HWK 0

Due January 27, 2017
Instructions for submission into your class SVN repository are on the webpage.

The purpose of this assignment is to give you a chance to refresh the math skills we expect you to have learned in prior classes. These particular skills will be essential to mastery of CS225, and we are unlikely to take much class time reminding you how to solve similar problems. Though you are not required to work independently on this assignment, we encourage you to do so because we think it may help you diagnose and remedy some things you might otherwise find difficult later on in the course. If this homework is difficult, please consider completing the discrete math requirement (CS173 or MATH 213) before taking CS225.

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Section (circle one):

Regular Sections:

Regular Se	ctions.		
Wednesday	5–7pm AYT	7–9pm AYB	
Thursday	9–11am AYC	11–1pm AYD	1–3pm AYE
	3–5pm AYF	5–7pm AYG	7–9pm AYH
Friday	9-11am AYQ	9–11am AYI	11-1pm AYJ
(1–3pm AYS	1–3pm AYK	3–5pm AYL
Laptop Sec	ctions:		
Wednesday	5–7pm AYM	7–9pm AYR	
Thursday	1–3pm AYN	3–5pm AYO	5–7pm AYP

Grade	Out of 60
Grader	

1. (3 points) Using 140 characters or less, post a synopsis of your favorite movie to the cour piazza space under the "HW0 tell me something!" notice, so that your post is visible everyone in the class, and tagged by #HW0num1. Also, use Piazza's code-formatting to to write a private post to course staff that includes at least 5 lines of code. It can be code your own or from a favorite project—it doesn't even have to be syntactically correct—but must be formatted as a code block in your post, and also include the tag #HW0num1. (Hi Check http://support.piazza.com/customer/portal/articles/1774756-code-blocking). Final please write the 2 post numbers corresponding to your posts here:

Favorite Movie Post (Public) number:	1642
Formatted Code Post (Private) number:	(6 49

2. (12 points) Simplify the following expressions as much as possible, without using an calc lator (either hardware or software). Do not approximate. Express all rational numb as improper fractions. Show your work in the space provided, and write your answer in box provided.

(a)
$$\prod_{k=2}^{n} \left(1 - \frac{1}{k^2}\right)$$
Answer for (a):
$$\prod_{k=2}^{n} \left(1 - \frac{1}{k^2}\right) \times C[-\frac{1}{3\times3}] \times C[-\frac{1}{4\times4}] \times C[-\frac{1}{12\times3}] \times C[-\frac{1}$$

(b) $3^{1000} \mod 7$

Answer for (b):

$$(c) \sum_{r=1}^{\infty} (\frac{1}{2})^r$$

(c)
$$\sum_{r=1}^{\infty} (\frac{1}{2})^r$$

$$\sum_{r=1}^{\infty} \frac{1}{2} \frac{$$

Answer for (c):

 $(d) \ \frac{\log_7 81}{\log_7 9}$

Answer for (d):

$$\frac{\log_7 81}{\log_7 9} = \frac{\log_7 3^4}{\log_7 3^2} = \frac{4\log_7 3}{2\log_7 3} = 2$$

(e) $\log_2 4^{2n}$

	710			L	7	
109	242N	Marin .	1092	2	- 1	4r

Answer for (e):

 $(f)\ \log_{17} 221 - \log_{17} 13$

Answer for (f):

109,7221-109,713 = (09,717

(n+1)

3. (8 points) Find the formula for $1+\sum_{j=1}^{n} j!j$, and show work proving the formula is correct using induction.

Formula:

Formula:

Gaess

$$S(n+1) = 1 + \sum_{j=1}^{n+1} j! j = (n+2)!$$
 $\sum_{j=1}^{n} j! j + (n+1)! (n+1)$
 $S(n+1) = (n+1)! + (n+1)! (n+1)$
 $S(n+1)! + (n+2)!$
 $S(n) = (n+2)!$

4. (8 points) Indicate for each of the following pairs of expressions (f(n), g(n)), whether f(n) is O, Ω , or Θ of g(n). Prove your answers to the first two items, but just GIVE an answer to the last two.

(a)
$$f(n) = 4^{\log_4 n}$$
 and $g(n) = 2n + 1$.

$$\therefore$$
 cg(n) \leq f(n) \leq (29cn)

(b)
$$f(n) = n^2$$
 and $g(n) = (\sqrt{2})^{\log_2 n}$.

$$f(n) = n^2$$

$$g(n) = \sqrt{2} \log_2 n$$

$$= 2n$$

$$0 \le c g(n) \le f(n)$$

Answer for (a):
$$f(n) \in \bigcap g(n)$$

Answer for (b):
$$f(n) \supseteq g(n)$$

(c)
$$f(n) = \log_2(n!)$$
 and $g(n) = n \log_2 n$.

$$f(n) = \frac{\log (n!)}{\log 2}$$

$$g(n) = \frac{\log n}{\log_2}$$
Answer for (c):

Answer for (c):
$$f(n) \bigcirc g(n)$$

(d)
$$f(n) = n^k$$
 and $g(n) = c^n$ where k and c are constants and $c > 1$.

$$f(n) = nk$$

$$g(n) = c^n$$

$$c > 1$$

$$hen n > \infty c^n > nk$$

Answer for (d):
$$f(n) \bigcirc g(n)$$

5. (9 points) Solve the following recurrence relations for integer n. If no solution exists, please explain the result.

(a)
$$T(n) = T(\frac{n}{2}) + 5$$
, $T(1) = 1$; assume *n* is a power of 2.

Answer for (a):
$$5 \log_2 n + 1$$

T(1) = $7 (\frac{1}{2}) + \frac{1}{2} = 1$

Set $4 \log_2 \frac{1}{2} + \frac{1}{2} = 1$
 $8 \log_2 \frac{1}{2} + \frac{1}$

(b)
$$T(n) = T(n-1) + \frac{1}{n}, T(0) = 0.$$

(c) Prove that your answer to part (a) is correct using induction.

$$n=3$$
 $T(2) = T(1)+5=6$
 $T(n)=5 \log_2 n+1$
 $T(2n) = 5 \cdot \log_2 2 \cdot n + 1 = 5 \cdot (\log_2 2 + \log_2 n) + 1 = 5 \cdot (+5\log_2 n)$

$$T(2n) = Tn+J$$

$$T_n = 5(ng_n+1)$$

- 6. (10 points) Suppose function call parameter passing costs constant time, independent of the size of the structure being passed.
 - (a) Give a recurrence for worst case running time of the recursive Binary Search function in terms of n, the size of the search array. Assume n is a power of 2. Solve the recurrence.

Recurrence:	T(->)+C
Base case:	T(2)=C
Recurrence Solution:	c logn

(b) Give a recurrence for worst case running time of the recursive Merge Sort function in terms of n, the size of the array being sorted. Solve the recurrence.

$$T(2n)=2T(n)+2n$$

$$=2n\log_2 n+2n$$

$$=2n(\log_2 2n-1)+2n$$

$$=2n\log_2 2n$$
which is consistent with 6
the expectation.

Recurrence:	27(2)+1
Base case:	T(c)=C
Running Time:	$nlog_2n$

7. (10 points) Consider the pseudocode function below.

derp(x, n)
 if (n == 0)
 return 1;
 if (n % 2 == 0)
 return derp(x^2, n/2);
 return x * derp(x^2, (n-1)/2);

(a) What is the output when passed the following parameters: $x=2,\,n=12$? Show your work (activation diagram or similar).

Answer for (a): 4096

(b) Briefly describe what this function is doing.

it calculates x

(c) Write a recurrence that models the running time of this function. Assume checks, returns, and arithmetic are constant time, but be sure to evaluate all function calls. *Hint:* what is the most n could be at each level of the recurrence?

T(n) = T (2)+(

(d) Solve the above recurrence for the running time of this function.

Tr= 10g 2n+d