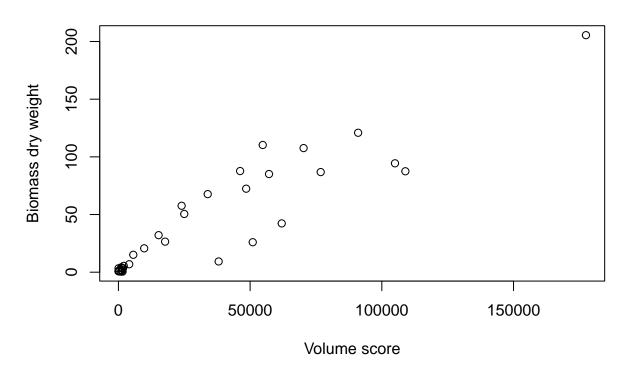
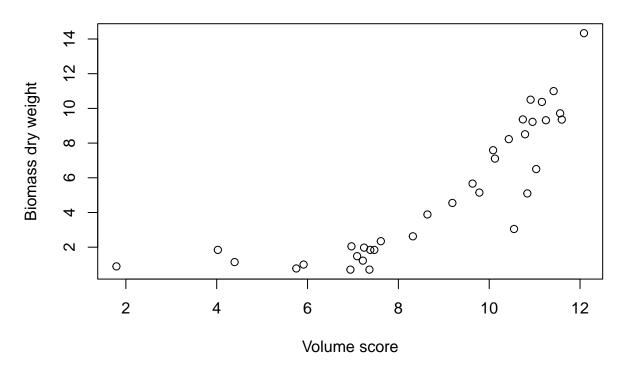
Initialization

```
knitr::opts_chunk$set(echo = TRUE)
dw<-read.table("dryweight.txt",header=T)</pre>
attach(dw)
## The following objects are masked from dw (pos = 13):
##
##
      dryweight, volume
## The following objects are masked from dw (pos = 14):
##
##
      dryweight, volume
# the entire table
#dw
# the independent/dependent variables
#volume
#dryweight
# volume is independent/predictor, dryweight is dependent
# volume is X, dryweight is Y
# volume score is volume of space occupied by the plant (in this case grass)
# Biomass dry weight is biomass dry weights for grass
plot(volume, dryweight, xlab="Volume score", ylab="Biomass dry weight",main="Volume
```

Volume scores vs. Biomass dry weights for grass



X = In(volume+1) vs. Y = sqrt(dryweight)



Fitting a linear model

```
fitlinear<-lm(Y~ X)
summary(fitlinear)</pre>
```

```
##
## Call:
## lm(formula = Y ~ X)
##
## Residuals:
      Min
               1Q Median
                               ЗQ
                                      Max
## -4.3918 -1.4560 -0.4075 1.1055
                                   4.8836
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -6.3281
                           1.3226
                                   -4.784 3.48e-05 ***
## X
                 1.3055
                           0.1446
                                    9.028 1.96e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.109 on 33 degrees of freedom
## Multiple R-squared: 0.7118, Adjusted R-squared: 0.7031
## F-statistic: 81.5 on 1 and 33 DF, p-value: 1.964e-10
```

```
step(fitlinear)
## Start: AIC=54.18
## Y ~ X
##
##
    Df Sum of Sq RSS
                            AIC
## <none> 146.78 54.177
## - X 1 362.53 509.32 95.720
## Call:
## lm(formula = Y ~ X)
## Coefficients:
## (Intercept)
     -6.328 1.306
##
Fitting a quadratic model
fitqr < -lm(Y \sim X + I(X^2))
summary(fitqr)
##
## Call:
## lm(formula = Y \sim X + I(X^2))
##
## Residuals:
            1Q Median
                       3Q
## -4.5032 -0.5126 0.2398 0.7353 2.4362
##
## Coefficients:
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.12914 1.95059 2.630 0.013032 *
           ## I(X^2)
            ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.397 on 32 degrees of freedom
## Multiple R-squared: 0.8774, Adjusted R-squared: 0.8697
## F-statistic: 114.5 on 2 and 32 DF, p-value: 2.608e-15
step(fitqr)
## Start: AIC=26.26
## Y \sim X + I(X^2)
```

AIC

Df Sum of Sq RSS

##

```
## <none> 62.446 26.263
## - X 1 30.196 92.642 38.069
## - I(X^2) 1 84.339 146.785 54.177

##
## Call:
## lm(formula = Y ~ X + I(X^2))
##
## Coefficients:
## (Intercept) X I(X^2)
## 5.1291 -2.0327 0.2145
```

Fitting a cubic model

```
fitcb<-lm(Y \sim X + I(X^2) + I(X^3))
summary(fitcb)
##
## Call:
## lm(formula = Y \sim X + I(X^2) + I(X^3))
## Residuals:
      Min
              1Q Median
                              ЗQ
                                     Max
## -4.2373 -0.2723 0.1035 0.7331 2.0993
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.31177 3.36006 0.093 0.9267
## X
              0.80114
                         1.70856 0.469 0.6424
## I(X^2)
             -0.23871 0.26315 -0.907 0.3713
## I(X^3)
              0.02138
                         0.01232 1.735 0.0927 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.355 on 31 degrees of freedom
## Multiple R-squared: 0.8882, Adjusted R-squared: 0.8774
## F-statistic: 82.13 on 3 and 31 DF, p-value: 7.621e-15
```

Backwards elimination for cubic model

```
#1. Fit the model with predictors (initial is all predictors)
#2. Find the predictor with the highest p-value
#3. If the predictor with the highest p-value has p-value > alpha, then remove that

$\to$ predictor

#4. Repeat to step 1. Or if all p-values are less than the alpha, then backwards

$\to$ elimination is complete.
```

```
# Using significance level alpha = 0.05,
# Also, will not be removing the intercept for the backwards elimination for now
# removing predictor X
fitcb2 < -lm(Y \sim I(X^2) + I(X^3))
summary(fitcb2)
##
## Call:
## lm(formula = Y \sim I(X^2) + I(X^3))
## Residuals:
      Min
             1Q Median
                               3Q
## -4.3041 -0.3511 0.2547 0.7649 2.0704
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.80585 1.05325
                                   1.715 0.0961 .
## I(X^2)
              -0.11733
                          0.04669 -2.513 0.0172 *
## I(X^3)
              0.01585
                          0.00357 4.440 0.0001 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.338 on 32 degrees of freedom
## Multiple R-squared: 0.8875, Adjusted R-squared: 0.8804
## F-statistic: 126.2 on 2 and 32 DF, p-value: 6.629e-16
# Backwards regression shows Y ~ I(X^2) + I(X^3) is best model
```

Stepwise regression for cubic model

```
step(fitcb)
```

```
## Start: AIC=25.02
## Y \sim X + I(X^2) + I(X^3)
           Df Sum of Sq
                           RSS
                                  AIC
           1 0.4037 57.323 23.267
## - X
## - I(X^2) 1
               1.5109 58.430 23.937
## <none>
                        56.919 25.020
## - I(X^3) 1
                5.5267 62.446 26.263
## Step: AIC=23.27
## Y \sim I(X^2) + I(X^3)
##
##
           Df Sum of Sq
                           RSS
## <none>
                        57.323 23.267
## - I(X^2) 1
                11.312 68.636 27.571
## - I(X^3) 1 35.319 92.642 38.069
```

```
##
## Call:
## lm(formula = Y ~ I(X^2) + I(X^3))
##
## Coefficients:
## (Intercept) I(X^2) I(X^3)
## 1.80585 -0.11733 0.01585

# Stepwise regression shows Y ~ I(X^2) + I(X^3) is best model
```

Fitting regression model with 4th degree polynomial

```
fit4d < -lm(Y \sim X + I(X^2) + I(X^3) + I(X^4))
summary(fit4d)
##
## Call:
## lm(formula = Y \sim X + I(X^2) + I(X^3) + I(X^4))
##
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -4.2659 -0.2809 0.0574 0.6924 2.0783
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                                               0.937
## (Intercept) -0.5233379 6.5245497 -0.080
              1.5063707 5.0058940
                                      0.301
                                               0.766
## I(X^2)
              -0.4204591 1.2392220 -0.339
                                               0.737
## I(X^3)
               0.0398440 0.1235873
                                      0.322
                                               0.749
## I(X^4)
              -0.0006484 0.0043170 -0.150
                                               0.882
##
## Residual standard error: 1.377 on 30 degrees of freedom
## Multiple R-squared: 0.8883, Adjusted R-squared: 0.8734
## F-statistic: 59.66 on 4 and 30 DF, p-value: 7.504e-14
step(fit4d)
## Start: AIC=26.99
## Y ~ X + I(X^2) + I(X^3) + I(X^4)
##
##
           Df Sum of Sq
                           RSS
                                   AIC
## - I(X^4) 1 0.042773 56.919 25.020
            1 0.171677 57.048 25.099
## - X
## - I(X^3) 1 0.197056 57.074 25.115
## - I(X^2) 1 0.218254 57.095 25.128
## <none>
                        56.877 26.994
##
```

Step: AIC=25.02

Y ~ X + $I(X^2)$ + $I(X^3)$

```
##
##
           Df Sum of Sq
                            RSS
                                   AIC
## - X
           1
                  0.4037 57.323 23.267
## - I(X^2) 1
                  1.5109 58.430 23.937
## <none>
                         56.919 25.020
## - I(X^3) 1
                  5.5267 62.446 26.263
##
## Step: AIC=23.27
## Y ~ I(X^2) + I(X^3)
##
            Df Sum of Sq
                            RSS
                                   AIC
                         57.323 23.267
## <none>
## - I(X^2) 1
                  11.312 68.636 27.571
## - I(X^3) 1
                  35.319 92.642 38.069
##
## Call:
## lm(formula = Y \sim I(X^2) + I(X^3))
##
## Coefficients:
                                  I(X^3)
## (Intercept)
                     I(X^2)
       1.80585
                   -0.11733
                                 0.01585
# Stepwise regression still says Y ~ I(X^2) + I(X^3) is best model.
# Then, the best model is from the 3rd degree polynomial.
```

Forcing origin to be 0

```
fit_best_model_no_origin<-lm(Y ~ 0 + I(X^2) + I(X^3))
summary(fit_best_model_no_origin)</pre>
```

```
##
## lm(formula = Y \sim 0 + I(X^2) + I(X^3))
##
## Residuals:
       Min
                1Q Median
                                ЗQ
                                       Max
## -4.4318 -0.4201 0.2784 0.9998 2.1299
##
## Coefficients:
           Estimate Std. Error t value Pr(>|t|)
## I(X^2) -0.044332
                      0.019720 -2.248
                                       0.0314 *
## I(X<sup>3</sup>) 0.010580
                      0.001866
                                5.670 2.55e-06 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.377 on 33 degrees of freedom
## Multiple R-squared: 0.9567, Adjusted R-squared: 0.9541
## F-statistic: 364.5 on 2 and 33 DF, p-value: < 2.2e-16
```

step(fit_best_model_no_origin)

```
## Start: AIC=24.34
## Y \sim 0 + I(X^2) + I(X^3)
##
          Df Sum of Sq RSS AIC
## <none>
                         62.589 24.344
## - I(X^2) 1
                 9.586 72.175 27.331
## - I(X^3) 1 60.977 123.566 46.150
##
## Call:
## lm(formula = Y \sim 0 + I(X^2) + I(X^3))
## Coefficients:
## I(X^2) I(X^3)
## -0.04433 0.01058
# It does not make sense to force the origin to be zero. Stepwise regression shows that
\rightarrow the model with the intercept included has a better fit to the the data.
# However, if you decide to force the origin to be zero, the model is still a great
\rightarrow fitting model. The fit to the data will definitely still be satisfactory if the
→ origin is forced to be zero.
```