

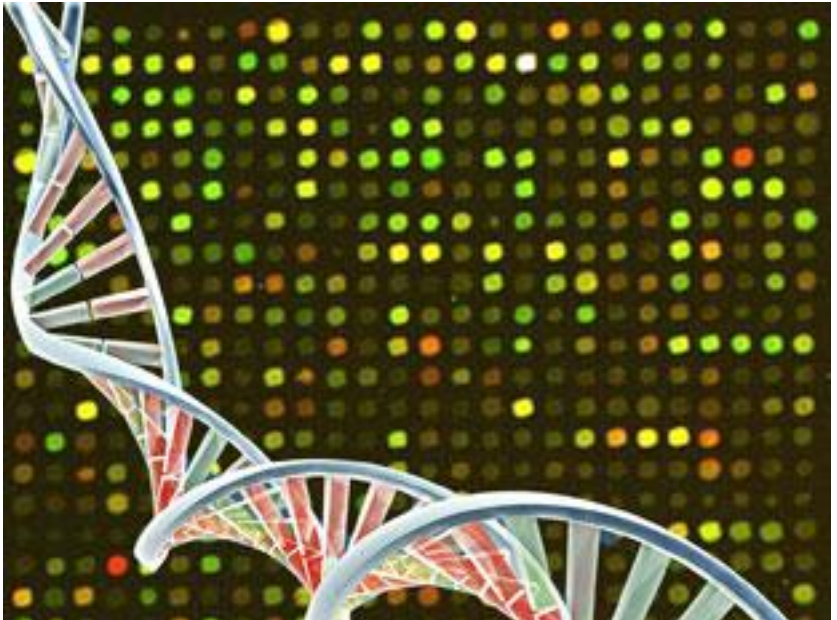
Gene Expression Analysis

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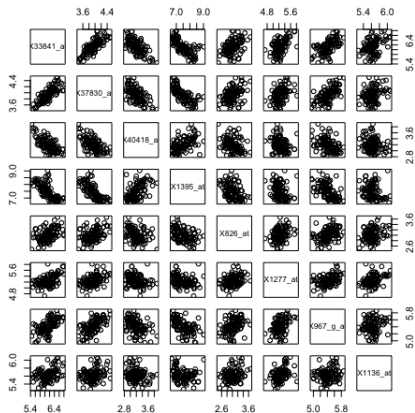
Brigham Young University

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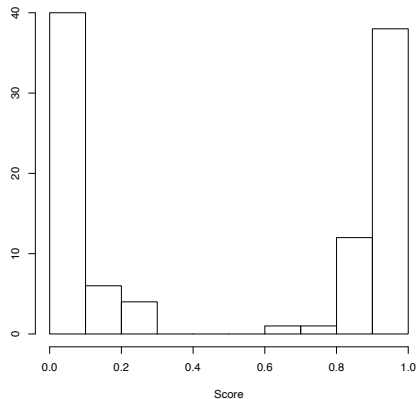
Problem Introduction



Cancer Patient Data



Histogram of Malignancy



Goals of the Analysis:

- Use the cancer patient data to determine which genes are associated with highly malignant tumors

Foreseeable Problems:

- We have more variables than observations, which may cause problems with common statistical methods used to approach this kind of problem.

LASSO Regression

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$$

\mathbf{y} = response vector ($n \times 1$)

\mathbf{X} = model matrix ($n \times p$)

$\boldsymbol{\beta}$ = model coefficients ($p \times 1$)

$\boldsymbol{\epsilon}$ = errors ($n \times 1$)

Estimated $\hat{\boldsymbol{\beta}}$ minimizes:

$$\min_{\boldsymbol{\beta}} \sum_{i=1}^n (\mathbf{y} - \mathbf{x}_i' \boldsymbol{\beta})^2 + \lambda \sum_{j=1}^p |\beta_j|$$

where λ is a penalty parameter.

Model Bootstrap

- Use bootstrap to obtain confidence intervals
- Keep same λ over each iteration

Centered 95% Confidence Interval Formula:

$$(2\hat{\beta} - \hat{\beta}_{\text{boot}}^{0.975}, 2\hat{\beta} - \hat{\beta}_{\text{boot}}^{0.025})$$

where $\hat{\beta}$ is the estimated coefficient and $\hat{\beta}_{\text{boot}}^t$ is the t percentile of the bootstrap estimates.

Advantages of Regression

- Estimated coefficients show the effect on tumor malignancy
- Confidence intervals show significance

Why choose LASSO?

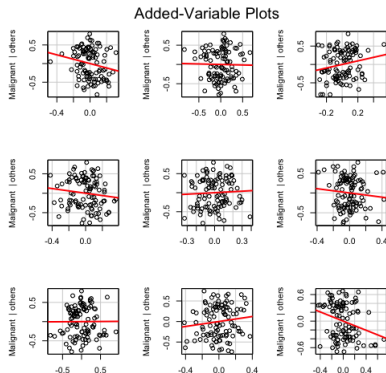
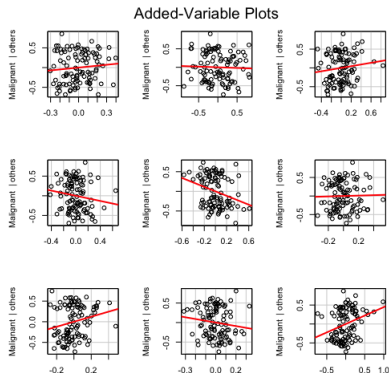
- Too many variables
- Implicit variable selection

Model Assumptions

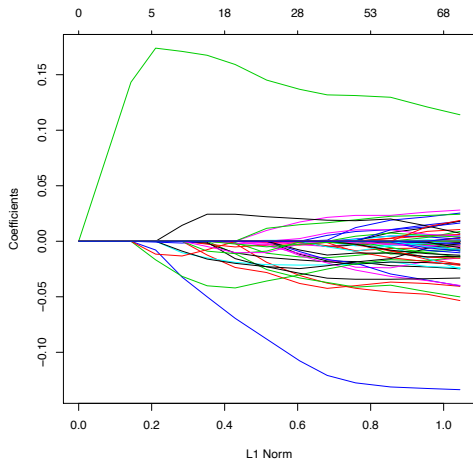
Linearity is the only assumption.

Hard to assess due to excess of covariates.

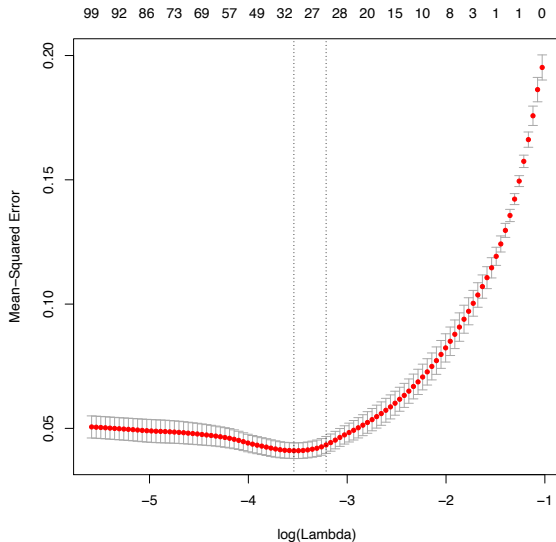
Random sample will suffice.



LASSO Model



Shrinkage Parameter



Model Performance

- Shrinkage Parameters:

Lambda Values	
	Result
Minimum	0.03
1 Std. Error	0.04

- How well did the model do?

Performance Assessment

	Result
MSE	0.04
R-squared	0.89

Results

- Reduced down to 29 genes
- 3 genes were significant
- Variables were standardized

Table of Significant Genes

	CI Lower	Estimate	CI Upper
(Intercept)	0.474	0.511	0.543
X33921_at	-0.063	-0.031	-0.005
X37639_at	0.085	0.139	0.206
X38087_s_at	-0.180	-0.101	-0.065

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RESULT: Activating and inhibiting these genes in the right way can significantly influence tumor malignancy

Conclusions

- We found 3 genes that significantly affected malignancy levels
- Shortcomings:
 - Handling collinear variables
- Next steps:
 - Exploring interactions between different genes