

1 Formulas

Maxwell's Equations (Differential and Integral Form)

- Gauss's Law

$$\nabla \cdot D = \rho$$
$$\iint_S D ds = \iiint_V \rho dV = Q$$

The divergence of electric flux at a point equals to the charge density at this point.

- Gauss's Law for Magnetic Fields

$$\nabla \cdot B = 0$$
$$\iint_S B ds = 0$$

There're no sink or source of B. B forms close loop.

- Farady's Law

$$\nabla \times E = -\frac{\delta B}{\delta t}$$
$$\oint E dL = - \iint_S \frac{\delta B}{\delta t} dS = V$$

Electric field E arise due to a time changing magnetic flux density.

- Ampere's Law

$$\nabla \times H = J_C + \frac{\delta D}{\delta t}$$
$$\oint_L H dL = \iint_S (J + \frac{\delta D}{\delta t}) ds = I$$

Magnetic field can arise due to conduction current density J or displacement current density.

Electric Field

$$E = \frac{Q}{4\pi\epsilon r^2}$$

, where $\epsilon = \epsilon_0\epsilon_r$, $\epsilon_0 = 8.85 \times 10^{-12} Fm^{-1}$

$$E = -grad(V)$$

Electric Flux

$$\Psi = \iint \epsilon E ds = \iint D ds$$

Electric Flux Density

$$D = \frac{\Psi}{A}$$

Capacitor

- $C = \frac{\epsilon A}{d}$
- $E = \frac{1}{2}CV^2$

Magnetic Flux

$$\Phi = \iint \mu H ds = \iint B ds$$

Magnetic Flux Density

$$B = \frac{\Phi}{A} = \mu H$$

Resistivity

$$\rho = \frac{RA}{l}$$

Drift Velocity

$$U_d = \mu_m E$$

Transmission Line

- Shunt Admittance: $Y = G + j\omega C$
- Series Impedance: $Z = R + j\omega L$
- Propagation Constant: \sqrt{ZY}
- Attenuation Constant: $Re\sqrt{ZY}$
- Phase Constant: $Im\sqrt{ZY}$
- Characteristic Impedance: $Z_{line} = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{R+j\omega L}{G+j\omega C}}$
- Propagation Speed: $\frac{1}{\sqrt{LC}}$
- Attenuation(in dB): $20\log_{10}exp(\alpha \times L)$
- Voltage Standing-Wave Ratio(VSWR): $VSWR = \frac{1+\Gamma_v}{1-\Gamma_v}$
- Reflection coefficient for V: $\Gamma_v = \frac{Z_L - Z_0}{Z_L + Z_0}$
- Reflection coefficient for I: $\Gamma_i = -\frac{Z_L - Z_0}{Z_L + Z_0} = -\Gamma_v$
- Reflected Voltage: $V_r = V_i \times \Gamma_v$
- Reflected Current: $I_r = I_i \times \Gamma_i$
- Reflected Current and Voltage: $V_r + V_i = V, I_r + I_i = I = \frac{V}{R_L}$

2 Definitions

- **Gauss's Law:** Total electric flux over a volume is equal to the charge enclosed by that volume.
- **Electric Field:** E at a point in an electric field is the force acting on the unit charge at this point.
- **Absolute Potential:** The work to move a unit charge from infinity to a radial distance r_1 .
- **Electric Flux:** Electric Flux through a surface is the integral of normal component of electric field multiplied by ϵ .
- **Electric Flux Density:** Electric flux divided by A .
- **Permittivity:** Permittivity of vacuum multiplied by relative permittivity.
- **Drift Velocity:** Mobility multiplied by E .
- **Magnetic Flux Density:** B equals to Magnetic flux Φ divided by area A .
- **Relative Permeability:** Ratio of effective permeability to absolute permeability.
- **Permeability:** The degree of magnetization of a material in response to a magnetic field.
- **Transmission Line:** Guide electromagnetic energy or info from one point to another.
- **Application of Transmission Lines:** Telephone, coaxial cables, micro strip tracks on a PCB
- **AC Circuit Theory:** $l \ll \lambda$
- **Permittivity:** Measures the resistance encountered when forming an electric field.

3 Tao Lu

3.1 Know D , find ρ

1. $\iint D ds = \rho$
2. Determine if the ρ from last step is what we want.
3. If isn't, for example, we want the ρ of a line, but we have ρ in a volume, then find the ρ we want.

3.2 Magnetic Flux Between Strips

1. $H = \frac{I}{W}$, where W is the width of the strip.
2. $\Phi = \mu H A$

3.3 Find EMF

1. Find EMF caused by change of B, $EMF = \frac{d\Phi}{dt} = \frac{AdB}{dt}$
2. Find EMF caused by $\int (v \times B) dL$
3. Add them together.

3.4 Wave Equation From Gauss's Law

1. We know $\nabla \times E = -\frac{dB}{dt}$
2. Calculate curl for both side. $\nabla \times \nabla \times E = \nabla \times \nabla \times -\frac{dB}{dt}$
3. Substitute $\nabla \times B = \mu_0\epsilon_0 \frac{dE}{dt}$ into the equation obtained before
4. $\nabla \times \nabla \times E = \nabla(\nabla \cdot E) - \nabla^2 E$, where $\nabla \cdot E$ is 0 in vacuum
5. $\nabla^2 E = \mu_0\epsilon_0 \frac{dE}{dt}$