# Natural Language Processing

Lecture 12: Lexical Semantics (part I) - Word Representations and Word Embeddings.

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COMS W4705
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### Jabberwocky

Can you identify what the words in this poem mean?



Beware the jabberwock, my son the jaws that bite, the claws that catch!

Beware the jubjub bird, and the frumious bandersnatch!

"Jabberwocky", Lewis Carroll, 1871

# Semantic Similarity and Relatedness

- We can often tell that two words are similar or related, even if they aren't exact synonyms.
- "fast" is similar to "rapid" and "speed"
- "tall" is similar to "high" and "height"
- Question answering:
  - Q: "How tall is Mt. Everest?"
  - Candidate A: "The official height of Mount Everest is 29029 feet"

#### Relatedness

- "cat" is more similar to "dog" than to "table"
- "table" is more similar to "chair" than to "dog"
- "run" is more similar to "fly" than to "think".
- "cat" is more similar to "meow" than to "bark".

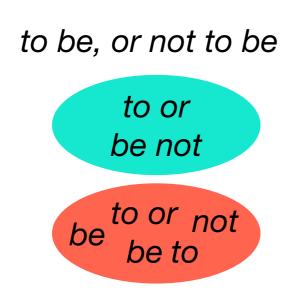
#### Supervised Learning for WSD

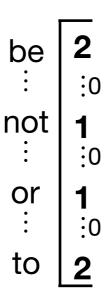
• Given: Training data consisting of training examples  $(\mathbf{x_1}, y_1), \dots, (\mathbf{x_n}, y_n)$ , where  $\mathbf{x_i}$  is an input example (a d-dimensional vector of attribute values) and  $y_i$  is the label.

	label				
1	X <sub>11</sub>	X <sub>12</sub>	•••	X <sub>1d</sub>	<b>y</b> 1
	• • •	•••	•••	•••	• • •
i	X <sub>i1</sub>	X <sub>i</sub> 2	•••	X <sub>id</sub>	Уi
	•••	•••	•••	•••	• • •
n	$x_{n1}$	$x_{n2}$	• • •	X <sub>nd</sub>	Уn

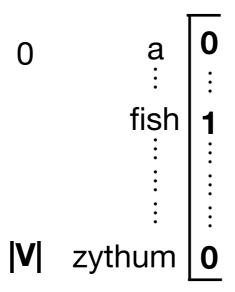
- Goal: learn a hypothesis function h(x) that approximates the true relationship between x and y.
- For many NLP problems the attributes contain words (in a specific position etc ...)
- How do we represent words in a vector?

# Document representation: Bag-of-Words features





# Single Word Representation: One-Hot Vector



What about unseen words?

#### Unknown Words

A bottle of **tesgüino** is on the table.

Everybody likes tesgüino.

Tesgüino makes you drunk.

We make tesgüino out of corn.

Example from Nida, 1975.

- Can you figure out from context what tesgüino means?
  - Some kind of alcoholic beverage, maybe beer or whisky.
- Intuition: Two words should be similar if they have similar typical word contexts.

How would you represent context?

### Distributional Hypothesis

- Wittgenstein ("Philosophical Investigations):
- "the meaning of a word is in its use in the language"
  - Zelig Harris (1954):
- "oculist and eye-doctor ... occur in almost the same environments"
- "If A and B have almost identical environments we say that they are synonyms."

- J.R. Firth (1957)
- "you shall know a word by the company it keeps!"

#### Co-occurence Matrix

	0	Ш	*	ф	<u></u>	分
$\mathfrak{R}$	51	20	84	0	3	0
	52	58	4	4	6	26
	115	89	10	42	33	17
0	59	39	23	4	0	0
*•*	98	14	6	2	1	0
*	12	17	3	2	9	27
$\bigcirc$	11	2	2	0	18	0

 $sim(\boxtimes, \mathbb{X}) = 0.770$   $sim(\boxtimes, *_*) = 0.939$  $sim(\boxtimes, \triangle) = 0.961$ 

- Numbers are co-occurence counts (how often the symbols appear together in context).
- Which symbol is most similar to ⊠?

### What it really looks like

	get	see	use	hear	eat	kill
knife	51	20	84	0	3	0
cat	52	58	4	4	6	26
dog	115	89	10	42	33	17
boat	59	39	23	4	0	0
cup	98	14	6	2	1	0
pig	12	17	3	2	9	27
berry	11	2	2	0	18	0

sim(dog,knife) = 0.770 sim(dog,boat) = 0.939sim(dog,cat) = 0.961

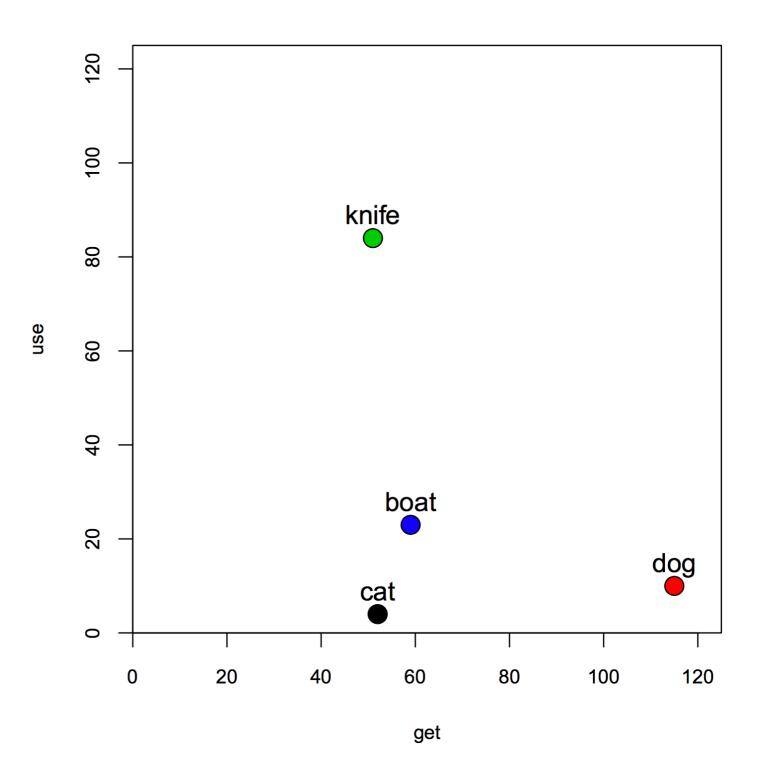
Verb-Object counts

- Row vector x<sub>dog</sub> describes usage of dog as a grammatical object in the corpus.
- Can be seen as coordinates in n-dimensional Euclidean space.

### Geometric Interpretation

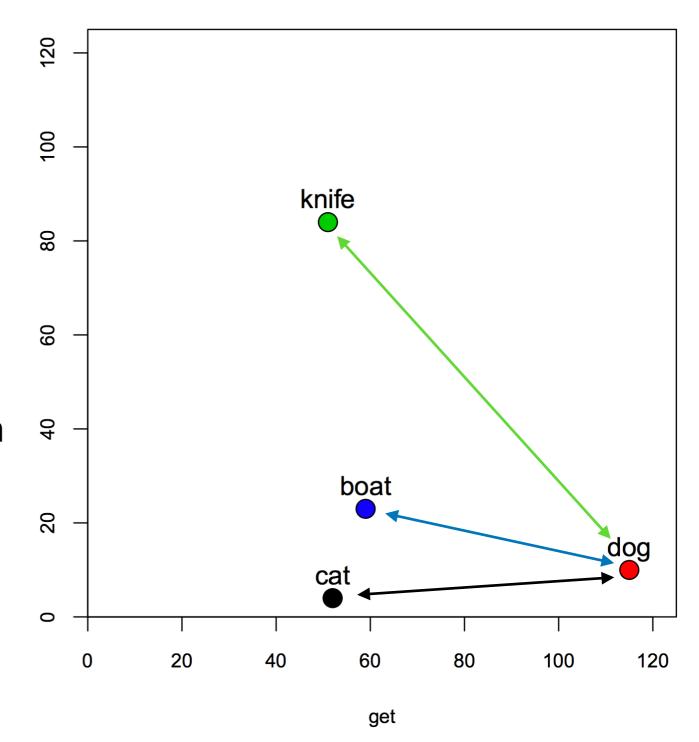
- Row vector x<sub>dog</sub> describes usage of dog in the corpus.
- Can be seen as coordinates in n-dimensional Euclidean space.
- Illustrated for two dimensions "get" and "use".

$$x_{dog} = (115, 10)$$



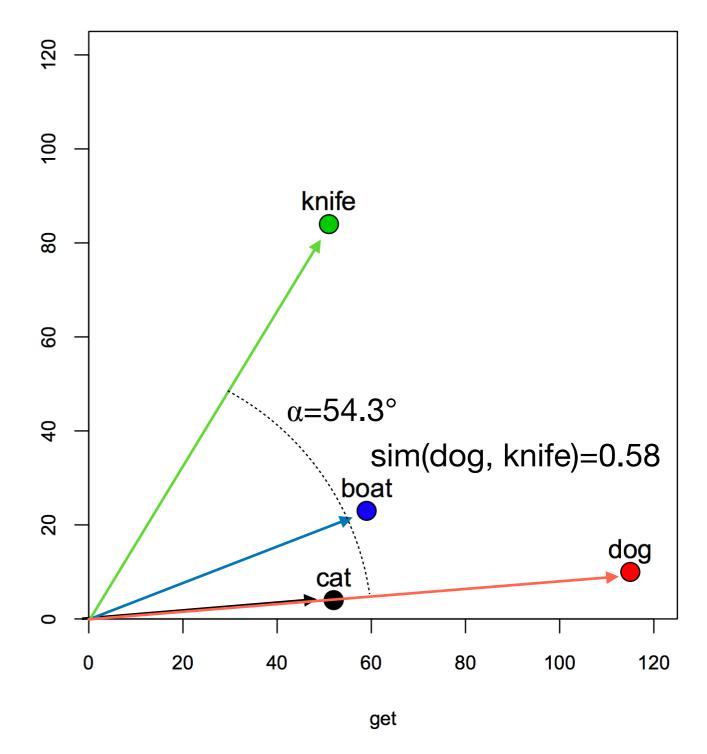
### Geometric Interpretation

- How should we compute similarity?
  - First approach: Spatial distance between words.
  - (lower distance = higher similarity)
  - Potential problem: location depends on frequency of noun count(dog) ≈ 2.7 count(cat)



### Geometric Interpretation

- How should we compute similarity?
  - Second approach:
    - Direction is more important than location.
    - Normalize "length" ||x<sub>dog</sub>|| of <sup>§</sup> vector.
    - or use angle  $\alpha$  as distance measure (or cos of these angles).



# Cosine Similarity

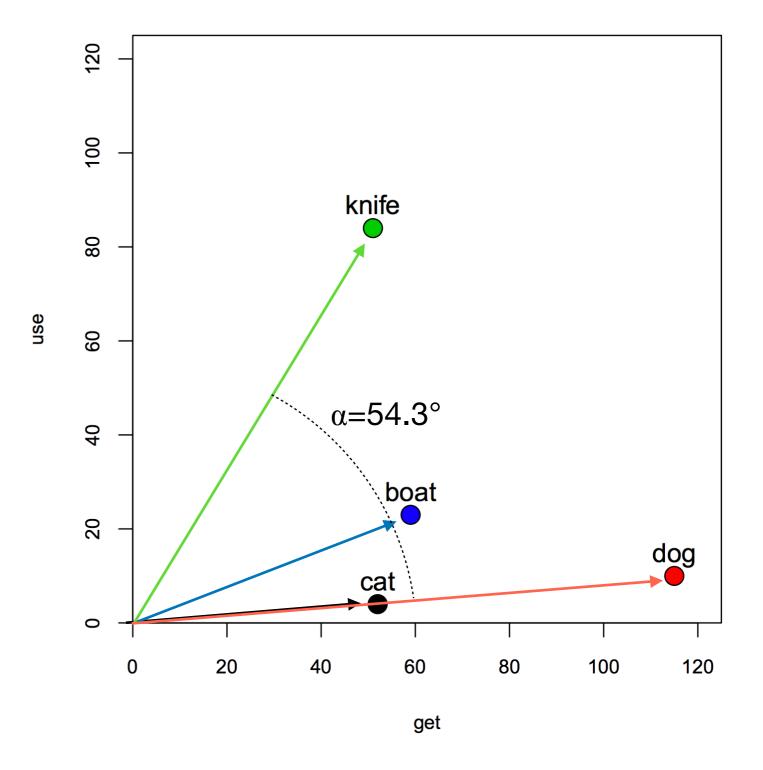
$$sim_{cos}(\mathbf{x},\mathbf{y}) = rac{\mathbf{x}\cdot\mathbf{y}}{\left|\mathbf{x}
ight|_2\cdot\left|\mathbf{y}
ight|_2} = rac{\sum_i x_i\cdot y_i}{\sqrt{\sum_i x_i^2}\sqrt{\sum_i y_i^2}}$$

Colinear vectors (same direction):

$$sim_{cos}(\mathbf{x},\mathbf{y})=1$$

Orthogonal vectors (90° angle, no shared attributes):

$$sim_{cos}(\mathbf{x},\mathbf{y})=0$$

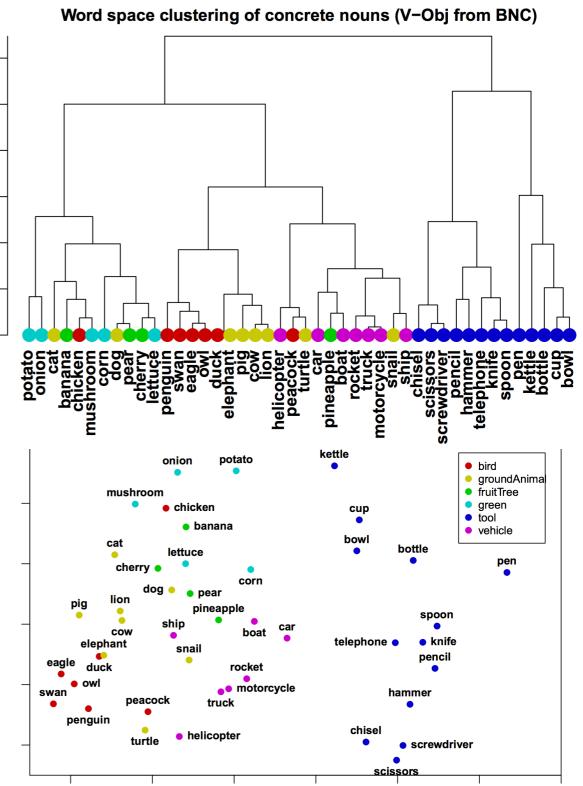


# What to do with DSM similarities

- Most similar to dog (cos similarities):
  horse(47.0), wife (48.8), baby (51.9), daughter (53.1), side (54.9), mother (55.6), boat (55.7), rest (56.3), night (56.7), cat (56.8), son (57.0), man (58.2), place (58.4), husband (58.5), thing (58.8), friend (59.6), . . .
- Most similar to school: country (49.3), church (52.1), hospital (53.1), house (54.4), hotel (55.1), industry (57.0), company (57.0), home (57.7), family (58.4), university (59.0), party (59.4), group (59.5), building (59.8), market (60.3), bank (60.4), business (60.9), area (61.4), department (61.6), club (62.7), town (63.3), library (63.3), room (63.6), service (64.4), police (64.7),...

# Clustering and Semantic Maps

- Distributional Similarity/Distance can be used to
  - find nearest neighbors (similar words)
  - cluster related words into hierarchical categories.
  - construct semantic maps.



### Variations of Distributional Semantic Models

- A Distributional Semantic Model (DSM) is any matrix M such that each row represents the distribution of a term x across contexts, together with a similarity measurement.
- The previous example shows one particular semantic space (frequency counts of Verb-object co-occurences).
- There are many different models we could choose.
- Different models might capture different "types" of similarity.

### Dimensions of Distributional Semantic Models

- 1. Preprocessing, definition of "terms" (word form, lemmas, POS, ...).
- 2. Context definition:
  - Type of context (word, syntactic dependents (with or without relation labels labels), remove stop-words, etc.)
  - Size of context window.
- 3. Feature scaling / term weighting (association measures).
- 4. Normalization of rows / columns.
- 5. Dimensionality reduction.
- 6. Similarity measure.

# Semantic Similarity vs. Relatedness

- Semantic Relatedness (syntagmatic relatedness)
  - Words that occur nearby each other, but are not necessarily similar.
  - function (car-drive), meronymy (car-tire), location (car-road), attribute (car-fast), other (car-gas.)
- Semantic Similarity (paradigmatic relatedness)
  - Can typically substitute one word for another.
  - synonyms (car–automobile), hypernyms (car-vehicle), sibling-hyponyms (car–truck–van–bike).

How would you define distributional context to capture each type of similarity?

#### Effect of context size

Nearest neighbors of dog

#### 2-word window:

cat, horse, fox, pet, rabbit, pig, animal, mongrel, sheep, pigeon

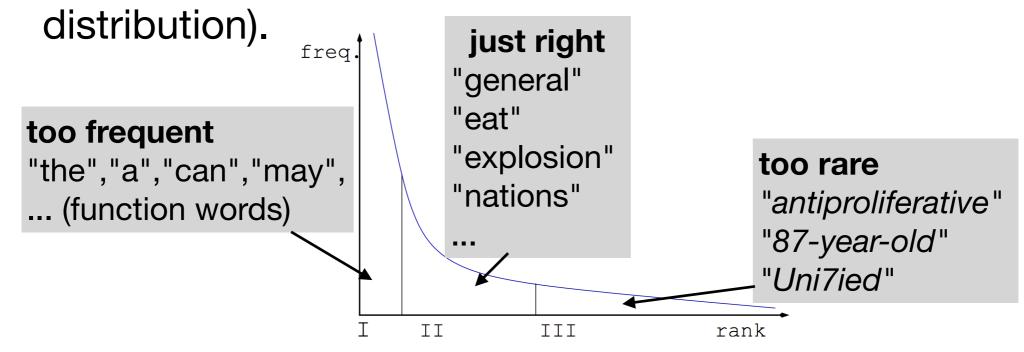
#### 30-word window:

kennel, puppy, pet, bitch, terrier, rottweiler, canine, cat, to bark, Alsatian

# Term Weighting

 Problem: Not all context terms are equally relevant to characterize the meaning of a word.

Some appear too often, some are too rare (Zipfian



 One solution: TF\*IDF (term frequency \* inverse-document frequency)

#### TF\*IDF

- Originates in document retrieval (find document relevant to a keyword). For DSM: 'document' = target word d.
- Term frequency: How often does the term t appear in the context window of the target word?

$$tf_{t,d} = count(d,t)$$

 Inverse document frequency: For how many words does t appear in the context window

$$idf_{t,D} = log rac{|D|}{|\{d \in D, count(d,t) > 0\}|}$$

• TF\*IDF:

$$tf_{t,d} \cdot idf_{t,D}$$

#### Sparse vs. Dense Vectors

- Full co-occurrence matrix is very big and contains a lot of 0 entries.
  - Potentially inconvenient to store. Slow computation.
  - Synonyms may still contain orthogonal dimensions, which are irrelevant.
- Word embeddings are representations of words in a low-dimensional, dense vector space. There are two main approaches:
  - Use matrix decomposition on co-occurence matrix, for example Singular Value Decomposition (SVD).
  - Learn embeddings using neural networks. Minimal featureengineering required.

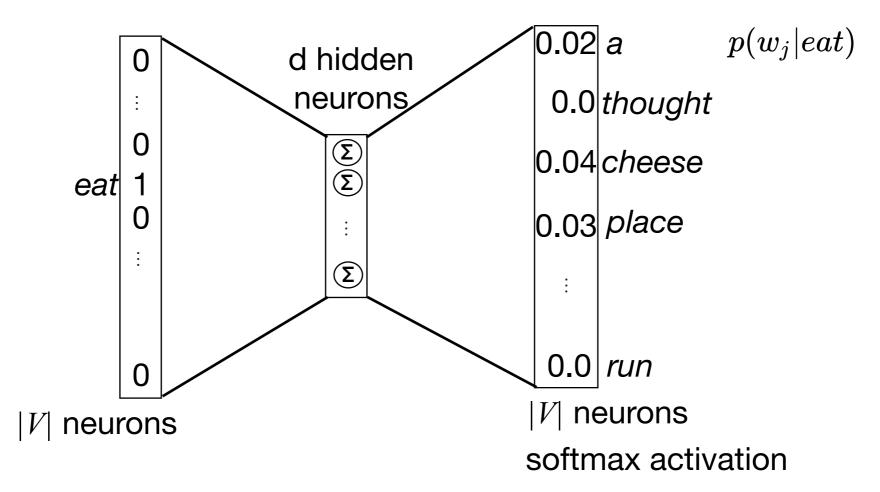
# Learning Word Embeddings with Neural Networks

- The neural network should capture the relationship between a word and its context.
- Two models: (Word2Vec, Mikolov et al. 2013)
  - Skip-Gram model: Input is a single word.
     Predict a probability for each context word.
  - Continuous bag-of-words (BOW):
     Input is a representation of the context window.

     Predict a probability for each target word.
- Inspired by Neural Language Models (Bengio et al. 2003)

# Skip-Gram Model

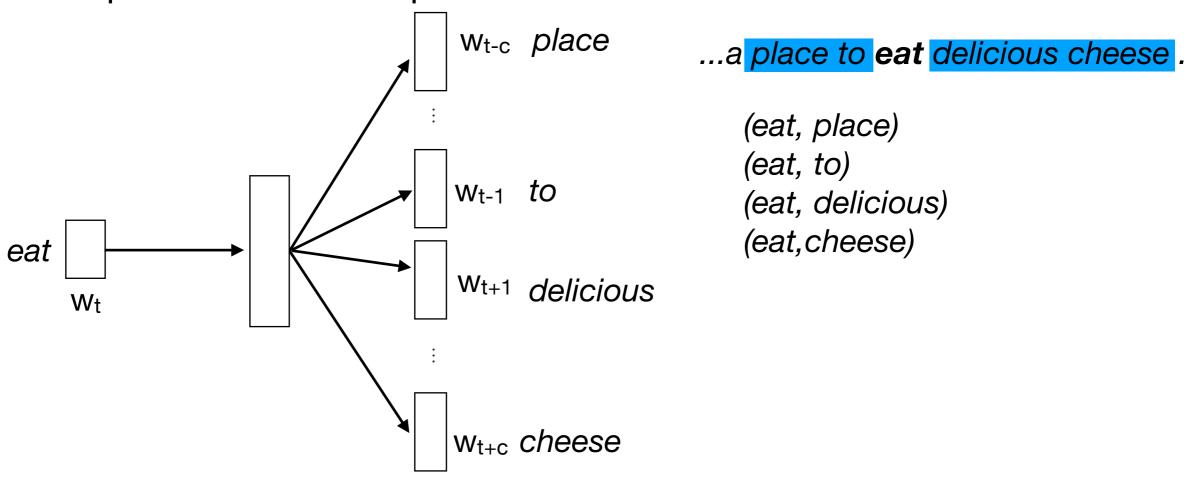
- Input:
   A single word in one-hot representation.
- Output: probability to see any single word as a context word.



Softmax function normalizes the activation of the output neurons to sum up to 1.0.

# Skip-Gram Model

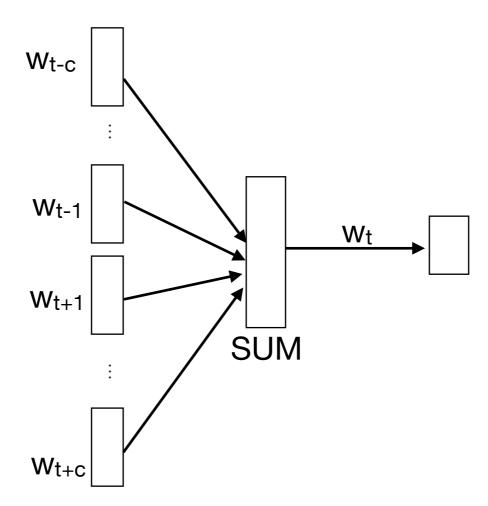
Compute error with respect to each context word.



 Combine errors for each word, then use combined error to update weights using back-propagation.

$$error = -\sum_{i=-c, i 
eq 0}^c \log p(w_{t+i}|w_t)$$

# Continuous Bag-of-Words Model (CBOW)

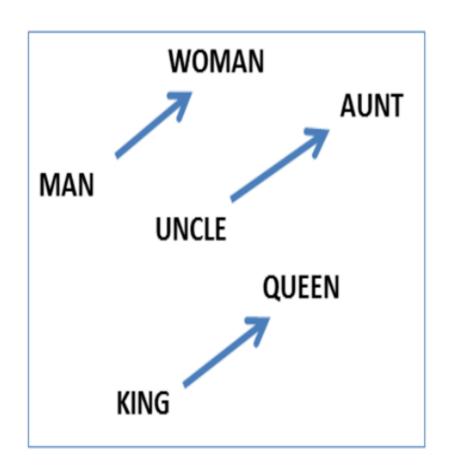


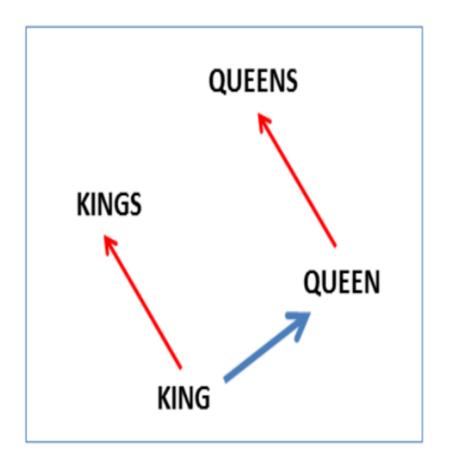
- Input: Context words. Averaged in the hidden layer.
- Output: Probability that each word is the target word.

# Embeddings are Magic

(Mikolov 2016)

vector('king') - vector('man') + vector('woman') ≈ vector('queen')





# Application: Word Pair Relationships

Table 8: Examples of the word pair relationships, using the best word vectors from Table 4 (Skipgram model trained on 783M words with 300 dimensionality).

Relationship	Example 1	Example 2	Example 3	
France - Paris	Italy: Rome	Japan: Tokyo	Florida: Tallahassee	
big - bigger	small: larger	cold: colder	quick: quicker	
Miami - Florida	Baltimore: Maryland	Dallas: Texas	Kona: Hawaii	
Einstein - scientist	Messi: midfielder	Mozart: violinist	Picasso: painter	
Sarkozy - France	Berlusconi: Italy Merkel: Germa		Koizumi: Japan	
copper - Cu	zinc: Zn	gold: Au	uranium: plutonium	
Berlusconi - Silvio	Sarkozy: Nicolas	Putin: Medvedev	Obama: Barack	
Microsoft - Windows	Google: Android	IBM: Linux	Apple: iPhone	
Microsoft - Ballmer	Google: Yahoo	IBM: McNealy	Apple: Jobs	
Japan - sushi	Germany: bratwurst	France: tapas	USA: pizza	

### Using Word Embeddings

- Word2Vec:
  - https://code.google.com/archive/p/word2vec/
- GloVe: Global Vectors for Word Representation
  - https://nlp.stanford.edu/projects/glove/
- Can either use pre-trained word embeddings or train them on a large corpus.

# Acknowledgments

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