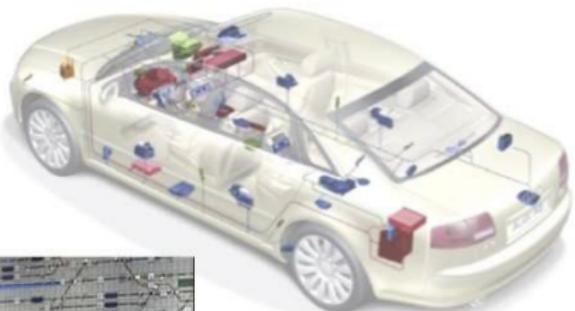


# Model Checking and Systems Verification (MCSV)

Instructor; M.K. Srivas  
TA: Zubin Duggal

August 11, 2020

# Embedded Systems



- ▶ Embedded (HW+SW+FW) systems are a complex parts of real life machines

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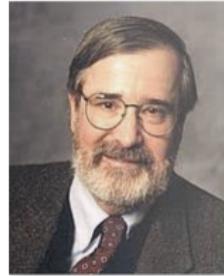
- ▶ Traditional methods: Simulation and testing
  - ▶ Do not guarantee 100% coverage
  - ▶ Expensive; Labour intensive and time consuming
- ▶ Can we have methods that guarantee 100% coverage
  - ▶ Formal Verification: Methods based on Logic and Automata theory
  - ▶ Model Checking is one such popular technique

# Model Checking: Cited for Turing Award in 2007 (Invented: 1986)



ACM Turing Award Hon...  
[cs.utexas.edu](http://cs.utexas.edu)

E. Allen Emerson



Introduction to Model C...  
[moves.rwth-aachen.de](http://moves.rwth-aachen.de)

Edmund Clarke



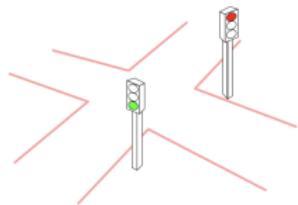
[Joseph Sifakis | French com...](#)  
[britannica.com](http://britannica.com)

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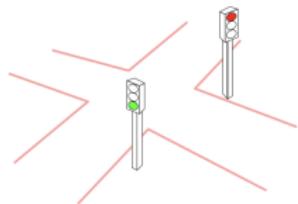
## CITATION

Together with E. Allen Emerson and Joseph Sifakis, for their role in developing Model-Checking into a highly effective verification technology that is widely adopted in the hardware and software industries.

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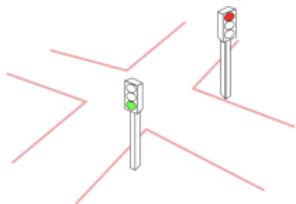


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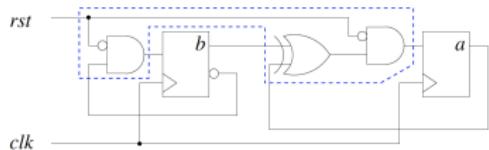


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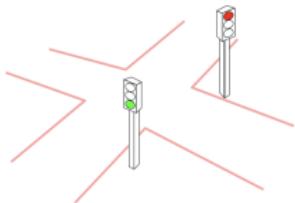
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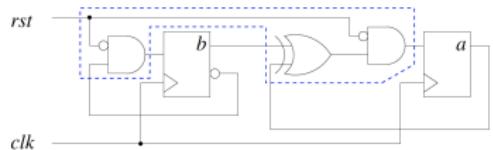
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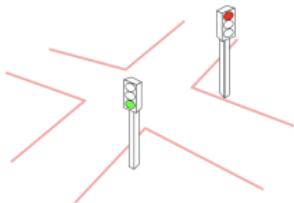


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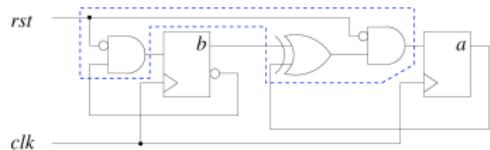


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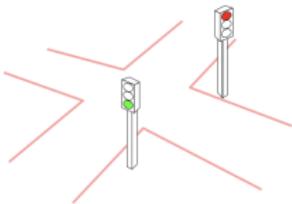
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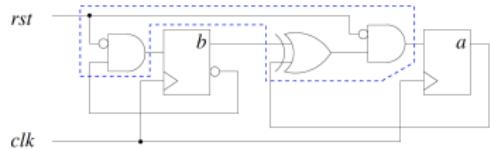
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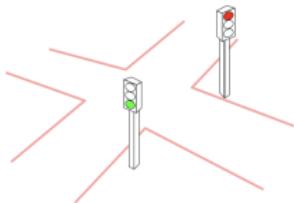


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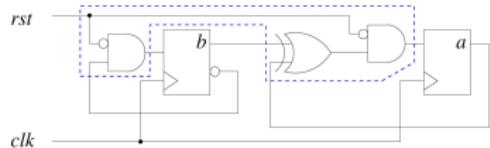
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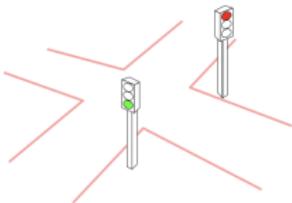
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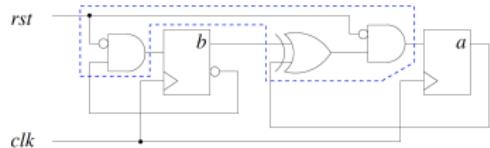
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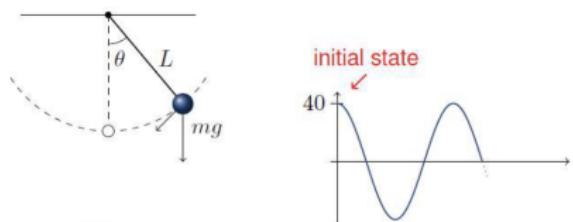
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"the program has no data races"

# What Kind of Systems Not

## An Example



Our model:

$$\frac{\delta^2 \theta}{\delta t^2} = -\frac{g}{L} \sin \theta$$

Plot of  $\theta$  over time

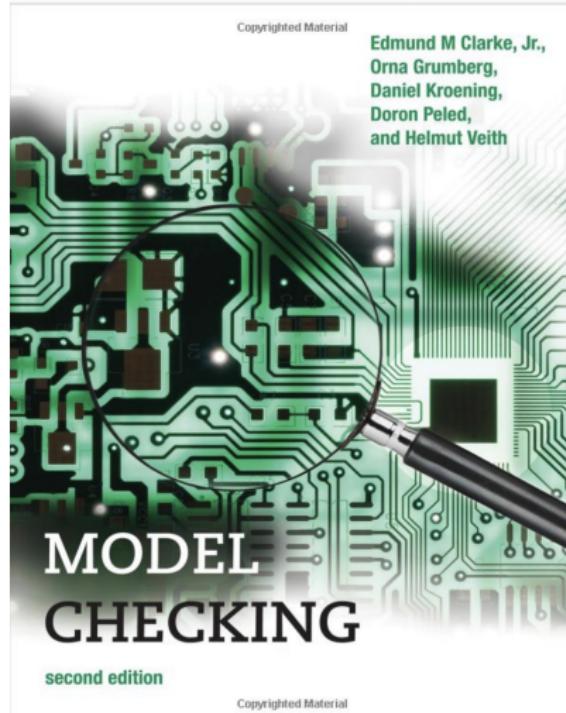
# Brief Course Outline

1. Modeling Systems (Kripke Structures)
2. Specifying Properties (Temporal logics: CTL, LTL, CTL\*)
3. Verifying Properties (Model Checking for Temporal logics)
4. Abstraction Techniques
5. Automata-Based Model Checking

## Course Work and Grade Distribution

1. Written Assignments: 30%
2. Tool Exercises: 30%
3. 2 Quizzes: 40%
  - ▶ One can be a small programming project

# Reference Text Book



eTextBook will be made available for class  
usage on shared (sign-up sheet) basis  
Access details will be shared on Moodle









## Some Definitions

- ▶ Bounded Satisfaction of a path:  $\pi \models_k \phi$ 
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  - ▶  $M \models_K \phi \implies M \models \phi$
  - ▶ why should such a  $K$  exist at all?