#### 1 Formulas

# Maxwell's Equations (Differential and Integral Form)

## • Gauss's Law

$$\nabla . D = \rho$$

$$\iint_{S} D ds = \iiint_{V} \rho dV = Q$$

The divergence of electric flux at a point equals to the charge density at this point.

# • Gauss's Law for Magnetic Fields

$$\nabla .B = 0$$

$$\iint_{S} B ds = 0$$

There're no sink or source of B. B forms close loop.

## • Farady's Law

$$\nabla \times E = -\frac{\delta B}{\delta t}$$
 
$$\oint E dL = -\iint_{S} \frac{\delta B}{\delta t} dS = V$$

Electric field E arise due to a time changing magnetic flux density.

# • Ampere's Law

$$\nabla \times H = J_C + \frac{\delta D}{\delta t}$$

$$\oint_L H dL = \iint_S (J + \frac{\delta D}{\delta t}) ds = I$$

Magnetic field can arise due to conduction current density J or displacement current current density.

### Electric Field

$$E = \frac{Q}{4\pi\epsilon r^2}$$

, where  $\epsilon = \epsilon_0 \epsilon_r$ ,  $\epsilon_0 = 8.85 \times 10^{-12} Fm^{-1}$ 

$$E = -grad(V)$$

Electric Flux

$$\Psi = \iint \epsilon E ds = \iint D ds$$

Electric Flux Density

$$D = \frac{\Psi}{A}$$

Capacitor

- $C = \frac{\epsilon A}{d}$
- $E = \frac{1}{2}CV^2$

Magnetic Flux

$$\Phi = \iint \mu H ds = \iint B ds$$

Magnetic Flux Density

$$B = \frac{\Phi}{A} = \mu H$$

Resistivity

$$\rho = \frac{RA}{l}$$

**Drift Velocity** 

$$U_d = \mu_m E$$

Transmission Line

• Shunt Admittance:  $Y = G + j\omega C$ 

• Series Impedance:  $Z = R + j\omega L$ 

• Propagation Constant:  $\sqrt{ZY}$ 

• Attenuation Constant: $Re\sqrt{ZY}$ 

• Phase Constant: $Im\sqrt{ZY}$ 

• Characteristic Impedance: $Z_{line} = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{R+j\omega L}{G+j\omega C}}$ 

• Propagation Speed:  $\frac{1}{\sqrt{LC}}$ 

• Attenuation(in dB):  $20log_{10}exp(\alpha \times L)$ 

• Voltage Standing-Wave Ratio(VSWR):  $VSWR = \frac{1+\Gamma_v}{1-\Gamma_v}$ 

• Reflection coefficient for  $V:\Gamma_v=rac{Z_L-Z_0}{Z_L+Z_0}$ 

• Reflection coefficient for I: $\Gamma_i = -\frac{Z_L - Z_0}{Z_L + Z_0} = -\Gamma_v$ 

• Reflected Voltage:  $V_r = V_i \times \Gamma_v$ 

• Reflected Current:  $I_r = I_i \times \Gamma_i$ 

• Reflected Current and Voltage:  $V_r + V_i = V$ ,  $I_r + I_i = I = \frac{V}{R_L}$ 

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#### 2 Definitions

- Gauss's Law: Total electric flux over a volumn is equal to the charge enclosed by that volumn.
- Electric Field: E at at a point in a Electric field is the force act on the unit charge at this point.
- **Absolute Potential**: The work move a unit charge from infinity to a radial distance r1.
- Electric Flux: Electric Flux through a surface is the integral of normal component of electric field multiplied by  $\epsilon$ .
- Electric Flux Density: Electric flux divided by A.
- **Permittivity**:Permittivity of vacuum multiplied by relative permittivity.
- Drift Velocity: Mobility multiplied by E.
- Magnetic Flux Density: B equals to Magnetic flux  $\Phi$  divided by area A.
- Relative Permeability: Ratio of effective permeability to absolute permeability.
- **Permeability**: The degree of magnetization of a material in response to a magnetic field.
- **Transmission Line**: Guide electromagnetic energy or info from one point to another.
- Application of Transmission Lines: Telephone, coaxial cables, micro strip tracks on a PCB ......
- AC Circuit Theory:  $l << \lambda$
- **Permittivity**: Measures the resistance encountered when forming an electric field.

### 3 Tao Lu

# 3.1 Know D, find $\rho$

- 1.  $\iint Dds = \rho$
- 2. Determine if the  $\rho$  from last step is what we want.
- 3. If isn't, for example, we want the  $\rho$  of a line, but we have  $\rho$  in a volumn, then find the  $\rho$  we want.

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### 3.2 Magnetic Flux Between Strips

- 1.  $H = \frac{I}{W}$ , where W is the width of the strip.
- 2.  $\Phi = \mu H A$

## 3.3 Find EMF

- 1. Find EMF caused by change of B,  $EMF = -\frac{d\Phi}{dt} = -\frac{AdB}{dt}$
- 2. Find EMF caused by  $\int (v \times B) dL$
- 3. Add them together.

### 3.4 Wave Equation From Gauss's Law

- 1. We know  $\nabla \times E = -\frac{dB}{dt}$
- 2. Calculate curl for both side.  $\nabla \times \nabla \times E = \nabla \times \nabla \times -\frac{dB}{dt}$
- 3. Substitute  $\nabla \times B = \mu_0 \epsilon_0 \frac{dE}{dt}$  into the equation obtained before
- 4.  $\nabla \times \nabla \times E = \nabla(\nabla \cdot E) \nabla^2 E$ , where  $\nabla \cdot E$  is 0 in vacuum
- 5.  $\nabla^2 E = \mu_0 \epsilon_0 \frac{dE}{dt}$