Classification of Hoops' Longwing Populations

Zane Billings

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Introduction

As part of the analysis of the Hoops' Longwing (*Heliconius hoopsus*) study data from my research project in Indonesia, one of the goals was to build a model to predict which subpopulation an individual butterfly is from.

Here, we will use the caret package in order to build a k-Nearest Neighbors (or kNN for short) model to predict where the butterflies are from.

Building the Model

First things first: let's load in the data and get the caret package loaded. Note that loading caret automatically loads some useful packages: notably, data.table, ggplot2, and dplyr.

Remember, we want to remove the first column of this particular csv file because it is not useful for us, and we also want to set the last column to be a **character** type vector, because we know it is not a true factor, but a string instead.

```
library(caret)
hoops <- read.csv("hoops_longwing_study.csv")
hoops <- hoops[ ,-1]
hoops$sample_id <- as.character(hoops$sample_id)</pre>
```

We might already have an idea of what the Hoops' longwing data looks like from our previous exploration, but let's look at the structure just to make sure everything has imported correctly.

```
str(hoops)
```

```
'data.frame':
                    100 obs. of 16 variables:
                        : num 28.2 12.2 12.8 16.2 31 ...
   $ wing length
##
   $ wing_width
                        : num 12.04 6.23 6.69 7.49 12.31 ...
##
   $ age
                              16 11 47 16 13 26 27 12 10 13 ...
                        : int
                              28 23 37 26 25 31 28 23 24 23 ...
   $ num_offspring
                        : int
##
   $ feeding_range
                        : num
                               3.95 3.62 20.23 2.32 3.79 ...
##
   $ color_peak
                        : num 402 393 393 400 390 ...
##
   $ num_mates
                        : int
                              11 3 2 5 12 3 3 2 9 4 ...
##
   $ avg_scale_size
                        : num 52 27.2 24.5 30.8 56.1 ...
                               6.08 2.44 2.68 3.72 6.39 3.69 3.42 2 5.27 3.37 ...
##
   $ antenna_length
                        : num
##
   $ num_spots
                              4 8 7 6 4 8 7 11 4 5 ...
                        : int
##
  $ population
                       : Factor w/ 3 levels "Kayoa", "Ternate", ...: 3 2 2 2 3 2 2 2 3 2 ...
  $ dispersal_distance: num 25.4 24.7 24.8 25.1 25.1 ...
   $ body length
                        : num 9.29 4.89 4.7 6.49 8.78 7.17 7.5 3.77 7.95 6.16 ...
  $ latitude
                        : num 0.716 0.818 0.818 0.818 0.716 ...
```

```
## $ longitude : num 127 127 127 127 ...
## $ sample_id : chr "Tid_001_EM" "Ter_002_EM" "Ter_003_ZB" "Ter_004_EM" ...
```

With the changes we've made, everything looks fine. Now we need to get our data ready for the model.

Basically, the way kNN works (I bet you have been eagerly waiting for me to actually explain this) is that we, the experimenters, choose a value, k, and a data point is assigned to a category by looking at the k number of neighboring points which have a Euclidean distance closest to it. (Remember the Euclidean distance is just the regular distance "as the crow flies" in real life, but it can be generalized to n-dimensions.)

So, we consider the set of k points with the lowest Euclidean distances to the point we want to assign to a category, and we ask all of those points "which category are you in", and we assign our new point to the plurality answer.

However, caret is so sleek and high-tech that it will even handle choosing the right value of k for us. All we have to do is specify some parameters.

Now, let's make some changes to the dataset that will help us during the modeling process.

So, we only want numeric data, and we'll exclude the latitude and longitude, because we don't want to use the geographic location where the butterfly was collected as our only way to predict what population the butterfly is from.

Then, we'll normalize the data, which can help to improve kNN accuracy (see Lantz, Machine Learning With R). Let's look at a summary of our data.

```
hoops_mod <- subset(hoops, select = -c(latitude, longitude, sample_id))
summary(hoops_mod)</pre>
```

```
##
     wing length
                       wing_width
                                                       num_offspring
                                             age
##
    Min.
            :10.85
                             : 4.380
                                                       Min.
                                                               :18.00
                     Min.
                                       Min.
                                               : 7.0
##
    1st Qu.:14.25
                     1st Qu.: 6.915
                                       1st Qu.:13.0
                                                       1st Qu.:24.00
                     Median: 7.900
                                       Median:16.5
                                                       Median :27.00
##
    Median :16.21
                                                               :27.31
##
    Mean
            :19.83
                     Mean
                             : 8.692
                                       Mean
                                               :20.8
                                                       Mean
##
    3rd Qu.:25.96
                     3rd Qu.:10.430
                                       3rd Qu.:26.0
                                                        3rd Qu.:30.00
##
    Max.
            :36.65
                             :14.710
                                       Max.
                                               :52.0
                                                       Max.
                                                               :37.00
                     Max.
                        color_peak
##
    feeding_range
                                          num_mates
                                                         avg_scale_size
##
    Min.
           : 0.610
                              :369.1
                      Min.
                                       Min.
                                               : 1.00
                                                         Min.
                                                                :22.12
##
    1st Qu.: 2.638
                      1st Qu.:383.8
                                       1st Qu.: 3.00
                                                         1st Qu.:27.81
##
    Median : 3.380
                      Median :391.5
                                       Median: 4.00
                                                         Median :30.82
##
    Mean
           : 5.102
                              :391.4
                                       Mean
                                               : 5.95
                                                                :37.66
                      Mean
                                                         Mean
                                       3rd Qu.: 9.00
##
    3rd Qu.: 4.518
                      3rd Qu.:398.9
                                                         3rd Qu.:47.71
##
    Max.
            :30.310
                              :411.3
                                       Max.
                                               :16.00
                                                         Max.
                                                                :75.03
                      Max.
##
    antenna_length
                       num_spots
                                        population dispersal_distance
##
    Min.
            :2.000
                     Min.
                             : 3.00
                                      Kayoa :11
                                                    Min.
                                                            :22.58
##
    1st Qu.:3.188
                     1st Qu.: 4.00
                                      Ternate:57
                                                     1st Qu.:23.99
    Median :3.700
                                      Tidore:32
##
                     Median: 6.00
                                                    Median :24.70
##
            :4.286
                             : 5.71
                                                            :24.62
    Mean
                     Mean
                                                    Mean
##
    3rd Qu.:5.670
                     3rd Qu.: 7.00
                                                    3rd Qu.:25.18
##
    Max.
            :7.140
                     Max.
                             :11.00
                                                    Max.
                                                            :26.48
##
     body_length
##
    Min.
            : 2.750
##
    1st Qu.: 4.995
##
    Median : 6.430
##
    Mean
            : 6.764
##
    3rd Qu.: 8.330
    Max.
            :11.520
```

We can see that all of our numeric variables are measured on different scales, which can lead to weird notions of distance between points. So, we'll set all of our data to a common scale of measure (this is call normalization). There are two major normalization methods to think about.

We could use min-max normalization:

$$X* = \frac{X - \min(X)}{\max(X) - \min(X)},$$

or we could use Z-score normalization:

$$X* = \frac{X - \bar{X}}{s_X}.$$

Min-max is more traditional for kNN, and works well if we are not concerned about cpredicting values outside the range of the values we currently have. On the other hand, z-score normalization works well if we think our sample is representative of the population. For now, we'll go with the min-max method, but feel free to see if using the z-score method gives you a different model.

```
normalize <- function(x) {
    xstar <- (x - min(x)) / (max(x) - min(x))
    return(xstar)
}
normalize_df <- function(cols) {
    nlist <- lapply(cols, normalize)
    return(as.data.frame(nlist))
}</pre>
```

We'll use these functions to normalize the data. However, note that we do NOT want to normalize our categorical response variable, population. So, this will require a little bit of finagling, but it isn't too bad.

```
##
      population wing_length
                                      wing_width
                                                            age
    Kayoa :11
                          :0.0000
                                            :0.0000
                                                              :0.0000
##
                  Min.
                                    Min.
                                                       Min.
    Ternate:57
                                    1st Qu.:0.2454
##
                  1st Qu.:0.1318
                                                       1st Qu.:0.1333
##
    Tidore:32
                  Median :0.2079
                                    Median :0.3408
                                                       Median :0.2111
##
                          :0.3479
                                            :0.4174
                                                               :0.3067
                  Mean
                                    Mean
                                                       Mean
##
                  3rd Qu.:0.5858
                                    3rd Qu.:0.5857
                                                       3rd Qu.:0.4222
                          :1.0000
                                                              :1.0000
##
                  Max.
                                    Max.
                                            :1.0000
                                                       Max.
##
    num_offspring
                      feeding_range
                                            color_peak
                                                              num_mates
##
    Min.
           :0.0000
                      Min.
                              :0.00000
                                          Min.
                                                 :0.0000
                                                            Min.
                                                                    :0.0000
##
    1st Qu.:0.3158
                      1st Qu.:0.06827
                                          1st Qu.:0.3475
                                                            1st Qu.:0.1333
##
    Median : 0.4737
                      Median: 0.09327
                                          Median :0.5308
                                                            Median :0.2000
            :0.4900
                                                 :0.5280
                                                                    :0.3300
##
    Mean
                      Mean
                              :0.15124
                                          Mean
                                                            Mean
##
    3rd Qu.:0.6316
                      3rd Qu.:0.13157
                                          3rd Qu.:0.7058
                                                            3rd Qu.:0.5333
##
    Max.
            :1.0000
                      Max.
                              :1.00000
                                          Max.
                                                 :1.0000
                                                            Max.
                                                                    :1.0000
##
    avg scale size
                      antenna length
                                          num spots
                                                           dispersal distance
            :0.0000
                              :0.0000
                                                                   :0.0000
##
    Min.
                      Min.
                                         Min.
                                                :0.0000
                                                           Min.
##
    1st Qu.:0.1075
                      1st Qu.:0.2310
                                         1st Qu.:0.1250
                                                           1st Qu.:0.3615
##
   Median :0.1645
                      Median :0.3307
                                         Median :0.3750
                                                           Median : 0.5423
    Mean
            :0.2938
                      Mean
                              :0.4447
                                         Mean
                                                :0.3387
                                                           Mean
                                                                   :0.5242
##
    3rd Qu.:0.4836
                      3rd Qu.:0.7140
                                         3rd Qu.:0.5000
                                                           3rd Qu.:0.6660
                              :1.0000
                                                :1.0000
    Max.
           :1.0000
                      Max.
                                         Max.
                                                           Max.
                                                                   :1.0000
```

```
## body_length
## Min. :0.0000
## 1st Qu.:0.2560
## Median :0.4196
## Mean :0.4577
## 3rd Qu.:0.6363
## Max. :1.0000
```

Now, we'll split our data into training and testing datasets. We'll also set a random seed to make our experiment reproducible. The function caret::createDataPartition() is an easy way to split up the data by random sampling.

The interested reader will note that if we examine table(hoops\$population), we have a class imbalance issue. Good job on spotting that! But I am going to ignore it for now. Something to think about in your spare time would be ways to remedy this issue.

Now we'll train the kNN model. There are some specifics for caret here that you can read about if you'd like, but basically you just need to know that trainControl() provides some important parameters for how the modeling process works in caret, and the function train(method = "knn") is what's actually fitting the model for us.

```
## k-Nearest Neighbors
##
## 71 samples
## 12 predictors
##
  3 classes: 'Kayoa', 'Ternate', 'Tidore'
##
## Pre-processing: centered (12), scaled (12)
## Resampling: Cross-Validated (10 fold, repeated 3 times)
## Summary of sample sizes: 64, 64, 63, 64, 64, 64, ...
## Resampling results across tuning parameters:
##
##
    k
        Accuracy
                    Kappa
##
     5 0.8577381 0.7370761
     7 0.8994048 0.8129549
##
     9 0.8625000 0.7460353
##
```

```
##
        0.8625000 0.7453439
        0.8535714 0.7271456
##
     13
##
     15
        0.8630952 0.7420610
##
     17
        0.8714286
                   0.7551841
##
     19
        0.8563492
                   0.7199171
     21
        0.8561508 0.7187819
##
        0.8561508 0.7189022
##
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was k = 7.
```

Well, we see that our optimal kNN model is k = 7 which gives us an accuray of about 90%. That isn't terrible, but it could probably be better if we messed around a little more. Now let's look at our predictions with the testing data.

```
test <- predict(knn_fit, newdata = hoops_test)
confusionMatrix(test, hoops_test$population)</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
##
  Prediction Kayoa Ternate Tidore
      Kayoa
##
      Ternate
                  1
                          17
                                   1
##
##
      Tidore
                  2
                           0
                                   8
##
## Overall Statistics
##
##
                  Accuracy : 0.8621
##
                     95% CI: (0.6834, 0.9611)
       No Information Rate: 0.5862
##
##
       P-Value [Acc > NIR] : 0.00139
##
                      Kappa: 0.729
##
##
    Mcnemar's Test P-Value: 0.26146
##
##
## Statistics by Class:
##
##
                         Class: Kayoa Class: Ternate Class: Tidore
                               0.0000
                                               1.0000
## Sensitivity
                                                              0.8889
## Specificity
                               1.0000
                                               0.8333
                                                              0.9000
## Pos Pred Value
                                  NaN
                                               0.8947
                                                              0.8000
## Neg Pred Value
                               0.8966
                                               1.0000
                                                              0.9474
## Prevalence
                               0.1034
                                               0.5862
                                                              0.3103
## Detection Rate
                               0.0000
                                                              0.2759
                                               0.5862
## Detection Prevalence
                               0.0000
                                               0.6552
                                                              0.3448
## Balanced Accuracy
                               0.5000
                                               0.9167
                                                              0.8944
```

Looking at this data, we can see wthat we are misclassifying almost all of the Kayoa butterflies. This is likely due to the issue with class imbalance where the number of Kayoa butterflies in the testing data is much lower than the number of Tidore and Ternate butterflies.

Conclusions

My guess is that we either need to deal with the class imbalance problem. Maybe z-score normalization would change the results also, but I am skeptical about that. Perhaps another algorithm would be a better classifier as well.

References

- $Machine\ Learning\ with\ R$, 2nd edition, by Brett Lantz. (This book describes how to implement kNN with the class package.)
- This website.