function that takes a list of arguments to a `ThrowsError LispVal`, the same type that is stored in our primitive list.

We also want a constructor to store user-defined functions. We store 4 pieces of information:

1. the names of the parameters, as they're bound in the function body
2. whether the function accepts a variable-length list of arguments, and if so, the variable name it's bound to
3. the function body, as a list of expressions
4. the environment that the function was created in

This is an example of a [record](#) type. Records are somewhat clumsy in Haskell, so we're only using them for demonstration purposes. However, they can be invaluable in large-scale programming.

Next, we'll want to edit our `show` function to include the new types:

- [live version](#)
- [discussion](#)
- [edit](#)
- [comment](#)
- [report an error](#)

```

88 showVal (PrimitiveFunc _) = "<primitive>"
89 showVal (Func {params = args, vararg = varargs, body = body,
    closure = env}) =
90   "(lambda (" ++ unwords (map show args) ++
91     (case varargs of
92       Nothing -> ""
93       Just arg -> " . " ++ arg) ++ ") ...)"

```

Instead of showing the full function, we just print out the word "<primitive>" for primitives and the header info for user-defined functions. This is an example of pattern-matching for records: as with normal algebraic types, a pattern looks exactly like a constructor call. Field names come first and the variables they'll be bound to come afterwards.

Next, we need to change `apply`. Instead of being passed the name of a function, it'll be passed a `LispVal` representing the actual function. For primitives, that makes the code simpler: we need only read the function out of the value and apply it.

```

131 apply :: LispVal -> [LispVal] -> IOThrowsError LispVal
132 apply (PrimitiveFunc func) args = liftThrows $ func args

```

The interesting code happens when we're faced with a user defined function. Records let you pattern match on both the field name (as shown above) or the field position, so we'll use the latter form:

```

133 apply (Func params varargs body closure) args =
134   if num params /= num args && varargs == Nothing
135   then throwError $ NumArgs (num params) args
136   else (liftIO $ bindVars closure $ zip params args) >>=
    bindVarArgs varargs >>= evalBody
137   where remainingArgs = drop (length params) args
138         num = toInteger . length
139         evalBody env = liftM last $ mapM (eval env) body
140         bindVarArgs arg env = case arg of
141           Just argName -> liftIO $ bindVars env [(argName,
142             List $ remainingArgs)]
143           Nothing -> return env

```

The very first thing this function does is check the length of the parameter list against the expected number of arguments. It throws an error if they don't match. We define a local function `num` to enhance readability and make the program a bit shorter.

Assuming the call is valid, we do the bulk of the call in monadic pipeline that binds the arguments to a new environment and executes the statements in the body. The first thing we do is `zip` the list of parameter names and the list of (already-evaluated) argument values together into a list of pairs. Then, we take that and the function's closure (not the current environment—this is what gives us lexical scoping) and use them to create a new environment to evaluate the function in. The result is of type `IO`, while the function as a whole is `IOThrowsError`, so we need to `liftIO` it into the combined monad.

Now it's time to bind the remaining arguments to the `varArgs` variable, using the local function `bindVarArgs`. If the function doesn't take `varArgs` (the `Nothing` clause), then we just return the existing environment. Otherwise, we create a singleton list that has the variable name as the key and the remaining args as the value, and pass that to `bindVars`. We define the local variable `remainingArgs` for readability, using the built-in function `drop` to ignore all the arguments that have already been bound to variables.

The final stage is to evaluate the body in this new environment. We use the local function `evalBody` for this, which maps the monadic function `eval env` over every statement in the body, and then returns the value of the last statement.

Since we're now storing primitives as regular values in variables, we have to bind them when the program starts up:

```

320 primitiveBindings :: IO Env
321 primitiveBindings = nullEnv >>= (flip bindVars $ map
    makePrimitiveFunc primitives)
322     where makePrimitiveFunc (var, func) = (var, PrimitiveFunc
    func)

```

This takes the initial null environment, makes a bunch of name/value pairs consisting of `PrimitiveFunc` wrappers, and then binds the new pairs into the new environment. We also want to change `runOne` and `runRepl` to `primitiveBindings` instead:

```

309 runOne :: String -> IO ()
310 runOne expr = primitiveBindings >>= flip evalAndPrint expr
311
312 runRepl :: IO ()
313 runRepl = primitiveBindings >>= until_ (== "quit") (readPrompt
    "Lisp>>> ") . evalAndPrint

```

Finally, we need to change the evaluator to support `lambda` and function `define`. We'll start by creating a few helper functions to make it a little easier to create function objects in the `IOThrowsError` monad:

```

367 makeFunc varargs env params body = return $ Func (map showVal
    params) varargs body env
368 makeNormalFunc = makeFunc Nothing
369 makeVarargs = makeFunc . Just . showVal

```

Here, `makeNormalFunc` and `makeVarArgs` should just be considered specializations of `makeFunc` with the first argument set appropriately for normal functions vs. variable args. This is a good example of how to use first-class functions to simplify code.

Now, we can use them to add our extra `eval` clauses. They should be inserted after the `define-variable` clause and before the function-application one:

```

115 eval env (List (Atom "define" : List (Atom var : params) :
    body)) =
116     makeNormalFunc env params body >>= defineVar env var

```

```

117 eval env (List (Atom "define" : DottedList (Atom var : params)
118           varargs : body)) =
119     makeVarargs varargs env params body >>= defineVar env var
120 eval env (List (Atom "lambda" : List params : body)) =
121     makeNormalFunc env params body
122 eval env (List (Atom "lambda" : DottedList params varargs :
123           body)) =
124     makeVarargs varargs env params body
125 eval env (List (Atom "lambda" : varargs@(Atom _) : body)) =
126     makeVarargs varargs env [] body
127 eval env (List (function : args)) = do
128     func <- eval env function
129     argVals <- mapM (eval env) args
130     apply func argVals

```

As you can see, they just use pattern matching to destructure the form and then call the appropriate function helper. In `define`'s case, we also feed the output into `defineVar` to bind a variable in the local environment. We also need to change the function application clause to remove the `liftThrows` function, since `apply` now works in the `IOThrowsError` monad.

The complete code is therefore:

Listing 8.1: A parser able to handle functions (functionparser.hs)

```

module Main where
import Monad
import System.Environment
import Control.Monad.Error
5 import Data.IORef
import Text.ParserCombinators.Parsec hiding (spaces)
import IO hiding (try)

main :: IO ()
10 main = do args <- getArgs
           case length args of
             0 -> runRepl
             1 -> runOne $ args !! 0
             otherwise -> putStrLn "Program takes only 0 or 1 argument"

15 symbol :: Parser Char
symbol = oneOf " ! $ % & | * + - / : < = > ? @ ^ _ ~ # "

readExpr :: String -> ThrowsError LispVal
20 readExpr input = case parse parseExpr "lisp" input of
  Left err -> throwError $ Parser err
  Right val -> return val

spaces :: Parser ()
25 spaces = skipMany1 space

data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
30 | Number Integer
  | String String
  | Bool Bool
  | PrimitiveFunc ([LispVal] -> ThrowsError LispVal)
  | Func {params :: [String], vararg :: (Maybe String),
35         body :: [LispVal], closure :: Env}

parseString :: Parser LispVal

```



```

parseString = do char '"'
                x <- many (noneOf "\"")
                char '"'
40         return $ String x

parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
                rest <- many (letter <|> digit <|> symbol)
45         let atom = [first] ++ rest
                return $ case atom of
                        "#t" -> Bool True
                        "#f" -> Bool False
50         otherwise -> Atom atom

parseNumber :: Parser LispVal
parseNumber = liftM (Number . read) $ many1 digit

55 parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

parseDottedList :: Parser LispVal
parseDottedList = do
60     head <- endBy parseExpr spaces
        tail <- char '.' >> spaces >> parseExpr
        return $ DottedList head tail

parseQuoted :: Parser LispVal
65 parseQuoted = do
        char '\''
        x <- parseExpr
        return $ List [Atom "quote", x]

70 parseExpr :: Parser LispVal
parseExpr = parseAtom
        <|> parseString
        <|> parseNumber
        <|> parseQuoted
75     <|> do char '('
            x <- (try parseList) <|> parseDottedList
            char ')'
            return x

80 showVal :: LispVal -> String
showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
showVal (Number contents) = show contents
showVal (Bool True) = "#t"
85 showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ " . " ++
    showVal tail ++ ")"
showVal (PrimitiveFunc _) = "<primitive>"
showVal (Func {params = args, vararg = varargs, body = body, closure =
    env}) =
90     "(lambda (" ++ unwords (map show args) ++
        (case varargs of
            Nothing -> ""
            Just arg -> " . " ++ arg) ++ ") ...) "

95 unwordsList :: [LispVal] -> String
unwordsList = unwords . map showVal

instance Show LispVal where show = showVal

100 eval :: Env -> LispVal -> IOThrowsError LispVal
eval env val@(String _) = return val
eval env val@(Number _) = return val
eval env val@(Bool _) = return val

```

```

eval env (Atom id) = getVar env id
105 eval env (List [Atom "quote", val]) = return val
eval env (List [Atom "if", pred, conseq, alt]) =
    do result <- eval env pred
    case result of
        Bool False -> eval env alt
110         otherwise -> eval env conseq
eval env (List [Atom "set!", Atom var, form]) =
    eval env form >>= setVar env var
eval env (List [Atom "define", Atom var, form]) =
    eval env form >>= defineVar env var
115 eval env (List (Atom "define" : List (Atom var : params) : body)) =
    makeNormalFunc env params body >>= defineVar env var
eval env (List (Atom "define" : DottedList (Atom var : params) varargs :
    body)) =
    makeVarargs varargs env params body >>= defineVar env var
eval env (List (Atom "lambda" : List params : body)) =
120 makeNormalFunc env params body
eval env (List (Atom "lambda" : DottedList params varargs : body)) =
    makeVarargs varargs env params body
eval env (List (Atom "lambda" : varargs@(Atom _) : body)) =
    makeVarargs varargs env [] body
125 eval env (List (function : args)) = do
    func <- eval env function
    argVals <- mapM (eval env) args
    apply func argVals
eval env badForm = throwError $ BadSpecialForm "Unrecognized special
    form" badForm

130
apply :: LispVal -> [LispVal] -> IOThrowsError LispVal
apply (PrimitiveFunc func) args = liftThrows $ func args
apply (Func params varargs body closure) args =
    if num params /= num args && varargs == Nothing
135     then throwError $ NumArgs (num params) args
    else (liftIO $ bindVars closure $ zip params args) >>=
        bindVarargs varargs >>= evalBody
    where remainingArgs = drop (length params) args
          num = toInteger . length
          evalBody env = liftM last $ mapM (eval env) body
140 bindVarargs arg env = case arg of
    Just argName -> liftIO $ bindVars env [(argName, List $
        remainingArgs)]
    Nothing -> return env

145 primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [( "+", numericBinop (+)),
    ("-", numericBinop (-)),
    ("*", numericBinop (*)),
    ("/", numericBinop div),
150    ("mod", numericBinop mod),
    ("quotient", numericBinop quot),
    ("remainder", numericBinop rem),
    ("=", numBoolBinop (==)),
   ("<", numBoolBinop (<)),
   (">", numBoolBinop (>)),
155    ("/=", numBoolBinop (/=)),
   (">=", numBoolBinop (>=)),
   ("<=", numBoolBinop (<=)),
   ("&&", boolBoolBinop (&&)),
    ("||", boolBoolBinop (||)),
160    ("string=?", strBoolBinop (==)),
    ("string?", strBoolBinop (>)),
    ("string<=?", strBoolBinop (<=)),
    ("string>=?", strBoolBinop (>=)),
165    ("car", car),
    ("cdr", cdr),
    ("cons", cons),

```

```

    ("eq?", eqv),
    ("eqv?", eqv),
170    ("equal?", equal)]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal] ->
    ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2 singleVal
175 numericBinop op params = mapM unpackNum params >>= return . Number .
    foldl1 op

boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) -> [LispVal]
    -> ThrowsError LispVal
boolBinop unpacker op args = if length args /= 2
    then throwError $ NumArgs 2 args
180    else do left <- unpacker $ args !! 0
        right <- unpacker $ args !! 1
        return $ Bool $ left `op` right

numBoolBinop = boolBinop unpackNum
185 strBoolBinop = boolBinop unpackStr
boolBoolBinop = boolBinop unpackBool

unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
190 unpackNum (String n) = let parsed = reads n in
    if null parsed
        then throwError $ TypeMismatch "number" $
            String n
        else return $ fst $ parsed !! 0

unpackNum (List [n]) = unpackNum n
195 unpackNum notNum = throwError $ TypeMismatch "number" notNum

unpackStr :: LispVal -> ThrowsError String
unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
200 unpackStr (Bool s) = return $ show s
unpackStr notString = throwError $ TypeMismatch "string" notString

unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
205 unpackBool notBool = throwError $ TypeMismatch "boolean" notBool

car :: [LispVal] -> ThrowsError LispVal
car [List (x : xs)] = return x
car [DottedList (x : xs) _] = return x
210 car [badArg] = throwError $ TypeMismatch "pair" badArg
car badArgList = throwError $ NumArgs 1 badArgList

cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
215 cdr [DottedList (_ : xs) x] = return $ DottedList xs x
cdr [DottedList [xs] x] = return x
cdr [badArg] = throwError $ TypeMismatch "pair" badArg
cdr badArgList = throwError $ NumArgs 1 badArgList

cons :: [LispVal] -> ThrowsError LispVal
cons [x1, List []] = return $ List [x1]
cons [x, List xs] = return $ List $ [x] ++ xs
cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs) xlast
cons [x1, x2] = return $ DottedList [x1] x2
225 cons badArgList = throwError $ NumArgs 2 badArgList

eqv :: [LispVal] -> ThrowsError LispVal
eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 == arg2
230 eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 == arg2
eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2

```

```

eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++ [x], List
  $ ys ++ [y]]
eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1 == length
  arg2) &&
  (and $ map eqvPair $
    zip arg1 arg2)
235   where eqvPair (x1, x2) = case eqv [x1, x2] of
    Left err -> False
    Right (Bool val) -> val
eqv [-, -] = return $ Bool False
eqv badArgList = throwError $ NumArgs 2 badArgList
240
data Unpacker = forall a. Eq a => AnyUnpacker (LispVal -> ThrowsError a)

unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError Bool
unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
245   do unpacked1 <- unpacker arg1
    unpacked2 <- unpacker arg2
    return $ unpacked1 == unpacked2
  `catchError` (const $ return False)

250 equal :: [LispVal] -> ThrowsError LispVal
equal [arg1, arg2] = do
  primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2)
    [AnyUnpacker unpackNum, AnyUnpacker unpackStr,
     AnyUnpacker unpackBool]
  eqvEquals <- eqv [arg1, arg2]
255   return $ Bool $ (primitiveEquals || let (Bool x) = eqvEquals in x)
equal badArgList = throwError $ NumArgs 2 badArgList

260 data LispError = NumArgs Integer [LispVal]
  | TypeMismatch String LispVal
  | Parser ParseError
  | BadSpecialForm String LispVal
  | NotFunction String String
  | UnboundVar String String
265   | Default String

showError :: LispError -> String
showError (UnboundVar message varname) = message ++ ": " ++ varname
showError (BadSpecialForm message form) = message ++ ": " ++ show form
270 showError (NotFunction message func) = message ++ ": " ++ show func
showError (NumArgs expected found) = "Expected " ++ show expected
  ++ " args: found values " ++
    unwordsList found
showError (TypeMismatch expected found) = "Invalid type: expected " ++
  expected
  ++ ", found " ++ show found
275 showError (Parser parseErr) = "Parse error at " ++ show parseErr

instance Show LispError where show = showError

instance Error LispError where
280   noMsg = Default "An error has occurred"
   strMsg = Default

type ThrowsError = Either LispError

285 trapError action = catchError action (return . show)

extractValue :: ThrowsError a -> a
extractValue (Right val) = val

290 flushStr :: String -> IO ()
flushStr str = putStr str >> hFlush stdout

readPrompt :: String -> IO String

```

```

readPrompt prompt = flushStr prompt >> getLine

295 evalAndPrint :: Env -> String -> IO ()
evalAndPrint env expr = evalString env expr >>= putStrLn

evalString :: Env -> String -> IO String
300 evalString env expr = runIOThrows $ liftM show $ (liftThrows $ readExpr
    expr) >>= eval env

until_ :: Monad m => (a -> Bool) -> m a -> (a -> m ()) -> m ()
until_ pred prompt action = do
    result <- prompt
305     if pred result
        then return ()
        else action result >> until_ pred prompt action

runOne :: String -> IO ()
310 runOne expr = primitiveBindings >>= flip evalAndPrint expr

runRepl :: IO ()
runRepl = primitiveBindings >>= until_ (== "quit") (readPrompt "Lisp>>>
    ") . evalAndPrint

315 type Env = IORef [(String, IORef LispVal)]

nullEnv :: IO Env
nullEnv = newIORef []

320 primitiveBindings :: IO Env
primitiveBindings = nullEnv >>= (flip bindVars $ map makePrimitiveFunc
    primitives)
    where makePrimitiveFunc (var, func) = (var, PrimitiveFunc func)

325 type IOThrowsError = ErrorT LispError IO

liftThrows :: ThrowsError a -> IOThrowsError a
liftThrows (Left err) = throwError err
liftThrows (Right val) = return val

330 runIOThrows :: IOThrowsError String -> IO String
runIOThrows action = runErrorT (trapError action) >>= return .
    extractValue

isBound :: Env -> String -> IO Bool
335 isBound envRef var = readIORef envRef >>= return . maybe False (const
    True) . lookup var

getVar :: Env -> String -> IOThrowsError LispVal
getVar envRef var = do env <- liftIO $ readIORef envRef
    maybe (throwError $ UnboundVar "Getting an
        unbound variable" var)
340         (liftIO . readIORef)
        (lookup var env)

setVar :: Env -> String -> LispVal -> IOThrowsError LispVal
setVar envRef var value = do env <- liftIO $ readIORef envRef
    maybe (throwError $ UnboundVar "Setting an
        unbound variable" var)
345         (liftIO . (flip writeIORef value))
        (lookup var env)
    return value

350 defineVar :: Env -> String -> LispVal -> IOThrowsError LispVal
defineVar envRef var value = do
    alreadyDefined <- liftIO $ isBound envRef var
    if alreadyDefined
        then setVar envRef var value >> return value

```

```

355         else liftIO $ do
            valueRef <- newIORef value
            env <- readIORef envRef
            writeIORef envRef ((var, valueRef) : env)
            return value
360
bindVars :: Env -> [(String, LispVal)] -> IO Env
bindVars envRef bindings = readIORef envRef >>= extendEnv bindings >>=
    newIORef
    where extendEnv bindings env = liftM (++ env) (mapM addBinding
        bindings)
        addBinding (var, value) = do ref <- newIORef value
365            return (var, ref)

makeFunc varargs env params body = return $ Func (map showVal params)
    varargs body env
makeNormalFunc = makeFunc Nothing
makeVarargs = makeFunc . Just . showVal

```

We can now compile and run our program, and use it to write real programs!

```

user>> ghc -package parsec -fglasgow-exts -o lisp
        functionparser.hs
user>> ./lisp
Lisp>>> (define (f x y) (+ x y))
        (lambda ("x" "y") ...)
Lisp>>> (f 1 2)
        3
Lisp>>> (f 1 2 3)
        Expected 2 args: found values 1 2 3
Lisp>>> (f 1)
        Expected 2 args: found values 1
Lisp>>> (define (factorial x) (if (= x 1) 1 (* x (factorial (-
        x 1)))))
        (lambda ("x") ...)
Lisp>>> (factorial 10)
        3628800
Lisp>>> (define (counter inc) (lambda (x) (set! inc (+ x inc))
        inc))
        (lambda ("inc") ...)
Lisp>>> (define my-count (counter 5))
        (lambda ("x") ...)
Lisp>>> (my-count 3)
        8
Lisp>>> (my-count 6)
        14
Lisp>>> (my-count 5)
        19

```

Chapter 9

Creating IO Primitives: File I/O

Our Scheme can't really communicate with the outside world yet, so it would be nice if we could give it some IO functions. Also, it gets really tedious typing in functions every time we start the interpreter, so it would be nice to load files of code and execute them.

The first thing we'll need is a new constructor for `LispVals`. `PrimitiveFuncs` have a specific type signature that doesn't include the `IO` monad, so they can't perform any IO. We want a dedicated constructor for primitive functions that perform IO:

```
35 | IOFunc ([LispVal] -> IOThrowsError LispVal)
```

While we're at it, let's also define a constructor for the Scheme data type of a `port`. Most of our IO functions will take one of these to read from or write to:

```
33 | Port Handle
```

A `Handle` is basically the Haskell notion of a port: it's an opaque data type, returned from `openFile` and similar `IO` actions, that you can read and write to.

For completeness, we ought to provide `showVal` methods for the new data types:

```
90 showVal (Port _) = "<IO port>"
91 showVal (IOFunc _) = "<IO primitive>"
```

This'll let the REPL function properly and not crash when you use a function that returns a port.

We'll need to make some minor changes to our parser to support `load`. Since Scheme files usually contain several definitions, we need to add a parser that will support several expressions, separated by whitespace. And it also needs to handle errors. We can re-use much of the existing infrastructure by factoring our basic `readExpr` so that it takes the actual parser as a parameter:

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```

16 readOrThrow :: Parser a -> String -> ThrowsError a
17 readOrThrow parser input = case parse parser "lisp" input of
18     Left err -> throwError $ Parser err
19     Right val -> return val
20
21 readExpr = readOrThrow parseExpr
22 readExprList = readOrThrow (endBy parseExpr spaces)

```

Again, think of both `readExpr` and `readExprList` as specializations of the newly-renamed `readOrThrow`. We'll be using `readExpr` in our REPL to read single expressions; we'll be using `readExprList` from within `load` to read programs.

Next, we'll want a new list of IO primitives, structured just like the existing primitive list:

```

378 ioPrimitives :: [(String, [LispVal] -> IOThrowsError LispVal)]
379 ioPrimitives = [ ("apply", applyProc),
380                  ("open-input-file", makePort ReadMode),
381                  ("open-output-file", makePort WriteMode),
382                  ("close-input-port", closePort),
383                  ("close-output-port", closePort),
384                  ("read", readProc),
385                  ("write", writeProc),
386                  ("read-contents", readContents),
387                  ("read-all", readAll)]

```

The only difference here is in the type signature. Unfortunately, we can't use the existing primitive list because lists cannot contain elements of different types. We also need to change the definition of `primitiveBindings` to add our new primitives:

```

327 primitiveBindings :: IO Env
328 primitiveBindings = nullEnv >>= (flip bindVars $ map (makeFunc
329                                                         ++ map (makeFunc
330                                                         PrimitiveFunc
331                                                         ) primitives
332                                                         )
333     where makeFunc constructor (var, func) = (var, constructor
334                                               func)

```

We've generalized `makeFunc` to take a constructor argument, and now call it on the list of `ioPrimitives` in addition to the plain old primitives.

Now we start defining the actual functions. `applyProc` is a very thin wrapper around `apply`, responsible for destructuring the argument list into the form `apply` expects:

```

389 applyProc :: [LispVal] -> IOThrowsError LispVal
390 applyProc [func, List args] = apply func args
391 applyProc (func : args) = apply func args

```


`makePort` wraps the Haskell function `openFile`, converting it to the right type and wrapping its return value in the `Port` constructor. It's intended to be partially-applied to the `IOMode`, `ReadMode` for open-input-file and `WriteMode` for open-output-file:

```
393 makePort :: IOMode -> [LispVal] -> IOThrowsError LispVal
394 makePort mode [String filename] = liftM Port $ liftIO $
    openFile filename mode
```

`closePort` also wraps the equivalent Haskell procedure, this time `hClose`:

```
396 closePort :: [LispVal] -> IOThrowsError LispVal
397 closePort [Port port] = liftIO $ hClose port >> (return $ Bool
    True)
398 closePort _ = return $ Bool False
```

`readProc` (named to avoid a name conflict with the built-in `read`) wraps the Haskell `hGetLine` and then sends the result to `parseExpr`, to be turned into a `LispVal` suitable for Scheme:

```
400 readProc :: [LispVal] -> IOThrowsError LispVal
401 readProc [] = readProc [Port stdin]
402 readProc [Port port] = (liftIO $ hGetLine port) >>= liftThrows
    . readExpr
```

Notice how `hGetLine` is of type `IO String` yet `readExpr` is of type `String -> ThrowsError LispVal`, so they both need to be converted (with `liftIO` and `liftThrows`, respectively) to the `IOThrowsError` monad. Only then can they be piped together with the monadic bind operator. `writeProc` converts a `LispVal` to a string and then writes it out on the specified port:

```
404 writeProc :: [LispVal] -> IOThrowsError LispVal
405 writeProc [obj] = writeProc [obj, Port stdout]
406 writeProc [obj, Port port] = liftIO $ hPrint port obj >> (
    return $ Bool True)
```

We don't have to explicitly call `show` on the object we're printing, because `hPrint` takes a value of type `Show a`. It's calling `show` for us automatically. This is why we bothered making `LispVal` an instance of `Show`; otherwise, we wouldn't be able to use this automatic conversion and would have to call `showVal` ourselves. Many other Haskell functions also take instances of `Show`, so if we'd extended this with other IO primitives, it could save us significant labor.

`readContents` reads the whole file into a string in memory. It's a thin wrapper around Haskell's `readFile`, again just lifting the IO action into an `IOThrowsError` action and wrapping it in a `String` constructor:

```
408 readContents :: [LispVal] -> IOThrowsError LispVal
409 readContents [String filename] = liftM String $ liftIO $
    readFile filename
```

The helper function `load` doesn't do what Scheme's `load` does (we handle that later). Rather, it's responsible only for reading and parsing a file full of

statements. It's used in two places: `readAll` (which returns a list of values) and `load` (which evaluates those values as Scheme expressions).

```
411 load :: String -> IOThrowsError [LispVal]
412 load filename = (liftIO $ readFile filename) >>= liftThrows .
    readExprList
```

`readAll` then just wraps that return value with the `List` constructor:

```
414 readAll :: [LispVal] -> IOThrowsError LispVal
415 readAll [String filename] = liftM List $ load filename
```

Implementing the actual Scheme `load` function is a little tricky, because `load` can introduce bindings into the local environment. `Apply`, however, doesn't take an environment argument, and so there's no way for a primitive function (or any function) to do this. We get around this by implementing `load` as a special form:

```
129 eval env (List [Atom "load", String filename]) =
130     load filename >>= liftM last . mapM (eval env)
```

Finally, we might as well change our `runOne` function so that instead of evaluating a single expression from the command line, it takes the name of a file to execute and runs that as a program. Additional command-line arguments will get bound into a list `args` within the Scheme program:

```
313 runOne :: [String] -> IO ()
314 runOne args = do
315     env <- primitiveBindings >>= flip bindVars [("args", List
316         $ map String $ drop 1 args)]
317     (runIOThrows $ liftM show $ eval env (List [Atom "load",
318         String (args !! 0)]))
319     >>= hPutStrLn stderr
```

That's a little involved, so let's go through it step-by-step. The first line takes the original primitive bindings, passes that into `bindVars`, and then adds a variable named `args` that's bound to a `List` containing `String` versions of all but the first argument. (The first argument is the filename to execute.) Then, it creates a Scheme form `(load "arg1")`, just as if the user had typed it in, and evaluates it. The result is transformed to a string (remember, we have to do this before catching errors, because the error handler converts them to strings and the types must match) and then we run the whole `IOThrowsError` action. Then we print the result on `STDERR`. (Traditional UNIX conventions hold that `STDOUT` should be used only for program output, with any error messages going to `STDERR`. In this case, we'll also be printing the return value of the last statement in the program, which generally has no meaning to anything.)

Then we change `main` so it uses our new `runOne` function. Since we no longer need a third clause to handle the wrong number of command-line arguments, we can simplify it to an `if` statement:

```
9 main :: IO ()
10 main = do args <- getArgs
11     if null args then runRepl else runOne $ args
```

Chapter 10

Towards a Standard Library: Fold and Unfold

Our Scheme is almost complete now, but it's still rather hard to use. At the very least, we'd like a library of standard list-manipulation functions that we can use to perform some common computations.

Rather than using a typical Scheme implementation, defining each list function in terms of a recursion on lists, we'll implement two primitive recursion operators (`fold` and `unfold`) and then define our whole library based on those. This style is used by the [Haskell Prelude](#): it gives you more concise definitions, less room for error, and good practice using `fold` to capture iteration.

We'll start by defining a few obvious helper functions. `not` and `null` are defined exactly as you'd expect it, using if statements:

```
(define (not x)
  (if x
    #f
    #t))

(define (null? obj)
  (if (eqv? obj '())
    #t
    #f))
```

We can use the `varArgs` feature to define `list`, which just returns a list of its arguments:

```
(define (list . objs)
  objs)
```

We also want an `id` function, which just returns its argument unchanged. This may seem completely useless—if you already have a value, why do you need a function to return it? However, several of our algorithms expect a function that tells us what to do with a given value. By defining `id`, we let those higher-order functions work even if we don't want to do anything with the value.

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```
(define (id obj)
  obj)
```

Similarly, it'd be nice to have a `flip` function, in case we want to pass in a function that takes its arguments in the wrong order:

```
(define (flip func)
  (lambda (arg1 arg2)
    (func arg2 arg1)))
```

Finally, we add `curry` and `compose`, which work like their Haskell equivalents (partial-application and the dot operator, respectively).

```
(define (curry func arg1)
  (lambda (arg)
    (apply func (cons arg1 arg))))

(define (compose f g)
  (lambda (arg)
    (f (apply g arg))))
```

We might as well define some simple library functions that appear in the Scheme standard:

```
(define zero?
  (curry = 0))

(define positive?
  (curry < 0))

(define negative?
  (curry > 0))

(define (odd? num)
  (= (mod num 2) 1))

(define (even? num)
  (= (mod num 2) 0))
```

These are basically done just as you'd expect them. Note the usage of `curry` to define `zero?`, `positive?` and `negative?`. We bind the variable `zero?` to the function returned by `curry`, giving us an unary function that returns true if its argument is equal to zero.

Next, we want to define a `fold` function that captures the basic pattern of recursion over a list. The best way to think about `fold` is to picture a list in terms of its infix constructors: $[1, 2, 3, 4] = 1:2:3:4:[]$ in Haskell or $(1 . (2 . (3 . (4 . \text{NIL}))))$ in Scheme. A `fold` function replaces every constructor with a binary operation, and replaces `NIL` with the accumulator. So, for example, $(\text{fold } + 0 '(1\ 2\ 3\ 4)) = (1 + (2 + (3 + (4 + 0))))$.

With that definition, we can write our `fold` function. Start with a right-associative version to mimic the above examples:

```
(define (foldr func end lst)
  (if (null? lst)
      end
      (func (car lst) (foldr func end (cdr lst)))))
```

The structure of this function mimics our definition almost exactly. If the list is null, replace it with the end value. If not, apply the function to the car of the list and to the result of folding this function and end value down the rest of the list. Since the right-hand operand is folded up first, you end up with a right-associative **fold**.

We also want a left-associative version. For most associative operations like $+$ and $*$, the two of them are completely equivalent. However, there is at least one important binary operation that is not associative: **cons**. For all our list manipulation functions, then, we'll need to deliberately choose between left- and right-associative **folds**.

```
(define (foldl func accum lst)
  (if (null? lst)
      accum
      (foldl func (func accum (car lst)) (cdr lst))))
```

This begins the same way as the right-associative version, with the test for null that returns the accumulator. This time, however, we apply the function to the accumulator and first element of the list, instead of applying it to the first element and the result of folding the list. This means that we process the beginning first, giving us left-associativity. Once we reach the end of the list, '(), we then return the result that we've been progressively building up.

Note that **func** takes its arguments in the opposite order from **foldr**. In **foldr**, the accumulator represents the rightmost value to tack onto the end of the list, after you've finished recursing down it. In **foldl**, it represents the completed calculation for the leftmost part of the list. In order to preserve our intuitions about commutativity of operators, it should therefore be the left argument of our operation in **foldl**, but the right argument in **foldr**.

Once we've got our basic **folds**, we can define a couple convenience names to match typical Scheme usage:

```
(define fold foldl)
(define reduce fold)
```

These are just new variables bound to the existing functions: they don't define new functions. Most Schemes call **fold** \textit{reduce} or plain old **fold**, and don't make the distinction between **foldl** and **foldr**. We define it to be **foldl**, which happens to be tail-recursive and hence runs more efficiently than **foldr** (it doesn't have to recurse all the way down to the end of the list before it starts building up the computation). Not all operations are associative, however; we'll see some cases later where we have to use **foldr** to get the right result.

Next, we want to define a function that is the opposite of **fold**. Given an unary function, an initial value, and a unary predicate, it continues applying

the function to the last value until the predicate is true, building up a list as it goes along. This is essentially what generators are in Python or Icon:

```
(define (lstlisting func init pred)
  (if (pred init)
      (cons init '())
      (cons init (unfold func (func init) pred))))
```

As usual, our function structure basically matches the definition. If the predicate is true, then we cons a '()' onto the last value, terminating the list. Otherwise, cons the result of unfolding the next value (`func init`) onto the current value.

In academic functional programming literature, folds are often called catamorphisms, unfolds are often called anamorphisms, and the combinations of the two are often called hylomorphisms. They're interesting because any for-each loop can be represented as a catamorphism. To convert from a loop to a `foldl`, package up all mutable variables in the loop into a data structure (records work well for this, but you can also use an algebraic data type or a list). The initial state becomes the accumulator; the loop body becomes a function with the loop variables as its first argument and the iteration variable as its second; and the list becomes, well, the list. The result of the fold function is the new state of all the mutable variables.

Similarly, every for-loop (without early exits) can be represented as a hylomorphism. The initialization, termination, and step conditions of a for-loop define an anamorphism that builds up a list of values for the iteration variable to take. Then, you can treat that as a for-each loop and use a catamorphism to break it down into whatever state you wish to modify.

Let's go through a couple examples. We'll start with typical `sum`, `product`, `and`, or functions:

```
(define (sum . lst)
  (fold + 0 lst))

(define (product . lst)
  (fold * 1 lst))

(define (and . lst)
  (fold && #t lst))

(define (or . lst)
  (fold || #f lst))
```

These all follow from the definitions:

```
(sum 1 2 3 4) = 1 + 2 + 3 + 4 + 0 = (fold + 0 '(1 . (2 . (3 .
  (4 . NIL)))))
(product 1 2 3 4) = 1 * 2 * 3 * 4 * 1 = (fold * 1 '(1 . (2 .
  (3 . (4 . NIL)))))
(and #t #t #f) = #t && #t && #f && #t = (fold && #t '(#t . (#t
  . (#f . NIL)))))
```

```
(or #t #t #f) = #t || #t || #f || #f = (fold || #f '(#t . (#t
  . (#f . NIL)))
```

Since all of these operators are associative, it doesn't matter whether we use `foldr` or `foldl`. We replace the `cons` constructor with the operator, and the `nil` constructor with the identity element for that operator.

Next, let's try some more complicated operators. `max` and `min` find the maximum and minimum of their arguments, respectively:

```
(define (max first . num-list)
  (fold (lambda (old new)
        (if (> old new) old new))
        first
        num-list))

(define (min first . num-list)
  (fold (lambda (old new)
        (if (< old new) old new))
        first
        num-list))
```

It's not immediately obvious what operation to fold over the list, because none of the built-ins quite qualify. Instead, think back to fold as a representation of a `foreach` loop. The accumulator represents any state we've maintained over previous iterations of the loop, so we'll want it to be the maximum value we've found so far. That gives us our initialization value: we want to start off with the leftmost variable in the list (since we're doing a `foldl`). Now recall that the result of the operation becomes the new accumulator at each step, and we've got our function. If the previous value is greater, keep it. If the new value is greater, or they're equal, return the new value. Reverse the operation for `min`.

How about length? We know that we can find the length of a list by counting down it, but how do we translate that into a `fold`?

```
(define (length lst)
  (fold (lambda (x y)
        (+ x 1))
        0
        lst))
```

Again, think in terms of its definition as a loop. The accumulator starts off at 0 and gets incremented by 1 with each iteration. That gives us both our initialization value—0—and our function—`(lambda (x y) (+ x 1))`. Another way to look at this is “The length of a list is 1 + the length of the sublist to its left.”

Let's try something a bit trickier: `reverse`.

```
(define (reverse lst)
  (fold (flip cons) '() lst))
```

The function here is fairly obvious: if you want to reverse two `cons` cells, you can just flip `cons` so it takes its arguments in the opposite order. However,

there's a bit of subtlety at work. Ordinary lists are right associative: $(1\ 2\ 3\ 4) = (1\ .\ (2\ .\ (3\ .\ (4\ .\ \text{NIL}))))$. If you want to reverse this, you need your fold to be left associative: $(\text{reverse}\ '(1\ 2\ 3\ 4)) = (4\ .\ (3\ .\ (2\ .\ (1\ .\ \text{NIL}))))$. Try it with a `foldr` instead of a `foldl` and see what you get.

There's a whole family of member and assoc functions, all of which can be represented with folds. The particular lambda expression is fairly complicated though, so let's factor it out:

```
(define (mem-helper pred op)
  (lambda (acc next)
    (if (and (not acc)
             (pred (op next)))
        next
        acc)))

(define (memq obj lst)
  (fold (mem-helper (curry eq? obj) id) #f lst))

(define (memv obj lst)
  (fold (mem-helper (curry eqv? obj) id) #f lst))

(define (member obj lst)
  (fold (mem-helper (curry equal? obj) id) #f lst))

(define (assq obj alist)
  (fold (mem-helper (curry eq? obj) car) #f alist))

(define (assv obj alist)
  (fold (mem-helper (curry eqv? obj) car) #f alist))

(define (assoc obj alist)
  (fold (mem-helper (curry equal? obj) car) #f alist))
```

The helper function is parameterized by the predicate to use and the operation to apply to the result if found. Its accumulator represents the first value found so far: it starts out with `#f` and takes on the first value that satisfies its predicate. We avoid finding subsequent values by testing for a non-`#f` value and returning the existing accumulator if it's already set. We also provide an operation that will be applied to the next value each time the predicate tests: this lets us customize `mem-helper` to check the value itself (for `member`) or only the key of the value (for `assoc`).

The rest of the functions are just various combinations of `eq?`/`eqv?`/`equal?` and `id`/`car`, folded over the list with an initial value of `#f`.

Next, let's define the functions `map` and `filter`. Map applies a function to every element of a list, returning a new list with the transformed values:

```
(define (map func lst)
  (foldr (lambda (x y)
           (cons (func x) y))
        '()
        lst))
```



```
lst))
```

Remember that `foldr`'s function takes its arguments in the opposite order as `fold`, with the current value on the left. `map`'s lambda applies the function to the current value, then conses it with the rest of the mapped list, represented by the right-hand argument. It's essentially replacing every infix `cons` constructor with one that conses, but also applies the function to its left-side argument.

`filter` keeps only the elements of a list that satisfy a predicate, dropping all others:

```
(define (filter pred lst)
  (foldr (lambda (x y)
          (if (pred x)
              (cons x y)
              y))
        '()
        lst))
```

This works by testing the current value against the predicate. If it's true, replacing `cons` with `cons`, i.e. don't do anything. If it's false, drop the `cons` and just return the rest of the list. This eliminates all the elements that don't satisfy the predicate, consing up a new list that includes only the ones that do.

The complete standard library is therefore:

Listing 10.1: Standard library (stdlib.scm)

```
(define (caar pair) (car (car pair)))
(define (cadr pair) (car (cdr pair)))
(define (cdar pair) (cdr (car pair)))
(define (cddr pair) (cdr (cdr pair)))
5 (define (caaar pair) (car (car (car pair))))
  (define (caadr pair) (car (car (cdr pair))))
  (define (cadar pair) (car (cdr (car pair))))
  (define (caddr pair) (car (cdr (cdr pair))))
  (define (cdaar pair) (cdr (car (car pair))))
10 (define (cdadr pair) (cdr (car (cdr pair))))
  (define (cddar pair) (cdr (cdr (car pair))))
  (define (cdddr pair) (cdr (cdr (cdr pair))))
  (define (caaaar pair) (car (car (car (car pair)))))
  (define (caaadr pair) (car (car (car (cdr pair)))))
15 (define (caadar pair) (car (car (cdr (car pair)))))
  (define (caaddr pair) (car (car (cdr (cdr pair)))))
  (define (cadaar pair) (car (cdr (car (car pair)))))
  (define (cadadr pair) (car (cdr (car (cdr pair)))))
  (define (caddar pair) (car (cdr (cdr (car pair)))))
20 (define (cadddr pair) (car (cdr (cdr (cdr pair)))))
  (define (cdaaar pair) (cdr (car (car (car pair)))))
  (define (cdaaadr pair) (cdr (car (car (cdr pair)))))
  (define (cdadar pair) (cdr (car (cdr (car pair)))))
  (define (cdaddr pair) (cdr (car (cdr (cdr pair)))))
25 (define (cddaar pair) (cdr (cdr (car (car pair)))))
  (define (cddadr pair) (cdr (cdr (car (cdr pair)))))
  (define (cdddar pair) (cdr (cdr (cdr (car pair)))))
  (define (cddddr pair) (cdr (cdr (cdr (cdr pair)))))

30 (define (not x) (if x #f #t))
  (define (null? obj) (if (eqv? obj '()) #t #f))
  (define (id obj) obj)
  (define (flip func) (lambda (arg1 arg2) (func arg2 arg1)))
  (define (curry func arg1) (lambda (arg) (func arg1 arg)))
```

```

35 (define (compose f g)      (lambda (arg) (f (g arg))))

  (define (foldl func accum lst)
    (if (null? lst)
        accum
        (foldl func (func accum (car lst)) (cdr lst))))

40

  (define (foldr func accum lst)
    (if (null? lst)
        accum
        (func (car lst) (foldr func accum (cdr lst)))))

45

  (define (unfold func init pred)
    (if (pred init)
        (cons init '())
        (cons init (unfold func (func init) pred))))

  (define fold foldl)
  (define reduce fold)

55 (define zero?      (curry = 0))
  (define positive?  (curry < 0))
  (define negative?  (curry > 0))
  (define (odd? num) (= (mod num 2) 1))
  (define (even? num) (= (mod num 2) 0))
60 (define (max x . num-list) (fold (lambda (y z) (if (> y z) y z)) x num-
  list))
  (define (min x . num-list) (fold (lambda (y z) (if (< y z) y z)) x num-
  list))
  (define (list . objs)      objs)
  (define (length lst)       (fold (lambda (x y) (+ x 1)) 0 lst))
  (define (append lst . lsts) (foldr (flip (curry foldr cons)) lst lsts))
65 (define (reverse lst)      (fold (flip cons) '() lst))
  (define (mem-helper pred op) (lambda (acc next) (if (and (not acc) (pred
  (op next))) next acc)))
  (define (memq obj lst)      (fold (mem-helper (curry eq? obj) id) #f
  lst))
  (define (memv obj lst)      (fold (mem-helper (curry eqv? obj) id) #f
  lst))
  (define (member obj lst)    (fold (mem-helper (curry equal? obj) id) #f
  lst))
70 (define (assq obj alist)    (fold (mem-helper (curry eq? obj) car) #f
  alist))
  (define (assv obj alist)    (fold (mem-helper (curry eqv? obj) car) #f
  alist))
  (define (assoc obj alist)   (fold (mem-helper (curry equal? obj) car) #
  f alist))

  (define (map func lst)      (foldr (lambda (x y) (cons (func x) y)) '()
  lst))
75 (define (filter pred lst)   (foldr (lambda (x y) (if (pred x) (cons x y)
  y)) '() lst))

  (define (sum . lst)         (fold + 0 lst))
  (define (product . lst)     (fold * 1 lst))
  (define (and . lst)         (fold && #t lst))
  (define (or . lst)          (fold || #f lst))
80 (define (any? pred . lst)   (apply or (map pred lst)))
  (define (every? pred . lst) (apply and (map pred lst)))

```

We can use the standard library by starting up our Lisp interpreter and typing (load "stdlib.scm"):

```

user>> ./lisp
Lisp>>> (load "stdlib.scm")
         (lambda ("pred" . lst) ...)

```

```
Lisp>>> (map (curry + 2) '(1 2 3 4))  
(3 4 5 6)  
Lisp>>> (filter even? '(1 2 3 4))  
(2 4)  
Lisp>>> quit
```

There are many other useful functions that could go into the standard library, including `list-tail`, `list-ref`, `append`, and various string-manipulation functions. Try implementing them as folds. Remember, the key to successful fold-programming is thinking only in terms of what happens on each iteration. Fold captures the pattern of recursion down a list, and recursive problems are best solved by working one step at a time.

Conclusion & Further Resources

You now have a working Scheme interpreter that implements a large chunk of the standard, including functions, lambdas, lexical scoping, symbols, strings, integers, list manipulation, and assignment. You can use it interactively, with a REPL, or in batch mode, running script files. You can write libraries of Scheme functions and either include them in programs or load them into the interactive interpreter. With a little text processing via `awk` or `sed`, you can format the output of UNIX commands as parenthesized Lisp lists, read them into a Scheme program, and use this interpreter for shell scripting.

There're still a number of features you could add to this interpreter. Hygienic macros let you perform transformations on the source code before it's executed. They're a very convenient feature for adding new language features, and several standard parts of Scheme (such as `let`-bindings and additional control flow features) are defined in terms of them. [Section 4.3](#) of R5RS defines the macro system's syntax and semantics, and there is a [whole collection](#) of papers on implementation. Basically, you'd want to intersperse a function between `readExpr` and `eval` that takes a form and a macro environment, looks for transformer keywords, and then transforms them according to the rules of the pattern language, rewriting variables as necessarily.

Continuations are a way of capturing "the rest of the computation", saving it, and perhaps executing it more than once. Using them, you can implement just about every control flow feature in every major programming language. The easiest way to implement continuations is to transform the program into [continuation-passing style](#), so that `eval` takes an additional continuation argument and calls it, instead of returning a result. This parameter gets threaded through all recursive calls to `eval`, but only is only manipulated when evaluating a call to `call-with-current-continuation`.

Dynamic-wind could be implemented by keeping a stack of functions to execute when leaving the current continuation and storing (inside the continuation data type) a stack of functions to execute when resuming the continuation.

If you're just interested in learning more Haskell, there are a large number of libraries that may help:

- For webapps: [WASH](#), a monadic web framework

- [live version](#)
- [discussion](#)
- [edit](#)
- [comment](#)
- [report an error](#)

- For databases: [HaskellDB](#), a library that wraps SQL as a set of Haskell functions, giving you all the type-safety of the language when querying the database
- For GUI programming: [Fudgets](#) and [wxHaskell](#). wxHaskell is more of a conventional MVC GUI library, while Fudgets includes a lot of new research about how to represent GUIs in functional programming languages
- For concurrency: [Software Transactional Memory](#), described in the paper *Composable Memory Transactions*
- For networking: GHC's [Networking libraries](#)

This should give you a starting point for further investigations into the language. Happy hacking!

Appendix A

Complete Parser

```
module Main where
import Monad
import System.Environment
import Control.Monad.Error
5 import Data.IORef
import Text.ParserCombinators.Parsec hiding (spaces)
import IO hiding (try)

main :: IO ()
10 main = do args <- getArgs
           if null args then runRepl else runOne $ args

symbol :: Parser Char
symbol = oneOf " !$%&|*+ - / : < = ? > @ ^ _ ~ # "
15

readOrThrow :: Parser a -> String -> ThrowsError a
readOrThrow parser input = case parse parser "lisp" input of
    Left err -> throwError $ Parser err
    Right val -> return val
20

readExpr = readOrThrow parseExpr
readExprList = readOrThrow (endBy parseExpr spaces)

spaces :: Parser ()
25 spaces = skipMany1 space

data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
30              | Number Integer
              | String String
              | Bool Bool
              | Port Handle
```

```

        | PrimitiveFunc ([LispVal] -> ThrowsError LispVal
        )
35      | IOFunc ([LispVal] -> IOThrowsError LispVal)
        | Func {params :: [String], vararg :: (Maybe
            String),
            body :: [LispVal], closure :: Env}

parseString :: Parser LispVal
40 parseString = do char '"'
                  x <- many (noneOf "\\")
                  char '"'
                  return $ String x

45 parseAtom :: Parser LispVal
parseAtom = do first <- letter <|> symbol
              rest <- many (letter <|> digit <|> symbol)
              let atom = [first] ++ rest
              return $ case atom of
50                  "#t" -> Bool True
                  "#f" -> Bool False
                  otherwise -> Atom atom

parseNumber :: Parser LispVal
55 parseNumber = liftM (Number . read) $ many1 digit

parseList :: Parser LispVal
parseList = liftM List $ sepBy parseExpr spaces

60 parseDottedList :: Parser LispVal
parseDottedList = do
    head <- endBy parseExpr spaces
    tail <- char '.' >> spaces >> parseExpr
    return $ DottedList head tail

65 parseQuoted :: Parser LispVal
parseQuoted = do
    char '\''
    x <- parseExpr
70    return $ List [Atom "quote", x]

parseExpr :: Parser LispVal
parseExpr = parseAtom
        <|> parseString
75        <|> parseNumber
        <|> parseQuoted
        <|> do char '('
              x <- (try parseList) <|> parseDottedList
              char ')'
80              return x

```



```

showVal :: LispVal -> String
showVal (String contents) = "\"" ++ contents ++ "\""
showVal (Atom name) = name
85 showVal (Number contents) = show contents
showVal (Bool True) = "#t"
showVal (Bool False) = "#f"
showVal (List contents) = "(" ++ unwordsList contents ++ ")"
showVal (DottedList head tail) = "(" ++ unwordsList head ++ "
    . " ++ showVal tail ++ ")"
90 showVal (Port _) = "<IO port>"
showVal (IOFunc _) = "<IO primitive>"
showVal (PrimitiveFunc _) = "<primitive>"
showVal (Func {params = args, vararg = varargs, body = body,
    closure = env}) =
    "(lambda (" ++ unwords (map show args) ++
95     (case varargs of
        Nothing -> ""
        Just arg -> " . " ++ arg) ++ ") ...) "

unwordsList :: [LispVal] -> String
100 unwordsList = unwords . map showVal

instance Show LispVal where show = showVal

eval :: Env -> LispVal -> IOThrowsError LispVal
105 eval env val@(String _) = return val
eval env val@(Number _) = return val
eval env val@(Bool _) = return val
eval env (Atom id) = getVar env id
eval env (List [Atom "quote", val]) = return val
110 eval env (List [Atom "if", pred, conseq, alt]) =
    do result <- eval env pred
    case result of
        Bool False -> eval env alt
        otherwise -> eval env conseq
115 eval env (List [Atom "set!", Atom var, form]) =
    eval env form >>= setVar env var
eval env (List [Atom "define", Atom var, form]) =
    eval env form >>= defineVar env var
eval env (List (Atom "define" : List (Atom var : params) :
    body)) =
120     makeNormalFunc env params body >>= defineVar env var
eval env (List (Atom "define" : DottedList (Atom var : params)
    varargs : body)) =
    makeVarargs varargs env params body >>= defineVar env var
eval env (List (Atom "lambda" : List params : body)) =
    makeNormalFunc env params body
125 eval env (List (Atom "lambda" : DottedList params varargs :
    body)) =
    makeVarargs varargs env params body

```

```

eval env (List (Atom "lambda" : varargs@(Atom _) : body)) =
  makeVarargs varargs env [] body
eval env (List [Atom "load", String filename]) =
130   load filename >=> liftM last . mapM (eval env)
eval env (List (function : args)) = do
  func <- eval env function
  argVals <- mapM (eval env) args
  apply func argVals
135 eval env badForm = throwError $ BadSpecialForm "Unrecognized
  special form" badForm

apply :: LispVal -> [LispVal] -> IOThrowsError LispVal
apply (PrimitiveFunc func) args = liftThrows $ func args
apply (IOFunc func) args = func args
140 apply (Func params varargs body closure) args =
  if num params /= num args && varargs == Nothing
  then throwError $ NumArgs (num params) args
  else (liftIO $ bindVars closure $ zip params args) >=>
    bindVarArgs varargs >=> evalBody
  where remainingArgs = drop (length params) args
145   num = toInteger . length
   evalBody env = liftM last $ mapM (eval env) body
   bindVarArgs arg env = case arg of
     Just argName -> liftIO $ bindVars env [(argName,
       List $ remainingArgs)]
     Nothing -> return env

150 primitives :: [(String, [LispVal] -> ThrowsError LispVal)]
primitives = [("+", numericBinop (+)),
  ("-", numericBinop (-)),
  ("*", numericBinop (*)),
155  ("/", numericBinop div),
  ("mod", numericBinop mod),
  ("quotient", numericBinop quot),
  ("remainder", numericBinop rem),
  ("=", numBoolBinop (==)),
 ("<", numBoolBinop (<)),
160 (">", numBoolBinop (>)),
  ("/=", numBoolBinop (/=)),
 (">=", numBoolBinop (>=)),
 ("<=", numBoolBinop (<=)),
165 ("&&", boolBoolBinop (&&)),
  ("||", boolBoolBinop (||)),
  ("string=?", strBoolBinop (==)),
  ("string?", strBoolBinop (>)),
  ("string<=?", strBoolBinop (<=)),
  ("string>=?", strBoolBinop (>=)),
170  ("car", car),
  ("cdr", cdr),
  ("cons", cons),

```

```

175         ("eq?", eqv),
        ("eqv?", eqv),
        ("equal?", equal)]

numericBinop :: (Integer -> Integer -> Integer) -> [LispVal]
              -> ThrowsError LispVal
numericBinop op singleVal@[_] = throwError $ NumArgs 2
              singleVal
180 numericBinop op params = mapM unpackNum params >>= return .
              Number . foldl1 op

boolBinop :: (LispVal -> ThrowsError a) -> (a -> a -> Bool) ->
           [LispVal] -> ThrowsError LispVal
boolBinop unpacker op args = if length args /= 2
                             then throwError $ NumArgs 2 args
                             else do left <- unpacker $ args
185                                     !! 0
                                     right <- unpacker $ args
                                     !! 1
                                     return $ Bool $ left `op`
                                     right

numBoolBinop = boolBinop unpackNum
190 strBoolBinop = boolBinop unpackStr
    boolBoolBinop = boolBinop unpackBool

unpackNum :: LispVal -> ThrowsError Integer
unpackNum (Number n) = return n
195 unpackNum (String n) = let parsed = reads n in
                           if null parsed
                           then throwError $ TypeMismatch "
                               number" $ String n
                           else return $ fst $ parsed !! 0
unpackNum (List [n]) = unpackNum n
200 unpackNum notNum = throwError $ TypeMismatch "number" notNum

unpackStr :: LispVal -> ThrowsError String
unpackStr (String s) = return s
unpackStr (Number s) = return $ show s
205 unpackStr (Bool s) = return $ show s
    unpackStr notString = throwError $ TypeMismatch "string"
        notString

unpackBool :: LispVal -> ThrowsError Bool
unpackBool (Bool b) = return b
210 unpackBool notBool = throwError $ TypeMismatch "boolean"
    notBool

car :: [LispVal] -> ThrowsError LispVal
car [List (x : xs)] = return x

```

```

car [DottedList (x : xs) _] = return x
215 car [badArg] = throwError $ TypeMismatch "pair" badArg
car badArgList = throwError $ NumArgs 1 badArgList

cdr :: [LispVal] -> ThrowsError LispVal
cdr [List (x : xs)] = return $ List xs
220 cdr [DottedList (_ : xs) x] = return $ DottedList xs x
cdr [DottedList [xs] x] = return x
cdr [badArg] = throwError $ TypeMismatch "pair" badArg
cdr badArgList = throwError $ NumArgs 1 badArgList

225 cons :: [LispVal] -> ThrowsError LispVal
cons [x1, List []] = return $ List [x1]
cons [x, List xs] = return $ List $ [x] ++ xs
cons [x, DottedList xs xlast] = return $ DottedList ([x] ++ xs
) xlast
cons [x1, x2] = return $ DottedList [x1] x2
230 cons badArgList = throwError $ NumArgs 2 badArgList

eqv :: [LispVal] -> ThrowsError LispVal
eqv [(Bool arg1), (Bool arg2)] = return $ Bool $ arg1 == arg2
eqv [(Number arg1), (Number arg2)] = return $ Bool $ arg1 ==
arg2
235 eqv [(String arg1), (String arg2)] = return $ Bool $ arg1 ==
arg2
eqv [(Atom arg1), (Atom arg2)] = return $ Bool $ arg1 == arg2
eqv [(DottedList xs x), (DottedList ys y)] = eqv [List $ xs ++
[x], List $ ys ++ [y]]
eqv [(List arg1), (List arg2)] = return $ Bool $ (length arg1
== length arg2) &&
                                                                    (and $ map
                                                                    eqvPair
                                                                    $ zip
                                                                    arg1
                                                                    arg2)

240 where eqvPair (x1, x2) = case eqv [x1, x2] of
                                                                    Left err -> False
                                                                    Right (Bool val) -> val

eqv [-, -] = return $ Bool False
eqv badArgList = throwError $ NumArgs 2 badArgList

245 data Unpacker = forall a. Eq a => AnyUnpacker (LispVal ->
ThrowsError a)

unpackEquals :: LispVal -> LispVal -> Unpacker -> ThrowsError
Bool
unpackEquals arg1 arg2 (AnyUnpacker unpacker) =
250 do unpacked1 <- unpacker arg1
unpacked2 <- unpacker arg2

```

```

        return $ unpacked1 == unpacked2
    'catchError' (const $ return False)

255 equal :: [LispVal] -> ThrowsError LispVal
    equal [arg1, arg2] = do
        primitiveEquals <- liftM or $ mapM (unpackEquals arg1 arg2
            )
            [AnyUnpacker unpackNum, AnyUnpacker
                unpackStr, AnyUnpacker unpackBool]
        eqvEquals <- eqv [arg1, arg2]
260     return $ Bool $ (primitiveEquals || let (Bool x) =
        eqvEquals in x)
    equal badArgList = throwError $ NumArgs 2 badArgList

data LispError = NumArgs Integer [LispVal]
                | TypeMismatch String LispVal
265         | Parser ParseError
                | BadSpecialForm String LispVal
                | NotFunction String String
                | UnboundVar String String
                | Default String

270 showError :: LispError -> String
    showError (UnboundVar message varname) = message ++ ": " ++
        varname
    showError (BadSpecialForm message form) = message ++ ": " ++
        show form
    showError (NotFunction message func) = message ++ ": " ++ show
        func
275 showError (NumArgs expected found) = "Expected " ++ show
        expected
            ++ " args: found values " ++
                unwordsList found
    showError (TypeMismatch expected found) = "Invalid type:
        expected " ++ expected
            ++ ", found " ++ show
                found
    showError (Parser parseErr) = "Parse error at " ++ show
        parseErr

280 instance Show LispError where show = showError

instance Error LispError where
    noMsg = Default "An error has occurred"
285    strMsg = Default

type ThrowsError = Either LispError

trapError action = catchError action (return . show)
290

```

```

extractValue :: ThrowsError a -> a
extractValue (Right val) = val

flushStr :: String -> IO ()
295 flushStr str = putStr str >> hFlush stdout

readPrompt :: String -> IO String
readPrompt prompt = flushStr prompt >> getLine

300 evalAndPrint :: Env -> String -> IO ()
evalAndPrint env expr = evalString env expr >>= putStrLn

evalString :: Env -> String -> IO String
evalString env expr = runIOThrows $ liftM show $ (liftThrows $
    readExpr expr) >>= eval env
305
until_ :: Monad m => (a -> Bool) -> m a -> (a -> m ()) -> m ()
until_ pred prompt action = do
    result <- prompt
    if pred result
310    then return ()
    else action result >> until_ pred prompt action

runOne :: [String] -> IO ()
runOne args = do
315    env <- primitiveBindings >>= flip bindVars [("args", List
        $ map String $ drop 1 args)]
    (runIOThrows $ liftM show $ eval env (List [Atom "load",
        String (args !! 0)]))
    >>= hPutStrLn stderr

runRepl :: IO ()
320 runRepl = primitiveBindings >>= until_ (== "quit") (readPrompt
    "Lisp>>> ") . evalAndPrint

type Env = IORef [(String, IORef LispVal)]

nullEnv :: IO Env
325 nullEnv = newIORef []

primitiveBindings :: IO Env
primitiveBindings = nullEnv >>= (flip bindVars $ map (makeFunc
    IOFunc) ioPrimitives
    ++ map (makeFunc
        PrimitiveFunc
    ) primitives
    )
330 where makeFunc constructor (var, func) = (var, constructor
    func)

```

```

type IOThrowsError = ErrorT LispError IO

liftThrows :: ThrowsError a -> IOThrowsError a
335 liftThrows (Left err) = throwError err
    liftThrows (Right val) = return val

runIOThrows :: IOThrowsError String -> IO String
runIOThrows action = runErrorT (trapError action) >>= return .
    extractValue

340 isBound :: Env -> String -> IO Bool
isBound envRef var = readIORef envRef >>= return . maybe False
    (const True) . lookup var

getVar :: Env -> String -> IOThrowsError LispVal
345 getVar envRef var = do env <- liftIO $ readIORef envRef
    maybe (throwError $ UnboundVar "
        Getting an unbound variable" var)
        (liftIO . readIORef)
        (lookup var env)

350 setVar :: Env -> String -> LispVal -> IOThrowsError LispVal
setVar envRef var value = do env <- liftIO $ readIORef envRef
    maybe (throwError $ UnboundVar "
        Setting an unbound variable"
        var)
        (liftIO . (flip writeIORef
            value))
        (lookup var env)
355 return value

defineVar :: Env -> String -> LispVal -> IOThrowsError LispVal
defineVar envRef var value = do
    alreadyDefined <- liftIO $ isBound envRef var
360 if alreadyDefined
    then setVar envRef var value >> return value
    else liftIO $ do
        valueRef <- newIORef value
        env <- readIORef envRef
365 writeIORef envRef ((var, valueRef) : env)
        return value

bindVars :: Env -> [(String, LispVal)] -> IO Env
bindVars envRef bindings = readIORef envRef >>= extendEnv
    bindings >>= newIORef
370 where extendEnv bindings env = liftM (++) env) (mapM
    addBinding bindings)
    addBinding (var, value) = do ref <- newIORef value
        return (var, ref)

```

```

makeFunc varargs env params body = return $ Func (map showVal
    params) varargs body env
375 makeNormalFunc = makeFunc Nothing
makeVarargs = makeFunc . Just . showVal

ioPrimitives :: [(String, [LispVal] -> IOThrowsError LispVal)]
ioPrimitives = [("apply", applyProc),
380     ("open-input-file", makePort ReadMode),
     ("open-output-file", makePort WriteMode),
     ("close-input-port", closePort),
     ("close-output-port", closePort),
     ("read", readProc),
385     ("write", writeProc),
     ("read-contents", readContents),
     ("read-all", readAll)]

applyProc :: [LispVal] -> IOThrowsError LispVal
390 applyProc [func, List args] = apply func args
applyProc (func : args) = apply func args

makePort :: IOMode -> [LispVal] -> IOThrowsError LispVal
makePort mode [String filename] = liftM Port $ liftIO $
    openFile filename mode
395

closePort :: [LispVal] -> IOThrowsError LispVal
closePort [Port port] = liftIO $ hClose port >> (return $ Bool
    True)
closePort _ = return $ Bool False

400 readProc :: [LispVal] -> IOThrowsError LispVal
readProc [] = readProc [Port stdin]
readProc [Port port] = (liftIO $ hGetLine port) >>= liftThrows
    . readExpr

writeProc :: [LispVal] -> IOThrowsError LispVal
405 writeProc [obj] = writeProc [obj, Port stdout]
writeProc [obj, Port port] = liftIO $ hPrint port obj >> (
    return $ Bool True)

readContents :: [LispVal] -> IOThrowsError LispVal
readContents [String filename] = liftM String $ liftIO $
    readFile filename
410

load :: String -> IOThrowsError [LispVal]
load filename = (liftIO $ readFile filename) >>= liftThrows .
    readExprList

readAll :: [LispVal] -> IOThrowsError LispVal
415 readAll [String filename] = liftM List $ load filename

```


Appendix B

Answers to Exercises

Section 2.3

Exercise 1

Part 1

```
parseNumber :: Parser LispVal
parseNumber = do x <- many1 digit
               (return . Number . read) x
```

Part 2

In order to answer this question, you need to do a bit of detective work! It is helpful to read up on `do` notation. Using the information there, we can mechanically transform the above answer into the following.

```
parseNumber = many1 digit >>= \x -> (return . Number . read) x
```

This can be cleaned up into the following:

```
parseNumber = many1 digit >>= return . Number . read
```

Exercise 2

We need to create a new parser action that accepts a backslash followed by either another backslash or a doublequote. This action needs to return only the second character.

```
escapedChars :: Parser String
escapedChars = do char '\\' — a backslash
                 x <- oneOf "\\\"" — either backslash or
                 doublequote
                 return [x] — make this character into a
                 string
```

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Once that is done, we need to make some changes to `parseString`.

```
parseString :: Parser LispVal
parseString = do char '"'
               x <- many $ many1 (noneOf "\"\\") <|>
                 escapedChars
               char '"'
               return $ String (concat x)
```

[\[edit section\]](#)

Exercise 3

```
escapedChars :: Parser String
escapedChars = do char '\\',
                 x <- oneOf "\\\"ntr"
                 case x of
                   '\\' -> do return [x]
                   '"' -> do return [x]
                   't' -> do return "\t"
                   'n' -> do return "\n"
                   'r' -> do return "\r"
```

[\[edit section\]](#)

Exercise 4

First, it is necessary to change the definition of `symbol`.

```
symbol :: Parser Char
symbol = oneOf " !$%&|*+ - / : <=> ? @ ^ _ ~ "
```

This means that it is no longer possible to begin an atom with the hash character. This necessitates a different way of parsing `#t` and `#f`.

```
parseBool :: Parser LispVal
parseBool = do string "#"
               x <- oneOf "tf"
               return $ case x of
                 't' -> Bool True
                 'f' -> Bool False
```

This in turn requires us to make changes to `parseExpr`.

```
parseExpr :: Parser LispVal
parseExpr = parseAtom
           <|> parseString
           <|> parseNumber
           <|> parseBool
```

`parseNumber` need to be changed to the following.

```
parseNumber :: Parser LispVal
parseNumber = do num <- parseDigital1 <|> parseDigital2 <|>
                  parseHex <|> parseOct <|> parseBin
                  return $ num
```

And the following new functions need to be added.

```

parseDigital1 :: Parser LispVal
parseDigital1 = do x <- many1 digit
                (return . Number . read) x

parseDigital2 :: Parser LispVal
parseDigital2 = do try $ string "#d"
                  x <- many1 digit
                  (return . Number . read) x

parseHex :: Parser LispVal
parseHex = do try $ string "#x"
             x <- many1 hexDigit
             return $ Number (hex2dig x)

parseOct :: Parser LispVal
parseOct = do try $ string "#o"
             x <- many1 octDigit
             return $ Number (oct2dig x)

parseBin :: Parser LispVal
parseBin = do try $ string "#b"
             x <- many1 (oneOf "10")
             return $ Number (bin2dig x)

oct2dig x = fst $ readOct x !! 0
hex2dig x = fst $ readHex x !! 0
bin2dig = bin2dig' 0
bin2dig' digint "" = digint
bin2dig' digint (x:xs) = let old = 2 * digint + (if x == '0'
                                then 0 else 1) in bin2dig' old xs

```

Exercise 5

[\[edit section\]](#)

```

data LispVal = Atom String
              | List [LispVal]
              | DottedList [LispVal] LispVal
              | Number Integer
              | String String
              | Bool Bool
              | Character Char

parseChar :: Parser LispVal
parseChar = do try $ string "#\\"
              x <- parseCharName <|> anyChar
              return $ Character x

```

```

parseCharName = do x <- try (string "space" <|> string "
  newline")
                    case x of
                      "space" -> do return ' '
                      "newline" -> do return '\n'

```

Note that this does not actually conform to the standard; as it stands, **space** and **newline** must be entirely lowercase; the standard states that they should be case insensitive.

```

parseExpr :: Parser LispVal
parseExpr = parseAtom
  <|> parseString
  <|> try parseNumber — we need the 'try' because
  <|> try parseBool — these can all start with the hash
    char
  <|> try parseChar

```

Appendix C

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