

Lab8B : RDD, FE and DID

Introduction to Econometrics, Fall 2020

Yi Wang

Nanjing University

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Section 1

RDD in Stata

Subsection 1

Review the Theory

- Review the Theory : Summary

In a Summary

RDD in the toolkit of Causal Inference

- It is so called the **nearest** method to RCT which identify causal effect of treatment on outcome.
- RDD needs a arbitrary cut-off and agents can **imperfect** manipulate the treatment.
- Two types
 - Sharp RD
 - Fuzzy RD
- Assumption: continued at the cut-off
- Concerns:
 - Functional form
 - Bandwidth selection
 - Bin selection

- Review the Theory : Main idea

Causal Inference and Regression Discontinuity Design

Main Idea of Regression Discontinuity Design

- Regression Discontinuity Design (RDD) exploits the facts that:
 - Some rules are *arbitrary* and generate a *discontinuity* in treatment assignment.
 - The treatment assignment is determined based on whether a unit exceeds some threshold on a variable (**assignment variable**, **running variable** or **forcing variable**)
 - Assume other factors *do NOT change* abruptly at threshold.
 - Then any change in outcome of interest can be attributed to the assigned treatment.

- Review the Theory : Two types

RDD: Theory and Application

Sharp RDD and Fuzzy RDD

- In general, depending on enforcement of treatment assignment, RDD can be categorized into two types:
 - 1 Sharp RDD:** nobody below the cutoff gets the “treatment”, everybody above the cutoff gets it
 - Everyone follows treatment assignment rule (all are compliers).
 - Local randomized experiment with perfect compliance around cutoff.
 - 2 Fuzzy RDD:** the probability of getting the treatment jumps discontinuously at the cutoff (NOT jump from 0 to 1)
 - Not everyone follows treatment assignment rule.
 - Local randomized experiment with partial compliance around cutoff.
 - Using initial assignment as an instrument for actual treatment.

- Review the Theory : Assumption

- **Deterministic Assumption**

$$D_i = 1(X_i \geq c)$$

- Treatment assignment is a deterministic function of the assignment variable X_i and the threshold c .

- **Continuity Assumption**

- $E[Y_{1i}|X_i]$ and $E[Y_{0i}|X_i]$ are continuous at $X_i = c$
 - Assume potential outcomes do not change at cutoff.
 - This means that except treatment assignment, all other unobserved determinants of Y_i are continuous at cutoff c .
 - This implies no other confounding factor affects outcomes at cutoff c .
 - Any observed discontinuity in the outcome can be attributed to treatment assignment.

- Review the Theory : Identification in Sharp RD

RDD: Theory and Application

Sharp RDD specification

- A simple RD regression is

$$Y_i = \alpha + \rho D_i + \gamma(X_i - c) + u_i$$

- Y_i is the outcome variable
 - D_i is the treatment variable (independent variable)
 - X_i is the running variable
 - c is the value of cut-off
 - u_i is the error term including other factors
- Question:** Which parameter do we care about the most?

- Review the Theory : Identification in Sharp RD

- More generally, we could also estimate two separate regressions for each side respectively.

$$Y_i^b = \beta^b + f(X_i^b - c) + u_i^b$$
$$Y_i^a = \beta^a + g(X_i^a - c) + u_i^a$$

- Can do all in one step; just use all the data at once and estimate:

$$Y_i = \alpha + \rho D_i + f(X_i - c) + D_i \times h(X_i - c) + u_i$$

where D_i is a dummy variable for treated status.

- Review the Theory : Identification in Fuzzy RD

- Encourage Variable:

$Z_i = 1$ if assign to treatment group

$Z_i = 0$ if assign to control group

- Then the **First Stage** of FRD regression:

$$P(D_i = 1|x_i) = \alpha_1 + \phi Z_i + f(x_i - c) + Z_i \times g(x_i - c) + \eta_{1i}$$

- The **second stage** regression is

$$Y_i = \alpha_2 + \delta \hat{D}_i + f(x_i - c) + \hat{D}_i \times g(x_i - c) + \eta_{2i}$$

- The **reduced form** regression in FRD is

$$Y_i = \alpha_3 + \beta Z_i + f(x_i - c) + Z_i \times g(x_i - c) + \eta_{3i}$$

Subsection 2

Introduction : Package & Commands

- Introduction : Package & Commands

- ▶ Package : [Install Link](#)
- ▶ **rdrobust** package : inference and graphical procedures using local polynomial and partitioning regression methods.
 - ★ *-rdrobust-* : Local Polynomial Regression Discontinuity Estimation with Robust Bias-Corrected Confidence Intervals and Inference Procedures.
 - ★ *-rdbwselect-* : Data-driven Bandwidth Selection,
 - ★ *-rdplot-* : Data-Driven Regression Discontinuity Plots.
- ▶ **rddensity** package : manipulation testing using local polynomial density methods.
- ▶ **Others** : *-cmogram-* ; *-rd-* ; *-rdcv-* ; *-DCdensity-* ; ...

Subsection 3

Example for Sharp RDD

- Example for Sharp RDD

- ▶ Data : the dataset comes from a study on **party advantages** in **U.S. Senate elections** for the period 1914–2010.
- ▶ We focus here on the RD effect of **the Democratic party winning a U.S. Senate seat** on **the vote share obtained in the following election for that same seat**.
- ▶ The unit of observation is the **state**.
- ▶ Main variables :
 - ★ *demmv* : ranges from -100 to 100 and records the Democratic party's margin of victory in the statewide election for a given U.S. Senate seat (the vote share of the Democratic party – the vote share of its strongest opponent).
 - ★ *demvotesfor2* : ranges from 0 to 100 and records the Democratic vote share in the following election for the same seat.
- ▶ To estimate the **incumbency advantage of parties** with an RD design.

RDD in Stata

- Example for Sharp RDD

- ▶ Re-labeling the three main variables

```
. use senate, clear
```

```
. sum
```

Variable	Obs	Mean	Std. Dev.	Min	Max
state	1,390	40.01367	21.99304	1	82
year	1,390	1964.63	28.05466	1914	2010
dopen	1,380	.2471014	.4314826	0	1
population	1,390	3827919	4436950	78000	3.73e+07
presdemvot_1	1,387	46.11975	14.31701	0	97.03408
demmv	1,390	7.171159	34.32488	-100	100
demvoteshl_1	1,349	52.69048	18.2706	0	100
demvoteshl_2	1,308	52.86918	18.23913	0	100
demvoteshf_1	1,341	52.41856	18.36641	0	100
demvoteshf_2	1,297	52.66627	18.12219	0	100
demwinprv1	1,349	.5441067	.4982355	0	1
demwinprv2	1,308	.543578	.4982879	0	1
dmidterm	1,390	.5136691	.4999993	0	1
dpresdem	1,390	.3884892	.4875822	0	1

- Example for Sharp RDD

- ▶ Re-labeling the three main variables

- ★ Assignment variable (running variable) : X
 - ★ Outcome variable: Y
 - ★ Treatment variable : T
 - ★ Threshold (cutoff) for treatment assignment : $c=0$

- Example for Sharp RDD

- ▶ Re-labeling the three main variables

```
. rename demmv X           //X--民主党获胜的差额
. rename demvoteshfor2 Y    //Y--t+2期民主党得票数

. gen T=.
. replace T=0 if X<0 & X!=.
. replace T=1 if X>=0 & X!=.
/* the Democratic party wins the election for that seat.*/

. label var T "Democratic Win at t"
```

- Example for Sharp RDD

- ▶ Check RD's type

```
. gen ranwin=(X>=0)  
. tab ranwin T
```

ranwin	Democratic Win at t		Total
	0	1	
0	640	0	640
1	0	750	750
Total	640	750	1,390

- Example for Sharp RDD

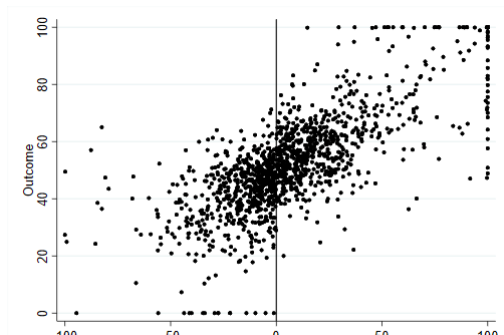
- ▶ Show the scatter plot of the raw data (where each point is an observation).

```
. twoway (scatter Y X, msize(vsmall)          ///  
          mcolor(black) xline(0, lcolor(black))), ///  
          graphregion(color(white)) ytitle(Outcome) ///  
          xtitle(Score)  
  
. graph export fig1.png, width(500) replace  
  (file fig1.png written in PNG format)
```

RDD in Stata

- Example for Sharp RDD

- ▶ Show the scatter plot of the raw data (where each point is an observation).
- ▶ Often hard to see "jumps" or discontinuities in the outcome-score relationship by simply looking at the raw data
- ▶ Two problems :
 - ★ 样本太多时不够直观;
 - ★ 实际分析时中跳跃现象可能不那么清晰。



- Example for Sharp RDD
 - ▶ Three Steps:
 - 1 Graph the data for visual inspection
 - 2 Estimate the treatment effect using regression methods
 - 3 Run checks on assumptions underlying research design

Subsection 4

Example for Sharp RDD : Step 1

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ A more useful approach is to aggregate or “smooth” the data before plotting.
 - ▶ The typical RD plot presents two ingredients :
 - ★ (i) a global polynomial fit, represented by a **solid line**, using the original **raw** data.
 - ★ (ii) local sample means, represented by **dots**, choosing bins of the score, calculating the mean of the outcome for the observations falling within each bin, and then plotting the **average outcome in each bin** against the mid point of the bin.

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*

```
preserve
rdplot Y X, nbins(20 20) genvars support(-100 100)
gen obs = 1
collapse (mean) rdplot_mean_x rdplot_mean_y (sum) obs, by (rdplot_id)
order rdplot_id
tabstat rdplot_mean_x rdplot_mean_y obs,by(rdplot_id)
restore
```


Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*

- ▶ Bin selection (1) : Choosing the Location of Bins

- ① **Evenly-spaced bins** : bins that have equal length.

```
. rdplot Y X, nbins(20 20) binsselect(es)    ///  
    graph_options(graphregion(color(white))) ///  
    xtitle(Score) ytitle(Outcome))
```

RD Plot with RD plot with manually set number of bins.

Cutoff c = 0	Left of c	Right of c	Number of obs	=	1297
			Kernel	=	Uniform
Number of obs	595	702			
Eff. Number of obs	595	702			
Order poly. fit (p)	4	4			
BW poly. fit (h)	100.000	100.000			
Number of bins scale	1.000	1.000			

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - Bin selection (1) : Choosing the Location of Bins
 - ① **Evenly-spaced bins** : bins that have equal length.

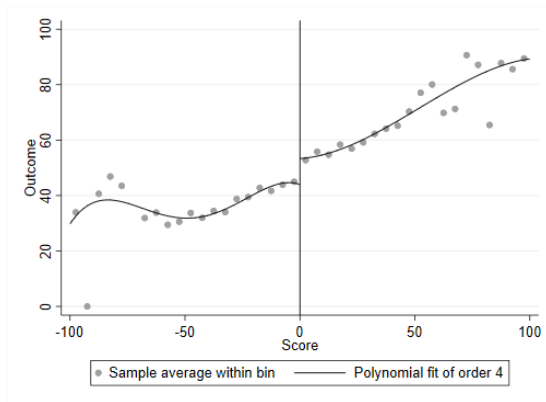
Outcome: Y. Running variable: X.

	Left of c	Right of c
Bins selected	20	20
Average bin length	5.000	5.000
Median bin length	5.000	5.000
IMSE-optimal bins	8	9
Mimicking Var. bins	15	35
Rel. to IMSE-optimal:		
Implied scale	2.500	2.222
WIMSE var. weight	0.060	0.084
WIMSE bias weight	0.940	0.916

```
. graph export fig2.png,width(500) replace
(note: file fig2.png not found)
(file fig2.png written in PNG format)
```

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - Bin selection (1) : Choosing the Location of Bins
 - ① **Evenly-spaced bins** : bins that have equal length.



Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*

- ▶ Bin selection (1) : Choosing the Location of Bins

- ② **Quantile-spaced bins** : bins that contain (roughly) the same number of observations.

```
. rdplot Y X, nbins(20 20) binselect(qs)    ///  
  graph_options(graphregion(color(white)))  ///  
  xtitle(Score) ytitle(Outcome))
```

RD Plot with RD plot with manually set number of bins.

Cutoff c = 0	Left of c	Right of c	Number of obs =	1297
			Kernel =	Uniform
Number of obs	595	702		
Eff. Number of obs	595	702		
Order poly. fit (p)	4	4		
BW poly. fit (h)	100.000	100.000		
Number of bins scale	1.000	1.000		

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (1) : Choosing the Location of Bins
 - ② **Quantile-spaced bins** : bins that contain (roughly) the same number of observations.

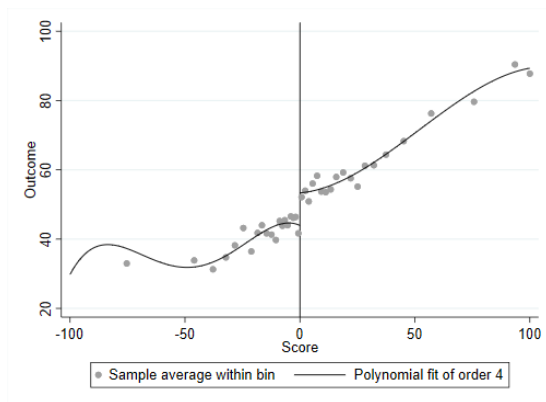
Outcome: Y. Running variable: X.

	Left of c	Right of c
Bins selected	20	20
Average bin length	5.000	5.000
Median bin length	1.912	2.771
IMSE-optimal bins	21	16
Mimicking Var. bins	28	49
Rel. to IMSE-optimal:		
Implied scale	0.952	1.250
WIMSE var. weight	0.537	0.339
WIMSE bias weight	0.463	0.661

```
. graph export fig3.png,width(500) replace
(note: file fig3.png not found)
(file fig3.png written in PNG format)
```

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (1) : Choosing the Location of Bins
 - ② **Quantile-spaced bins** : bins that contain (roughly) the same number of observations.



Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ① Integrated Mean Squared Error (IMSE) Method
 - ★ If we choose a large number of bins (narrower) :
 - ★ **small bias** – the bins are smaller and the **local constant** fit is better.
 - ★ **less precisely** – less observations **per bin**, thus more variability within bin.
 - ★ balance squared-bias and variance so that the IMSE is (approximately) minimized.

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*

- ▶ Bin selection (2) : Choosing the Number of Bins

- ① Integrated Mean Squared Error (IMSE) Method

```
. rdplot Y X, binselect(es)          ///  
    graph_options(graphregion(color(white))) ///  
    xtitle(Score) ytitle(Outcome)
```

/* The IMSE criterion leads to different numbers of ES bins above and below the cutoff.*/

RD Plot with evenly spaced number of bins using spacings estimators.

Cutoff c = 0	Left of c	Right of c	Number of obs =	1297
			Kernel =	Uniform
Number of obs	595	702		
Eff. Number of obs	595	702		
Order poly. fit (p)	4	4		
BW poly. fit (h)	100.000	100.000		
Number of bins scale	1.000	1.000		

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - Bin selection (2) : Choosing the Number of Bins
 - ① Integrated Mean Squared Error (IMSE) Method

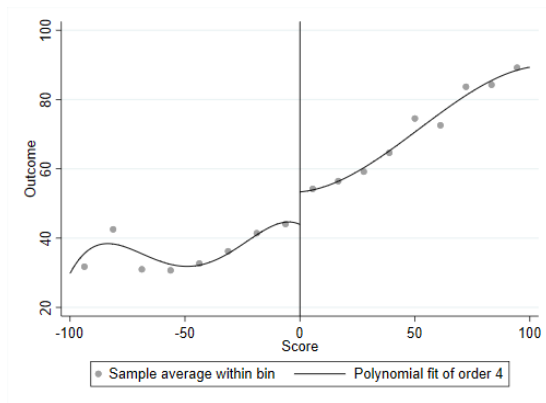
Outcome: Y. Running variable: X.

	Left of c	Right of c
Bins selected	8	9
Average bin length	12.500	11.111
Median bin length	12.500	11.111
IMSE-optimal bins	8	9
Mimicking Var. bins	15	35
Rel. to IMSE-optimal:		
Implied scale	1.000	1.000
WIMSE var. weight	0.500	0.500
WIMSE bias weight	0.500	0.500

```
. graph export fig4.png,width(500) replace
(note: file fig4.png not found)
(file fig4.png written in PNG format)
```

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ① Integrated Mean Squared Error (IMSE) Method



Example for Sharp RDD

- RDD graphical analysis : -*rdplot*-
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ① Integrated Mean Squared Error (IMSE) Method

```
rdplot Y X, binselect(qs)          ///  
    graph_options(graphregion(color(white))) ///  
    xtitle(Score) ytitle(Outcome))
```

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ② Mimicking Variance (MV) Method
 - ★ “mimics” the overall variability in the raw scatter plot of the data.
 - ★ MV method leads to a larger number of bins than the IMSE method.
 - ★ More dots representing local means, thus giving a better sense of the variability of the data.

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ② Mimicking Variance (MV) Method

```
. rdplot Y X, binselect(esmv)          ///Default
  graph_options(graphregion(color(white)) ///
  xtitle(Score) ytitle(Outcome))
```

RD Plot with evenly spaced mimicking variance number of bins using spacings estimated

Cutoff $c = 0$	Left of c	Right of c	Number of obs =	1297
			Kernel =	Uniform
Number of obs	595	702		
Eff. Number of obs	595	702		
Order poly. fit (p)	4	4		
BW poly. fit (h)	100.000	100.000		
Number of bins scale	1.000	1.000		

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ② Mimicking Variance (MV) Method

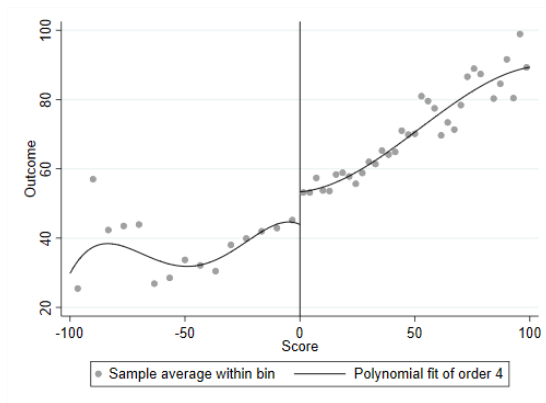
Outcome: Y. Running variable: X.

	Left of c	Right of c
Bins selected	15	35
Average bin length	6.667	2.857
Median bin length	6.667	2.857
IMSE-optimal bins	8	9
Mimicking Var. bins	15	35
Rel. to IMSE-optimal:		
Implied scale	1.875	3.889
WIMSE var. weight	0.132	0.017
WIMSE bias weight	0.868	0.983

. graph export fig5.png,width(500) replace
(file fig5.png written in PNG format)

Example for Sharp RDD

- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ② Mimicking Variance (MV) Method



Example for Sharp RDD

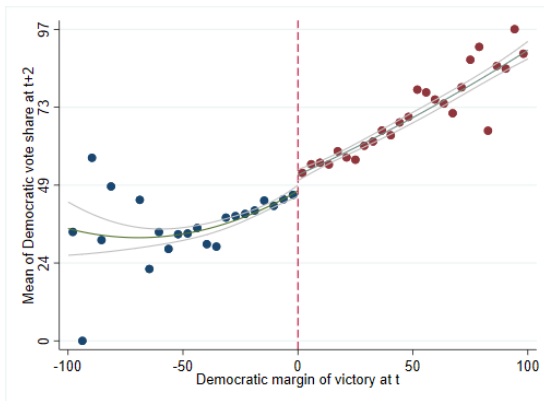
- RDD graphical analysis : *-rdplot-*
 - ▶ Bin selection (2) : Choosing the Number of Bins
 - ② Mimicking Variance (MV) Method

```
rdplot Y X, binselect(qsmv)          ///  
    graph_options(graphregion(color(white))) ///  
    xtitle(Score) ytitle(Outcome))
```


Example for Sharp RDD

- RDD graphical analysis : -*cmogram*-

```
. cmogram Y X, cut(0) scatter lineat(0) qfitci  
  
. graph export fig6.png,width(500) replace  
(note: file fig6.png not found)  
(file fig6.png written in PNG format)
```



Subsection 5

Example for Sharp RDD : Step 2

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - There are 2 types of strategies for correctly specifying the functional form in a RDD:
 - ① **Parametric/global method:** Use all available observations and Estimate treatment effects based on a specific functional form for the outcome and assignment variable relationship.
 - ② **Nonparametric/local method:** Use the observations around cutoff: Compare the outcome of treated and untreated observations that lie within specific bandwidth.

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Parametric/Global Approach (全局多项式回归)

```
sum X
local hvalueR=r(max)
local hvalueL= abs(r(min))

rdrobust Y X, h(`hvalueL' `hvalueR')           //自动选择阶数
rdrobust Y X, h(`hvalueL' `hvalueR') p(2)      //二阶拟合
rdrobust Y X, h(`hvalueL' `hvalueR') p(3)      //三阶拟合
```

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ▶ 三种方法(任选):
 - ★ 方法一: standard least-squares estimation (OLS)
 - ★ 方法二: -rdrobust-进行的非参数估计
 - ★ 方法三: -rd-进行的非参数估计

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法一: standard least-squares estimation (OLS)

```
. rdbwselect Y X, c(0) kernel(uni) bwselect(mserd) //选择最优带宽h
```

Bandwidth estimators for sharp RD local polynomial regression.

Cutoff c =	Left of c	Right of c	Number of obs =	1297
			Kernel =	Uniform
			VCE method =	NN
Number of obs	595	702		
Min of X	-100.000	0.036		
Max of X	-0.079	100.000		
Order est. (p)	1	1		
Order bias (q)	2	2		

Outcome: Y. Running variable: X.

Method	BW est. (h)		BW bias (b)	
	Left of c	Right of c	Left of c	Right of c
mserd	11.597	11.597	22.944	22.944

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法一: standard least-squares estimation (OLS)

```
preserve
keep if X>=-11.597 & X<=11.597

local i=1
forvalues i=2/4
    gen X`i'=X^`i'

// 产生分配变量的平方、三次方、四次方

eststo x1 : qui reg Y 1.T, r
eststo x2 : qui reg Y T##c.X, r //局部线性回归法, 一阶
eststo x3 : qui reg Y T##c.(X X2), r //局部线性回归法, 选择2阶多项式
eststo x4 : qui reg Y T##c.(X X2 X3), r //局部线性回归法, 选择3阶多项式
eststo x5 : qui reg Y T##c.(X X2 X3 X4), r //局部线性回归法, 选择4阶多项式

esttab x1 x2 x3 x4 x5, ///
    star(* .1 ** .05 * .01) ///
    nogap nonumber replace ///
    drop(0.T*) se(%5.4f) ar2 aic(%10.4f) bic(%10.4f)
restore
```

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法一: standard least-squares estimation (OLS)

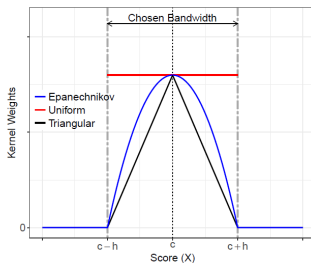
	Y	Y	Y	Y	Y
1.T	9.762* (0.8349)	7.202* (1.6332)	8.832* (2.3939)	13.27* (3.1258)	16.08* (3.8665)
X		0.240 (0.2028)	-1.670** (0.7598)	-2.793 (1.8143)	-7.721** (3.7073)
1.T#c.X		-0.0122 (0.2585)	3.029* (0.9956)	0.566 (2.3214)	6.207 (4.7669)
X2			-0.169** (0.0667)	-0.405 (0.3493)	-2.285* (1.3548)
1.T#c.X2			0.0691 (0.0860)	1.110** (0.4670)	2.708 (1.7333)
X3				-0.0135 (0.0196)	-0.265 (0.1819)
1.T#c.X3				-0.0341 (0.0267)	0.256 (0.2288)
X4					-0.0109 (0.0079)
1.T#c.X4					0.00921 (0.0099)
_cons	44.28* (0.6010)	45.60* (1.2794)	41.91* (1.8869)	40.71* (2.5757)	37.51* (3.1696)
N	506	506	506	506	506
adj. R-sq	0.209	0.211	0.224	0.230	0.231
AIC	3709.6679	3710.3097	3704.0478	3702.2052	3703.7348
BIC	3718.1210	3727.2159	3729.4070	3736.0175	3746.0002

Standard errors in parentheses

* p<.1, ** p<.05, * p<.01

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法二: *-rdrobust*-进行的非参数估计
 - ★ *p* : set the order of the polynomial. Default is $p(1)$.
 - ★ *kernel* : set the kernel. Default is *kernel(triangular)*.



- ★ *h* : choose the bandwidth manually.
- ★ *c* : sets the RD cutoff. Default is $c(0)$.

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法二: `-rdrobust`-进行的非参数估计
 - ★ `bwselect()` : bandwidth selection procedure to be used. Default is `bwselect(mserd)`.
 - ★ If a smaller h :
 - ★ fewer observations—increase the variance of the estimated coefficients.
 - ★ local polynomial approximation—will reduce treatment effect biase.
 - ★ MSE : bias-variance trade-off.

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法二: *-rdrobust*-进行的非参数估计

```
rdrobust Y X, kernel(uniform) p(1)
rdrobust Y X, c(0) kernel(uni) bwselect(mserd) p(2) h(11.597) all
rdrobust Y X, c(0) kernel(uni) bwselect(mserd) p(3) h(11.597) all
rdrobust Y X, c(0) kernel(uni) bwselect(mserd) p(4) h(11.597) all
```

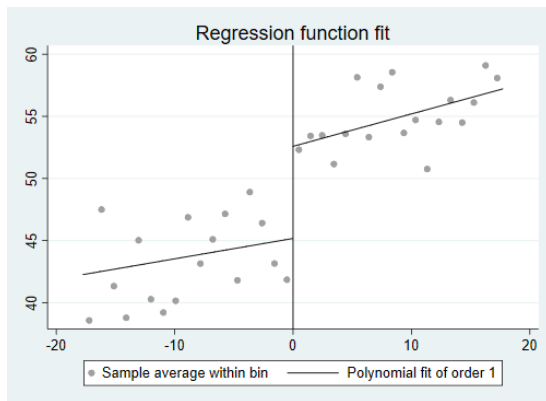
Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法二: *-rdrobust*-进行的非参数估计

```
* Using rdrobust and showing the associated rdplot  
  
. rdrobust Y X, p(1) kernel(triangular) bwselect(mserd)  
. eret list  
. local bandwidth = e(h_1)  
. rdplot Y X if abs(X) <= `bandwidth`, p(1) h(`bandwidth`) kernel(triangular)  
  
. graph export fig7.png,width(500) replace
```

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法二: *-rdrobust*-进行的非参数估计



Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法三: *-rd*-进行的非参数估计

```
. rd Y X, mbw(100) gr z0(0) kernel(tri) //给出了带宽取最优带宽50%和200%的回归结果
```

```
Two variables specified; treatment is  
assumed to jump from zero to one at Z=0.
```

```
Assignment variable Z is X
```

```
Treatment variable X_T unspecified
```

```
Outcome variable y is Y
```

```
Command used for graph: lpoly; Kernel used: triangle (default)
```

```
Bandwidth: 7.5496767; loc Wald Estimate: 9.6449759
```

```
(93 missing values generated)
```

```
(93 missing values generated)
```

```
(93 missing values generated)
```

```
Estimating for bandwidth 7.549676665805968
```

Y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
lwald	9.644976	2.1155	4.56	0.000	5.498673	13.79128

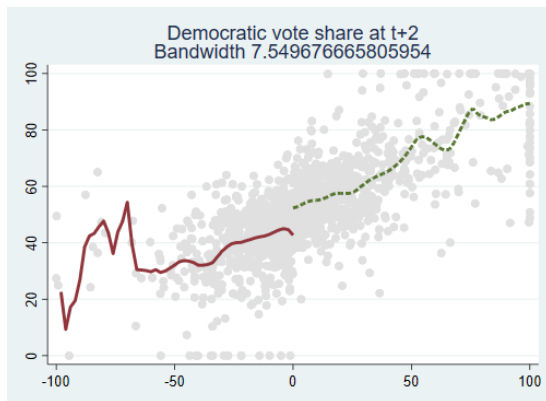
```
. graph export fig8.png,width(500) replace
```

```
(note: file fig8.png not found)
```

```
(file fig8.png written in PNG format)
```

Example for Sharp RDD

- Estimate the treatment effect using regression methods
 - ▶ Nonparametric/Local Approach : local linear regression (局部线性回归)
 - ★ 方法三: -rd-进行的非参数估计



Subsection 6

Example for Sharp RDD : Step 3

Example for Sharp RDD

- Testing the Validity of the RDD
 - ① **Test involving covariates(Nonoutcome Variable)** : Test whether other covariates exhibit a jump at the discontinuity
 - ② **Test sorting behavior** : Testing discontinuity in the density of assignment variable X
 - ③ **Falsification Tests** :
 - ① Placebo Cutoffs
 - ② Sensitivity to Observations near the Cutoffs
 - ③ Sensitivity to Bandwidth Choice

Example for Sharp RDD

- Testing the Validity of the RDD

- 1 Test involving covariates(Nonoutcome Variable)**

- ★ Using rdbwselect with covariates.

```
. global covariates "presdemvoteshlag1 demvoteshlag1 demvoteshlag2 demwinprv1 demwinprv2 dmidte rm dpresdemwinprv2"
. rdrobust Y X, covs($covariates) p(1) kernel(tri) bwselect(mserd)
```

Covariate-adjusted sharp RD estimates using local polynomial regression.

Cutoff c = 0	Left of c	Right of c	Number of obs =	1213
Number of obs	555	658	BW type	= mserd
Eff. Number of obs	326	295	Kernel	= Triangular
Order est. (p)	1	1	VCE method	= NN
Order bias (q)	2	2		
BW est. (h)	17.266	17.266		
BW bias (b)	27.178	27.178		
rho (h/b)	0.635	0.635		

Outcome: Y. Running variable: X.

Method	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
Conventional	7.0876	1.4767	4.7995	0.000	4.19327	9.98194
Robust	-	-	4.0449	0.000	3.67067	10.572

Covariate-adjusted estimates. Additional covariates included: 7

Example for Sharp RDD

- Testing the Validity of the RDD

- ① **Test involving covariates(Nonoutcome Variable)**

- ★ Test whether other covariates exhibit a jump at the discontinuity.

- * There should be no jump in other covariates.
 - * 从图形, 似乎是存在跳跃的, 但这并不严格, 要看回归结果

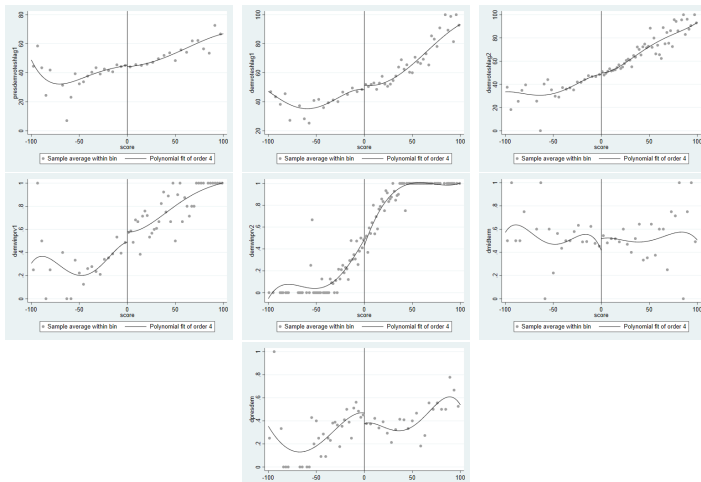
```
foreach y of global covariates {  
  qui rdplot `y' X, graph_options(xtitle("score")) saving(`y')  
  
  graph export fig_`y'.png, width(500) replace  
}
```

Example for Sharp RDD

- Testing the Validity of the RDD

- 1 Test involving covariates(Nonoutcome Variable)**

★ Test whether other covariates exhibit a jump at the discontinuity.



Example for Sharp RDD

- Testing the Validity of the RDD

- ① **Test involving covariates(Nonoutcome Variable)**

- ★ Test whether other covariates exhibit a jump at the discontinuity.

```
* 估计具体系数看是否显著

. est clear
foreach y of global covariates {
  eststo : qui rdrobust `y' X, all
}

. esttab est1 est2 est3 est4 est5 est6 est7 , ///
      se r2 mtitle star(* 0.1 ** 0.05 *** 0.01) compress
```

Example for Sharp RDD

- Testing the Validity of the RDD

- 1 Test involving covariates(Nonoutcome Variable)**

- ★ Test whether other covariates exhibit a jump at the discontinuity.

	(1) est1	(2) est2	(3) est3	(4) est4	(5) est5	(6) est6	(7) est7
Conventi_l	-1.363 (1.383)	2.459 (2.052)	1.001 (1.918)	0.0728 (0.0724)	-0.0270 (0.0712)	0.0696 (0.0662)	-0.1000 (0.0714)
Bias-cor_d	-1.193 (1.383)	2.898 (2.052)	1.495 (1.918)	0.0773 (0.0724)	-0.0386 (0.0712)	0.0828 (0.0662)	-0.102 (0.0714)
Robust	-1.193 (1.633)	2.898 (2.454)	1.495 (2.246)	0.0773 (0.0866)	-0.0386 (0.0845)	0.0828 (0.0772)	-0.102 (0.0854)
N	1387	1349	1308	1349	1308	1390	1390
R-sq							

Standard errors in parentheses

* p<0.1, ** p<0.05, *** p<0.01

Example for Sharp RDD

- Testing the Validity of the RDD

- ② Test sorting behavior

- ★ Testing discontinuity in the density of assignment variable X

- ★ *-rddensity-*

```
. rdrobust Y X
. local h = e(h_1) //获取最优带宽
. rddensity X, p(1) h(`h' `h') plot
```

RD Manipulation Test using local polynomial density estimation.

Cutoff c = 0	Left of c	Right of c	Number of obs =	1390
			Model =	unrestricted
Number of obs	640	750	BW method =	manual
Eff. Number of obs	377	346	Kernel =	triangular
Order est. (p)	1	1	VCE method =	jackknife
Order bias (q)	2	2		
BW est. (h)	17.754	17.754		

Running variable: X.

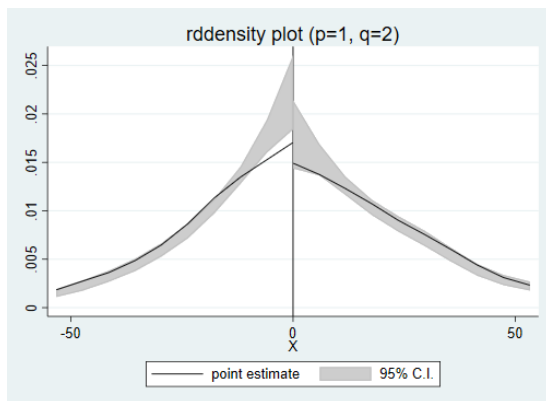
Method	T	P> T
Robust	-1.5083	0.1315

Example for Sharp RDD

- Testing the Validity of the RDD

- ② **Test sorting behavior**

- ★ Testing discontinuity in the density of assignment variable X
 - ★ *-rddensity-*



Example for Sharp RDD

- Testing the Validity of the RDD

- ② **Test sorting behavior**

- ★ Testing discontinuity in the density of assignment variable X
 - ★ Histogram(直方图)

```
. qui rddensity X
. local bandwidth_left = e(h_l)
. local bandwidth_right = e(h_r)

. twoway (histogram X if X >= -`bandwidth_left' & X < 0, freq width(1) color(blue) lcolor(black) lwidth(vthin)) ///
        (histogram X if X >= 0 & X <= `bandwidth_right', freq width(1) color(red) lcolor(black) lwidth(vthin)), ///
        xlabel(-20(10)30) graphregion(color(white)) xtitle(Score) ytitle(Number of Observations) legend(off)

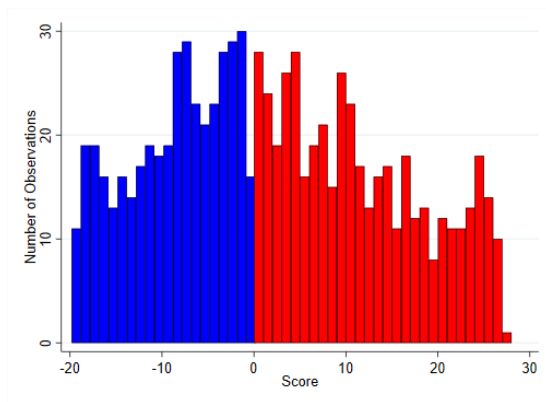
. graph export fig10.png, width(500) replace
(file fig10.png written in PNG format)
```

Example for Sharp RDD

- Testing the Validity of the RDD

- ② **Test sorting behavior**

- ★ Testing discontinuity in the density of assignment variable X
 - ★ Histogram(直方图)



Example for Sharp RDD

• Testing the Validity of the RDD

② Test sorting behavior

- ★ Testing discontinuity in the density of assignment variable X
- ★ a more formal test : **McCrary(2008) test** - *DCdensity*-

```
. preserve
. DCdensity X, breakpoint(0) generate(Xj Yj r0 fhat se_fhat) // McCrary test

Using default bin size calculation, bin size = 1.84133021
Using default bandwidth calculation, bandwidth = 25.8493835
Discontinuity estimate (log difference in height): -.100745626
                                                    (.117145041)

Performing LLR smoothing.
110 iterations will be performed
.....
. gen t= -.100745626/.117145041 // 产生t值, 这个需要你根据系数提取出来
. display 2*ttail(50, t)      // 得到p值, 50是自由度
1.6061102

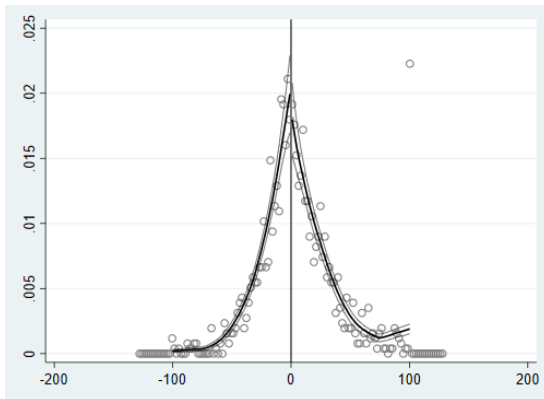
. graph export fig11.png, width(500) replace
(note: file fig11.png not found)
(file fig11.png written in PNG format)
. restore
. /**可以看出在5%显著性水平下实际上McCrary检验是通不过的, 证明没有操纵**/
```

Example for Sharp RDD

- Testing the Validity of the RDD

- ② **Test sorting behavior**

- ★ Testing discontinuity in the density of assignment variable X
 - ★ a more formal test : **McCrary(2008) test** - *DCdensity*-



Example for Sharp RDD

- Testing the Validity of the RDD

- 3 Falsification Tests**

- ▶ Check 1 : Placebo Cutoffs
- ▶ 选择一个不同于断点的值作为安慰剂断点 (placebo cutoff points), 分别取真实断点两侧25%、50%、75%样本分位数处作为断点。

```
. sum X
  Variable | Obs   Mean   Std. Dev.   Min   Max
-----+-----+-----+-----+-----+-----
          X | 1,390   7.171159   34.32488   -100   100
. local xmax=r(max)
. local xmin=r(min)

forvalues i=1(1)3{
  local jr=`xmax'/(4/(4-`i`))
  local jl=`xmin'/(4/(4-`i`))
  qui rdrobust Y X if X>0, c(`jr`)
  est store jl`i'
  qui rdrobust Y X if X<0, c(`jl`)
  est store jr`i'
}

. qui rdrobust Y X ,c(0)    //加上真实断点的回归结果，作为benchmark结果
. est store jbaseline
```

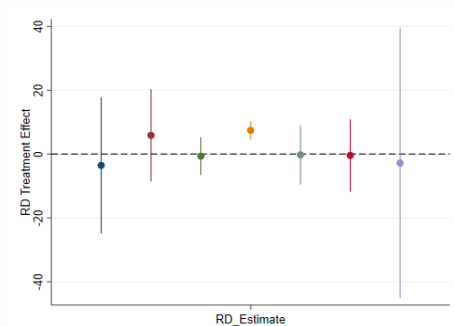
Example for Sharp RDD

- Testing the Validity of the RDD

- ③ Falsification Tests

- ▶ Check 1 : Placebo Cutoffs

```
. local vlist "j11 j12 j13 jbaseline jr3 jr2 jr1 "  
. coefplot `vlist`, yline(0, lcolor(black) lpattern(dash)) drop(_cons) vertical ///  
    graphregion(color(white)) ytitle("RD Treatment Effect") legend(off)  
  
. graph export fig12.png, width(500) replace  
(file fig12.png written in PNG format)
```



Example for Sharp RDD

- Testing the Validity of the RDD

- ③ Falsification Tests

- ▶ Check 2 : Sensitivity to Observations near the Cutoffs

- ★ 由于越接近断点的样本，越有动机去人为操控，删除最接近断点的样本，来观察回归是否显著（甜甜圈效应, donut hole approach）。
 - ★ 分别删除断点附近 1%，2%，3%，4% 和 5% 的样本，进行了 5 组稳健性检验。
 - ★ 图形给出了回归系数和 95% 的置信区间。

```
. sum X
. local xmax=r(max)

forvalues i=1(1)5{
  local j=`xmax'*0.01*`i'
  qui rdrobust Y X if abs(X)>`j'
  est store obrob`i'
}
```

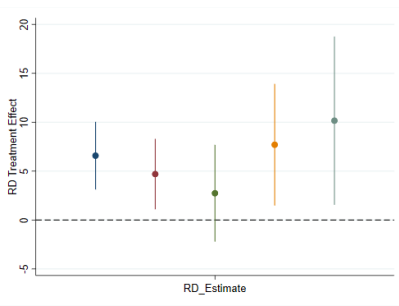
Example for Sharp RDD

- Testing the Validity of the RDD

- ③ Falsification Tests

- ▶ Check 2 : Sensitivity to Observations near the Cutoffs

```
. local vlist "obrob1 obrob2 obrob3 obrob4 obrob5"  
. coefplot `vlist', yline(0, lcolor(black) lpattern(dash)) drop(_cons) vertical ///  
    graphregion(color(white)) legend(off) ytitle("RD Treatment Effect")  
  
. graph export fig13.png, width(500) replace  
(note: file fig13.png not found)  
(file fig13.png written in PNG format)
```



Example for Sharp RDD

- Testing the Validity of the RDD

- ③ Falsification Tests

- ▶ Check 3 : Sensitivity to Bandwidth Choice

- ★ 带宽长度会显著影响回归结果，一个稳健的结果要求对带宽长度不那么敏感。
 - ★ 提取最优带宽 h ，然后分别手动设置带宽为 h 的 25%-400% 倍，看回归结果是否仍旧显著。
 - ★ 图形给出了回归系数和95%的置信区间。

```
. qui rdrobust Y X    //自动选择最优带宽
. local h = e(h_1)    //获取最优带宽

forvalues i=1(1)8{
  local hrobust=`h'*0.25*`i'
  qui rdrobust Y X ,h(`hrobust`)
  est store hrob`i'
}
```

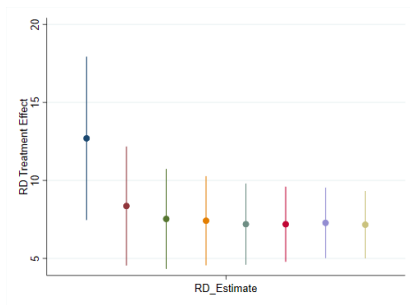
Example for Sharp RDD

- Testing the Validity of the RDD

- ③ Falsification Tests

- ▶ Check 3 : Sensitivity to Bandwidth Choice

```
. local vlist "hrob1 hrob2 hrob3 hrob4 hrob5 hrob6 hrob7 hrob8 "  
. coefplot `vlist`, yline(0, lcolor(black) lpattern(dash)) drop(_cons) vertical ///  
    graphregion(color(white)) ytitle("RD Treatment Effect") legend(off)  
  
. graph export fig14.png, width(500) replace  
(note: file fig14.png not found)  
(file fig14.png written in PNG format)
```



Subsection 7

Example for Fuzzy RDD

Example for Fuzzy RDD

- 三种方法(任选):
 - ▶ 方法一: *-rd-*
 - ▶ 方法二: *-rdrobust-*
 - ▶ 方法三: IV估计

Example for Fuzzy RDD

- 方法一: *-rd-*

- ▶ Syntax

```
rd y d x, z0(real) strineq mbw(numlist) graph bdep oxline    ///  
    kernel(rectangle) covar(varlist) x(varlist)
```

```
mbw(numlist)           //用来指定最优带宽的倍数，默认值为mbw(50 100 200)  
z0(real)               //用来指定断点的位置，默认值为z0(0)，即断点为原点  
*如果此处省去D，则为SRD，并根据分组变量X来计算处理变量  
graph                 //根据每一带宽，画出局部线性回归图  
bdep                  //根据画图来考察断点回归估计量对带宽的依赖性  
oxline                //在此图的默认带宽上画出一条直线，以便识别  
kernel(rectangle)     //使用均匀核 (uniform)，默认triangle  
covar(varlist)        //用来指定加入局部线性回归的协变量  
x(varlist)             //检验这些协变量在断点处是否存在跳跃（估计跳跃值  
和显著性）
```

Example for Fuzzy RDD

- 方法一: *-rd-*

- ▶ Example background

- ★ 在美国国会,有一个民主党代表可能是被认为是对国会选区的一种treatment。
 - ★ 美国国会选区,如果有民主党众议员,对该选区的联邦政府的开支具有一定影响。
 - ★ 传统意义上,民主党会更倾向于政府,如果当选,会加大对联邦政府的开支。
 - ★ 然而直接对二者进行回归,可能会遗漏变量问题或者双向因果关系。
 - ★ 为此选择该民主党候选人的得票比例作为分组变量, Z 是民主党候选人获得的选票份额。
 - ★ 以0.5为断点 (在民主党与共和党的政治中, $Z \geq 0.5$, 则当选, 反之落选), 进行RDD。

Example for Fuzzy RDD

- 方法一: *-rd-*

- ▶ Example Data

```
. ssc inst rd, replace
. net get rd
. use votex, clear

* lne    //选取联邦政府开支的对数
* d      //分组变量, 民主党派候选人的得票比例减去0.5, 以标准化
* win    //民主党派候选人当选
* 另外还包括一些协变量

. desc
```

Example for Fuzzy RDD

● 方法一: *-rd-*

► SRD

```
//OLS回归
reg lne win i votpop bla-vet
*回归结果虽然win表示当选了, 会增加lne的支出, 但是不显著

//选择默认的带宽以及triangle kernel进行RD
rd lne d, gr mbw(100)
*不显著, 说明拥有民主党候选人当选的选区并不能显著的增加联邦政府开支

//加入协变量进行RD, 省略作图
rd lne d, mbw(100) cov(i votpop black blucllr farmer fedwrkr forborn manuf unemployd union urban veterans)
*显示估计值虽然为正, 但是依然不显著

//去掉协变量, 同时估计三种带宽, 并画出估计值对带宽的依赖性
rd lne d, gr bdep oxline
*改变带宽对估计值有一定的影响, 但是三个估计值全部为负, 且依然不显著。可以看出, 各个断点回归估计量对带宽的依赖性不大。

//检验协变量在断点处是否存在跳跃
rd lne d, mbw(100) x(i votpop black blucllr farmer fedwrkr forborn manuf unemployd union urban veterans)
*farmer的P值为 0.036, 其余的协变量的条件密度函数在断点处都是连续的, 即只有farmer (农民占人口比例) 存在跳跃。
```


Example for Fuzzy RDD

- 方法一: -rd-

- ▶ FRD

```
. //生成一个新的处理变量randwin, 使得randwin不完全由分组变量d决定。  
. set seed 20181203  
. g byte randwin=cond(uniform()<.1,1-win,win)  
. tab randwin win
```

randwin	Dem Won Race		Total
	0	1	
0	123	14	137
1	8	204	212
Total	131	218	349

*结果显示randwin与win基本相同, 但不完全相同, 说明randwin不完全由分组变量d决定。

Example for Fuzzy RDD

- 方法一: -rd-

- ▶ FRD

```
. //使用最优带宽与默认的triangle kernel进行FRD(含协变量)
. rd lne randwin d, gr mbw(100) cov(i votpop black blueclr farmer fedwrkr forborn manuf unemploy
> d union urban veterans)
```

Three variables specified; jump in treatment
at Z=0 will be estimated. Local Wald Estimate
is the ratio of jump in outcome to jump in treatment.

Assignment variable Z is d

Treatment variable X_T is randwin

Outcome variable y is lne

Command used for graph: lpoly; Kernel used: triangle (default)

Bandwidth: .29287776; loc Wald Estimate: -.09974965

Estimating for bandwidth .2928777592534943

A predicted value of treatment at cutoff lies outside feasible range;
switching to local mean smoothing for treatment discontinuity.

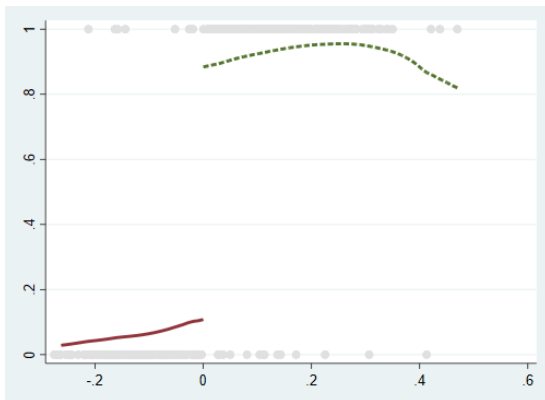
lne	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
numer	.0543733	.0900181	0.60	0.546	-.1220589	.2308055
denom	.8734363	.0301089	29.01	0.000	.814424	.9324487
lwald	.0622522	.1028807	0.61	0.545	-.1393903	.2638946

```
. graph export fig15.png, width(500) replace
(file fig15.png written in PNG format)
```

Example for Fuzzy RDD

- 方法一: *-rd-*

- FRD



Example for Fuzzy RDD

- 方法二: *-rdrobust-*

```
* options : fuzzy(fuzzyvar [sharpbw])

. rdrobust lne d, fuzzy(randwin)
```

Fuzzy RD estimates using local polynomial regression.

Cutoff c = 0	Left of c	Right of c	
Number of obs	131	218	Number of obs = 349
Eff. Number of obs	73	105	BW type = mserd
Order est. (p)	1	1	Kernel = Triangular
Order bias (q)	2	2	VCE method = NN
BW est. (h)	0.142	0.142	
BW bias (b)	0.186	0.186	
rho (h/b)	0.762	0.762	

First-stage estimates. Outcome: randwin. Running variable: d.

Method	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
Conventional	.74178	.09171	8.0888	0.000	.562043	.921522
Robust	-	-	7.3050	0.000	.53871	.933789

Treatment effect estimates. Outcome: lne. Running variable: d. Treatment Status: randwin.

Method	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
Conventional	-.12768	.20294	-0.6292	0.529	-.525433	.270072
Robust	-	-	-0.6411	0.521	-.665039	.3372

Example for Fuzzy RDD

● 方法三：IV估计

```
. use frd.dta, clear
. sum
```

Variable	Obs	Mean	Std. Dev.	Min	Max
anno	120	1998.667	3.831171	1993	2004
esse_m	120	0	6.230853	-10	10
mc	120	9.792913	.1016675	9.522602	9.995189
mcn	120	9.726134	.093931	9.46739	9.921432
mf	120	6.100074	.1004518	5.892969	6.368767
pen	120	.4036111	.3359836	0	.9861111
obsc	120	88.175	35.007	21	184
obscn	120	88.175	35.007	21	184
obsf	120	88.11667	34.99176	21	184
obsp	120	88.175	35.007	21	184
anno1993	120	-7.45e-09	.3742406	-.1666667	.8333333
anno1995	120	-7.45e-09	.3742406	-.1666667	.8333333
anno1998	120	-7.45e-09	.3742406	-.1666667	.8333333
anno2000	120	-7.45e-09	.3742406	-.1666667	.8333333
anno2002	120	-7.45e-09	.3742406	-.1666667	.8333333
anno2004	120	-7.45e-09	.3742406	-.1666667	.8333333
elig	120	.5	.5020964	0	1
esse_m2	120	38.5	32.55583	1	100
esse_m3	120	0	446.6576	-1000	1000
esse_m4	120	2533.3	3231.493	1	10000
sel	120	1	0	1	1
mc_neg	60	9.861339	.0171739	9.83221	9.88535
mc_pos	60	9.724487	.0307325	9.674244	9.769611
mcn_neg	60	9.787027	.0135329	9.763389	9.805106
mcn_pos	60	9.665241	.0282369	9.618672	9.706251
mf_neg	60	6.159085	.0148918	6.135935	6.182206

Example for Fuzzy RDD

- 方法三：IV估计

- ▶ `mcn`, `mf` : 非耐用品和食品支出(**Y**)
- ▶ `ess_m` : 已经退休的年数, 负数表示还未到退休年龄
- ▶ `pen` : 退休概率, 内生变量, 依赖于`ess_m`, 断点处存在不连续跳跃(**X**)
- ▶ `elig` : 退休资格虚拟变量, 若`ess_m` ≥ 0 , `elig` = 1, 否则为0(**Z**)

Example for Fuzzy RDD

- 方法三：IV估计

```
. ivregress 2sls mcn (pen=elig) esse_m esse_m2 anno1995-anno2004, first robust  
First-stage regressions
```

```
Number of obs      =       120  
F(   8,   111)     =       177.06  
Prob > F           =       0.0000  
R-squared          =       0.9230  
Adj R-squared      =       0.9175  
Root MSE          =       0.0965
```

pen	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
esse_m	.0169943	.0031324	5.43	0.000	.0107873	.0232013
esse_m2	-.0005738	.000294	-1.95	0.054	-.0011564	8.82e-06
anno1995	.0230442	.0305492	0.75	0.452	-.0374911	.0835796
anno1998	.0508942	.0336146	1.51	0.133	-.0157153	.1175038
anno2000	.1172279	.0326428	3.59	0.000	.0525441	.1819118
anno2002	.1400281	.0327296	4.28	0.000	.0751722	.204884
anno2004	.1693907	.0333298	5.08	0.000	.1033455	.2354359
elig	.4349947	.0362406	12.00	0.000	.3631815	.5068078
_cons	.2082045	.018284	11.39	0.000	.1719736	.2444355

Example for Fuzzy RDD

- 方法三：IV估计

```
Instrumental variables (2SLS) regression      Number of obs   =      120
                                             Wald chi2(8)    =     332.96
                                             Prob > chi2     =      0.0000
                                             R-squared      =      0.6223
                                             Root MSE      =      .05749
```

mcn	Robust					
	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
pen	-.0983277	.0544996	-1.80	0.071	-.2051449	.0084895
esse_m	-.0055121	.0025899	-2.13	0.033	-.0105881	-.000436
esse_m2	-.000288	.000145	-1.99	0.047	-.0005722	-3.84e-06
anno1995	.0018884	.0179095	0.11	0.916	-.0332135	.0369903
anno1998	-.0334648	.0181819	-1.84	0.066	-.0691007	.002171
anno2000	.0121598	.019791	0.61	0.539	-.0266299	.0509495
anno2002	.0210096	.0229841	0.91	0.361	-.0240384	.0660575
anno2004	.0843976	.0194665	4.34	0.000	.0462439	.1225512
_cons	9.77691	.0244502	399.87	0.000	9.728988	9.824831

```
Instrumented:  pen
Instruments:  esse_m esse_m2 anno1995 anno1998 anno2000 anno2002 anno2004
              elig
```


Example for Fuzzy RDD

- 方法三：IV估计

```
. ivregress 2sls mf (pen=elig) esse_m esse_m2 anno1995-anno2004, first robust
First-stage regressions
```

```
Number of obs      =       120
F(   8,   111)      =       177.06
Prob > F            =       0.0000
R-squared           =       0.9230
Adj R-squared       =       0.9175
Root MSE           =       0.0965
```

pen	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
esse_m	.0169943	.0031324	5.43	0.000	.0107873	.0232013
esse_m2	-.0005738	.000294	-1.95	0.054	-.0011564	8.82e-06
anno1995	.0230442	.0305492	0.75	0.452	-.0374911	.0835796
anno1998	.0508942	.0336146	1.51	0.133	-.0157153	.1175038
anno2000	.1172279	.0326428	3.59	0.000	.0525441	.1819118
anno2002	.1400281	.0327296	4.28	0.000	.0751722	.204884
anno2004	.1693907	.0333298	5.08	0.000	.1033455	.2354359
elig	.4349947	.0362406	12.00	0.000	.3631815	.5068078
_cons	.2082045	.018284	11.39	0.000	.1719736	.2444355

Example for Fuzzy RDD

• 方法三：IV估计

```
Instrumental variables (2SLS) regression      Number of obs   =      120
                                             Wald chi2(8)    =     325.13
                                             Prob > chi2     =      0.0000
                                             R-squared      =      0.7124
                                             Root MSE      =      .05365
```

mf	Robust					
	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
pen	-.1409689	.0523376	-2.69	0.007	-.2435487	-.0383891
esse_m	-.0027591	.0024779	-1.11	0.266	-.0076157	.0020975
esse_m2	-.0000821	.0001355	-0.61	0.545	-.0003478	.0001835
anno1995	-.0675309	.0144149	-4.68	0.000	-.0957835	-.0392782
anno1998	-.1365082	.0154907	-8.81	0.000	-.1668694	-.106147
anno2000	-.13855	.0177911	-7.79	0.000	-.1734199	-.1036801
anno2002	-.1420846	.017727	-8.02	0.000	-.176829	-.1073403
anno2004	-.1042948	.0179742	-5.80	0.000	-.1395236	-.0690661
_cons	6.160132	.0223924	275.10	0.000	6.116244	6.20402

```
Instrumented:  pen
Instruments:  esse_m esse_m2 anno1995 anno1998 anno2000 anno2002 anno2004
              elig
```

Section 2

FE in Stata

Subsection 1

Panel Data

- Panel Data

- ▶ Panel data refers to data with observations on **multiple entities**, where each entity is observed at **two or more points in time**.
- ▶ We focus on **balanced** and **micro** panel data.
- ▶ **Balanced** panel: each unit of observation i is observed the same number of time periods, T .
- ▶ **Micro** : large N , and small T , more similar to cross-section data.

Subsection 2

Review the Theory

- Review the Theory

- ▶ Fixed effects regression is a method for **controlling for omitted variables** in panel data when the omitted variables **vary across entities (states)** but do **not change over time**.
- ▶ Specification :

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \beta_2 Z_i + u_{it} \quad (11.1)$$

- Because Z_i varies from one state to the next but is constant over time, then let $\alpha_i = \beta_0 + \beta_2 Z_i$, the Equation becomes

$$Y_{it} = \beta_1 X_{it} + \alpha_i + u_{it} \quad (11.2)$$

- This is the **fixed effects regression model**, in which α_i are treated as *unknown intercepts* to be estimated, one for each state. The interpretation of α_i as a *state-specific intercept* in Equation (11.2).
- Arbitrarily omit the binary variable $D1_i$ for the first group. Accordingly, the fixed effects regression model in Equation (7.2) can be written equivalently as

$$Y_{it} = \beta_0 + \beta_1 X_{it} + \gamma_2 D2_i + \gamma_3 D3_i + \dots + \gamma_n Dn_i + u_{it} \quad (7.3)$$

- Review the Theory

- ▶ Estimation:

- ★ entity-demeaned :

$$\hat{\beta}_{demean} = \frac{\sum_{i=1}^n \sum_{t=1}^T \tilde{Y}_{it} \tilde{X}_{it}}{\sum_{i=1}^n \sum_{t=1}^T \tilde{X}_{it}^2}$$

- ★ first-difference estimator :

$$\hat{\beta}_{fd} = \frac{\sum_{i=1}^n \sum_{t=2}^T \Delta Y_{it} \Delta X_{it}}{\sum_{i=1}^n \sum_{t=2}^T \Delta X_{it}^2}$$

- Summary

- ▶ FE实质上就是在传统的线性回归模型中加入 $N-1$ 个虚拟变量;
- ▶ 使得每个截面都有自己的截距项, 截距项的不同反映了个体的某些不随时间改变的特征;
- ▶ 我们关注的是 X 的系数, 而非每个截面的截距项。

Subsection 3

Examples for FE

- Examples for FE
 - ▶ unbalance —> balance

```
. use abond.dta, clear
. xtset id year
    panel variable:  id (unbalanced)
    time variable:  year, 1976 to 1984
                  delta:  1 unit
```

- Examples for FE

► unbalance —> balance

```
. xtides      /*unbalanced*/
      id:  1, 2, ..., 140          n =      140
      year: 1976, 1977, ..., 1984  T =        9
      Delta(year) = 1 unit
      Span(year)  = 9 periods
      (id*year uniquely identifies each observation)
```

Distribution of T_i:

	min	5%	25%	50%	75%	95%	max
	7	7	7	7	8	9	9

Freq.	Percent	Cum.	Pattern
62	44.29	44.29	1111111..
39	27.86	72.14	.1111111.
19	13.57	85.71	.11111111
14	10.00	95.71	111111111
4	2.86	98.57	11111111.
2	1.43	100.00	..1111111
140	100.00		XXXXXXXXX

FE in Stata

- Examples for FE

► unbalance —> balance

```
. sum
```

/*many missing values*/					
Variable	Obs	Mean	Std. Dev.	Min	Max
c1	0				
ind	1,031	5.123181	2.678095	1	9
year	1,031	1979.651	2.21607	1976	1984
emp	1,031	7.891677	15.93492	.104	108.562
wage	1,031	23.9188	5.648418	8.0171	45.2318
cap	1,031	2.507432	6.248712	.0119	47.1079
indoutpt	1,031	103.8012	9.938008	86.9	128.3653
n	1,031	1.056002	1.341506	-2.263364	4.687321
w	1,031	3.142988	.2630081	2.081577	3.8118
k	1,031	-.4415775	1.514132	-4.431217	3.852441
ys	1,031	4.638015	.0939611	4.464758	4.85488
rec	1,031	516	297.7684	1	1031
yearm1	1,031	1979.644	2.213454	1976	1984
id	1,031	73.20369	41.23333	1	140
nL1	891	1.083518	1.338469	-2.095571	4.687321
nL2	751	1.107716	1.333478	-2.079442	4.687321
wL1	891	3.132166	.2639638	2.081577	3.8118
kL1	891	-.4131872	1.501461	-4.431217	3.852441
kL2	751	-.392113	1.486371	-4.431217	3.852441
ysL1	891	4.651039	.0923352	4.464758	4.85488

- Examples for FE

- unbalance —> balance

```
. xtbalance, rang(1978 1982) miss(_all)    /*written by arlion*/
(331 observations deleted due to out of range)
(62 observations deleted due to missing)
(238 observations deleted due to discontinues)
. xtides
      id:  5, 6, ..., 140                      n =          80
     year: 1978, 1979, ..., 1982                T =           5
           Delta(year) = 1 unit
           Span(year)  = 5 periods
           (id*year uniquely identifies each observation)

Distribution of T_i:  min      5%      25%      50%      75%      95%      max
                   5          5          5          5          5          5

      Freq.  Percent   Cum. | Pattern
-----|-----
      80    100.00  100.00 | 11111
-----|-----
      80    100.00         | XXXXX
```

- Examples for FE

- ▶ Data : Baum(2006)
- ▶ 包含美国48个州1982-1988年交通死亡率相关变量:
 - ★ fatal (交通死亡率)
 - ★ beertax (啤酒税)
 - ★ spircons (酒精消费量)
 - ★ unrate (失业率)
 - ★ perinck (人均收入,千元)
 - ★ state (州)
 - ★ year (年)

- Examples for FE

- ▶ Pooled OLS & Pooled OLS with Time (Wrong)

```
. use traffic, clear
. est clear
. eststo : qui reg fatal beertax
(est1 stored)
. eststo : qui reg fatal beertax i.year
(est2 stored)

. esttab, star(* .1 ** .05 * .01)    ///
      nogap nonumber replace        ///
      se(%5.4f) ar2
```


FE in Stata

- Examples for FE

- ▶ Pooled OLS & Pooled OLS with Time (Wrong)

	fatal	fatal
beertax	0.365* (0.0622)	0.366* (0.0626)
1982.year		0 (.)
1983.year		-0.0820 (0.1117)
1984.year		-0.0717 (0.1117)
1985.year		-0.111 (0.1117)
1986.year		-0.0161 (0.1117)
1987.year		-0.0155 (0.1117)
1988.year		-0.00103 (0.1117)
_cons	1.853* (0.0436)	1.895* (0.0857)
N	336	336
adj. R-sq	0.091	0.079

Standard errors in parentheses

* p<.1, ** p<.05, * p<.01

- Examples for FE

- ▶ Fixed effects regression

```
. xtset state year    //设定state与year为面板（个体）变量及时间变量
      panel variable:  state (strongly balanced)
      time variable:  year, 1982 to 1988
                delta:  1 unit

. xtodes
      state:  1, 4, ..., 56                                n =          48
      year:  1982, 1983, ..., 1988                        T =           7
      Delta(year) = 1 unit
      Span(year)  = 7 periods
      (state*year uniquely identifies each observation)

Distribution of T_i:  min    5%    25%    50%    75%    95%    max
                   7      7      7      7      7      7      7

      Freq.  Percent   Cum. | Pattern
      -----|-----
      48     100.00  100.00 | 1111111
      -----|-----
      48     100.00         | XXXXXXX
```

FE in Stata

- Examples for FE

- ▶ Fixed effects regression

```
. xtsum fatal beertax spircons unrates perinck state year
```

Variable		Mean	Std. Dev.	Min	Max	Observations	
fatal	overall	2.040444	.5701938	.82121	4.21784	N =	336
	between		.5461407	1.110077	3.653197	n =	48
	within		.1794253	1.45556	2.962664	T =	7
beertax	overall	.513256	.4778442	.0433109	2.720764	N =	336
	between		.4789513	.0481679	2.440507	n =	48
	within		.0552203	.1415352	.7935126	T =	7
spircons	overall	1.75369	.6835745	.79	4.9	N =	336
	between		.6734649	.8614286	4.388572	n =	48
	within		.147792	1.255119	2.265119	T =	7
unrates	overall	7.346726	2.533405	2.4	18	N =	336
	between		1.953377	4.1	13.2	n =	48
	within		1.634257	4.046726	12.14673	T =	7
perinck	overall	13.88018	2.253046	9.513762	22.19345	N =	336
	between		2.122712	9.95087	19.51582	n =	48
	within		.8068546	11.43261	16.55782	T =	7
state	overall	30.1875	15.30985	1	56	N =	336
	between		15.44883	1	56	n =	48
	within		0	30.1875	30.1875	T =	7

FE in Stata

- Examples for FE

- ▶ Fixed effects regression

```
. xtline fatal if year==1982  
. graph export fefig1.png,width(500) replace  
(file fefig1.png written in PNG format)
```



FE in Stata

- Examples for FE

- Fixed effects regression

```
. xtreg fatal beertax spircons unrates perinck, fe
Fixed-effects (within) regression              Number of obs   =       336
Group variable: state                        Number of groups =       48
R-sq:                                         Obs per group:
    within = 0.3526                           min =           7
    between = 0.1146                          avg =          7.0
    overall = 0.0863                           max =           7
                                         F(4,284)        =      38.68
corr(u_i, Xb) = -0.8804                      Prob > F         =      0.0000
```

	fatal	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax		-.4840728	.1625106	-2.98	0.003	-.8039508	-.1641948
spircons		.8169652	.0792118	10.31	0.000	.6610484	.9728819
unrates		-.0290499	.0090274	-3.22	0.001	-.0468191	-.0112808
perinck		.1047103	.0205986	5.08	0.000	.064165	.1452555
_cons		-.383783	.4201781	-0.91	0.362	-1.210841	.4432754
sigma_u		1.1181913					
sigma_e		.15678965					
rho		.98071823	(fraction of variance due to u_i)				

```
F test that all u_i=0: F(47, 284) = 59.77                      Prob > F = 0.0000
. est store FE
```

FE in Stata

- Examples for FE

- ▶ Fixed effects regression
- ▶ clustered standard errors

```
. xtreg fatal beertax spircons unrates perinck, fe vce(cluster state)
Fixed-effects (within) regression      Number of obs   =       336
Group variable: state                 Number of groups =       48
R-sq:                                Obs per group:
    within = 0.3526                      min =          7
    between = 0.1146                     avg =         7.0
    overall = 0.0863                      max =          7
                                         F(4,47)         =      21.27
corr(u_i, Xb) = -0.8804                 Prob > F         =      0.0000
                                         (Std. Err. adjusted for 48 clusters in state)
```

fatal	Robust					
	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax	-.4840728	.2218754	-2.18	0.034	-.9304285	-.037717
spircons	.8169652	.1272627	6.42	0.000	.5609456	1.072985
unrates	-.0290499	.0094581	-3.07	0.004	-.0480772	-.0100227
perinck	.1047103	.0341455	3.07	0.004	.0360184	.1734022
_cons	-.383783	.7091738	-0.54	0.591	-1.810457	1.042891
sigma_u	1.1181913					
sigma_e	.15678965					
rho	.98071823	(fraction of variance due to u_i)				

```
. _b_ est store FE_cse
```

FE in Stata

- Examples for FE
 - ▶ Fixed effects regression
 - ▶ Both Entity and Time Fixed Effects

```
. xtreg fatal beertax spircons unrte perinck i.year, fe vce(cluster state)
Fixed-effects (within) regression              Number of obs   =        336
Group variable: state                        Number of groups =         48
R-sq:                                         Obs per group:
    within = 0.4528                          min =           7
    between = 0.1090                         avg =          7.0
    overall = 0.0770                         max =           7
                                           F(10,47)        =       14.13
corr(u_i, Xb) = -0.8728                      Prob > F         =       0.0000
                                           (Std. Err. adjusted for 48 clusters in state)
```

fatal	Robust					
	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
beertax	-.4347195	.2442775	-1.78	0.082	-.9261425	.0567036
spircons	.805857	.1161087	6.94	0.000	.5722764	1.039438
unrate	-.0549084	.011763	-4.67	0.000	-.0785725	-.0312443
perinck	.0882636	.0322971	2.73	0.009	.0232901	.153237
year						
1983	-.0533713	.0312438	-1.71	0.094	-.1162256	.0094831
1984	-.1649828	.0439375	-3.75	0.000	-.2533737	-.076592
1985	-.1997376	.0496167	-4.03	0.000	-.2995535	-.0999218
1986	-.0508034	.0661756	-0.77	0.447	-.1839315	.0823248
1987	-.1000728	.0756768	-1.32	0.192	-.2523149	.0521693

FE in Stata

- Examples for FE

- Fixed effects regression

```
. esttab FE FE_cse FE_TW, star(* .1 ** .05 * .01) ///  
>      nogap nonumber replace se(%5.4f) ar2 drop(1982.year)
```

	fatal	fatal	fatal
beertax	-0.484* (0.1625)	-0.484** (0.2219)	-0.435* (0.2443)
spircons	0.817* (0.0792)	0.817* (0.1273)	0.806* (0.1161)
unrate	-0.0290* (0.0090)	-0.0290* (0.0095)	-0.0549* (0.0118)
perinck	0.105* (0.0206)	0.105* (0.0341)	0.0883* (0.0323)
1983.year			-0.0534* (0.0312)
1984.year			-0.165* (0.0439)
1985.year			-0.200* (0.0496)
1986.year			-0.0508 (0.0662)
1987.year			-0.100 (0.0757)
1988.year			-0.134 (0.0864)
_cons	-0.384 (0.4202)	-0.384 (0.7092)	0.129 (0.6238)
N	336	336	336
adj. R-sq	0.236	0.345	0.436

Standard errors in parentheses

* p<.1, ** p<.05, * p<.01

Section 3

DID in Stata

Subsection 1

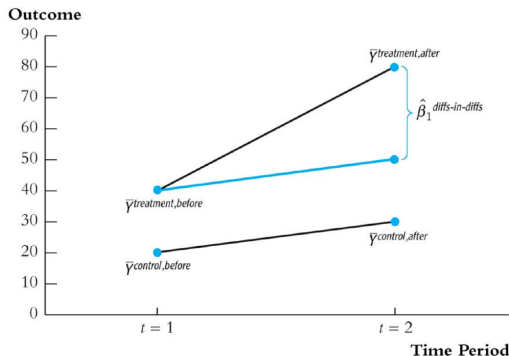
Review the Theory

- Review the Theory

DID estimator

- The DID estimator is

$$\hat{\beta}_{DID} = (\bar{Y}_{treat,post} - \bar{Y}_{treat,pre}) - (\bar{Y}_{control,post} - \bar{Y}_{control,pre})$$



- Review the Theory

Difference in Differences

Card and Krueger(1994): Minimum Wage on Employment

Regression DD - Card and Krueger

- A 2×2 matrix table

		treat or control	
		NJ=0(control)	NJ=1(treat)
pre or post	d=0(pre)	α	$\alpha + \gamma$
	d=1(post)	$\alpha + \lambda$	$\alpha + \gamma + \lambda + \delta$

- Then DID estimator

$$\begin{aligned}
 \hat{\beta}_{DID} &= (\bar{Y}_{treat,post} - \bar{Y}_{treat,pre}) - \\
 &\quad (\bar{Y}_{control,post} - \bar{Y}_{control,pre}) \\
 &= (NJ_{post} - NJ_{pre}) - (PA_{post} - PA_{pre}) \\
 &= [(\alpha + \gamma + \lambda + \delta) - (\alpha + \gamma)] - [(\alpha + \lambda) - \alpha] \\
 &= \delta
 \end{aligned}$$

- Review the Theory

- ▶ Specification :

$$Y_{ist} = \alpha + \beta D_{st} + \gamma Treat_s + \delta Post_t + \Gamma X'_{ist} + u_{ist}$$

- Where D_{st} means $(Treat \times Post)_{st}$
 - Using Fixed Effect Models further to transform into

$$Y_{ist} = \beta D_{st} + \alpha_s + \delta_t + \Gamma X'_{ist} + u_{ist}$$

- α_s is a set of groups fixed effects, which captures $Treat_s$.
 - δ_t is a set of time fixed effects, which captures $Post_t$.

Subsection 2

Examples for DID

- Examples for DID

- ▶ Data :

- ★ 历史上A、B、C、D、E、F、G这7个地区非常相似
 - ★ 然而1994年后E、F和G三个地区（treatment group）颁布了一项政策
 - ★ 其余4个地区（control group）没有。

```
. use did, clear
```

• Examples for DID

```
. * 假设政策执行时间为1994年，设置虚拟变量  
. gen time = (year>=1994) & !missing(year)  
  
. * 假设政策执行地为大于4的地方，设置虚拟变量  
. gen treated = (country>4) & !missing(country)  
  
. * 构建DID估计量，即时间和空间的交互项  
. gen did = time*treated
```


• Examples for DID

```
. * DID <方法一>
. * 显然在10%水平上，政策实施有显著的负效应
. reg y did time treated, r
```

Linear regression

```
Number of obs   =      70
F(3, 66)        =      2.17
Prob > F         =     0.0998
R-squared        =     0.0827
Root MSE        =     3.0e+09
```

y	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
did	-2.52e+09	1.45e+09	-1.73	0.088	-5.42e+09	3.81e+08
time	2.29e+09	9.00e+08	2.54	0.013	4.92e+08	4.09e+09
treated	1.78e+09	1.05e+09	1.70	0.094	-3.11e+08	3.86e+09
_cons	3.58e+08	7.61e+08	0.47	0.640	-1.16e+09	1.88e+09

```
. * DID <方法二>
. qui reg y time##treated, r
```

DID in Stata

• Examples for DID

```
. * DID <方法三>
. * 与前两种方法结果一样

. *ssc install diff
. diff y, t(treated) p(time)
DIFFERENCE-IN-DIFFERENCES ESTIMATION RESULTS
Number of observations in the DIFF-IN-DIFF: 70
      Before      After
Control: 16      24      40
Treated: 12      18      30
       28      42
```

Outcome var.	y	S. Err.	t	P> t
Before				
Control	3.6e+08			
Treated	2.1e+09			
Diff (T-C)	1.8e+09	1.1e+09	1.58	0.120
After				
Control	2.6e+09			
Treated	1.9e+09			
Diff (T-C)	-7.4e+08	9.2e+08	0.81	0.422
Diff-in-Diff	-2.5e+09	1.5e+09	1.73	0.088*

R-square: 0.08
* Means and Standard Errors are estimated by linear regression
Inference: * p<0.01; ** p<0.05; * p<0.1

- Examples for DID

- ▶ Test Paralled Trend

- ★ 只有当地区在政策前足够相似才能够保证DID提取的是政策的因果效应；
 - ★ 因此，需要知道两组地区在政策前有多大差异；
 - ★ 生成年份虚拟变量 \times 实验组虚拟变量的交互项，捕捉两组地区在每一年的差异；
 - ★ 如果两组地区的确有Paralled Trend，那么预期在1994年前的那些交互项的回归结果将不显著，而1994年后的将显著。

- Examples for DID

- ▶ Test Paralled Trend

```
. *生成年份虚拟变量与实验组虚拟变量的交互项(此处选在政策前后各3年)
. gen Dyear = year-1994
. gen Before3 = (Dyear== -3 & treated==1)
. gen Before2 = (Dyear== -2 & treated==1)
. gen Before1 = (Dyear== -1 & treated==1)
. gen Current = (Dyear== 0 & treated==1)
. gen After1 = (Dyear== 1 & treated==1)
. gen After2 = (Dyear== 2 & treated==1)
. gen After3 = (Dyear== 3 & treated==1)
```

DID in Stata

• Examples for DID

► Test Paralled Trend

```
. * 将以上交互项作为解释变量进行回归
. * 可以看出Before3 Before2 Before1 的系数均不显著，After1的系数负向显著

. xtreg y time treated Before3 Before2 Before1 Current After1 After2 After3 i.year,
note: treated omitted because of collinearity
note: 1999.year omitted because of collinearity
Fixed-effects (within) regression              Number of obs   =          70
Group variable: country                       Number of groups  =           7
R-sq:                                         Obs per group:
    within = 0.3885                           min =          10
    between = 0.0116                          avg =         10.0
    overall = 0.3040                          max =          10
                                             F(16,47)         =         1.87
corr(u_i, Xb) = -0.0654                     Prob > F          =        0.0497
```

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
time	1.62e+09	1.40e+09	1.16	0.250	-1.18e+09	4.43e+09
treated	0	(omitted)				
Before3	5.26e+08	2.30e+09	0.23	0.820	-4.10e+09	5.16e+09
Before2	1.94e+09	2.30e+09	0.84	0.404	-2.69e+09	6.57e+09
Before1	-4.53e+08	2.30e+09	-0.20	0.845	-5.08e+09	4.18e+09
Current	-8.06e+08	2.30e+09	-0.35	0.728	-5.44e+09	3.82e+09
After1	-7.15e+09	2.30e+09	-3.10	0.003	-1.18e+10	-2.52e+09
After2	-9.04e+08	2.30e+09	-0.39	0.696	-5.54e+09	3.73e+09
After3	3.21e+08	2.30e+09	0.14	0.890	-4.31e+09	4.95e+09

• Examples for DID

- ▶ Test Paralled Trend
- ▶ -coefplot-图示

```
. * keep() : 保留关键变量
. * vertical : 转置
. * recast(connect) : 系数连线, 观察动态效果:
. * yline(0) : 增加直线y=0

. coefplot reg, keep(Before3 Before2 Before1 Current After1 After2 After3) ///
    vertical recast(connect) scheme(s1mono) msymbol(circle_hollow) ///
    yline(0, lwidth(vthin) lpattern(dash) lcolor(teal)) ///
    xline(4, lwidth(vthin) lpattern(dash) lcolor(teal)) ///
    ciopts(lpattern(dash) recast(rcap) msize(medium))

. graph export did.png,width(500) replace
(note: file did.png not found)
(file did.png written in PNG format)
```

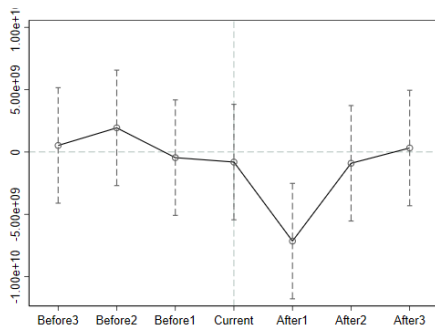
DID in Stata

- Examples for DID

- ▶ Test Paralled Trend

- ▶ `-coefplot-` 图示

- ★ 发现系数在政策前在0附近波动，而政策后一年系数显著为负，但很快又回到0附近；
 - ★ 说明treatment group和控制 group可以进行比较，而政策效果可能出现在颁布后一年，随后又很快消失。



Happy Christmas and New Year! & Get Good Marks in the Final Exam!

