1 Formulas

Maxwell's Equations

• Gauss's Law

$$\nabla.D = \rho$$

$$\iint_{S} D.ds = \iiint_{V} \rho dV = Q$$

The divergence of electric flux at a point equals to the charge density at this point.

• Gauss's Law for Magnetic Fields

$$\nabla .B = 0$$

$$\iint_{S} B dS = 0$$

There're no sink or source of B. B forms close loop.

• Farady's Law

$$\nabla \times E = -\frac{\delta B}{\delta t}$$

$$\oint E dL = -\int E dL = V = -\iint_{S} \frac{\delta B}{\delta t} dS$$

Electric field E arise due to a time changing magnetic flux density.

• Ampere's Law

$$\nabla \times H = J_C + \frac{\delta D}{\delta t}$$

$$\int_L H dL = \iint (J + \frac{\delta D}{\delta t}) dS = I$$

Magnetic field can arise due to conduction current density J or displacement current density.

Electric Field

$$E = \frac{Q}{4\pi\epsilon r^2}$$

, where $\epsilon = \epsilon_0 \epsilon_r$, $\epsilon_0 = 8.85 \times 10^{-12} Fm^{-1}$

$$E = -grad(V)$$

$$E = \frac{Q_1}{4\pi\epsilon_0} \frac{(x - x_1, y - y_1, z - z_1)}{((x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2)^{\frac{3}{2}}}$$

, where x_1, y_1, z_1 are the coordinates for the charge

Electric Flux

$$\Psi = \iint \epsilon E ds = \iint D ds$$

Electric Flux Density

$$D = \frac{\Psi}{A}$$

Capacitor

•
$$C = \frac{\epsilon A}{d}$$

$$\bullet \ E = \frac{1}{2}CV^2$$

Magnetic Flux

$$\Phi = \iint \mu H ds = \iint B ds$$

Magnetic Flux Density

$$B = \frac{\Phi}{A} = \mu H$$

Resistivity

$$\rho = \frac{RA}{l}$$

Drift Velocity

$$U_d = \mu_m E$$

Transmission Line

• Shunt Admittance: $Y = G + j\omega C$

• Series Impedance: $Z = R + j\omega L$

• Propagation Constant: \sqrt{ZY}

• Attenuation Constant: $Re\sqrt{ZY}$

• Phase Constant: $Im\sqrt{ZY}$

• Characteristic Impedance: $Z_{line} = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{R+j\omega L}{G+j\omega C}}$

• Propagation Speed: $\frac{1}{\sqrt{LC}}$

• Attenuation(in dB): $20log_{10}exp(\alpha \times L)$

• Voltage Standing-Wave Ratio(VSWR): $VSWR = \frac{1+\Gamma_v}{1-\Gamma_v}$

• Reflection coefficient for $V:\Gamma_v = \frac{Z_L - Z_0}{Z_L + Z_0}$

• Reflection coefficient for I: $\Gamma_i = -\frac{Z_L - Z_0}{Z_L + Z_0} = -\Gamma_v$

• Reflected Voltage: $V_r = V_i \times \Gamma_v$

• Reflected Current: $I_r = I_i \times \Gamma_i$

Poynting Vector

Table 1: Povnting Vector

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Property	Circuit	Field
Voltage	V	E
Current	I	H
Impedance	R	$Z = \sqrt{\frac{\mu}{\epsilon}}$
Average Power 1	$\frac{1}{2}Re(VI^*)$	$Z = \sqrt{\frac{\mu}{\epsilon}}$ $\frac{1}{2}Re(EH^*)$
Average Power 2	$\frac{1}{2} \times \frac{V^2}{R}$	$\frac{1}{2} \times \frac{E^2}{Z}$
Average Power 3	$\frac{1}{2}I^2R^n$	$\frac{1}{3}H^2\tilde{Z}$

2 Definitions

- Gauss's Law: Total electric flux over a volumn is equal to the charge enclosed by that volumn.
- Electric Field: E at at a point in a Electric field is the force act on the unit charge at this point.
- Absolute Potential: The work move a unit charge from infinity to a radial distance r1.
- Electric Flux: Electric Flux through a surface is the integral of normal component of electric field multiplied by ϵ .
- Electric Flux Density: Electric flux divided by A.
- Permittivity:Permittivity of vacuum multiplied by relative permittivity.
- **Drift Velocity**: The drift velocity is the flow velocity that a particle, such as an electron, attains in a material due to an electric field.
- Magnetic Flux Density: B equals to Magnetic flux Φ divided by area A.
- Relative Permeability: Ratio of effective permeability to absolute permeability.
- Permeability: The degree of magnetization of a material in response to a magnetic field.
- Transmission Line: Guide electromagnetic energy or info from one point to another.
- Application of Transmission Lines: Telephone, coaxial cables, micro strip tracks on a PCB
- AC Circuit Theory: $l << \lambda$
- Permittivity: Measures the resistance encountered when forming an electric field.

3 Tao Lu

3.1 Know D, find ρ

- 1. $\iint Dds = \rho$
- 2. Determine if the ρ from last step is what we want.
- 3. If isn't, for example, we want the ρ of a line, but we have ρ in a volumn, then find the ρ we want. We can multiply the ρ_v by S to obtain the ρ_L

3.2 Magnetic Flux Between Strips

- 1. $H = \frac{I}{W}$, where W is the width of the strip.
- 2. $\Phi = \mu H A$

3.3 Find EMF

- 1. Find EMF caused by change of B, $EMF = -\frac{d\Phi}{dt} = -\frac{AdB}{dt}$
- 2. Find EMF caused by $\int (v \times B) dL$
- 3. Add them together.

3.4 Wave Equation From Gauss's Law

- 1. We know $\nabla \times E = -\frac{dB}{dt}$
- 2. Calculate curl for both side. $\nabla \times \nabla \times E = \nabla \times \nabla \times -\frac{dB}{dt}$
- 3. Substitute $\nabla \times B = \mu_0 \epsilon_0 \frac{dE}{dt}$ into the equation obtained before
- 4. $\nabla \times \nabla \times E = \nabla(\nabla \cdot E) \nabla^2 E$, where $\nabla \cdot E$ is 0 in vacuum
- 5. $\nabla^2 E = \mu_0 \epsilon_0 \frac{dE}{dt}$

3.5 Finding Attenuation

- 1. Find α
- 2. Calculate $20log_{10}(exp(\alpha \times x))$, where x has the unit of meter.

3.6 Laplace Equation From Gauss's Law

- 1. $\nabla . D = \rho$
- 2. $D = \epsilon E = -\epsilon \nabla V$
- 3. $\nabla^2 V = \frac{\rho}{\epsilon}$
- 4. In free space, it is 0.