

1 **Optimization of heterogeneous continuous flow**
2 **hydrogenation using FTIR inline analysis: a comparative**
3 **study of multi-objective Bayesian optimization and kinetic**
4 **modeling**

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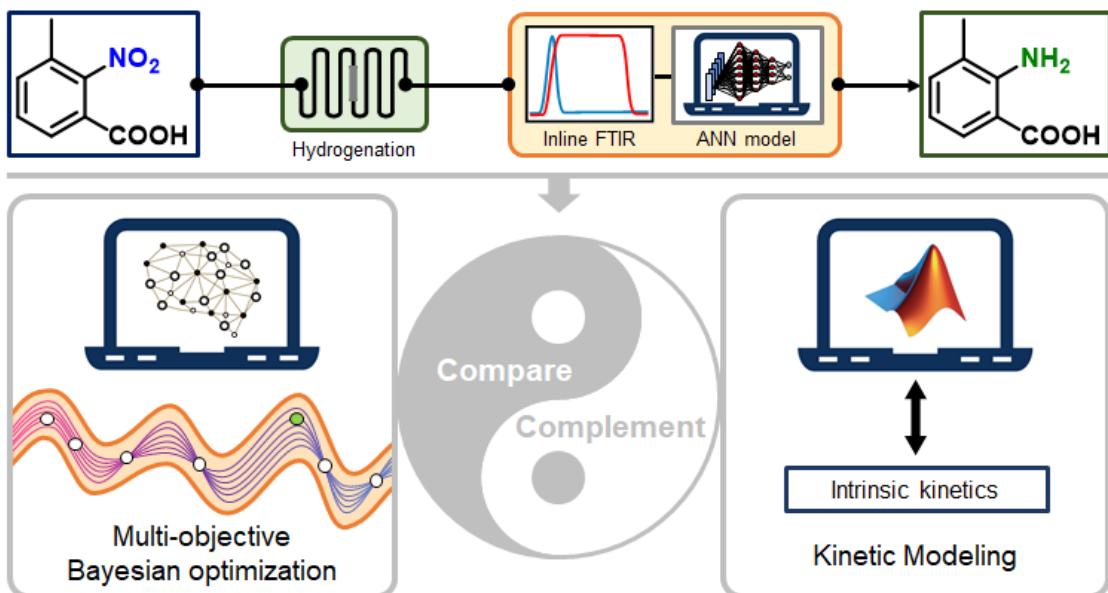
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27

Graphical Abstract



28

29 **Abstract**

30 The heterogeneous continuous flow hydrogenation is pivotal in chemical research and
31 production, yet its reaction optimization has historically been intricate and labor-
32 intensive. This study introduces a heterogeneous continuous flow hydrogenation
33 system specifically designed for the preparation of 2-amino-3-methylbenzoic acid
34 (AMA), employing FTIR inline analysis coupled with an artificial neural network
35 model for monitoring. We explored two distinct reaction optimization strategies: multi-
36 objective Bayesian optimization (MOBO) and intrinsic kinetic modeling, executed in
37 parallel to optimize the reaction conditions. Remarkably, the MOBO approach achieved
38 an optimal AMA yield of 99% and a productivity of 0.64 g/hour within a limited
39 number of iterations. Conversely, despite requiring extensive experimental data
40 collection and equation fitting, the intrinsic kinetic modeling approach yielded a similar
41 optimal AMA yield but a higher productivity of 1.13 g/hour, attributed to increased
42 catalyst usage. Our findings indicate that while MOBO offers a more efficient route
43 with fewer required experiments, kinetic modeling provides deeper insights into the
44 reaction optimization landscape but is limited by its assumptions.

45

46 **Keywords**

47 Multi-objective Bayesian optimization; Kinetic modeling; continuous flow;
48 heterogeneous hydrogenation; Reaction optimization; Inline analysis

49 **Introduction**

50 Heterogeneous catalytic hydrogenation is pivotal in organic synthetic chemistry, with
51 broad applications across the dye, pharmaceutical, and fine chemical industries.[1-3]
52 Traditional intermittent hydrogenation processes, however, are constrained by critical
53 safety concerns associated with reaction temperature and pressure, prompting a shift
54 towards continuous flow hydrogenation as a safer and more efficient alternative.[4, 5]
55 The reaction optimization within these continuous flow systems has emerged as a
56 research focus.[6, 7] Historically, the reaction optimization process predominantly
57 employed the one factor at a time (OFAT) method [8], which relies on a sequential,
58 factor-based optimization guided by chemical intuition[9-12]. Despite its widespread
59 use, the OFAT approach is often criticized for its inefficiency and inaccuracy, primarily
60 due to its inability to account for potential synergistic effects among various factors,
61 potentially leading to misinterpretation of the chemical processes.[13] Consequently,
62 there is a pressing need for developing systematic approaches to reaction optimization.

63

64 Kinetic modeling, grounded in a comprehensive understanding of chemical processes,
65 represents a classical and crucial strategy for reaction optimization, especially for
66 heterogeneous hydrogenation reactions.[14-17] For instance, Su et al. demonstrated the
67 application of kinetic modeling in the heterogeneous flow hydrogenation of
68 hexafluoroacetone trihydrate, revealing an adsorption-desorption mechanism with
69 competitive adsorption of H₂ dissociation.[18] Similarly, Yu et al. conducted a
70 continuous hydrogenation study of 2-(4-nitrophenyl) butanoic acid and kinetics study
71 in a micropacked-bed reactor, employing kinetic analysis to elucidate the impacts of
72 internal and external diffusion, as well as salt formation.[19] Despite these advances,
73 the application of kinetic modeling in heterogeneous catalysis is often hampered by the
74 complexities associated with non-chemical kinetics phenomena.[20-24]

75

76 Multi-objective Bayesian Optimization (MOBO) has revolutionized the optimization
77 of continuous-flow reactions by adeptly handling competing objectives.[25-28] It

78 leverages the surrogate model and acquisition function to systematically explore the
79 Pareto Front, aiming to strike an optimal balance among objectives. Using probabilistic
80 models, MOBO predicts outcomes for specific reaction conditions, guiding the
81 optimization process toward superior performance metrics. Recent significant
82 implementations of MOBO include Jensen et al.'s optimization of multistep synthetic
83 routes on an automated platform [25], Bourne et al.'s achievement of an 81% yield
84 through the simultaneous optimization of telescoped reactions [29], and Lapkin et al.'s
85 application of MOBO in medicinal chemistry for yield optimization [30]. Despite its
86 advancements, MOBO's comparison with traditional optimization methods is less
87 studied.

88

89 Inline analytical techniques, including inline FTIR, NMR, and UV/vis spectroscopy,
90 are becoming integral to reaction optimization due to their ability to provide real-time
91 data, which facilitates the creation of self-optimizing systems when combined with
92 Bayesian optimization.[29, 31, 32] Kappe et al. have notably advanced this field by
93 integrating four complementary inline analysis instruments and developing advanced
94 data analysis models, which quantify desired products, intermediates, and impurities
95 inline across various stages of a multi-step synthetic pathway.[33] Furthermore, they
96 have successfully applied artificial neural networks (ANN) for processing NMR and
97 UV/vis spectra of multiple components.[34] Besides enhancing Bayesian optimization,
98 inline analysis is also anticipated to improve the efficiency of traditional optimization
99 techniques, such as kinetic modeling.

100

101 In this study, we focused on the synthesis of 2-amino-3-methylbenzoic acid, a key
102 intermediate for the pesticide chlorantraniliprole, to serve a case study for optimizing
103 heterogeneous continuous flow hydrogenation. We designed a continuous flow
104 hydrogenation system equipped with an FTIR for inline monitoring and analysis of
105 reaction data. Multi-objective Bayesian optimization and kinetic modeling were
106 conducted in parallel to optimize the reaction process, allowing us to compare the
107 advantages and limitations of these two approaches directly.

108

109 **Materials and Methods**

110 **Materials.** 3-Methyl-2-nitrobenzoic acid (98%, MNA), 2-amino-3-methylbenzoic acid
111 (98%, AMA), methanol (MeOH, analytical grade), and silica (100-200 mesh) were
112 purchased from Sinopharm Chemical Reagent Co., Ltd. (SCRC) without further
113 purification. Hydrogen (H₂, 99.999%) and nitrogen (N₂, 99.999%) were purchased from
114 Hangzhou Jingong Special Gas Co., Ltd. The catalyst Pd@SBA-15 was synthesized
115 following the method reported in our previous work.[35]

116

117 **Experimental setup.** Metering pump (JJRZ-10004F) was purchased from Hangzhou
118 Jingjin Technology Co., Ltd. High performance liquid chromatography (HPLC)
119 column (5 mm in diameter and 50 mm long) was purchased from Dalian Baijia Lida
120 Technology Co., Ltd. Check valve, T-joint mixer, temperature sensor, pressure gauge,
121 back pressure regulator, and stainless steel tube (1/8" and 1/16" outside diameter) were
122 purchased from Beijing Xiongchuan Technology Co., Ltd. Polytetrafluoroethylene
123 (PTFE) tube (1/8" and 1/16" outside diameter) was purchased from Nanjing Runze
124 Fluid Control Equipment Co., Ltd. Inline FTIR (ReactIR 702L) was purchased from
125 Mettler Toledo Technology Co., Ltd. Mass flow controller (D07) was purchased from
126 Beijing Sevenstar Flow Co., Ltd. Water bath was purchased from Heidolph Instruments
127 Co., Ltd. Experimental setup was shown in Figure S1a.

128

129 **Heterogeneous continuous flow hydrogenation system.** MNA was dissolved in
130 MeOH and pumped into the continuous flow system through a metering pump. The
131 flow rate and pressure of H₂ involved in the hydrogenation were controlled by adjusting
132 the mass flow controller and the pressure gauge, respectively. The gas and liquid flow
133 tubes were fitted with check valves to avoid backflow. The hydrogen and MNA solution
134 were mixed in a T-joint mixer and then flowed into a 1.0-meter pretreatment tube to
135 reach hydrogenation temperature. The synthesized catalyst Pd@SBA-15 was pre-
136 loaded in an HPLC column and the remaining space was filled with silica. Then, sieve

137 plates were installed at the ends of the HPLC column as a micro pack-bed reactor
138 (MPBR). The MPBR was placed vertically in a hot water bath, which facilitates full
139 contact between the gas-liquid mixture and the catalyst. The gas-liquid mixture
140 undergoes hydrogenation in the MPBR. The pressure of the entire system was
141 controlled by a manual back pressure regulator. The water bath and temperature sensor
142 accurately control the hydrogenation temperature together. The check valve and back
143 pressure regulator ensured that the continuous flow system was isolated from air. Then,
144 the gas-liquid mixture flowed into a 1.0-meter pretreatment tube in a cold water bath to
145 reach 20 °C. Inline FTIR monitored the concentrations of MNA and AMA after the
146 hydrogenation in real-time. The tubes for solution flow through the inline FTIR were
147 PTFE tubes and all other tubes were stainless steel tubes. The entire heterogeneous
148 continuous flow hydrogenation system was controlled by adjusting the reaction
149 parameters, such as temperature, flow rate, and hydrogen pressure.

150

151 **Concentration determination.** Concentrations of MNA and AMA in the reaction
152 solution were monitored in real-time by inline FTIR. ANN modeling was performed as
153 a processing approach for inline FTIR spectra data according to the reported literature
154 (Figure S2a).[34] Several groups of MNA and AMA in methanol solution with different
155 concentrations were prepared and their inline FTIR spectra data were collected as
156 training set and validation set. Here the verification set is equivalent to the test set
157 (Table S1). Next, 5000 analog spectra are generated from a linear combination of two
158 pure components, and Gaussian noise is added to augment the training set. Some of the
159 data simulating the experimental process were also added to the training set and
160 validation set. To improve the stability and performance of the ANN training phase, all
161 spectra data were normalized. Next, during the training process, an architecture of one
162 convolutional layer followed by dense layers was investigated. The spectra data was
163 processed at the Conv1D convolutional layer for characteristic extraction to screen the
164 weights of the data. Then, data dimension reduction was performed through different
165 functions in the dense layers. Finally, the output layer outputs the predicted
166 concentrations of MNA and AMA. Compared with the known concentration in the test

167 set, the predicted results of the model are basically consistent, indicating that the ANN
168 model framework developed for this purpose is suitable (Figure S2b). The inline FTIR
169 spectra data monitored during the experiment were used to quickly predict the
170 concentrations of MNA and AMA through the ANN model. The conversion of the
171 MNA ($\text{Conversion}_{\text{MNA}}$), the yield of the AMA ($\text{Yield}_{\text{AMA}}$), and the productivity of the
172 AMA ($\text{Productivity}_{\text{MNA}}$) in the continuous flow hydrogenation system were calculated
173 through Equation 1, Equation 2, and Equation 3, respectively:

174
$$\text{Conversion}_{\text{MNA}} = 1 - \frac{C_{\text{MNA}}}{C_{\text{MNA}}^0} \quad (1)$$

175
$$\text{Yield}_{\text{AMA}} = \frac{C_{\text{AMA}}}{C_{\text{MNA}}^0} \quad (2)$$

176
$$\text{Productivity}_{\text{MNA}} = C_{\text{AMA}} F_{\text{MNA}} M_{\text{AMA}} \quad (3)$$

177 where C_{MNA}^0 was the initial concentration of the MNA in the solution; C_{MNA} and
178 C_{AMA} were the concentration of the MNA and the AMA in the collected solution,
179 respectively; F_{MNA} was the flow rate of the MNA solution; M_{AMA} was the molar mass
180 of the AMA.

181
182 **Multi-objective Bayesian Optimization.** MOBO was performed according to the
183 following process in general.[36, 37] The Bayesian optimizer was initialized by the
184 design of experiments (DoE) or the random collection of initial experimental condition
185 parameters and results. The expectation and uncertainty of each point were predicted
186 based on a probabilistic surrogate model generated from the initial experimental results,
187 with the trade-off between exploration and exploitation of the response space. Among
188 them, the exploration region had high uncertainty, while the exploitation focuses on the
189 part with high predictive expectations. New experimental condition parameters were
190 obtained to perform new experiments after maximizing the acquisition function. The
191 experimental dataset was then extended and reused to train a more accurate surrogate
192 model. This process was iterated until obtaining satisfactory reaction yield and
193 productivity.

194
195 The initial sampling, the surrogate model, and the acquisition function as the three core

196 sections formed the MOBO model.[38, 39] Latin Hypercube Sampling (LHS) was used
197 as the initial sampling approach to avoid the presence of excessive data aggregation in
198 simple random sampling. The LHS divided the sampling units into different layers
199 according to some characterization or some rules, and then extracted samples
200 independently and randomly from the different layers. Notably, the LHS uses fewer
201 samples than the traditional OFAT or DoE approach when the same threshold is reached,
202 thus reducing the complexity of the calculation.

203

204 MOBO was a response surface approach to uncertainty guidance, in which the
205 performance of the surrogate model represented the predictive accuracy of the
206 optimizer.[36] The efficiency of the surrogate model could only be recognized if its
207 estimations of expectation and variance were close enough to the true response
208 surface.[36] Gaussian process (GP) was an infinite-dimensional extended function
209 distribution frequently used as the surrogate model.[39] GP allowed the construction of
210 joint probability distributions of variables for estimating the variance and mean of the
211 predicted data based on the available data. The Matérn class was a commonly used class
212 of covariance functions in GP, *via* Equation 4:[40]

$$213 \quad M_{\text{Matérn}}(x, y) = \frac{2^{1-\nu}\sigma^2}{\Gamma(\nu)} (\sqrt{2\nu}\|x - y\|)^{\nu} K_{\nu}(\sqrt{2\nu}\|x - y\|) \quad (4)$$

214 Where $\sigma^2 > 0$ and $\nu > 0$; ν , σ^2 , $\Gamma(\nu)$, $\|x - y\|$, and K_{ν} were the non-negative
215 parameter, the output variance, the gamma function, the distance between two points,
216 and the Bessel function, respectively.

217

218 Furthermore, the acquisition function was crucial for the desired optimization
219 performance. Among them, probabilistic improvement (PI), expected improvement
220 (EI), and upper confidence bound (UCB) are frequently used to tune hyperparameters.
221 The q -noisy expected hypervolume improvement (q NEHVI) function was superior to
222 other existing acquisition functions for MOBO, for example, it enabled one-step
223 hypervolume maximization in both noisy and noise-free environments, *via* Equation
224 5:[41, 42]

225

$$\alpha_{q\text{NEHVI}}(\chi_{\text{cand}}|\mathcal{P}) = \frac{1}{\tilde{N}} \sum_{t=1}^{\tilde{N}} \text{HVI}\left(\tilde{f}_t(\chi_{\text{cand}}|\mathcal{P})\right) \quad (5)$$

226 where \tilde{N} , HVI, \tilde{f}_t , χ_{cand} , and \mathcal{P} were the number of samples, the hypervolume
227 improvement, the posterior sample, the candidate sample, and the Pareto boundary,
228 respectively.

229

230 In this work, the q NEHVI function was used to optimize the yield of the AMA
231 ($\text{Yield}_{\text{AMA}}$) and the productivity of the AMA ($\text{Productivity}_{\text{MNA}}$) in the continuous flow
232 hydrogenation system.

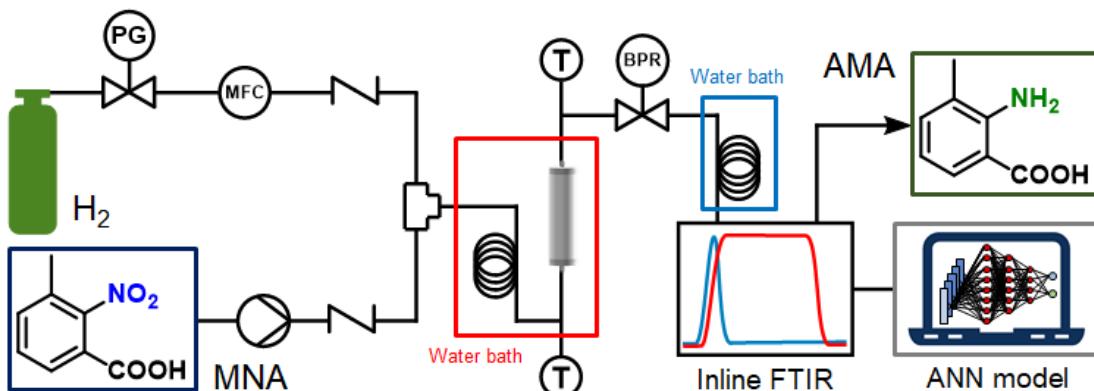
233

234 Results and discussion

235

236 In this study, a continuous flow hydrogenation system (Figure 1) was constructed to
237 perform the hydrogenation of MNA using an MPBR filled with Pd@SBA-15 catalyst.
238 Real-time reaction monitoring was achieved through an inline FTIR instrument, the
239 ReactIR 702L. The data collected via inline FTIR were processed using an ANN model,
240 enabling the acquisition of real-time concentration for MNA and AMA. These data
241 points were subsequently utilized in Bayesian optimization and kinetic modeling
242 studies to optimize the reaction system.

243



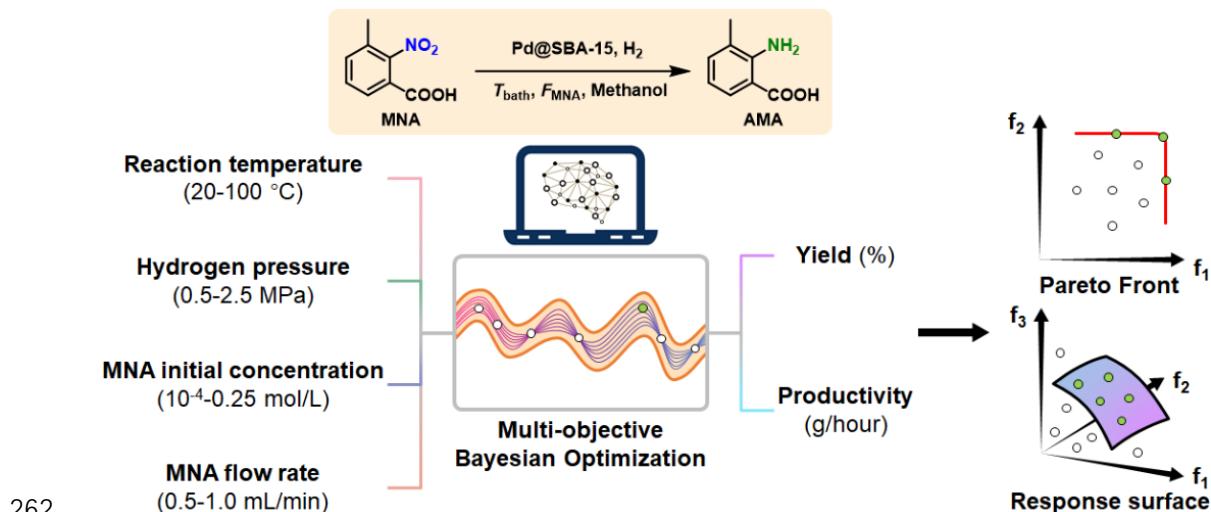
244
245 **Figure 1.** Heterogeneous continuous flow hydrogenation of MNA and its inline analysis
246

247

248 **MOBO for reaction optimization.**

249 MOBO was applied to optimize four key reaction parameters (Figure 2): reaction
250 temperature (T_{bath}), hydrogen pressure (P_{H_2}), initial MNA concentration (C_{MNA}^0), and
251 MNA solution flow rate (F_{MNA}), to maximize yield and productivity. Initially, Latin
252 Hypercube Sampling (LHS) was used to create four sets of experimental conditions,
253 and the outcomes of these experiments formed the initial training data for a Gaussian
254 Process (GP) surrogate model. Utilizing this GP model, the acquisition function known
255 as qNEHVI [43] then recommended a new set of experimental conditions. With each
256 new experiment conducted, the GP model was updated with the results, and qNEHVI
257 continued to make further recommendations. This process was repeated iteratively until
258 the desired levels of yield and productivity were reached. Ultimately, this method led
259 to the identification of the optimal experimental parameters located on the Pareto Front,
260 achieving a balance between yield and productivity.

261



263 **Figure 2.** The MOBO of the continuous flow hydrogenation of MNA

264

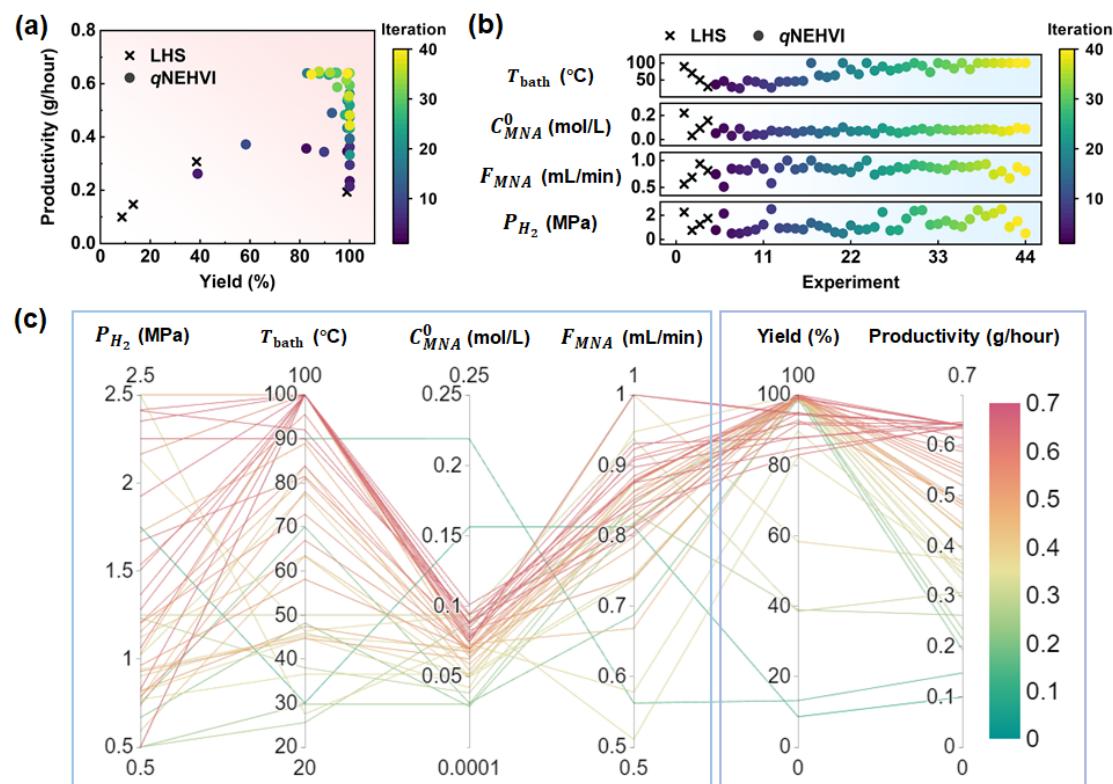
265 The parameter space for the reaction was initially delineated in Figure 2. To ensure
266 experimental safety, the hydrogen pressure and reaction temperature were capped at 2.5
267 MPa and 100 °C, respectively. The solubility of MNA in methanol dictated its
268 concentration limit, setting the upper boundary at 0.25 mL/min. The residence time,
269 crucial for reaction completion, was adjusted by modulating the solution's flow rate.

270 An excessively high flow rate could result in undue pressure build-up within the reactor
271 tubes, while a markedly low flow rate might increase the gas phase's proportion,
272 complicating the monitoring of MNA concentration. Consequently, the flow rate was
273 confined to 0.5-1.0 mL/min to balance these factors.

274

275 The MOBO results are presented in Figure 3, with Figure 3a highlighting the evolution
276 of the Pareto Front. Initial data points, marked by black crosses, were derived from LHS.
277 The colored dots, varying in color based on iteration count, represent the data points
278 suggested by the acquisition function. Through operation iterations with the GP model
279 and the qNEHVI function, the data converged to form a compact Pareto Front. The data
280 points in the upper right corner indicate the best balance between yield and productivity,
281 showing nearly 99% yield and 0.64 g/hour productivity. The conclusive set of
282 experimental parameters and results, which includes three sets capable of attaining
283 these optimal levels, is detailed in Table S2.

284



285

286 **Figure 3.** Results of the MOBO campaign. (a) The Pareto Front of the yield and productivity.
287 (b) Optimization progress: each parameter *versus* experiment number. (c) Parallel coordinate
288 plot showing the interactions between experimental parameters and results.

289

290 Figure 3b demonstrates the evolution of four optimization parameters—reaction
291 temperature, concentration, flow rate, and hydrogen pressure—throughout the
292 optimization process. It is observed that the reaction temperature, concentration, and
293 flow rate values gradually stabilize, indicating that the MOBO successfully identified
294 their optimal levels. In contrast, hydrogen pressure displayed continuous fluctuations,
295 implying uncertainty regarding its impact on the optimization goals.

296

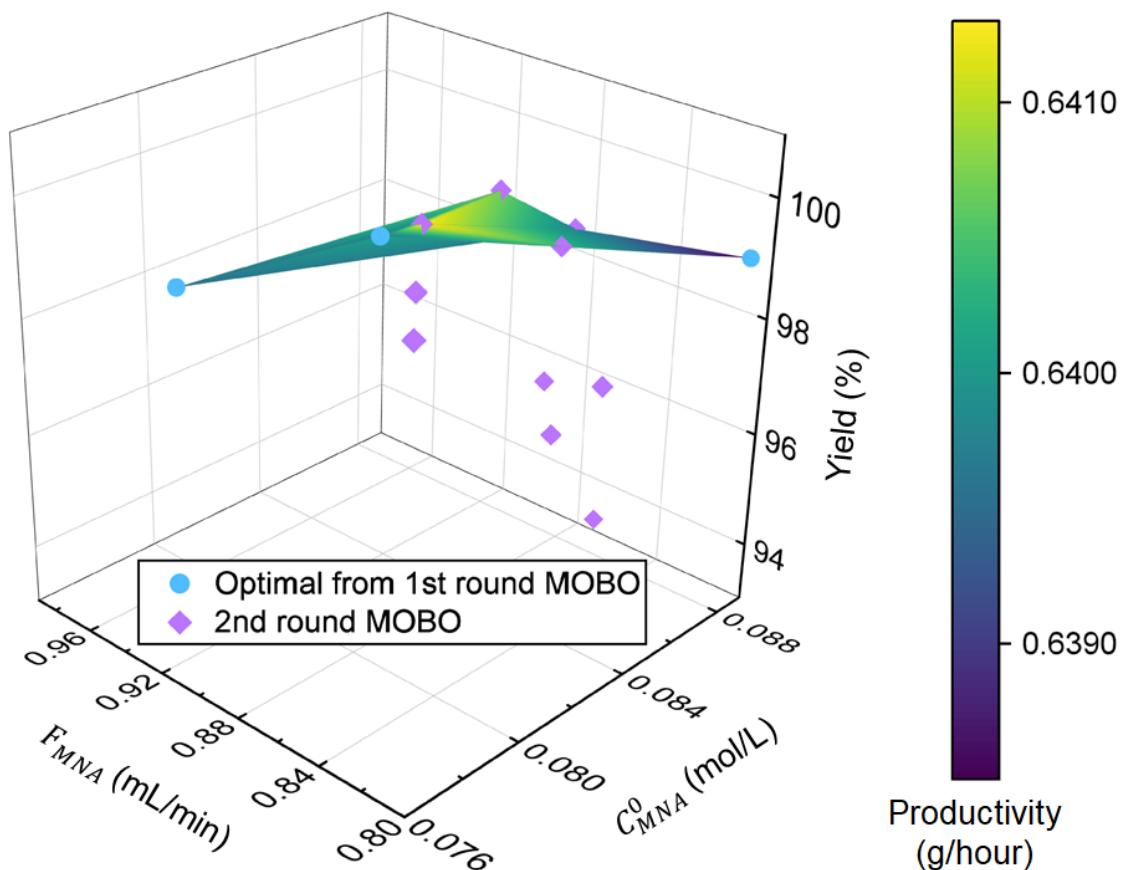
297 Further insights are provided by a parallel coordinate plot (Figure 3c), which delineates
298 the preferred reaction parameter values as determined by MOBO for enhancing both
299 yield and productivity. Notably, optimal reaction temperatures are concentrated around
300 the upper boundary of 100 °C, suggesting a preference for higher temperatures to
301 maximize yield and productivity while minimizing by-product formation. This
302 observation highlights the advantage of multi-objective optimization, demonstrating
303 that a 99% yield is attainable at various temperatures when yield is the sole
304 consideration. Moreover, the plot shows that the optimal concentration and flow rate
305 settle at approximately 0.08 mol/L and 0.86 mL/min, respectively, with neither
306 parameter reaching its maximum or minimum limit. The analysis also indicates that
307 hydrogen pressure does not significantly influence the optimization objectives, hinting
308 that even the minimum hydrogen pressure level might suffice for the reaction.

309

310 For the later comparison with kinetic modeling which uses the response surface method
311 for optimization, we performed another round of MOBO to fully explore the response
312 surface surrounding the optimal points, with the three sets of optimal experimental
313 parameters obtained in the previous round as the initial training set. The reaction
314 temperature and hydrogen pressure were fixed at 100 °C and 0.5 MPa, respectively,
315 acknowledging the positive correlation of high temperature and the optimization
316 objectives and the negligible impact of hydrogen pressure. The exploration ranges for
317 concentration and flow rate were narrowed to 0.0770-0.0884 mol/L and 0.8036-0.9227
318 mL/min, aiming for a thorough investigation of this refined reaction space. After 10

319 iterations, the results (Table S3) show that an additional four sets of experimental
320 parameters are able to achieve the same optimal yield and productivity as the original
321 three sets. Mapping these seven optimal sets of experimental data onto the reaction
322 space form a response surface with an irregular shape (Figure 4).

323



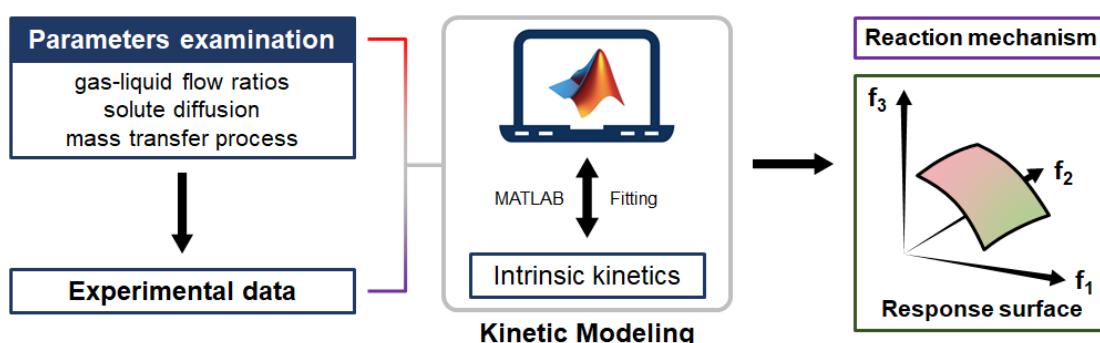
324
325 **Figure 4.** 3D response surface of objective values formed through fitting the optimal
326 experimental data underwent two rounds of MOBO. The blue points represent the three
327 optimal data points from the first round, which were used as the initial training set for the
328 second round. The purple points indicate all the data points gathered during the second round.
329

330 **Kinetic modeling for reaction optimization.**

331 Concurrently, kinetic modeling was conducted in alignment with our previously
332 established intrinsic kinetic modeling methodology[18]. It is important to note that non-
333 chemical kinetic phenomena, such as gas-liquid interfacial area, fluid kinetics, solute
334 diffusion, and mass transfer limitations, can significantly impact the accuracy of
335 intrinsic kinetic modeling.[18] A comprehensive examination of reaction parameters
336 (e.g., gas-to-liquid flow ratio, mean residence time) was performed to minimize these

337 effects, ensuring that the reaction rate data were obtained under conditions of kinetic
338 control (see **Supporting Information**). Subsequently, experimental data were
339 collected on the flow synthesis of AMA across various temperatures and mean
340 residence times. This data formed the basis for our kinetic modeling efforts, during
341 which the parameters across all models were estimated using the gPROMS (PSE, UK)
342 parameter estimation tool [44]. Upon identifying the optimal model, a detailed
343 examination of the reaction mechanism and the scope of this optimization approach was
344 conducted (Figure 5).

345



346

347 **Figure 5.** The overall approach for the kinetic modeling

348

349 The Langmuir-Hinshelwood-Hougen-Watson (LHHW) methodology is widely
350 recognized for its efficacy in the kinetic modeling of heterogeneous catalytic
351 hydrogenation processes.[44] This approach distinctively elucidates the adsorption and
352 dissociation stages inherent in catalytic hydrogenation, thereby aiding in the accurate
353 derivation of the reaction mechanism. The LHHW framework is structured around three
354 pivotal stages: the Langmuir adsorption of reactants onto the catalyst surface, the
355 surface reaction involving the adsorbed intermediates, and the subsequent desorption
356 of the products. Typically, the surface reaction step acts as the rate-determining phase.
357 Based on the variations in adsorption and dissociation behaviors of the reactants, four
358 LHHW models, each characterized by unique rate expressions (r_{MNA}), have been
359 formulated (Table 1).

360

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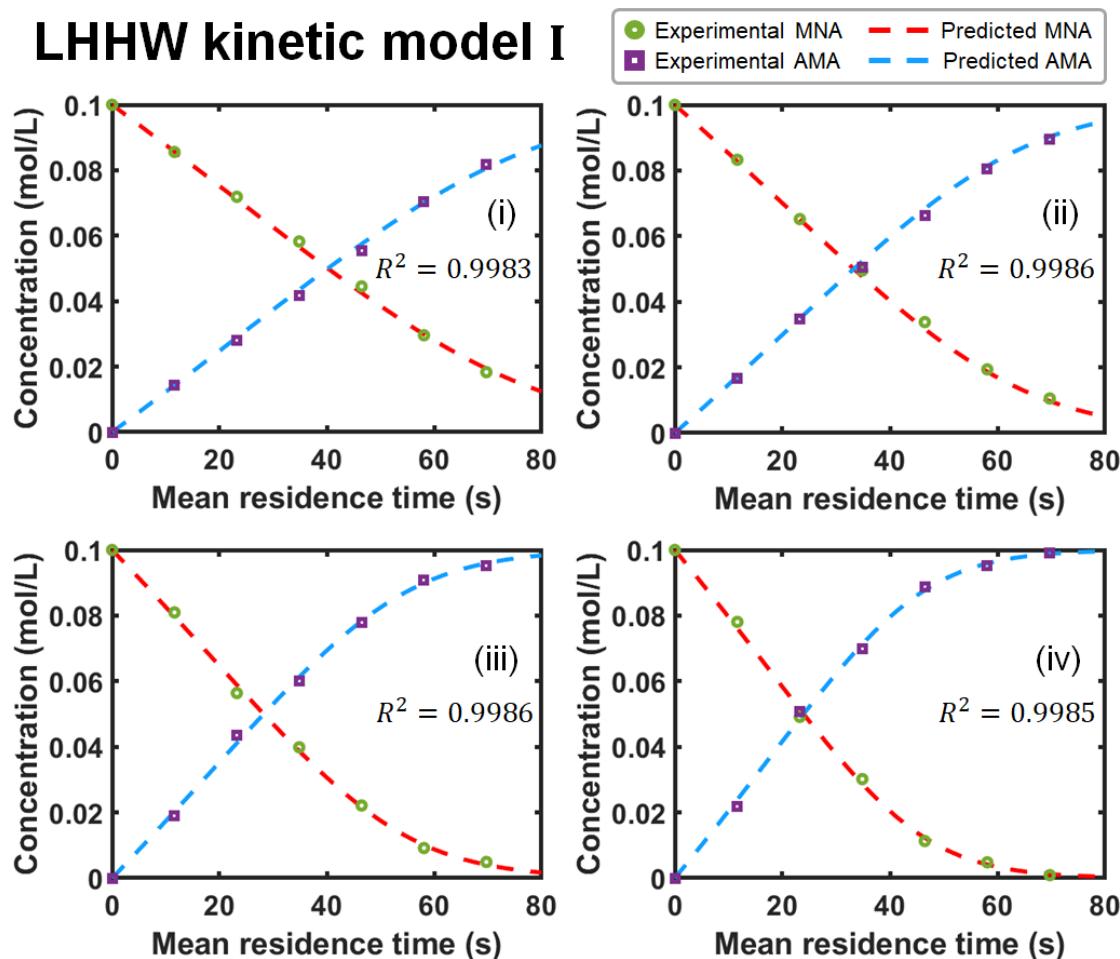
Table 1. The LHHW kinetic models I-IV for MNA hydrogenation

| Model ^{a,b} | Description | Initial rate expression |
|----------------------|--|--|
| I | competitive adsorption dissociative adsorbed H ₂ | $r_{\text{MNA}} = \frac{-k_1 K_{\text{H}_2} K_{\text{MNA}} C_{\text{MNA}}}{\{1 + \sqrt{K_{\text{H}_2} P_{\text{H}_2}} + K_{\text{MNA}} C_{\text{MNA}} + K_{\text{AMA}} C_{\text{AMA}}\}^3}$ |
| II | competitive adsorption nondissociative adsorbed H ₂ | $r_{\text{MNA}} = \frac{-k_1 K_{\text{H}_2} K_{\text{MNA}} C_{\text{MNA}} P_{\text{H}_2}}{\{1 + K_{\text{H}_2} P_{\text{H}_2} + K_{\text{MNA}} C_{\text{MNA}} + K_{\text{AMA}} C_{\text{AMA}}\}^2}$ |
| III | noncompetitive adsorption dissociative adsorbed H ₂ | $r_{\text{MNA}} = \frac{-k_1 K_{\text{H}_2} K_{\text{MNA}} C_{\text{MNA}} P_{\text{H}_2}}{\{1 + K_{\text{MNA}} C_{\text{MNA}} + K_{\text{AMA}} C_{\text{AMA}}\} \{1 + \sqrt{K_{\text{H}_2} P_{\text{H}_2}}\}^2}$ |
| IV | noncompetitive adsorption nondissociative adsorbed H ₂ | $r_{\text{MNA}} = \frac{-k_1 K_{\text{H}_2} K_{\text{MNA}} C_{\text{MNA}} P_{\text{H}_2}}{\{1 + K_{\text{MNA}} C_{\text{MNA}} + K_{\text{AMA}} C_{\text{AMA}}\} \{1 + K_{\text{H}_2} P_{\text{H}_2}\}}$ |

^a k_1 is the reaction rate constant of r_{MNA} ; K_{H_2} , K_{MNA} , and K_{AMA} are adsorption equilibrium constants of H₂, MNA, and AMA, respectively; C_{MNA} and C_{AMA} are the concentration of MNA and AMA in the collected solution, respectively; P_{H_2} is the pressure of H₂. ^bExperimental conditions for data collection: C_{MNA}^0 (0.1 mol/L), F_{MNA} (0.5 mL/min), F_{H_2} (20 mL/min), P_{H_2} (0.5 MPa).

364 The experimental data obtained were subsequently employed to fit these LHHW rate
 365 expressions as objective functions in MATLAB, achieved through the fmincon function
 366 with a Sequential Quadratic Programming (SQP) method. The ordinary differential
 367 equations (ODEs) were solved using the ODE45 function. We fitted the kinetic models
 368 to the experimental data obtained at the reaction temperatures of 30 °C (303.15 K), 40
 369 °C (313.15 K), 50 °C (323.15 K), and 60 °C (333.15 K), with the results of these fittings
 370 shown in Figure 6 and Figure S3.

LHHW kinetic model I



372
373 **Figure 6.** Fitted curves of the LHHW kinetic model I: (i) 30 °C, (ii) 40 °C, (iii) 50 °C, and (iv)
374 60 °C.

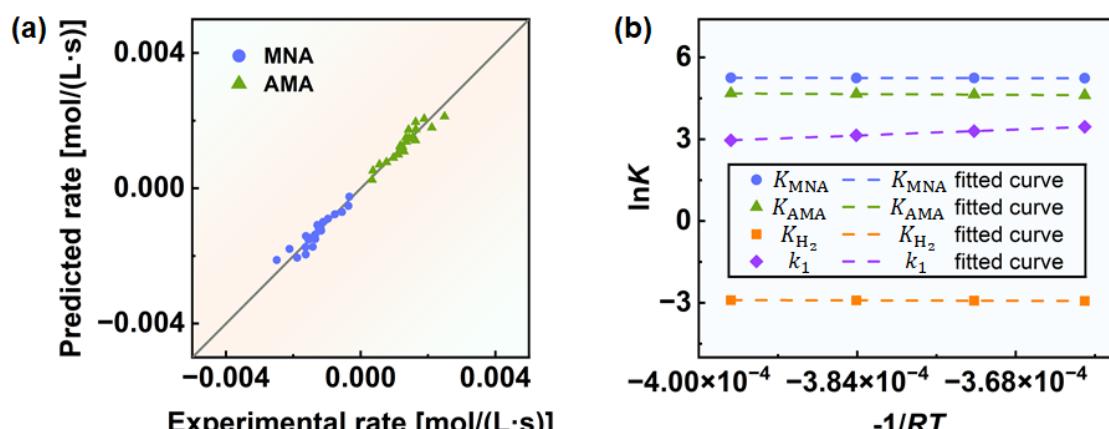
375
376 Each LHHW kinetic model was evaluated by estimating model parameters using the
377 gPROMS parameter estimation tool. Based on these estimated parameters, various
378 statistical indicators were calculated to assess the fitting performance of each model
379 (see **Supporting Information**). The selection criteria for the optimal model included
380 the highest value of regression coefficient (R^2) alongside the lowest sum of squared
381 residuals (SSR) and mean relative error (MRE). Upon comparison of these indicators
382 in Table 2, the LHHW kinetic model I emerged as the most fitting according to these
383 criteria, thereby establishing it as the optimal kinetic model. Furthermore, the chosen
384 LHHW kinetic model I was further evaluated by comparing the experimental reaction
385 rates with those predicted by the model in Figure 7a. This alignment between
386 experimental and predicted rates underscores the robustness of the LHHW kinetic
387 model I in simulating the reaction kinetics under study.

388

389 **Table 2.** Statistical evaluations related to experimental and predicted concentrations of MNA
390 for different LHHW kinetic models

| Model | Stat. param. | 30 °C | 40 °C | 50 °C | 60 °C |
|-------|-------------------|--------|--------|--------|--------|
| I | R^2 | 0.9983 | 0.9986 | 0.9986 | 0.9985 |
| | $SSR \times 10^5$ | 0.874 | 0.953 | 1.07 | 1.29 |
| | MRE (%) | 2.23 | 3.20 | 5.51 | 10.2 |
| II | R^2 | 0.9964 | 0.9984 | 0.9979 | 0.9983 |
| | $SSR \times 10^5$ | 1.90 | 1.07 | 1.67 | 1.54 |
| | MRE (%) | 4.32 | 4.86 | 6.25 | 11.9 |
| III | R^2 | 0.9967 | 0.9982 | 0.9983 | 0.9979 |
| | $SSR \times 10^5$ | 1.72 | 1.18 | 1.32 | 1.89 |
| | MRE (%) | 3.95 | 4.94 | 7.71 | 12.4 |
| IV | R^2 | 0.9969 | 0.9982 | 0.9978 | 0.9979 |
| | $SSR \times 10^5$ | 1.64 | 1.19 | 1.72 | 1.88 |
| | MRE (%) | 3.80 | 4.28 | 8.19 | 12.7 |

391



392

393 **Figure 7.** (a) Comparison of experimental reaction rate and predicted reaction rate using the
394 LHHW kinetic model I. (b) Fitted curves of Arrhenius equation for LHHW model I.

395

396 The kinetic and thermodynamic parameters of the LHHW model I are determined and
397 shown in Table 3. The k_1 , K_{H_2} , K_{MNA} , and K_{AMA} were obtained through kinetic
398 model fitting in MATLAB. The activation energy (E) and the pre-exponential factor
399 (k_0) were obtained from the Arrhenius equation (Equation 6) and its variant (Equation

400 7) for the surface reaction:

401

$$k = k_0 e^{-\frac{E}{RT}} \quad (6)$$

402

$$\ln k = -\frac{E}{RT} + \ln k_0 \quad (7)$$

403 where k is the reaction rate constant; k_0 is the pre-exponential factor; E is the
404 activation energy; R is the universal gas constant; T the temperature in K.

405

406 Table 3. Various kinetic and thermodynamic parameters of the LHHW model I

| Para. | Temperature (K) | | | | Thermodynamic parameters | |
|--|-----------------|--------|--------|--------|-----------------------------|--|
| | 303.15 | 313.15 | 323.15 | 333.15 | E (kJ mol ⁻¹) | k_0 (mol L ⁻¹ s ⁻¹) |
| k_1 (mol L ⁻¹ s ⁻¹) | 19.290 | 23.072 | 26.972 | 31.590 | 13.740 | 4.503×10^3 |

| Para. | Temperature (K) | | | | Thermodynamic parameters | |
|----------------------------------|-----------------|---------|---------|---------|-------------------------------|--------------------------------|
| | 303.15 | 313.15 | 323.15 | 333.15 | E_a (kJ mol ⁻¹) | K_0 |
| K_{MNA} (L mol ⁻¹) | 190.988 | 189.882 | 188.768 | 187.866 | -0.465 | 158.823 (L mol ⁻¹) |
| K_{AMA} (L mol ⁻¹) | 107.645 | 105.101 | 102.990 | 100.703 | -1.849 | 51.685 (L mol ⁻¹) |
| K_{H_2} (MPa ⁻¹) | 0.0548 | 0.0543 | 0.0538 | 0.0533 | -0.776 | 0.0403 (MPa ⁻¹) |

407

408 The activation energy of the surface reaction is 13.740 kJ/mol through the linear fitting
409 method, and the adsorption heats (E_a) of H₂, MNA, and AMA are all negative,
410 signifying that the adsorption process is exothermic (Figure 7b). The adsorption heat
411 (E_a) and the pre-exponential factor (K_0) were also estimated using the Arrhenius
412 equation (Equation 8) for the adsorption process:

413

$$\ln K = -\frac{E_a}{RT} + \ln K_0 \quad (8)$$

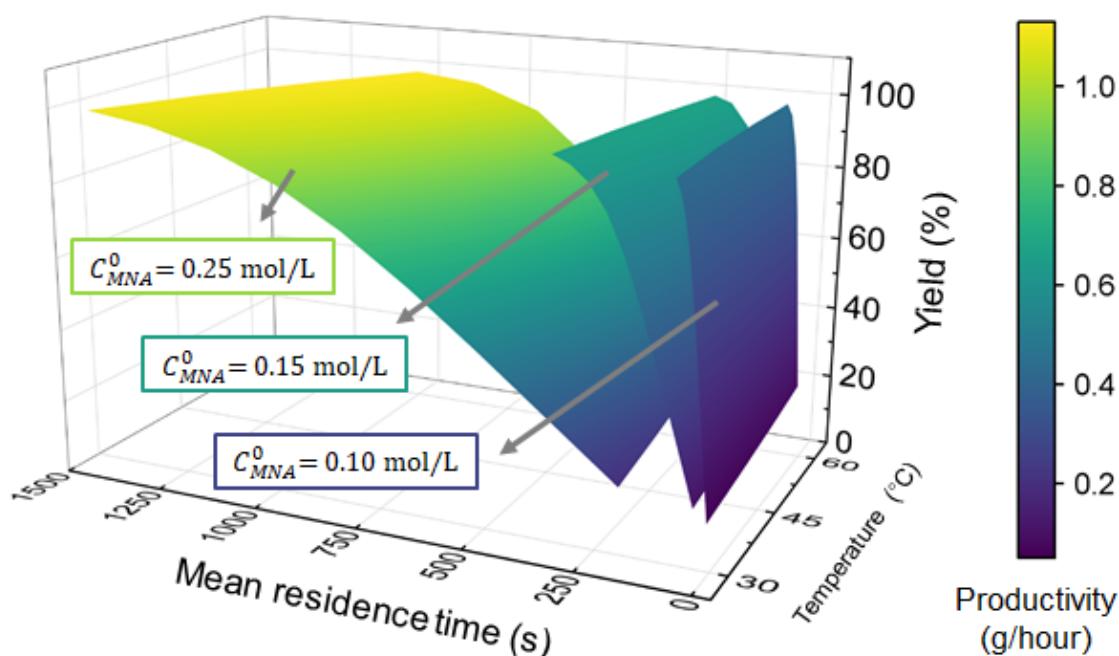
414 where K is the adsorption equilibrium constant; K_0 is the pre-exponential factor; E_a
415 is the adsorption heat; R is the universal gas constant; T the temperature in K.

416

417 To achieve reaction optimization via intrinsic kinetic modeling, response surfaces of
418 the kinetic model were generated across various MNA concentrations, with yield
419 represented on the Z axis and the productivity illustrated through a color map (Figure

420 8). While it is feasible to attain a yield nearing 99% at a lower concentration and reduced
421 mean residence time, optimizing both productivity and yield simultaneously—targeting
422 the yellow area in Figure 8—requires an increase in both the mean residence time and
423 MNA concentration. Under these optimized conditions, it is possible to achieve both a
424 yield and productivity of up to 99% and 1.13 g/hour, respectively. The results predicted
425 by the kinetic model at the optimized conditions were all confirmed by experimental
426 results (Table S4).

427



428

429 **Figure 8.** 3D response surface of objective values formed through the LHHW kinetic model I

430

431 **Comparison of MOBO and kinetic modeling.**

432 Table 4 presents the optimal reaction parameters and results from the two optimization
433 approaches. The MOBO achieved an optimal yield of approximately 99% and
434 productivity of 0.64 g/hour, respectively. Conversely, kinetic modeling achieved a
435 similar optimal yield (~99%) but attained higher productivity (1.13 g/hour). The
436 variation in optimal productivity was attributed to the distinct strategies for
437 manipulating the residence time of the two approaches. MOBO modulated the
438 residence time by adjusting the solution's flow rate, keeping the catalyst mass constant

439 within the MPBR. This approach was favored because MOBO was implemented in an
440 automated manner, discouraging altering the catalyst quantity in the MPBR. Manually
441 increasing the catalyst quantity could further increase productivity. Conversely, the
442 intrinsic kinetic modeling methodology, which presumes that non-chemical kinetics
443 phenomena (e.g., mass transfer, solute diffusion, flow dynamics) minimally impact the
444 reaction, does not permit free variation of the flow rate but requires adjustment of the
445 catalyst mass to maintain a constant solution flow rate.

446

447 Table 4. The optimal reaction parameters and results of MOBO and kinetic modeling

| Data type ^a | C_{MNA}^0 (mol/L) | F_{MNA} (mL/min) | Yield (%) | Productivity (g/hour) |
|------------------------|---------------------|--------------------|----------------|-----------------------|
| MOBO | 0.0770 | 0.9227 | 99.25 | 0.6396 |
| | 0.0805 | 0.8763 | 99.99 | 0.6397 |
| | 0.0884 | 0.8036 | 99.09 | 0.6385 |
| | 0.0854 | 0.8547 | 99.18 | 0.6404 |
| | 0.0868 | 0.8648 | 99.08 | 0.6398 |
| | 0.0846 | 0.8741 | 99.99 | 0.6407 |
| | 0.0817 | 0.8733 | 99.99 | 0.6413 |
| Data type ^b | T_{bath} (°C) | MRT (s) | Yield (%) | Productivity (g/hour) |
| | | | Predicted data | Experimental data |
| Kinetic modeling | 60 | 980 | 99.16 | 1.1242 |
| | 55 | 1050 | 99.02 | 1.1226 |
| | 50 | 1150 | 99.02 | 1.1226 |
| | 45 | 1280 | 99.11 | 1.1237 |
| | 40 | 1400 | 99.06 | 1.1231 |

^aExperimental conditions for data collection: T_{bath} (100 °C), P_{H_2} (0.5 MPa). ^bExperimental conditions for data collection: C_{MNA}^0 (0.25 mol/L), F_{MNA} (0.5 mL/min), F_{H_2} (20 mL/min), P_{H_2} (0.5 MPa).

448

449 Regarding optimization efficiency, MOBO excels in swiftly identifying the optimal
450 reaction space by utilizing the Pareto Front. With an additional round of optimization,
451 it effectively narrowed down the search to the seven promising parameter combinations
452 (Figure 4). These selected points are subsequently used to construct the response
453 surface for the optimization objectives, effectively mapping out the optimal reaction
454 space from a broader set of possibilities. The integration of inline FTIR with MOBO
455 enhances its capability to optimize reactions rapidly and with high precision. In contrast,

456 kinetic modeling requires significant time and resources. The process involves the
457 collection of large amounts of experimental data, the fitting of kinetic equations, and
458 the derivation of scientific models. This approach is more labor intensive and slower
459 than the simplified and data-saving process of MOBO.

460

461 Although kinetic modeling is may not be as efficient as MOBO for reaction
462 optimization, it offers a distinct advantage in terms of understanding reaction kinetics.
463 While Bayesian Optimization is engineered for rapid convergence to optimal solutions,
464 it lacks the capability to generate a comprehensive response surface across the full
465 reaction space (Figure 4). In contrast, kinetic modeling allows for the calculation of a
466 spectrum of optimal reaction parameters by leveraging predictions from scientific
467 models. The response surfaces derived from kinetic modeling (Figure 8) provide
468 valuable insights into reaction optimization by offering a visual representation of the
469 entire reaction space, thereby highlighting trends and delineating the boundaries of
470 optimization possibilities [7, 45].

471

472 **Conclusions**

473 In this work, we developed a heterogeneous continuous flow hydrogenation system
474 enhanced with real-time inline infrared monitoring utilizing an ANN model for
475 optimizing the synthesis of the crucial pesticide intermediate, AMA. This work
476 systematically undertook and compared MOBO and kinetic modeling approaches to
477 optimize the reaction process. In only 40 iterations, MOBO efficiently identified the
478 Pareto optimal parameter combinations within the vast and intricate reaction space. The
479 compromise between yield and productivity was impressively achieved. Conversely,
480 intrinsic kinetic modeling revealed the activation energy of this hydrogenation reaction
481 and characterized the hydrogen adsorption as competitive dissociative adsorption. This
482 approach provided a comprehensive understanding of how variations in parameters
483 affect the reaction results. Simultaneous optimization of yield and productivity was also
484 achieved by leveraging the response surfaces generated from the kinetic model.

485
486 While MOBO is efficient and accurate in determining the optimal reaction conditions,
487 kinetic modeling provides insight into the mechanistic details of the reaction and offers
488 comprehensive optimization possibilities over the entire reaction space. Thus, the in-
489 depth study of heterogeneous continuous flow hydrogenation systems benefits from the
490 synergistic application of MOBO and kinetic modeling. This dual approach enriches
491 our understanding of reaction optimization and provides a deeper exploration of
492 continuous-flow hydrogenation systems, offering valuable prospects for future research
493 and development in this field.

494

495 **Declaration of Competing Interest**

496 The authors declare that they have no known competing financial interests or personal
497 relationships that could have appeared to influence the work reported in this paper.

498

499 **Acknowledgments**

500 This research was supported by the Joint Funds of the Zhejiang Provincial Natural
501 Science Foundation of China under Grant No. LHDMZ23B060001, Zhejiang Province
502 Science and Technology Plan Project under Grant No. 2022C01179, and the National
503 Natural Science Foundation of China under Grant No. 22108252).

504

505 **Appendix A. Supplementary data**

506 Supplementary data to this article can be found online at XXXXXXXXXXXXXXXXX.

507

508 **References**

- 509 [1] R.Y. Qu, K. Junge, M. Beller, Hydrogenation of Carboxylic Acids, Esters, and Related Compounds
510 over Heterogeneous Catalysts: A Step toward Sustainable and Carbon-Neutral Processes, *Chem. Rev.*
511 123 (3) (2023) 1103-1165, <https://doi.org/10.1021/acs.chemrev.2c00550>.
- 512 [2] T. Wagener, A. Heusler, Z. Nairoukh, K. Bergander, C.G. Daniliuc, F. Glorius, Accessing
513 (Multi)Fluorinated Piperidines Using Heterogeneous Hydrogenation, *ACS Catal.* 10 (20) (2020) 12052-
514 12057, <https://doi.org/10.1021/acscatal.0c03278>.

- 515 [3] L. Lückemeier, T. De Vos, L. Schlichter, C. Gutheil, C.G. Daniliuc, F. Glorius, Chemoselective
516 Heterogeneous Hydrogenation of Sulfur Containing Quinolines under Mild Conditions, *J. Am. Chem.*
517 *Soc.* (2024) Advance Article, <https://doi.org/10.1021/jacs.3c11163>.
- 518 [4] T. Yasukawa, R. Masuda, S. Kobayashi, Development of heterogeneous catalyst systems for the
519 continuous synthesis of chiral amines via asymmetric hydrogenation, *Nat. Catal.* 2 (12) (2019) 1088-
520 1092, <https://doi.org/10.1038/s41929-019-0371-y>.
- 521 [5] Y. Saito, Y. Sato, S. Kobayashi, Continuous-Flow Enantioselective Hydrogenative Enyne Cyclization
522 with Chiral Heterogeneous Rh Catalysts, *ACS Catal.* 14 (4) (2024) 2202-2206,
523 <https://doi.org/10.1021/acscatal.3c05868>.
- 524 [6] M. González-Esguevillas, D.F. Fernández, J.A. Rincón, M. Barberis, O. de Frutos, C. Mateos, S.
525 García-Cerrada, J. Agejas, D.W.C. MacMillan, Rapid Optimization of Photoredox Reactions for
526 Continuous-Flow Systems Using Microscale Batch Technology, *ACS Cent. Sci.* 7 (7) (2021) 1126-1134,
527 <https://doi.org/10.1021/acscentsci.1c00303>.
- 528 [7] C.J. Taylor, A. Pomberger, K.C. Felton, R. Grainger, M. Barecka, T.W. Chamberlain, R.A. Bourne,
529 C.N. Johnson, A.A. Lapkin, A Brief Introduction to Chemical Reaction Optimization, *Chem. Rev.* 123
530 (6) (2023) 3089-3126, <https://doi.org/10.1021/acs.chemrev.2c00798>.
- 531 [8] D. Lendrem, M. Owen, S. Godbert, DOE (design of experiments) in development chemistry: Potential
532 obstacles, *Org. Process Res. Dev.* 5 (3) (2001) 324-327, <https://doi.org/10.1021/op000025i>.
- 533 [9] M. Strohmann, A. Bordet, A.J. Vorholt, W. Leitner, Tailor-made biofuel 2-butyltetrahydrofuran from
534 the continuous flow hydrogenation and deoxygenation of furfuralacetone, *Green Chem.* 21 (23) (2019)
535 6299-6306, <https://doi.org/10.1039/c9gc02555c>.
- 536 [10] Y.T. Wang, P. Prinsen, K.S. Triantafyllidis, S.A. Karakoulia, P.N. Trikalitis, A. Yepez, C. Len, R.
537 Luque, Comparative Study of Supported Monometallic Catalysts in the Liquid-Phase Hydrogenation of
538 Furfural: Batch Versus Continuous Flow, *ACS Sustainable Chem. Eng.* 6 (8) (2018) 9831-9844,
539 <https://doi.org/10.1021/acssuschemeng.8b00984>.
- 540 [11] M. Kundra, T. Grall, D. Ng, Z.L. Xie, C.H. Hornung, Continuous Flow Hydrogenation of Flavorings
541 and Fragrances Using 3D-Printed Catalytic Static Mixers, *Ind. Eng. Chem. Res.* 60 (5) (2021) 1989-2002,
542 <https://doi.org/10.1021/acs.iecr.0c05671>.
- 543 [12] P.X. Wang, Z.P. Peng, X.P. Wang, Y. Lin, H.B. Hong, F. Chen, X.K. Chen, J.S. Zhang, Continuous
544 hydrogenation of nitriles to primary amines with high selectivity in flow, *Chem. Eng. Sci.* 269 (2023)
545 118460, <https://doi.org/10.1016/j.ces.2023.118460>.
- 546 [13] M.D. Peris-Díaz, M.A. Sentandreu, E. Sentandreu, Multiobjective optimization of liquid
547 chromatography-triple-quadrupole mass spectrometry analysis of underivatized human urinary amino
548 acids through chemometrics, *Anal. Bioanal. Chem.* 410 (18) (2018) 4275-4284,
549 <https://doi.org/10.1007/s00216-018-1083-x>.
- 550 [14] B. Zhang, A. Mathoor, T. Junkers, High Throughput Multidimensional Kinetic Screening in
551 Continuous Flow Reactors, *Angew. Chem., Int. Ed.* 62 (38) (2023) e202308838,
552 <https://doi.org/10.1002/anie.202308838>.
- 553 [15] P. Rojahn, K.D.P. Nigam, F. Schael, Experimental study and kinetic modeling of continuous flow
554 conversion of fructose to 5-(chloromethyl)furfural using micro- and millistructured coiled flow inverter,
555 *Chem. Eng. J.* 450 (2022) 138243, <https://doi.org/10.1016/j.cej.2022.138243>.
- 556 [16] Z.F. Yan, C.C. Du, Y.B. Wang, J. Deng, G.S. Luo, Dehydrochlorination of β -chlorohydrin in
557 continuous microflow system: Reaction kinetics and process intensification, *Chem. Eng. J.* 444 (2022)
558 136498, <https://doi.org/10.1016/j.cej.2022.136498>.

- 559 [17] X.Y. Lin, K. Wang, B.Y. Zhou, G.S. Luo, A microreactor-based research for the kinetics of polyvinyl
560 butyral (PVB) synthesis reaction, Chem. Eng. J. 383 (2020) 123181,
561 <https://doi.org/10.1016/j.cej.2019.123181>.
- 562 [18] H.T. Xue, T.T. Qi, W.K. Su, K.J. Wu, A. Su, Heterogeneous Continuous Flow Hydrogenation of
563 Hexafluoroacetone Trihydrate and Its Kinetic Modeling, Ind. Eng. Chem. Res. 62 (15) (2023) 6121-6129,
564 <https://doi.org/10.1021/acs.iecr.3c00291>.
- 565 [19] Z.Q. Yu, M.N. Ren, P. Li, J.D. Zhou, N. Li, X. Li, H.C. Fan, Continuous hydrogenation of 2-(4-
566 nitrophenyl) butanoic acid: Kinetics study in a micropacked-bed reactor, Chem. Eng. Sci. 271 (2023)
567 118565, <https://doi.org/10.1016/j.ces.2023.118565>.
- 568 [20] N.K. Razdan, T.C. Lin, A. Bhan, Concepts Relevant for the Kinetic Analysis of Reversible Reaction
569 Systems, Chem. Rev. 123 (6) (2023) 2950-3006, <https://doi.org/10.1021/acs.chemrev.2c00510>.
- 570 [21] T. Dahou, F. Defoort, B. Khiari, M. Labaki, C. Dupont, M. Jeguirim, Role of inorganics on the
571 biomass char gasification reactivity: A review involving reaction mechanisms and kinetics models,
572 Renewable Sustainable Energy Rev. 135 (2021) 110136, <https://doi.org/10.1016/j.rser.2020.110136>.
- 573 [22] Z.H. Yu, N. Ji, X.Y. Li, R. Zhang, Y.A. Qiao, J. Xiong, J. Liu, X.B. Lu, Kinetics Driven by Hollow
574 Nanoreactors: An Opportunity for Controllable Catalysis, Angew. Chem., Int. Ed. 62 (3) (2023)
575 e202213612, <https://doi.org/10.1002/anie.202213612>.
- 576 [23] C. Wang, Y. Yang, Z.L. Huang, J.Y. Sun, J.D. Wang, Y.R. Yang, B. Du, Gas-liquid mass transfer in
577 a gas-liquid-solid three-phase moving bed, Chem. Eng. J. 420 (2021) 130449,
578 <https://doi.org/10.1016/j.cej.2021.130449>.
- 579 [24] C. Wang, Y. Yang, Z.L. Huang, J.Y. Sun, Z.W. Liao, J.D. Wang, Y.R. Yang, B. Du, Flow regimes in
580 a gas-liquid-solid three-phase moving bed, AIChE J. 67 (11) (2021) e17374,
581 <https://doi.org/10.1002/aic.17374>.
- 582 [25] A.M.K. Nambiar, C.P. Breen, T. Hart, T. Kulesza, T.F. Jamison, K.F. Jensen, Bayesian Optimization
583 of Computer-Proposed Multistep Synthetic Routes on an Automated Robotic Flow Platform, ACS Cent.
584 Sci. 8 (6) (2022) 825-836, <https://doi.org/10.1021/acscentsci.2c00207>.
- 585 [26] J.H. Dunlap, J.G. Ethier, A.A. Putnam-Neeb, S. Iyer, S.X.L. Luo, H.S. Feng, J.A.G. Torres, A.G.
586 Doyle, T.M. Swager, R.A. Vaia, P. Mirau, C.A. Crouse, L.A. Baldwin, Continuous flow synthesis of
587 pyridinium salts accelerated by multi-objective Bayesian optimization with active learning, Chem. Sci.
588 14 (30) (2023) 8061-8069, <https://doi.org/10.1039/d3sc01303k>.
- 589 [27] O.J. Kershaw, A.D. Clayton, J.A. Manson, A. Barthelme, J. Pavay, P. Peach, J. Mustakis, R.M.
590 Howard, T.W. Chamberlain, N.J. Warren, R.A. Bourne, Machine learning directed multi-objective
591 optimization of mixed variable chemical systems, Chem. Eng. J. 451 (2023) 138443,
592 <https://doi.org/10.1016/j.cej.2022.138443>.
- 593 [28] A.M. Schweidtmann, A.D. Clayton, N. Holmes, E. Bradford, R.A. Bourne, A.A. Lapkin, Machine
594 learning meets continuous flow chemistry: Automated optimization towards the Pareto front of multiple
595 objectives, Chem. Eng. J. 352 (2018) 277-282, <https://doi.org/10.1016/j.cej.2018.07.031>.
- 596 [29] A.D. Clayton, E.O. Pyzer-Knapp, M. Purdie, M.F. Jones, A. Barthelme, J. Pavay, N. Kapur, T.W.
597 Chamberlain, A.J. Blacker, R.A. Bourne, Bayesian Self-Optimization for Telescopied Continuous Flow
598 Synthesis, Angew. Chem., Int. Ed. 62 (3) (2023) e202214511, <https://doi.org/10.1002/anie.202214511>.
- 599 [30] C.J. Taylor, K.C. Felton, D. Wigh, M.I. Jeraal, R. Grainger, G. Chessari, C.N. Johnson, A.A. Lapkin,
600 Accelerated Chemical Reaction Optimization Using Multi-Task Learning, ACS Cent. Sci. 9 (5) (2023)
601 957-968, <https://doi.org/10.1021/acscentsci.3c00050>.
- 602 [31] P.W. Liu, H. Jin, Y. Chen, D.R. Wang, H.H. Yan, M.Z. Wu, F. Zhao, W.P. Zhu, Process analytical

- 603 technologies and self-optimization algorithms in automated pharmaceutical continuous manufacturing,
604 Chin. Chem. Lett. 35 (3) (2024) 108877, <https://doi.org/10.1016/j.cclet.2023.108877>.
- 605 [32] J. Britton, S. Majumdar, G.A. Weiss, Continuous flow biocatalysis, Chem. Soc. Rev. 47 (15) (2018)
606 5891-5918, <https://doi.org/10.1039/c7cs00906b>.
- 607 [33] P. Sagmeister, R. Lebl, I. Castillo, J. Rehrl, J. Kruisz, M. Sipek, M. Horn, S. Sacher, D. Cantillo, J.D.
608 Williams, C.O. Kappe, Advanced Real-Time Process Analytics for Multistep Synthesis in Continuous
609 Flow, Angew. Chem., Int. Ed. 60 (15) (2021) 8139-8148, <https://doi.org/10.1002/anie.202016007>.
- 610 [34] P. Sagmeister, R. Hierzegger, J.D. Williams, C.O. Kappe, S. Kowarik, Artificial neural networks and
611 data fusion enable concentration predictions for inline process analytics, Digital Discovery 1 (2022)
612 405-412, <https://doi.org/10.1039/D2DD00006G>.
- 613 [35] K.J. Chai, R.Q. Shen, T.T. Qi, J.L. Chen, W.K. Su, A. Su, Continuous-Flow Hydrogenation of
614 Nitroaromatics in Microreactor with Mesoporous Pd@SBA-15, Processes 11 (4) (2023) 1074,
615 <https://doi.org/10.3390/pr11041074>.
- 616 [36] R.Z. Liang, X.N. Duan, J.S. Zhang, Z.H. Yuan, Bayesian based reaction optimization for complex
617 continuous gas-liquid-solid reactions, React. Chem. Eng. 7 (3) (2022) 590-598,
618 <https://doi.org/10.1039/d1re00397f>.
- 619 [37] E. Braconi, E. Godineau, Bayesian Optimization as a Sustainable Strategy for Early-Stage Process
620 Development? A Case Study of Cu-Catalyzed C-N Coupling of Sterically Hindered Pyrazines, ACS
621 Sustainable Chem. Eng. 11 (28) (2023) 10545-10554, <https://doi.org/10.1021/acssuschemeng.3c02455>.
- 622 [38] A. Navid, S. Khalilarya, M. Abbasi, Diesel engine optimization with multi-objective performance
623 characteristics by non-evolutionary Nelder-Mead algorithm: Sobol sequence and Latin hypercube
624 sampling methods comparison in DoE process, Fuel 228 (2018) 349-367,
625 <https://doi.org/10.1016/j.fuel.2018.04.142>.
- 626 [39] T.T. Qi, G.H. Luo, H.T. Xue, F. Su, J.L. Chen, W.K. Su, K.J. Wu, A. Su, Continuous heterogeneous
627 synthesis of hexafluoroacetone and its machine learning-assisted optimization, J. Flow Chem. 13 (3)
628 (2023) 337-346, <https://doi.org/10.1007/s41981-023-00273-1>.
- 629 [40] N. Leonenko, A. Malyarenko, Matérn Class Tensor-Valued Random Fields and Beyond, J. Stat. Phys.
630 168 (6) (2017) 1276-1301, <https://doi.org/10.1007/s10955-017-1847-2>.
- 631 [41] J.Y.Z. Zhang, N. Sugisawa, K.C. Felton, S. Fuse, A.A. Lapkin, Multi-objective Bayesian
632 optimisation using q -noisy expected hypervolume improvement (q NEHVI) for the Schotten-Baumann
633 reaction, React. Chem. Eng. (2024) Advance Article, <https://doi.org/10.1039/d3re00502j>.
- 634 [42] G.H. Luo, X.L. Yang, W.K. Su, T.T. Qi, Q.L. Xu, A. Su, Optimizing telescoped heterogeneous
635 catalysis with noise-resilient multi-objective Bayesian optimization, ChemRxiv (2024) Advance
636 Article, <https://doi.org/10.26434/chemrxiv-2024-9257k>.
- 637 [43] S. Daulton, M. Balandat, E. Bakshy, Parallel Bayesian Optimization of Multiple Noisy Objectives
638 with Expected Hypervolume Improvement, Advances in Neural Information Processing Systems 34
639 (2021) 2187-2200.
- 640 [44] B.R. Patil, A.H. Bari, D.V. Pinjari, A.B. Pandit, Intrinsic Kinetics of Three-Phase Slurry
641 Hydrogenation of *o*-Nitrocardanol to *o*-Aminocardanol over Raney Nickel Catalyst, Ind. Eng. Chem.
642 Res. 56 (39) (2017) 11034-11041, <https://doi.org/10.1021/acs.iecr.7b02523>.
- 643 [45] F. Wagner, P. Sagmeister, C.E. Jusner, T.G. Tampone, V. Manee, F.G. Buono, J.D. Williams, C.O.
644 Kappe, A Slug Flow Platform with Multiple Process Analytics Facilitates Flexible Reaction Optimization,
645 Adv. Sci. (2024) 2308034, <https://doi.org/10.1002/advs.202308034>.