

Steps to Find Time Complexity:

1. Identify the input size (n).
 2. Count the number of basic operations (like comparisons, assignments, loops).
 3. Focus on the dominant term (ignore constants and lower-order terms).
 4. Express in Big O notation.
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☒ Basic Examples to Understand

□ Example 1: Simple Loop

```
for(int i = 0; i < n; i++) {  
    cout << i;  
}
```

- **Operation Count:** Runs n times.
 - **Time Complexity:** $O(n)$
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□ Example 2: Nested Loop

```
for(int i = 0; i < n; i++) {  
    for(int j = 0; j < n; j++) {  
        cout << i << j;  
    }  
}
```

- Outer loop runs n times.
 - Inner loop runs n times **for each iteration** of outer loop.
 - **Total operations:** $n \times n = n^2$
 - **Time Complexity:** $O(n^2)$
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□ Example 3: Loop with Divide by 2

```
for(int i = n; i > 0; i /= 2) {  
    cout << i;  
}
```

- Each time, i is divided by 2.
- Number of iterations $\approx \log_2(n)$
- **Time Complexity:** $O(\log n)$

□ Example 4: Combination

```
for(int i = 0; i < n; i++) {           // O(n)
    for(int j = 0; j < n; j++) {       // O(n)
        cout << i << j;
    }
}
for(int k = 0; k < n; k++) {           // O(n)
    cout << k;
}
```

- First part: $O(n^2)$
 - Second part: $O(n)$
 - **Total Time Complexity:** $O(n^2 + n) \rightarrow O(n^2)$ (since n^2 is dominant)
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□ Important Rules:

Code Pattern	Time Complexity
Sequential (one after another)	Add them $\rightarrow O(n) + O(n^2) = O(n^2)$
Nested loops	Multiply them $\rightarrow O(n) \times O(n) = O(n^2)$
Divide input each time	$O(\log n)$
Binary Search	$O(\log n)$
Loop through array once	$O(n)$

□ Tips:

- Ignore constants: $O(2n) \rightarrow O(n)$
- Focus on worst-case time.
- Know common complexities:
 $O(1) < O(\log n) < O(n) < O(n \log n) < O(n^2) < O(2^n) < O(n!)$