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Genetic Optimization for Multirotor UAV Design

Section I. Project Summary

Introduction

Multirotor unmanned air vehicles (UAVs) are becoming an increasingly valuable asset in a variety of professional fields. Their vertical take-off and landing capability makes them particularly well-suited for a broad range of tasks. A primary weakness of multirotor aircraft however is limited flight time. Typical multirotor UAVs have a flight time of 20 to 35 minutes. While the greatest factor in limited flight time is battery energy density, great improvements in flight time can be achieved through optimal multirotor power systems configurations. In this project I implement a genetic optimization algorithm to find the optimal set of motors, propellers, and batteries in order to maximize multirotor flight time.

Objective (Primary)

Maximize Total Flight Time

Chromosome Fitness: fitness = flight time

Algorithm Parameters

Generation Size: N = 50

Number of Generations: n_gen = 20

Crossover Probability: p_crossover = 0.50 Mutation Probability: p_mutation = 0.10 Roulette Exponent: roulette_exponent = 2 Dynamic Mutation parameter, β: beta = 1

Algorithm Methods

Selection: Roulette Wheel Selection

Crossover: Blend Crossover & Point Crossover

Mutation: Dynamic Mutation

Elitism: Most-fit of current and previous generation

Optimal Design

```
optimal_design = [1, 2, 1, 4, 1, 1]
optimal_fitness = 0.9643 (hours)
```

Section II. Procedure

Chromosome and Fitness

The first step in implementing the genetic algorithm was to define the algorithm chromosome or set of design variables. For this problem, the chromosome consists of six integer variables that each represent an aspect of the multirotor's design. A complete description of the chromosome is given in Figure 1.

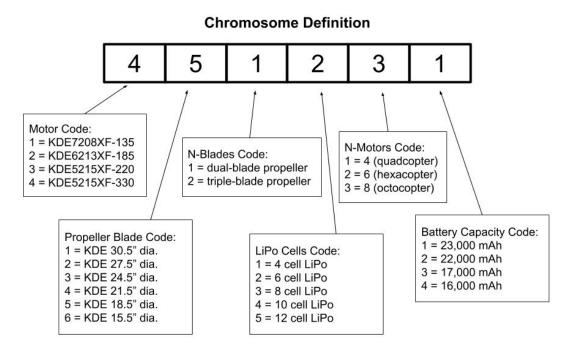


Figure 1. Chromosome representing the six design variables

After defining the chromosome, the next step is to define chromosome fitness and to construct a model to evaluate the fitness of any given chromosome. Since the goal of the optimization is to maximize flight time, fitness was simply defined as total predicted flight time for the given design. Evaluation of chromosome fitness proceeded as follows and can be seen in *compute_fitness.m* given in the Appendix:

- 1) Compute total mass of the design defined by the chromosome
 - mass = f(motor, prop-dia, n-motors, battery, ...)
 - See compute_mass.m in Appendix
- 2) Compute required thrust from each motor needed to hover
- 3) Look-Up the current draw for the given motor, propeller, and battery at the required thrust
 - For the given design, fit a polynomial curve to the motor, propeller, and battery data obtained from KDE Direct (brushless DC motor manufacturer)
 - Evaluate the individual motor current draw using the polynomial fit
 - See *get_amps.m* in Appendix
- 4) Compute the total current draw at hover for the given design
 - total_current = individual_current * n_motors
- 5) Compute total predicted flight time (fitness)

Note: As mentioned in step 3 above, the current draw for a given design was approximated according to published motor testing data from the motor manufacturer. Although there is bound to be some error in the polynomial curve fit (since the manufacturer only supplies limited data points), using actual test data and constructing 'Look-Up' routines was identified as being a more accurate approach than to attempt to fully define a mathematical model to predict motor performance. Motor-propeller performance is particularly difficult to model due to many sources of uncertainty (actual aerodynamic forces and coefficients, actual motor output, drag, friction, viscous effects, turbulent flow, etc.). Because the results of this optimization were intended to be realistic and usable, using actual test data was determined to be the best route to success.

With the ability to evaluate fitness of any given design, the genetic process can now begin.

Genetic Process

The genetic process consists of four primary steps namely selection, crossover, mutation, and elitism. Details on each of these steps are given below:

Selection—For this algorithm a 'roulette wheel' selection routine was chosen and implemented. In this method, parent chromosomes are randomly selected from the current generation with chromosomes having greater fitness having a greater chance of being selected. To slightly increase fitness pressure, a roulette exponent of 2 was used. Further details of this method can be seen in *roulette_selection.m* given in the Appendix.

Crossover—Two types of crossover were implemented and experimented with in the tuning of the algorithm. The first was 'blend crossover'. This method has the advantage of being able to mix the genes of the parents in order to produce a child. The second was 'single point crossover'. In this method crossover takes place by simply swapping the genetic material of the two parent chromosomes after a randomly chosen crossover point. In both cases the crossover probability was dialed in to be 0.5. After several trials, blend crossover was found to be slightly more robust at producing fit children than point crossover (although in most cases, both methods produced good results). See *blend_crossover.m* and *point_crossover.m* in the Appendix for more details.

Mutation—To introduce variety into each generation, a mutation step was performed. In this genetic algorithm, a 'dynamic mutation' routine was implemented. Dynamic mutation has the advantage of allowing greater mutations in earlier generations, and less mutation in later generations—which is oftentimes favorable. Through experimentation, a mutation probability of 0.10 was found to give good results paired with the mutation parameter $\beta = 1$. See *dynamic_mutation.m* in the Appendix.

Elitism—To ensure that only the most-fit chromosomes survived to the next generation, an elitism step was performed on each generation. After a new generation has been formed through several iterations of selection, crossover, and mutation, only the N most-fit designs from the new-generation *and* the previous generation were actually chosen to represent the next generation. Implementation details of this step can be seen in *elitism.m* in the Appendix.

A generation size of 50 with a total of 20 generations was found to be a robust and efficient set of global algorithm parameters for consistently finding the global optimum design.

Section III. Results

Single Objective Results

The optimal design found by the genetic process is given below:

```
optimal_design = [1, 2, 1, 4, 1, 1]
Optimal Design Specifications:
motor: KDE7208XF-135
propeller: KDE 27.5 inch diameter dual-blade prop
motor configuration: 4 motors (quadcopter)
battery: 10S 37.0V 23,000 mAh LiPo
```

Which had a fitness of **0.9343 hours** or **56.1 minutes**. Since the space of this particular problem was not excessively large (approximately 3,000 possible designs), and all parameters have discrete values, a brute-force search for the optimum was also performed. This search verified that the optimal design found by the algorithm represented the **global optimum** of the design space.

The inspiration for this project came from a past internship where I was working with a pair of industrial multirotor UAVs. A chromosome representing their design is:

```
previous_design = [4, 5, 1, 2, 3, 1]
```

The optimal design given by the genetic algorithm represents a **119.8%** (more than double) increase in total flight time over this previous design! Evaluating the previous design was also a good validity check for the objective model. Using the objective model, the previous design resulted in a flight time (fitness) of 25.5 minutes. This almost exactly matches the performance I experienced with this particular design on my internship, and further increases confidence in the developed model.

In addition to finding the optimum, the genetic algorithm performed very consistently and steadily increased the overall fitness of designs with each successive generation. The algorithm found the global optimum ~95% of the time and found a solution within 5% of the global optimum 99% of the time. The plots in Figure 2 and Figure 3 show the average fitness as a function of generation number for two separate executions of the algorithm.

Dual objective Results

Maximizing flight time is an important factor in multirotor design but there are also other objectives to consider. One possible objective is total rotor-disc area. Rotor-disc area is simply the combined area of the lifting discs formed by the spinning rotors. In many cases reducing rotor-disc area is important so that the multirotor can maintain a lower aerodynamic profile—which naturally increases its resistance to wind disturbances. To explore the effect of also trying to minimize rotor disc area, I defined a second fitness function as:

```
fitness = rotor disc area
```

I then used this function along with the previous objective of maximizing flight time to compute the *Maximin* fitness of each design in the population (see *pareto.m* in the Appendix). Using this new fitness, I was able to identify the Pareto front of the dual objective space and a plot of this is given in Figure 4.

Based on the dual objective Pareto front, I selected the following as the 'best' overall design:

pareto design* =
$$[3, 4, 1, 5, 1, 1]$$

Selecting this design results in only a **10.3%** decrease in total flight time when compared to the single-objective optimum, and also gives a **38.9%** decrease in rotor disc area.

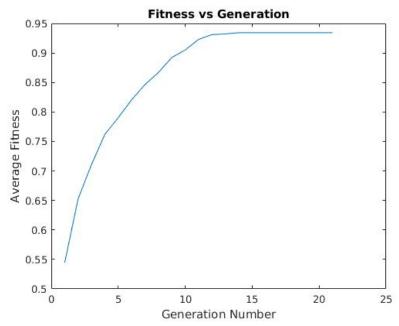


Figure 2

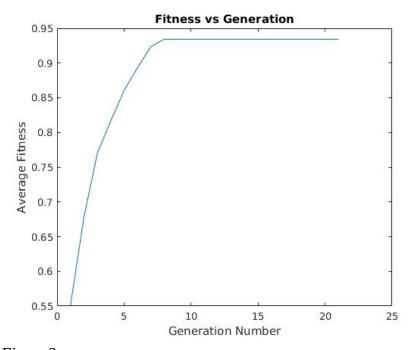


Figure 3

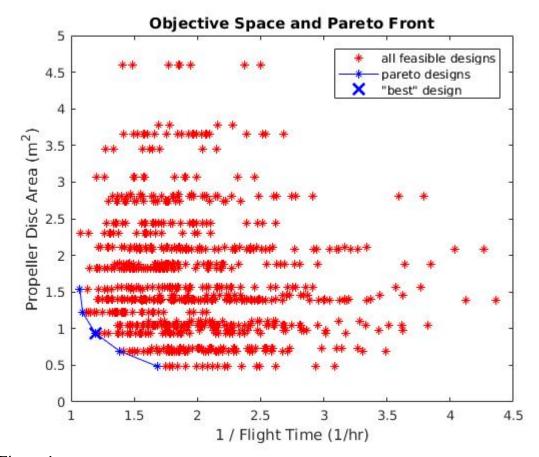


Figure 4

Section IV. Discussion

The results given previously provide good evidence that the developed algorithm is indeed an effective implementation of the genetic optimization approach. Although the design space for this particular problem is relatively small (\sim 3,000) possible designs, I believe that the algorithm would also perform well in much larger design spaces. The results of the optimization also seem to be very reasonable and support the notion that the developed model accurately represents reality. In general, larger propellers at lower rotational speeds are known to be more efficient than smaller propellers at higher speeds, and the results also support this.

Although the algorithm found the global optimum $\sim 95\%$ of the time, further performance increases could likely be achieved by additional fine-tuning of the algorithm parameters. Increasing generation size and number of generations seems to help in general, but doing so also costs additional (and sometimes very significant) computation time.

Section V. Appendix

A listing of all MATLAB scripts and functions is given below in alphabetical order by filename:

Main Optimization Script: genetic_multi_optimization.m

```
clc
clear
close all
% Algorithm Tuning Params
N = 50; % Generation size
n_gen = 20; % Number of generations
p crossover = 0.5; % Probability that crossover occurs
p mutation = 0.10; % Probability that mutation occurs
roulette exponent = 2; % Fitness pressure (larger exponents give designs
              % with greatest fitness a greater chance of being
              % selected as parents)
beta = 1:
                  % dynamic mutation param
% Other Params
                % Number of genes (design variables) per chromosome
n genes = 6;
% -----
% Chromosome Definition
% -----
% A chromosome for this problem is defined by 6 integer design variables:
% Variable 1: Motor
% Values: 1, 2, 3, or 4 corresponding to four different brushles DC
%
         motors available from a manufacturer
% Variable 2: Propeller Blade
% Values: 1, 2, 3, 4, 5, or 6 corresponding to six available propeller
%
         blade profiles
% Variable 3: Number of Propeller Blades
   Values: 1, or 2 corresponding to 2 or 3 propeller blades per motor
% Variable 4: Number of LiPo Battery Cells
     Values: 1, 2, 3, 4, or 5 corresponding to 4, 6, 8, 10, or 12 lithium
%
          polymer battery cells (each nominally 3.7 volts)
%
% Variable 5: Number of Motors
% Values: 1, 2, or 3 corresponding to 4 (quadcopter), 6 (hexacopter),
%
         or 8 (octocopter) motors and arms
%
% Variable 6: Battery Capacity
% Values: 1, 2, 3, or 4 corresponding to 23, 22, 17, and 16 amp hour
         (Ah) capacities available from a battery manufacurer
% End Chromosome Definition
% -----
% Memory Allocation
generation = zeros(N, n genes);
```

```
avg fitness = [];
% Randomly select the first generation
feasible = zeros(N,1);
for i = 1:N
  while ~feasible(i)
     for j = 1:n genes
       switch i
          case 1
            generation(i,j) = randi(4);
            generation(i,j) = randi(6);
          case 3
            generation(i,j) = randi(2);
          case 4
            generation(i,j) = randi(5);
          case 5
            generation(i,j) = randi(3);
          case 6
            generation(i,j) = randi(4);
          otherwise
            disp("Error. Number of genes does not match number of cases.")
       end
     end
     % Check to see if the current chromosome is feasible
     check feasible = get amps(1, generation(i,:));
     if check_feasible == -1
       feasible(i) = 0;
       % disp("bad design")
       feasible(i) = 1;
     end
  end
end
first generation = generation;
% disp(first generation)
avg fit = compute average fitness(first generation);
avg_fitness = [avg_fitness; avg_fit];
for i=1:n gen
  % Allocate memory for the new generation
  new_generation = zeros(N, n_genes);
  spots remaining = N;
  count = 0;
  % while there's room to add at least two more children to the new
  % generation...
  while spots_remaining >= 2
     count = count + 1;
```

```
% SELECTION STEP:
    % Pick two designs from the current generation to become parents
    parents = roulette selection(generation, roulette exponent);
    % CROSSOVER STEP:
    children = blend crossover(parents, p crossover);
    %children = point crossover(parents, p crossover);
    % MUTATION STEP:
    for k=1:2
       children(k,:) = dynamic mutation(children(k,:), p mutation, i, n gen, beta);
    end
    % add the children to the new generation
    new generation(2*count-1,:) = children(1,:);
    new generation(2*count,:) = children(2,:);
    spots remaining = spots remaining - 2;
  end
  % The new generation is full, now we perform elitism to ensure that the
  % new generation has superior fitness
  % ELITISM STEP:
  % Take the most fit chromosomes from the old generation and the new
  % generation to represent the next generation
  generation = elitism(generation, new generation);
  avg_fit = compute_average_fitness(generation)
  avg fitness = [avg fitness; avg fit];
end
% Get the best design from the final generation and this is your optimal
% design produced by the genetic algorithm:
optimal design = get best of generation(generation);
opt fit = compute fitness(optimal design);
% This is the design that most-closely represents LLNL's current copter
% Flight time is ~ 25 minutes
starting design = [4, 5, 1, 2, 3, 1];
fit0 = compute fitness(starting design);
diff = opt fit - fit0;
percent improvement = (diff/fit0) * 100:
disp('---->')
disp("Genetic Algorithm Finished.")
optimal design
minutes = opt fit * 60;
disp("Total flight time (minutes): " + num2str(minutes))
disp(newline)
```

```
disp("Objective increase from initial design: " + num2str(percent improvement) + "%")
disp(newline)
parse and display design(optimal design);
% plots
figure(1), clf
generations = 1:n gen + 1;
plot(generations, avg fitness)
xlabel('Generation Number')
ylabel('Average Fitness')
title('Fitness vs Generation')
blend_crossover.m:
function children = blend crossover(parents, p crossover)
[n parents, n genes] = size(parents);
% Pick a random value between 0 and 1
val = rand(1):
% Determine whether or not crossover takes place
if val <= p crossover
  % Perform blend crossover
else
  % No crossover occurs and the children are clones of the parents
  children = parents;
  return
end
% Initialize matrix to hold children
children = zeros(n_parents, n_genes);
for i=1:n genes
  % Pick a random value between 0 and 1
  r = rand(1);
  % Perform the blend crossover
  children(1,i) = r*parents(1,i) + (1-r)*parents(2,i);
  children(2,i) = (1-r)*parents(1,i) + r*parents(2,i);
  % Since each gene of the children chromosomes (designs) must be an
  % integer value in order to be valid, we round to the closest integer
  children(1,i) = round(children(1,i));
  children(2,i) = round(children(2,i));
  % And since each gene has a valid range of values, we saturate the
  % values to their max or min
  switch i
     case 1
       children(1,i) = saturate(children(1,i), 4, 1);
       children(2,i) = saturate(children(2,i), 4, 1);
     case 2
       children(1,i) = saturate(children(1,i), 6, 1);
       children(2,i) = saturate(children(2,i), 6, 1);
```

```
case 3
       children(1,i) = saturate(children(1,i), 2, 1);
       children(2,i) = saturate(children(2,i), 2, 1);
       children(1,i) = saturate(children(1,i), 5, 1);
       children(2,i) = saturate(children(2,i), 5, 1);
     case 5
       children(1,i) = saturate(children(1,i), 3, 1);
       children(2,i) = saturate(children(2,i), 3, 1);
       children(1,i) = saturate(children(1,i), 4, 1);
       children(2,i) = saturate(children(2,i), 4, 1);
     otherwise
       disp("Error. Number of genes does not match number of cases.")
       return
  end
end
end
function rval = saturate(val, max, min)
if val > max
  rval = max;
elseif val < min
  rval = min;
else
  rval = val;
end
end
compute_average_fitness.m:
function avg fitness = compute average fitness(generation)
[rows, \sim] = size(generation);
fit vals = zeros(rows, 1);
for i=1:rows
  fit vals(i) = compute fitness(generation(i,:));
avg_fitness = sum(fit_vals)/rows;
end
```

compute_fitness.m:

```
function fitness = compute fitness(design)
% Fitness will be predicted flight time
% Higher values are better
% Flight time will be computed as capacity of the battery in amp hours
% (Ah) divided by current (Amps) required to maintain hover. (h = Ah /
% Amps).
% INPUTS:
% design = [motor code, prop blade code, n blades code, n cells code,
        n motors code, bat cap code]
% Constants accross all designs:
mass_body = 5; % mass of the central hub of the multirotor (kg)
delta = 0.05; % clearance between adjacent propellers (meters)
mass arm = 0.5; % mass per meter of material used to construct arms (kg/m)
% first check to see if we even have motor data for the given design
check = get amps(5, design);
if check == -1
  fitness = 0;
  return
end
% Get the mass of the motor for the given design
motor code = design(1);
switch motor code
  % mass motor (kg)
  case 1
    mass motor = 0.445;
  case 2
    mass motor = 0.415;
  case 3
    mass_motor = 0.360;
  case 4
    mass motor = 0.360;
  otherwise
    fitness = 0;
    return
end
% Get the propeller diameter for the given design
prop blade code = design(2);
switch prop blade code
  % D = propeller diameter (meters)
```

```
case 1
     D = 30.5 * 0.0254; % convert inches to meters
     D = 27.5 * 0.0254;
  case 3
     D = 24.5 * 0.0254;
  case 4
     D = 21.5 * 0.0254;
  case 5
     D = 18.5 * 0.0254;
  case 6
     D = 15.5 * 0.0254;
  otherwise
     fitness = 0;
     return
end
% Get the number of battery cells for the given design
n_cells_code = design(4);
switch n cells code
  % (int) n_cells = number of LiPo cells
  case 1
     n_{cells} = 4;
  case 2
     n_cells = 6;
  case 3
     n_cells = 8;
  case 4
    n_cells = 10;
  case 5
     n_{cells} = 12;
  otherwise
     fitness = 0;
     return
end
% Get the number of motors for the given design
n_motors_code = design(5);
switch n_motors_code
  % (int) n = number of motors
  case 1
     n = 4;
```

```
case 2
    n = 6;
  case 3
    n = 8;
  otherwise
    fitness = 0;
     return
end
% Get the battery capacity for the given design
bat_cap_code = design(6);
switch bat_cap_code
  % bat_cap = battery capacity in amp hours (Ah)
  case 1
    bat_cap = 23;
  case 2
    bat_cap = 22;
  case 3
    bat cap = 17;
  case 4
    bat_cap = 16;
  otherwise
    fitness = 0;
     return
end
if bat cap == 23
  cell_mass = 0.413;
elseif bat cap == 22
  cell mass = 0.422;
elseif bat_cap == 17
  cell mass = 0.321;
elseif bat cap == 16
  cell_mass = 0.310;
else
  fitness = 0;
  return
end
% compute battery mass
mass_battery = cell_mass * n_cells;
% compute total mass of multirotor design
mass_total = compute_mass(n, D, delta, mass_body, mass_motor, mass_battery, mass_arm);
% compute hover thrust (equal to total weight)
thrust_total = mass_total * 9.81;
% compute required thrust per motor
thrust_motor = thrust_total / n;
```

```
% compute current draw (Amps) per motor
amps motor = get amps(thrust motor, design);
% compute total current draw
amps = amps_motor * n;
% finally, compute fitness or total flight time (hours)
flight time = bat cap / amps;
fitness = flight time;
end
compute_fitness2.m:
function fitness = compute fitness2(design)
% Fitness will be rotor disc area
% Lower values are better for wind resistance
% Rotor disc area will be computed as A = n * (pi * (D/2)^2).
% INPUTS:
% design = [motor code, prop blade code, n blades code, n cells code,
        n motors code, bat cap code]
% first check to see if we even have motor data for the given design
check = get amps(5, design);
if check == -1
  fitness = 999;
  return
end
% Get the propeller diameter for the given design
prop_blade_code = design(2);
switch prop blade code
  % D = propeller diameter (meters)
     D = 30.5 * 0.0254; % convert inches to meters
  case 2
    D = 27.5 * 0.0254;
  case 3
    D = 24.5 * 0.0254;
  case 4
     D = 21.5 * 0.0254;
  case 5
```

```
D = 18.5 * 0.0254;
  case 6
     D = 15.5 * 0.0254;
  otherwise
     fitness = 999;
     return
end
% Get the number of propeller blades
n_blade_code = design(3);
switch n_blade_code
  case 1
     n_blades = 2;
  case 2
     n_blades = 3;
  otherwise
     fitness = 999;
     return
end
% Get the number of motors for the given design
n_motors_code = design(5);
switch n_motors_code
  % (int) n = number of motors
  case 1
     n = 4;
  case 2
     n = 6;
  case 3
     n = 8;
  otherwise
     fitness = 999;
     return
end
% compute the rotor disc area
A = n * (pi * (D/2)^2);
if n blades == 3
  \bar{A} = A * 1.5;
end
% fitness
fitness = A;
```

case 1

x max = 4;

compute_mass.m: function m total = compute mass(n, D, delta, mass body, mass motor, mass battery, mass arm) % inputs % n = number of motors/arms % D = propeller Diameter (m) % delta = desired clearance between adjacent spinning props (m) % mass body = mass of multirotor hub (center frame, autopilot, etc)(kg) % mass motor = mass of each individual motor (kg) % mass battery = battery mass (kg) % mass arm = mass per meter of the tube material used to make the arms (kg/m) % Angle between arms theta = 2*pi/n; % Compute the required arm length $I \text{ arm} = (D + \text{delta}) / (2*\sin(\text{theta/2}));$ % Compute total mass $m_{total} = n*(l_{arm} * mass_{arm}) + mass_{body} + n*mass_{motor} + mass_{battery};$ end dynamic_mutation.m: function new chromosome = dynamic mutation(chromosome, p mutation, j, M, beta) num genes = length(chromosome); % Compute alpha (eq. 6.9) $alpha = (1-((i-1)/M))^beta;$ % minimum value for all genes is 1 x min = 1;for i=1:num genes % pick a random number to decide if mutation occurs val = rand(1); if val <= p_mutation % mutate the current gene else % skip to the next gene without mutating continue end switch i

```
case 2
       x_max = 6;
     case 3
       x_max = 2;
     case 4
       x max = 5;
     case 5
       x max = 3;
     case 6
       x max = 4;
     otherwise
       disp("Error. Number of genes does not match number of cases.")
  end
  % pick a random number between the min and max allowed values for the
  % current gene
  r = random_number_between_two_values(x_min, x_max);
  % get the gene's current value
  x = chromosome(1, i);
  % eq 6.8
  if r <= x
    chromosome(1,i) = x_min + ((r - x_min)^alpha)*((x - x_min)^(1-alpha));
     chromosome(1,i) = x_max - ((x_max - r)^alpha)*((x_max - x)^(1-alpha));
  end
  % round to the nearest integer value
  chromosome(1,i) = round(chromosome(1,i));
  % saturate just in case
  chromosome(1,i) = saturate(chromosome(1,i), x max, x min);
end
new_chromosome = chromosome;
end
function r = random_number_between_two_values(x_min, x_max)
r = x_min + (x_max - x_min) .* rand(1);
end
function rval = saturate(val, max, min)
if val > max
  rval = max;
elseif val < min
  rval = min;
else
  rval = val;
end
end
```

```
elitism.m:
```

```
function next generation = elitism(generation, new generation)
[rows, cols] = size(generation);
% memory allocation
next_generation = zeros(rows, cols);
% the composite generation is the old and new generation stacked on top of
% each other
comp gen = vertcat(generation, new generation);
% vector to hold the fitnesses of each chromosome
comp fitness = zeros(2*rows, 1);
for i=1:2*rows
  % evaluate the fitness of each chromosome (design) and store it in our
  % vector
  comp fitness(i) = compute fitness(comp gen(i,:));
end
% sort the comp fitness vector in descending order (greatest ---> smallest)
% and get the indexes
[~, index] = sort(comp_fitness, 'descend');
% add the best chromosomes (designs) to the next generation
for i=1:rows
  % value of mIndex is the index from comp gen corresponding to one of
  % the top 10 best (most fit) desings
  mIndex = index(i);
  % fill out the next generation by grabbing the mIndex-th row from the
  % composite generation
  next_generation(i,:) = comp gen(mIndex,:);
end
end
get_amps.m:
function amps = get amps(thrust, design)
% INPUTS:
% thrust: Required thrust in Newtons for each motor given the design
% design: Array of the design variables in integer representations
% design = [motor code, prop blade code, n blades code, n cells code,
        n motors code, bat cap code]
% motor codes:
% 1 = KDE7208XF-135
% 2 = KDE6213XF-185
```

```
% 3 = KDE5215XF-220
% 4 = KDE5215XF-330
% prop blade codes:
% 1 = KDE 30.5"
% 2 = KDE 27.5"
% 3 = KDE 24.5"
% 4 = KDE 21.5"
\% 5 = KDE 18.5"
% 6 = KDE 15.5"
% n blades codes:
% 1 = dual-blade
% 2 = triple-blade
% n cells codes:
% 1 = 45
% 2 = 65
% 3 = 85
% 4 = 10S
% 5 = 12S
% n motors codes:
% 1 = 4 (quad)
% 2 = 6 \text{ (hex)}
% 3 = 8 (octo)
% bat cap codes
% 1 = 23,000 \text{ mAh}
% 2 = 22,000 \text{ mAh}
% 3 = 17,000 \text{ mAh}
% 4 = 16,000 \text{ mAh}
% get the first 4 elements of design that represent the power system
design = design(1:4);
% convert to a number code
str = sprintf('%d%d%d%d', design(1), design(2), design(3), design(4));
design_code = str2double(str);
switch design code
  % Test data from KDE Direct
  % Thr = [...] are KDE's Thrust measurements in Newtons
  % Amp = [...] are KDE's current measurements in Amps
  % Cases for motor 1:
  case 1312
     Thr = [2.75, 5.69, 9.90, 14.81, 19.81, 25.6, 33.73];
     Amp = [0.5, 1.2, 2.4, 4.2, 6.4, 9.4, 13.1];
  case 1322
     Thr = [3.43, 6.96, 11.96, 17.75, 23.73, 30.11, 38.44];
     Amp = [0.6, 1.6, 3.2, 5.6, 8.7, 12.8, 17.5];
  case 1212
     Thr = [4.02, 8.63, 14.42, 20.99, 28.54, 36.48, 45.70];
```

```
Amp = [0.6, 1.7, 3.7, 6.4, 10.0, 14.4, 19.2];
case 1222
  Thr = [4.81, 10.20, 16.97, 24.81, 32.56, 40.70, 49.43];
  Amp = [0.8, 2.3, 4.7, 8.5, 12.8, 18.1, 24.2];
case 1112
  Thr = [5.69, 11.38, 19.32, 26.67, 35.89, 44.42, 56.00];
  Amp = [0.8, 2.3, 5.2, 8.4, 13.6, 19.3, 26.8];
case 1313
  Thr = [4.81, 9.32, 16.28, 24.61, 33.15, 41.87, 53.25];
  Amp = [0.7, 1.9, 3.6, 6.8, 10.3, 14.8, 20.3];
case 1323
  Thr = [5.98, 11.57, 20.20, 28.34, 37.46, 46.68, 58.84];
  Amp = [0.8, 2.3, 5.2, 8.7, 13.9, 19.9, 27.0];
case 1213
  Thr = [6.86, 14.71, 23.54, 34.52, 45.31, 54.92, 63.37];
  Amp = [1.1, 2.9, 5.7, 10.1, 15.6, 22.4, 29.3];
case 1223
  Thr = [8.04, 17.16, 27.56, 38.64, 49.43, 59.43, 73.06];
  Amp = [1.3, 3.6, 7.5, 13.2, 19.5, 27.6, 35.8];
case 1314
  Thr = [7.45, 14.71, 25.11, 36.38, 45.40, 59.33, 74.04];
  Amp = [1.1, 2.6, 5.6, 9.6, 13.1, 20.8, 29.1];
case 1324
  Thr = [8.92, 17.55, 29.22, 41.48, 51.98, 64.23, 76.88];
  Amp = [1.3, 3.4, 7.6, 13.1, 19.8, 26.6, 40.6];
case 1214
  Thr = [10.40, 21.18, 33.73, 47.37, 59.43, 69.04, 80.22];
  Amp = [1.5, 4.0, 8.1, 14.5, 22.3, 32.9, 42.1];
case 1315
  Thr = [10.79, 19.61, 32.95, 45.31, 62.86, 78.85, 88.75];
  Amp = [1.5, 3.3, 6.9, 10.9, 19.4, 29.6, 40.1];
% Cases for motor 2:
case 2512
  Thr = [2.16, 4.22, 6.86, 10.20, 13.73, 17.65, 23.05];
  Amp = [0.6, 1.2, 2.1, 3.4, 5.1, 7.3, 9.9];
case 2522
  Thr = [2.55, 5.20, 8.43, 12.55, 16.87, 21.67, 28.24];
  Amp = [0.7, 1.5, 2.6, 4.4, 6.7, 9.7, 13.2];
case 2412
  Thr = [3.92, 7.45, 11.96, 17.36, 23.34, 30.50, 38.74];
  Amp = [0.9, 1.9, 3.6, 6.1, 9.5, 13.9, 18.2];
case 2422
  Thr = [4.61, 8.83, 14.42, 20.79, 27.46, 35.89, 45.90];
  Amp = [1.0, 2.2, 4.5, 7.9, 11.8, 16.8, 23.5];
```

```
case 2312
  Thr = [5.69, 10.30, 16.97, 25.01, 32.75, 41.78, 52.96];
  Amp = [1.2, 2.6, 5.2, 9.1, 13.4, 19.4, 25.9];
case 2322
  Thr = [6.77, 12.36, 20.20, 28.44, 37.36, 45.99, 57.47];
  Amp = [1.5, 3.3, 6.9, 11.4, 17.5, 24.7, 33.2];
case 2513
  Thr = [4.12, 7.26, 11.57, 16.48, 22.36, 30.11, 38.34];
  Amp = [0.9, 1.8, 3.1, 5.1, 7.9, 11.7, 15.5];
case 2523
  Thr = [4.61, 8.34, 13.73, 19.91, 26.97, 35.99, 46.09];
  Amp = [1.1, 2.1, 4.0, 6.5, 9.9, 14.7, 20.1];
case 2413
  Thr = [6.28, 11.87, 19.22, 28.24, 37.66, 47.37, 61.19];
  Amp = [1.2, 2.8, 5.6, 9.5, 14.2, 20.1, 28.3];
case 2423
  Thr = [7.55, 14.42, 22.65, 33.05, 43.15, 54.33, 70.51];
  Amp = [1.5, 3.5, 6.8, 11.8, 17.1, 24.2, 35.2];
case 2313
  Thr = [9.02, 16.77, 26.67, 39.32, 50.50, 64.63, 79.73];
  Amp = [1.8, 3.9, 7.7, 13.7, 19.7, 29.2, 38.8];
case 2323
  Thr = [10.89, 20.50, 32.17, 43.93, 56.68, 70.71, 85.71];
  Amp = [2.2, 5.4, 10.6, 17.0, 26.6, 39.0, 51.1];
case 2514
  Thr = [6.28, 10.49, 16.57, 23.54, 34.23, 43.44, 55.02];
  Amp = [1.2, 2.3, 4.3, 6.8, 11.2, 16.0, 21.4];
case 2524
  Thr = [7.06, 12.45, 19.91, 28.15, 40.99, 52.27, 65.41];
  Amp = [1.4, 2.9, 5.4, 8.6, 14.7, 21.7, 28.0];
case 2414
  Thr = [9.12, 17.36, 28.44, 40.01, 54.03, 67.47, 85.81];
  Amp = [1.6, 3.8, 7.6, 12.5, 19.4, 28.3, 39.2];
case 2424
  Thr = [10.89, 21.08, 33.54, 45.01, 60.80, 76.10, 96.50];
  Amp = [2.0, 5.0, 9.9, 15.1, 22.9, 36.2, 50.8];
case 2314
  Thr = [13.04, 25.11, 40.21, 53.45, 70.51, 89.34, 106.99];
  Amp = [2.3, 5.7, 11.3, 17.3, 27.0, 43.3, 57.1];
case 2324
  Thr = [15.69, 28.44, 43.54, 57.96, 74.53, 95.12, 113.86];
  Amp = [3.0, 7.1, 13.8, 21.5, 34.3, 50.0, 69.9];
```

case 2515

```
Thr = [8.43, 14.22, 22.06, 34.03, 45.21, 58.74, 74.53];
  Amp = [1.6, 3.0, 5.3, 9.5, 14.4, 20.6, 28.3];
case 2525
  Thr = [9.81, 17.06, 26.87, 41.78, 54.52, 71.10, 86.00];
  Amp = [1.8, 3.7, 6.9, 12.8, 18.9, 28.5, 36.6];
case 2415
  Thr = [12.75, 23.93, 37.27, 52.56, 71.29, 91.40, 106.89];
  Amp = [2.1, 5.1, 9.6, 16.0, 25.8, 40.2, 51.4];
case 2425
  Thr = [14.91, 27.36, 42.07, 58.94, 79.63, 100.03, 116.99];
  Amp = [2.6, 6.1, 11.4, 19.1, 33.9, 45.1, 59.1];
case 2315
  Thr = [17.95, 33.24, 49.92, 69.82, 90.61, 107.28, 126.31];
  Amp = [3.1, 6.9, 13.0, 22.2, 37.8, 52.7, 76.2];
% Cases for motor 3:
case 3512
  Thr = [2.45, 4.41, 6.96, 10.30, 14.02, 18.83, 23.73];
  Amp = [0.7, 1.3, 2.2, 3.6, 5.4, 8.0, 10.4];
case 3522
  Thr = [2.75, 5.49, 8.63, 12.75, 17.26, 22.85, 28.73];
  Amp = [0.7, 1.6, 2.8, 4.6, 6.9, 10.0, 13.7];
case 3412
  Thr = [4.12, 7.55, 12.26, 18.04, 23.83, 30.40, 39.23];
  Amp = [0.9, 2.0, 3.8, 6.5, 9.7, 13.9, 18.7];
case 3422
  Thr = [4.81, 9.12, 14.91, 21.57, 28.54, 36.09, 45.60];
  Amp = [1.1, 2.6, 4.9, 8.3, 12.6, 18.0, 23.8];
case 3613
  Thr = [2.26, 4.41, 7.06, 10.10, 13.83, 18.53, 23.83];
  Amp = [0.6, 1.3, 2.1, 3.3, 4.8, 7.1, 9.6];
case 3623
  Thr = [2.75, 5.39, 8.63, 12.36, 16.57, 22.26, 28.54];
  Amp = [0.8, 1.6, 2.7, 4.1, 6.1, 9.1, 12.3];
case 3513
  Thr = [4.41, 7.55, 11.87, 17.06, 22.65, 30.20, 39.13];
  Amp = [1.0, 1.9, 3.3, 5.5, 8.1, 12.0, 16.2];
case 3523
  Thr = [5.20, 8.92, 14.51, 20.69, 27.26, 36.19, 46.09];
  Amp = [1.2, 2.2, 4.3, 6.9, 10.4, 15.5, 20.6];
case 3413
  Thr = [6.67, 12.26, 20.10, 28.05, 37.85, 47.46, 61.49];
  Amp = [1.4, 3.0, 5.8, 9.4, 14.7, 20.3, 28.4];
case 3423
  Thr = [7.94, 15.00, 24.61, 34.13, 44.52, 54.72, 68.94];
```

```
Amp = [1.7, 3.9, 7.3, 12.5, 18.5, 25.8, 35.0];
case 3614
  Thr = [4.12, 6.67, 10.59, 15.69, 20.69, 26.87, 35.11];
  Amp = [1.0, 1.7, 2.9, 4.6, 6.8, 9.9, 13.4];
case 3624
  Thr = [4.71, 8.14, 12.85, 18.93, 25.01, 32.46, 41.68];
  Amp = [1.1, 2.0, 3.6, 5.6, 8.7, 13.0, 17.0];
case 3514
  Thr = [6.57, 11.18, 17.55, 24.91, 34.72, 43.93, 56.00];
  Amp = [1.3, 2.5, 4.5, 7.3, 11.6, 16.6, 22.2];
case 3524
  Thr = [8.14, 13.53, 20.89, 29.52, 40.89, 51.98, 65.41];
  Amp = [1.6, 3.1, 5.6, 9.4, 15.1, 21.8, 28.2];
case 3414
  Thr = [9.71, 18.14, 28.34, 40.80, 53.35, 67.47, 84.44];
  Amp = [1.8, 4.1, 7.9, 13.0, 20.1, 28.8, 37.9];
case 3424
  Thr = [11.57, 21.87, 34.23, 47.76, 62.37, 78.65, 97.58];
  Amp = [2.1, 5.3, 10.3, 16.0, 24.7, 38.2, 49.7];
case 3615
  Thr = [6.08, 9.51, 14.61, 21.28, 28.24, 36.87, 47.56];
  Amp = [1.3, 2.1, 3.7, 6.1, 9.1, 13.0, 17.4];
case 3625
  Thr = [6.67, 11.08, 17.06, 25.40, 34.42, 44.03, 55.70];
  Amp = [1.5, 2.6, 4.4, 7.6, 11.6, 16.6, 21.9];
case 3515
  Thr = [9.02, 15.20, 23.05, 34.91, 46.48, 59.13, 75.12];
  Amp = [1.7, 3.1, 5.6, 10.0, 15.1, 21.2, 28.7];
case 3525
  Thr = [10.30, 17.75, 27.85, 41.68, 54.82, 69.73, 86.30];
  Amp = [1.9, 3.9, 7.2, 13.0, 19.2, 27.8, 36.7];
case 3415
  Thr = [13.04, 24.91, 37.85, 53.74, 71.10, 90.91, 111.31];
  Amp = [2.3, 5.6, 10.0, 16.8, 26.0, 39.4, 51.3];
% Cases for motor 4:
case 4511
  Thr = [2.45, 5.20, 8.24, 11.96, 16.38, 21.48, 27.95];
  Amp = [1.1, 2.3, 4.1, 6.7, 10.3, 14.7, 20.3];
case 4521
  Thr = [3.33, 6.28, 10.0, 14.42, 19.71, 25.60, 33.05];
  Amp = [1.3, 2.8, 5.2, 8.4, 13.0, 19.1, 26.4];
case 4411
  Thr = [4.51, 8.43, 13.73, 20.01, 26.77, 35.30, 44.03];
  Amp = [1.6, 3.5, 6.9, 11.8, 18.2, 27.7, 36.4];
```

```
case 4421
     Thr = [5.59, 10.30, 16.48, 23.54, 30.99, 39.42, 49.43];
     Amp = [2.0, 4.5, 9.0, 15.0, 23.2, 33.7, 45.4];
  case 4612
     Thr = [3.33, 6.28, 10.20, 14.81, 20.10, 27.85, 35.50];
     Amp = [1.3, 2.6, 4.6, 7.2, 10.8, 17.1, 22.5];
  case 4622
     Thr = [4.22, 7.75, 12.26, 17.75, 23.93, 32.46, 41.19];
     Amp = [1.6, 3.1, 5.7, 9.3, 14.2, 21.6, 29.0];
  case 4512
     Thr = [5.88, 10.40, 16.67, 24.12, 33.24, 43.74, 55.60];
     Amp = [2.0, 3.9, 7.3, 12.0, 19.0, 28.3, 37.9];
  case 4522
     Thr = [7.06, 12.45, 20.01, 28.93, 39.03, 50.99, 63.74];
     Amp = [2.3, 4.8, 9.3, 15.8, 24.1, 35.3, 48.2];
  case 4412
     Thr = [8.92, 17.16, 26.87, 39.32, 49.92, 63.84, 81.10];
     Amp = [2.8, 6.5, 12.5, 21.9, 32.0, 48.2, 65.5];
  case 4613
     Thr = [6.57, 10.59, 16.97, 25.11, 34.42, 44.33, 57.27];
     Amp = [2.2, 3.8, 6.8, 11.5, 17.9, 25.5, 35.4];
  case 4623
     Thr = [7.94, 12.85, 20.10, 29.32, 40.21, 52.07, 65.80];
     Amp = [2.5, 4.7, 8.4, 13.9, 22.6, 33.0, 44.5];
  case 4513
     Thr = [9.81, 17.75, 27.07, 38.54, 54.03, 71.10, 85.71];
     Amp = [3.0, 6.1, 11.1, 18.2, 30.0, 45.1, 57.3];
  case 4523
     Thr = [11.18, 20.59, 31.58, 44.52, 62.57, 79.34, 96.40];
     Amp = [3.2, 7.2, 13.5, 22.5, 38.9, 52.9, 73.1];
  otherwise
     Thr = [];
     Amp = [];
end
% If we have data for the given design code:
if ~isempty(Thr)
  Thr = Thr';
  Amp = Amp';
  % A matrix for LS polynomial curve fit
  A = [ones(length(Thr),1), Thr, Thr.^2, Thr.^3];
  % solve for coefficients of polynomial using pseudo-inverse
  x = A \setminus Amp;
```

```
% using the polynomial curve fit, 'look up' the amps for the given thrust
  amps = x(1) + x(2)*thrust + x(3)*thrust^2 + x(4)*thrust^3;
else
  amps = -1;
end
end
get_best_of_generation.m:
function best_design = get_best_of_generation(generation)
[rows, \sim] = size(generation);
% vector to hold the fitnesses of each chromosome
fitnesses = zeros(rows, 1);
for i=1:rows
  % evaluate the fitness of each chromosome (design) and store it in our
  % vector
  fitnesses(i) = compute_fitness(generation(i,:));
end
% sort the fitnesses vector in descending order (greatest ---> smallest)
% and get the indexes
[~, index] = sort(fitnesses, 'descend');
% the best index is the first one since they're sorted in descending order
bestIndex = index(1);
best_design = generation(bestIndex,:);
end
pareto.m:
clc
clear
close all
all_designs = [];
f1 = [];
f2 = [];
count = 0;
% Look at all possible designs by brute-force
for i=1:4
  for j=1:6
     for k=1:2
```

```
for I=1:5
          for m=1:3
            for n=1:4
               % increment counter
               count = count + 1;
               % fill out the design
               design = [i, j, k, l, m, n];
               % check to see if design is feasible
               check = get amps(5, design);
               if check \sim = -1
                  % add design to our giant matrix
                  all designs = [all designs; design];
                  % add the fitness to our big fitness vector
                  f1 = [f1; 1/(compute fitness(design))];
                  f2 = [f2; compute fitness2(design)];
               end
             end
          end
       end
     end
  end
end
% compute the maximin values
maximin vals = zeros(length(f1), 1);
for i = 1:length(f1)
  mins = [];
  for j = 1:length(f1)
     if i \sim = i
       mins = [mins; min(f1(i)-f1(j), f2(i)-f2(j))];
     end
  end
  maximin_vals(i) = max(mins);
% make an array of just the pareto designs
pareto_designs = [];
for i = 1:length(maximin vals)
  if maximin vals(i) < 0
     pareto_designs = [pareto_designs; all_designs(i,:)];
  end
end
[rows, ~] = size(pareto_designs);
f1 pareto = zeros(rows, 1);
f2_pareto = zeros(rows, 1);
for i = 1:rows
```

```
f1 pareto(i,1) = 1/compute fitness(pareto designs(i,:));
  f2 pareto(i,1) = compute fitness2(pareto designs(i,:));
end
plot(f1, f2, 'r*')
xlabel('1 / Flight Time (1/hr)')
ylabel('Propeller Disc Area (m^2)')
hold on
plot(f1 pareto, f2 pareto, 'b-*')
% plot(f1 pareto, f2 pareto, 'b')
title('Objective Space and Pareto Front')
% select pareto design(3,:) as the 'best design'
pareto row = 3;
% do some fancy printing stuff
max flight time = compute fitness(pareto designs(1,:));
pareto3_flight_time = compute_fitness(pareto_designs(pareto_row,:));
diff ft = max flight time - pareto3 flight time;
percent ft = (diff ft/max flight time) * 100;
percent_ft_str = num2str(percent_ft);
pareto1 area = compute fitness2(pareto designs(1,:));
pareto3 area = compute fitness2(pareto designs(pareto row,:));
diff area = pareto1 area - pareto3 area;
percent area = (diff area/pareto1 area) * 100;
percent area str = num2str(percent area);
s1 = "Results in only a ";
s2 = "% decrease in flight time but yields a ";
s3 = "% decrease in propeller disc area";
s = strcat(s1, percent ft str, s2, percent area str, s3);
disp('Selecting pareto design: ')
disp(pareto designs(3,:))
disp(s)
disp(newline)
flight time = num2str(pareto3 flight time * 60);
s4 = "Total flight time: ";
s5 = " minutes";
s = strcat(s4, flight time, s5);
disp(s)
disp(newline)
area = num2str(pareto3 area);
s6 = "Total disc area: ";
s7 = "m^2";
s = strcat(s6, area, s7);
disp(s)
plot(f1 pareto(pareto row), f2 pareto(pareto row), 'bx', 'MarkerSize', 12, 'LineWidth', 2)
legend('all feasible designs', 'pareto designs', '"best" design')
```

```
point_crossover.m:
function children = point crossover(parents, p crossover)
[n parents, n genes] = size(parents);
% Pick a random value between 0 and 1
val = rand(1):
% Determine whether or not crossover takes place
if val <= p crossover
  % Perform blend crossover
else
  % No crossover occurs and the children are clones of the parents
  children = parents;
  return
end
% Initialize children to be clones of the parents
children = parents;
% Choose the crossover point
point cross = randi(n genes);
if point cross == n genes
  % No tail to swap so children = parents
  return
else
  % Chop off the tails of the parent chromosomes at the crossover point
  parent 1 tail = parents(1, point cross + 1:end);
  parent 2 tail = parents(2, point cross + 1:end);
  % Swap the tails and now we have two children chromosomes
  children(1,point cross + 1:end) = parent 2 tail;
  children(2,point cross + 1:end) = parent 1 tail;
end
end
roulette_selection.m:
function parents = roulette selection(generation, roulette exponent)
% Get the number of chromosomes (designs) in the generation
[gen_size, chromosome_size] = size(generation);
```

```
% Initialize a column vector to hold generation fitness data
fitnesses = zeros(gen size, 1);
% Initialize a column vector to hold the widths on the roulette wheel that
% each design occupies
widths = zeros(gen size, 1);
```

```
% Initialize matrix to hold parent chromosomes
parents = zeros(2, chromosome size);
% Get the fitness for each chromosome
for i = 1:gen size
  fitnesses(i) = compute fitness(generation(i,:));
% Normalize all of the widths to sum to 1
for i = 1:gen size
  widths(i) = fitnesses(i)^(roulette_exponent)/sum(fitnesses.^roulette_exponent);
end
% Here we make a sliding window defined by a left and right bound that
% represents the current segment or bin (whose width is widths(i)) of our
% roulette wheel. If the random value we picked earlier falls into the
% current segment, then we select the design corresponding to this segment
% to be a parent chromosome. We do this twice to get two parents.
for n=1:2
  % Pick a random value between 0 and 1
  val = rand(1);
  % Initilize the bounds
  left = 0;
  right = 0;
  for i=1:gen size
     % Define the left side of the current bin of width = widths(i)
     if i \sim = 1
       left = left + widths(i-1);
     end
     % Define the right side of the current bin of width = widths(i)
     right = right + widths(i);
     if left <= val && val <= right
       break
     end
  end
  % Store the chosen parent chromosomes
  parents(n,:) = generation(i,:);
end
% fitnesses
% widths
end
```

ME 575

Project 2: Genetic Algorithm Project Due: Tuesday April 10, 11:50 p.m.

Description

For this project, you are to implement a real-value based genetic algorithm, which you develop, on a problem of your choice, which you should also develop. Please note,

- You should choose a problem that has at least six variables, at least two of which must be discrete. More is better.
- The problem can be constrained or unconstrained. It does not have to be an engineering problem.
- The problem can have one objective or two objectives.
- You should implement a value based algorithm (see Chap. 6 of your notes). This means, among other things, that you will consider crossover, mutation, etc. for each variable.
- You should determine an appropriate set of parameters (generation size, crossover probability, etc.) as well as select a scheme for crossover, choosing parents, etc.
- The primary objective of this project is to gain experience with genetic algorithms. Genetic algorithms are quite robust and will often make progress even if not particularly well implemented. I would like to be impressed, however, that you have a *good* genetic algorithm. I will be concerned if anything about the algorithm seems extreme, e.g. a mutation rate of 90%, a crossover probability of 10% or a tournament size equal to half the population size. If, for some reason, your algorithm works better with a low crossover rate, then you should explore why. It may be that a different kind of crossover should be used.
- You can use any programming language you wish. MATLAB is preferred. Please use good programming practices.

Report

For the report, you should discuss the problem, your implementation of the genetic algorithm, the solution, and any experimenting you did to determine optimal parameters. You should impress me with a complete and concise report. The basic format should be Summary, Procedure, Results, Discussion of Results, Appendix. You will need a complete discussion of the model and of your algorithm, since you are developing both. The key elements (which should be discussed) of a genetic algorithm are design representation, fitness selection and pressure, inheritance and diversity. Graphs showing the progress of the algorithm from generation to generation should be included. Include a listing of your code in the Appendix. Turn in through Learning Suite as a pdf or doc file.

PowerPoint Slides

As part of your report, prepare a few (i.e. half a dozen) PowerPoint slides that discuss the problem, the model, the algorithm, the design variables, the objective, and the results. Compare the beginning and the final designs. Show the fitness as a function of generation. Be prepared to give a 5-10 minute presentation in class. Turn in through Learning Suite as a separate (PowerPoint) file.

The difficulty of the project will be considered when giving a grade. However, it is better to choose a project you can thoroughly explore rather than choose something so large and/or difficult that you don't complete the optimization. Sometimes you can define a simpler problem to start with and, once you have a working algorithm, make it more complex or explore variations of it.

You may work on projects in groups of up to three if you wish.

The biggest problem people have with the project is waiting to begin until it is too late. **Start now!** Remember that software projects always take longer than you think.

Late projects will be penalized 5% per day late.

Projects from a previous semester:

Disneyland ride scheduling

Touring baseball parks for the shortest route to watch a home game

Age of Empires optimization

Metallic glass matrix optimization

NBA team selection

Optimization of Provo's street re-pavement plan

Playing Ticket to Ride

NFL team optimization

Optimizing a traffic control system

Optimal path to cure a pandemic

Genetic algorithm-based protein structure prediction

UAV Camera position optimization

Optimal allocation of political campaign funds

Optimizing temple site and size selection

Optimization, Runes and League of Legends

Genetic algorithm design of a fireworks display

Building a fantasy basketball team