2-Dimensional Finite Difference Hartree-Fock Program

with Libxc, OpenMP and p-thread support

User's Guide

 \bigodot 1996-2023 Jacek Kobus August 2023

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1 Description of input data

x2dhf program accepts input data that consist of separate lines that contain

- a label
- a label followed by a string of characters, integer(s) and/or real number(s)
- a string of characters, integer(s) and/or real number(s)

Real numbers can be written in a fixed-point or scientific notation. Note that

- labels and strings can be in upper or lower case,
- the compulsory labels must follow the order given below; the optional ones can be inserted anywhere between the **title** and **stop** labels,
- optional parameters are enclosed in square brackets,
- -r denotes a real number, i an integer, c a string of characters,
- an exclamation mark or a hash placed anywhere in an input line starts a comment and what follows "!" or "#" is ignored.

1.1 Mandatory labels

The following labels must be specified in the specified order:

TITLE

Format: title c

c is any string of up to 74 characters describing the current case. This string is added as a header to a text file with a .dat extension that contains basic data identifying a given case, i.e. atomic numbers of nuclei, grid size and the number of electrons and orbital and exchange functions.

NUCLEI

Format: nuclei Z_A Z_B R [c]

Set the nuclei charges and the bond length.

 Z_A : nuclear charge of centre A (real)

 Z_B : nuclear charge of centre B (real)

R: bond length (real)

c: angstrom – the internuclear separation can be given in Ångström if this string is included (the conversion factor 0.529177249 is used)

If $|Z_A - Z_B| < 10^{-6}$ then the molecule is considered to be a homonuclear one (see initVariables).

CONFIG

Format: config i

i: the total charge of a system

The following cards define molecular orbitals and their occupation in inverse order - the highest orbitals are on top and the lowest on bottom. Note that the last orbital description card (corresponding to the deepest lying orbital) must contain the *end* label.

The possible formats are:

Format: i c

- i: number of fully occupied orbitals of a given irreducible representation (irrep) of the $C_{\infty v}$ group; two electrons make σ orbitals fully occupied and four electrons orbitals of other symmetries
- c: symbol of the $C_{\infty v}$ irrep to which the orbitals belong (sigma, pi, delta or phi)

Format: i c_1 c_2

- i: number of fully occupied orbitals of a given irrep of the $D_{\infty h}$ group
- c_1 : symbol of the $C_{\infty v}$ irrep to which the orbitals belong (sigma, pi, delta or phi)
- c_2 : symbol for the inversion symmetry of the $D_{\infty h}$ irreps (u or g)

Use this format for a homonuclear molecule unless break card is included.

Format: $i \ c_1 \ c_2 \ [c_3 \ [c_4 \ [c_5]]]$

- i: number of orbitals of a given irrep of the $C_{\infty v}$ group
- c_1 : symbol for the $C_{\infty v}$ irreps to which the orbitals belong (sigma, pi, delta, phi)
- $c_2\hbox{-} c_5\colon +,\, -$ or . (a dot); +/- denotes spin up/down electron and . denotes an unoccupied spin-orbital

Format: $i \ c_1 \ c_2 \ c_3 \ [c_4 \ [c_5 \ [c_6]]]$

- i: number of orbitals of a given irrep of the $D_{\infty h}$ group
- c_1 : symbol for the $C_{\infty v}$ irrep to which the orbitals belong (sigma, pi, delta, phi)
- c_2 : symbol for the inversion symmetry of the $D_{\infty h}$ irrep (u or g)
- c_3 - c_6 : +, or . (a dot); +/- denotes spin up/down electron and . denotes an unoccupied spin-orbital

GRID

Format: grid N_{ν} R_{∞}

An integer and a real define a single two-dimensional grid.

 N_{ν} : the number of grid points in ν variable

 R_{∞} : the practical infinity

 N_{μ} is calculated so as to make the step size in μ variable equal to the step size in ν variable. N_{ν} and N_{μ} have to meet special conditions due to the order of discretization used and the multi-threaded version of the MCSOR routine. If the conditions are not fulfilled the nearest (but smaller) appropriate values are used.

Format: grid $N_{\nu} N_{\mu} R_{\infty}$

Two integers and one real define a single two-dimensional grid.

 N_{ν} : the number of grid points in ν variable

 N_{μ} : the number of grid points in μ variable

 R_{∞} : the practical infinity

This format may be needed when interpolation between grids is attempted.

ORBPOT

Format: orbpot c[i]

where c a character string determining the initial source of orbitals and potentials. The following values of c are allowed:

- gauss GAUSSIAN output is used to retrieve the basis set and the molecular orbital expansion coefficients. The GAUSSIAN output is assumed to be contained in gaussian.out and gaussian.pun files. Coulomb and exchange potentials are initialized as in the hydrogen case; see prepGauss for more details. To generate the necessary output from GAUSSIAN, you need to specify punch=mo gfinput in the route section of the GAUSSIAN input file. When you've run GAUSSIAN, you should end up with a file fort.7 that contains the molecular orbitals. To run x2dhf, put the log file in the working directory as gaussian.out and the molecular orbitals from fort.7 as gaussian.pun, which will be parsed by the program.
- hf radial Hartree—Fock orbitals for the centre A and B obtained from the qrhf program are retrieved from disk (see \$X2DHF_DIRECTORY/hf_orbitals directory) and Coulomb and exchange potentials are initialized unless the OED method is chosen (see routine initHF for details). Note that the mixing coefficients are by default set to 1; use lcao4lda label to change the values. Note also that the environment variable X2DHF_DIRECTORY must be set as the root of the x2dhf installation. If you don't set X2DHF_DIRECTORY, the program will try to read the orbitals from the current working directory.
- hydrogen molecular orbitals are formed as a linear combination of hydrogenic functions on centres A and B as defined via the **lcao** label. In the case of HF or HFS calculations Coulomb (exchange) potentials are approximated as a linear combination of Thomas-Fermi (1/r) potentials at the two centres. If the OED method is chosen the potential function is approximated as a linear combination of Z_A/r_1 and Z_B/r_2 terms and the exchange potentials are set to zero.
- lda radial LDA orbitals for the centre A and B obtained from the Helfem program² are retrieved from disk (see \$X2DHF_DIRECTORY/lda_orbitals directory) and Coulomb and exchange potentials are initialized unless the OED method is chosen (see routine initLDA for details). Note that the mixing coefficients are by default set to 1; use lcao4lda label to change the values. Note also that the environment variable X2DHF_DIRECTORY must be set as the root of the x2dhf installation. If you don't set X2DHF_DIRECTORY, the program will try to read the orbitals from the current working directory.
- noexch orbitals and Coulomb potentials are retrieved from disk files and exchange potentials are initialized as in hydrogen case; this is useful when going from DFT/HFS to HF calculations.
- nodat initial orbitals and potentials are retrieved from disk files but the content of a 2dhf_input.dat file is retrieved from a 2dhf_input.orb (binary) file. Use this value when reading binary data generated by the earlier than 2.0 versions of the program.
- old initial orbitals, Coulomb, and exchange potentials are retrieved from disk files (2dhf_input.orb, 2dhf_input.coul and 2dhf_input.exch, respectively) created in a previous run. Data defining the case are retrieved from a 2dhf_input.dat textfile.
- qrhf radial Hartree–Fock orbitals for the centre A and B obtained from the qrhf program³ are retrieved from disk files 1dhf_centreA.orb and 1dhf_centreB.orb, respectively, and Coulomb and exchange potentials are initialized as in the *hydrogen* case (see routine initHF for details).

i is an optional parameter that is used only for cases other than old. To perform SCF iterations stabely when both orbitals and potentials are being relaxed the potentials should correspond to the orbitals being relaxed. However, this is not the case at the very beginning of the SCF process. Therefore, at the onset of the SCF iterations with the

¹The program has been tested on output files produced by the 94, 03, 09 and 16 versions of the GAUSSIAN system of programs.

²S.Lehtola, Fully numerical Hartree-Fock and density functional calculations. I. Atoms, Int. J. Quantum Chem. doi:10.1002/qua.25945

³J. Kobus and Ch. Froese Fischer, Quasi-Relativistic Hartree-Fock program for Atoms, to be published.

fairly good initial orbitals, the orbitals can be kept fixed and only Coulomb and exchange potentials should undergo relaxation. These initial relaxations of the potentials are performed until the maximum error in the orbital energy is lower than 10^{-i} for nscfextra iterations (by default nscfextra=3 and i=1; see initVariables). If i=0 (the default value) then both the orbitals and potentials are relaxed at every SCF iteration.

STOP

Format: stop

This label indicates the end of input data.

1.2 Optional labels

The following additional labels can be specified in any order:

ALTSWEEP[S]

Format: altsweep or altsweeps

In the case of near-degenerate orbitals, i.e. when performing calculations for homonuclear molecules without inforced symmetry (no "HOMO" label), especially when the external electric field is applied, one can improve convergence by changing the direction of the SOR sweeps, i.e. using forward/backward sweeps for even/odd SCF iterations.

BREAK

Format: break

When this label is present homonuclear molecules are calculated in $C_{\infty v}$ symmetry and the $D_{\infty h}$ symmetry labels (u or g) are redundant.

CONV

```
Format: conv [i_1 [i_2 [i_3]]]
```

Sometimes the requested accuracy of a solution is set too high and cannot be satisfied on a selected grid. As a result SCF/SOR iteration process may continue in vain. To save CPU time the iterations are stopped if orbital energies or orbital norms display no improvement over the i_2 and i_3 most recent iterations, respectively (20 by default). This mechanism is activated after i_1 initial iterations (600 by default).

DEBUG

```
Format: debug [i_1 [i_2...] i_{40}]
```

Up to 40 different debug flags can be set at a time. If the integer i_k is present the debug flag i_k is set, i.e. $idbg(i_k) = 1$ ($1 \le i_k < 999$). These are used to generate additional debugging information by adding the lines of the form

```
if (idbg(ik).eq.1) then
    print *, ''debugging something ...''
    ...
endif
```

DFT

```
Format: dft [c_1] [c_2]
```

 c_i : specifies the type of DFT exchange-correlation functional(s) to be used in Fock equations. Any of the suitable LDA, GGA, and hybrid functionals implemented in Libxc

library⁴ can in principle be used, e.g. xc_lda_x, xc_lda_c_wigner, xc_lda_c_xalpha, xc_gga_c_gam, etc; use lxcctl list utility to generate the list of available functionals (the utility can also be used to test the functionals, see lxcctl help).

For backward compatibility the following functionals can also be selected:

-lda – the local density approximation with the potential

$$V_X(\alpha) = -\frac{3}{2}\alpha \left(\frac{3}{\pi}\right)^{1/3} 2^{-2/3} \sum_{\sigma} \rho_{\sigma}^{1/3}$$

where α is by default set to 2/3 (the Slater exchange potential). To change this value use the **xalpha** label. This functional is equivalent to lda_x one of the Libxc library.

If xalpha parameter is set to 1/3 then lda functional is equivalent to $xc_lda_c_xalpha$ one.

- $-\ b88$ the Becke exchange potential; this functional is equivalent to $xc_gga_x_b88$ one from the Libxc library 5
- lyp the correlation potential of Lee, Yang and Parr; this functional is equivalent to $xc_gga_c_lyp$ one from the Libxc library
- -vwn the correlation potential of Vosko, Wilk and Nusair; this functional is equivalent to lda_c_vwn one from the Libxc library⁶

When the bare label is present and the method selected is HF then the exchange contributions (LDA, B88) and the correlation contributions (LYP and VWN) to the total energy are calculated upon completion of the SCF iterations.

DENSTHLD

Format: densthld [r]

r: sets the value of dens_threshold parameter used in the Libxc library to avoid returning NaN values (the default value is defined in initVariables subroutine.

FASTSCF

Format: fastscf

This label causes the SCF process to automatically skip relaxing orbitals (and also Coulomb and exchange potentials) for which the orbital energy threshold has been reached. This is a very desirable behaviour when (and the default one) when the OED method is used to calculate a set of virtual orbitals.

FEFIELD

Format: fefield r

r: a strength of an external static electric field directed along the internuclear axis (in atomic units)

FERMI

Format: fermi $[r_A [r_B]]$

When this label is present the Fermi nuclear charge distribution is used. Optional parameters r_A and r_B define the atomic masses (in atomic mass units, amu) of nuclei A and B. If omitted the corresponding values are taken from the table of atomic masses compiled by Wapstra and Audi (see blk_data).

 $^{^4}$ Susi Lehtola, Conrad Steigemann, Micael J.T. Oliveira, and Miguel A.L. Marques, Recent developments in Libxc - A comprehensive library of functionals for density functional theory, Software X 7, 1 (2018)

⁵Cf. the results of test sets he/set-09, he/set-10 and he/set-11.

 $^{^6}$ In case the Hartree-Fock orbitals of the FH molecule are used to calculate the correlation contribution the functional vwn gives -0.699579 while $xc_lda_c_vwn$ gives a slightly smaller value, namely, -0.704211.

FIXORB

Format: fixorb [i_1 [i_2 ...] i_{40}]

This label is used to specify orbitals to be kept frozen during SCF/SOR process (they are not being renormalized nor orthogonalized during the process). i_1, i_2, \ldots are the numbers of these orbitals as they appear on the program's listing, i.e. their order is reversed to that used when defining the electronic configuration (see the **config** card). Up to 40 different orbitals can be set at a time. Use the bare label to keep all orbitals frozen.

FIXPOT

Format: fixpot

If this label is present then all Coulomb and exchange potentials are kept frozen during the SCF/SOR process.

GAUSS

Format: gauss $[r_A \ [r_B]]$

When this label is present the Gauss nuclear charge distribution is used. Optional parameters r_A and r_B define the atomic masses (in amu) of nuclei A and B. If omitted, the corresponding values are taken from the table of atomic masses compiled by Wapstra and Audi (see blk_data).

HOMO

Format: homo

This label is used to impose explicitly $D_{\infty h}$ symmetry upon orbitals of homonuclear molecules to improve SCF/SOR convergence.

INOUT

Format: inout c_1 c_2

The x2dhf program can be compiled to support calculation using three different combinations of integer/real data types: i32 (4-byte integers, 8-byte reals), i64 (8-byte integers, 8-byte reals) and r128 (8-byte integers, 16-byte reals). Strings c_1 and c_2 determine the combination appropriate for the format of input and output data, respectively, and each string can be i32, i64 or r128.

To facilitate the exchange of binary data generated on machines of different architectures or using different compilers additional formats are available, namely i32f, i64f or r128f. They can be used to export/import data in the formatted instead of the (default) unformatted form.

INTERP

Format: interp [$\operatorname{iord}_{\nu}^{\operatorname{orb}} \operatorname{iord}_{\mu}^{\operatorname{orb}} \operatorname{iord}_{\nu}^{\operatorname{coul}} \operatorname{iord}_{\mu}^{\operatorname{coul}} \operatorname{iord}_{\nu}^{\operatorname{exch}} \operatorname{iord}_{\mu}^{\operatorname{exch}}$]

Use this label to change the grid between separate runs of the program. The interpolation order in the ν and μ directions used for the orbitals, Coulomb potential and exchange potentials can be set with the six optional parameters. Supported orders for the interpolation are 2, 4 (default), 6, and 8.

KINPOT

Format: kinpot

Upon the completion of the SCF process the Pauli, $v^P(\mathbf{r})$, and von Weizsäcker kinetic potentials, $v^W(\mathbf{r})$, are calculated along the internuclear axis and written to out4kinpot.dat file together with the total density, $\rho(\mathbf{r})$, $\nabla^2 \rho(\mathbf{r})$, $\tau(\mathbf{r})$ (the kinetic energy density) and $\tau^W(\mathbf{r}) = |\nabla \rho(\mathbf{r})|^2/(8\rho(\mathbf{r}))$,

LCAO

Format: lcao [i]

If the source of orbitals is declared as *hydrogen* then this card must be present. In such a case the initialization of each of the orbitals has to be defined in terms of the linear combination of atom centred hydrogen-like functions. For each orbital include a card of the following format (make sure that the order of orbitals should match the order specified under the **config** label):

Format: c_A n_A l_A ζ_A c_B n_B l_B ζ_B $[i_1$ $[i_2]]$ where

 c_A – relative mixing coefficient for a hydrogenic orbital on the Z_A centre (real),

 n_A – its principal quantum number (integer)

 l_A – its orbital quantum number (integer)

 ζ_A – the effective nuclear charge if i=1 (default) or a screening parameter if i=2 (real)

 c_B – relative mixing coefficient for a hydrogenic orbital on the Z_B centre (real),

 n_B – its principal quantum number (integer)

 l_B – its orbital quantum number (integer)

 ζ_B – the effective nuclear charge if i=1 (default) or a screening parameter if i=2 (real)

 i_1 — (integer) if set to 1 (the default) indicates that this orbital should be initialized as a linear combination of hydrogenic functions and not taken from a disk orbital file (integer). When the source of orbitals is declared as old and the orbital and Coulomb potential data files contain fewer functions than defined by config card this flag can be used to indicate which orbitals are missing in orbital data files and require initialization. This can be useful when generating virtual orbitals for a potential formed from the already given set of converged orbitals. Indicate such orbitals by setting this parameter to 0.

 i_2 – (integer) if set to 0 (1, the default) indicates that this orbital will not contribute (will contribute) to the electron density when evaluating DFT functionals. It allows therefore to generate virtual orbitals within the DFT calculations since a local potential can be built from a given subset of orbitals that are kept frozen during the SCF process (see **fixorb** label).

The mixing coefficients are normalized so that $|c_A| + |c_B| = 1$

LCAO4LDA

Format: $lcao4lda [c_A [c_B]]$

If the source of orbitals is declared as lda then use this card to adjust the mixing coefficients (by default $c_A = c_B = 1.0$); see label **LCAO**.

LM

Format:
$$\text{Im } i_1 \ i_2 \ [\ i_3 \ i_4\] \ \dots [\ i_{N-1} \ i_N\]$$

For closed-shell systems, the off-diagonal Lagrange multipliers are set to zero. However, for some such systems the SCF/SOR convergence can be improved if for some pair(s) of orbitals the non-zero values of the Lagrange multipliers are used (see, for example, the o2, li2-elprop or f2-elprop test suits).

MCSOR|MCSOR-O

Format: mcsor-mcsor-o $[i_1 [i_2 [i_3]]$

Selects the MCSOR method for solving the Poisson equations for orbitals and the SOR method – for Coulomb and exchange potentials. i_1 parameter can be used to set the number of threads employed. The default value depends on the parallelization method

used; see initVariables. Use i_2 and i_3 to set the value of the MCSOR micro relaxation sweeps during a single SCF cycle for orbitals and potentials, respectively (by default 2 = i3 = 10).

When the MCSOR method is selected via this label then the single-threaded version of the multi-colour SOR method is chosen by default to relax orbitals. When OPENMP/PTHREAD/TPOOL directive is present the parallelized version of MCSOR is employed. Coulomb and exchange potentials are relaxed in parallel using the single-threaded SOR method. However, when the MCSOR-CE label together with OPENMP directive is used, also the potentials are relaxed using the parallelized version of the MCSOR routine (in the case of PTHREAD/TPOOL directive is used the SOR method must be used to avoid nested parallel regions).

Labels MCSOR-O and MCSOR-CE were added to force the usage of the MCSOR selectively for orbitals and Coulomb/exchange potentials, respectively. See relaxDriver for more details.

b

MCSOR-CE

Format: mcsor-ce[i]

When OPENMP directive is used this label selects the MCSOR method for solving the Poisson equations for Coulomb and exchange potentials and, if i > 0, sets the number of threads used. In case of PTHREAD/TPOOL directive the SOR method is used (see coulExchSORPT).

METHOD

Format: method c

Select the type of calculation.

- c: HF the Hartree-Fock method
- c: DFT the Hartree-Fock method with the $X\alpha$ exchange potential ($\alpha = 2/3$); see the **dft** label to choose another exchange or correlation potential
- c: HFS the Hartree-Fock-Slater method (Hartree-Fock with the $X\alpha$ exchange potential) with the optimum value of the α parameter (see src/commons.F90)
- c: OED One Electron Diatomic ground and excited states can be calculated for the Coulomb potential in the prolate spheroidal coordinates (default). It is also possible to specify the Coulomb and Kramers-Henneberger potentials in cylindrical coordinates (see the **poth3**, **potkh**, **potharm2**, **potharm3** labels, respectively). When more than one orbital is specified calculations are carried out as if in the case of a multielectron system.⁸
- c: TED Two Electron Diatomic ground and excited states can be calculated for Hooke's atom (harmonium). See **POTHOOKE** label.
- c: SCMC the Hartree–Fock method with $X\alpha$ exchange where the α parameter is calculated according to the self-consistent multiplicative constant method⁹

MMOMENTS

Format: mmoments

Calculate the multipole moments for the converged orbitals relative to the geometric centre and the centre of mass. The total charge densities at (0,0,-R/2) and (0,0,+R/2) are also evaluated.

 $^{^7}$ The TPOOL directive should be used together with the MUTEX one (see x2dhfctl -t -X.

⁸In this type of calculations convergence rates differ greatly between orbitals. Therefore, if for a given orbital the orbital energy threshold is reached it is being frozen.

⁹V. V. Karasiev and E. V. Ludeña, Self-consistent multiplicative constant method for the exchange energy in density functional theory, Phys. Rev. A **65** (2002) 062510. doi:10.1103/PhysRevA.65.062510

MULTIPOL

Format: multipol r [i]

- r: if r > 0 multipole moment expansion coefficients are recalculated when the maximum error in orbital energy is changed by r (the default value is 1.15; see <code>initVariables</code>). To suppress recalculation of the coefficients set r to a negative real number. This is useful when generating potentials from a set of fixed orbitals, e.g. from GAUSSIAN orbitals.
- i: the number of terms in the multipole expansion used to calculate the boundary values for potentials $(2 \le i \le 8 \text{ and the default is } 4)$.

OMEGA

Format: omega ω_{orb} [ω_{pot}]

One or two real numbers setting over-relaxation parameters for relaxation of orbitals and potentials; see also **OMEGAOPT**. The negative value of $\omega_{orb}/\omega_{pot}$ indicates that its value should be set to a near optimum value obtained from a semiempirical formula (see initCBlocks and setOmega for details).

OMEGAOPT

Format: omegaopt [i [r_{orb} [r_{pot}]]]

The optional integer parameter can be set to 1 (default) or 2. In the former case the over-relaxation parameters are based on tests performed for the FH molecule on 157x229/45 grid and scaled down a bit (by 0.979 and 996 for orbitals and potentials, respectively). In the latter, the values are calculated from a formula for the optimal value of the over-relaxation parameter in case the model Poisson equation is discretized using the second-order stencil.

This label should only be used for test purposes.

where c a character string determining the initial source of orbitals

ORDER

Format: order c

where c is a character string defining the ordering of mesh points: "col-wise" – natural column-wise, "middle" – 'middle' type of sweep (default), "row-wise" – natural row-wise, "rcol-wise" – reversed natural column-wise (see mesh routine for details)

PLOT

Format: plot $[i_1 [i_2]]$

Orbital values are written in formatted form to be plotted. For i_1 equal to 1, 2 or 3 values $(z_j, x_k, f(z_j, x_k))$, $(\nu_j, \mu_k, f(\nu_j, \mu_k))$ or $(\eta_j, \xi_k, f(\eta_j, \xi_k))$ are written, respectively, and every i_2^{th} value in each variable is selected, i.e. $j = 1, N_{\nu}, i_2$ and $k = 1, N_{\mu}, i_2$. By default $i_1 = 1$ and $i_2 = 2$. The values in the tail region are omitted if they are smaller that a given threshold (by default 10^{-10} ; see plotThreshold variable in initVariables routine).

POTGSZ

Format: potgsz

When the OED method is chosen then this label selects a model potential due to Green, Sellin and Zachor. The For a given atom this potential produces HF-like orbitals and it has been found useful in finding decent starting orbitals for diatomic molecules as well. Note, however, that the superposition of atomic potentials (SAP) guess (keyword: potsap) is much more accurate, as it is not restricted to a simple analytic form.

POTGSZG

Format: potgszg

When the OED method is chosen then this label selects a model potential due to Green, Sellin and Zachor and the Gauss nuclear charge distribution. For a given atom this potential produces HF-like orbitals but it has been found useful in finding decent starting orbitals for any molecular system.

POTHOOKE

¹⁰A. E. S. Green, D. L. Sellin, and A. S. Zachor, Analytic Independent-Particle Model for Atoms, Phys. Rev. 184 (1969) 1-9. doi:10.1103/PhysRev.184.1

 $^{^{11}}$ J. E. Whalen and A. E. S. Green, Analytic Independent Particle Model for Molecules, Am. J. Phys. 40, (1972) 1484. doi:10.1119/1.1986874; K. J. Miller and A. E. S. Green, Energy levels and potential energy curves for H2, N2, and O2 with an independent particle model, J. Chem. Phys. 60, (1974) 2617. doi:10.1063/1.1681415; T. Sawada, P. S. Ganas, and A. E. S. Green, Elastic scattering of electrons from N_2 , Phys. Rev. A 9, (1974) 1130. doi:10.1103/PhysRevA.9.1130

¹²S. Lehtola, Assessment of Initial Guesses for Self-Consistent Field Calculations. Superposition of Atomic Potentials: Simple yet Efficient, J. Chem. Theory Comput. 15, (2019) 1593-1604. doi:10.1021/acs.jctc.8b01089

Format: pothooke k

When the HF method is chosen this label selects the potential of the Hooke atom: $-\frac{1}{2}k^2(r_1^2+r_2^2)$ (k=1/2 by default), where r_1 and r_2 denote the distances of the two electrons from the center A and thus the nuclear charges should be set accordingly, e.g. $Z_1=2$ and $Z_2=0$.

POTHARM2

Format: potharm2 k

When the OED method is chosen then this label selects a two-dimensional model potential of the form $-k^2(x^2+y^2)$, where k is a strength of the potential (real).

POTHARM3|EXTRACUL[E]

Format: potharm3|extracule[e][k]

When the OED method is chosen then this label selects a three-dimensional model potential of the form $-k^2(x^2+y^2+z^2)$, where k is a strength of the potential (real, k=1/2 by default).

POTCOUL2

Format: potcoul2 $m \ a \ V_0$

When the OED method is chosen then this label selects a two-dimensional model potential of the form $-V_0/\sqrt{a^2+x^2+y^2}$. The following parameters can be set

m: magnetic quantum number of a state (integer)

a: width of the model potential (real)

 V_0 : depth of the model potential (real)

POTCOUL3

Format: potcoul3 m a V_0

When the OED method is chosen then this label selects a two-dimensional model potential of the form $-V_0/\sqrt{a^2+x^2+y^2+z^2}$. The following parameters can be set

m: magnetic quantum number of a state (integer)

a: width of the model potential (real)

 V_0 : depth of the model potential (real)

To get the hydrogen Coulomb potential set a = 0.0 and $V_0 = 1.0$. Set a > 0 and V > 0 to choose its smoothed variant.

POTKH

Format: potkh $m \in \omega [a[V_0[N]]]$

When the OED method is chosen, then this label selects the Kramers-Henneberger potential. The following parameters can be set

m: magnetic quantum number of a state being calculated (integer)

 ε : laser intensity (real)

 ω : laser cycle frequency (real)

a: original (before averaging over one laser cycle) soft-core potential width (a positive real number, by default a=1.0)

 V_0 : original soft-core potential depth (by default $V_0 = 1.0$)

N: number of intervals in the Simpson quadrature (an integer, N = 1000 by default)

POTSAP

Format: potsap

When the OED method is chosen, this label selects a pretabulated, screened atomic exchange potential that has been found to reproduce results in molecular calculations.¹³ The potentials of the present implementation¹⁴ are from highly accurate finite element calculations carried out with the Helfem program.

PRINT

```
Format: print [i_1 [i_2...] i_{40}]
```

Up to 40 different printing flags can be set at a time. If the integer i_k is encountered the printing flag i_k is set, i.e. $\operatorname{iprint}(i_k) = 1$ ($1 \le i_k < 999$). These are used to generate additional printouts by adding the lines of the form

```
if (iprint(ik).eq.1) then
    print *, ''printing something ...''
    ...
endif
```

Set

- $i_1=110$ to print a total radial density relative to the centre A along the internuclear axis $(-R_\infty \le z \le -R/2)$
- $i_2=111$ to print a total radial density relative to the centre B along the internuclear axis $(R/2 \le z \le R_{\infty})$

See inputData for a list of available flags.

PRTEVERY

Format: prtevery i_1 i_2

Routine pmtx can be used to output two-dimensional arrays in a tabular row-wise form with every i_1 -th row and i_2 -th column being printed (by default every 10th row and column is selected)

SCF

```
Format: scf [i_1 [i_2 [i_3 [i_4 [i_5]]]]]
```

- i_1 : maximum number of SCF iterations (default 1000); to skip the SCF step set i_1 to a negative integer,
- i_2 : every i_2 SCF iterations orbitals and potentials are saved to disk (default 20). If $i_2 = 0$ functions are saved on disk upon completion of the SCF process. If $i_2 < 0$ functions are never written to disk,
- i_3 : if the maximum error in orbital energy is less than 10^{-i_3} for *nscfextra* iterations (3 by default; see initVariables), than the SCF process is terminated ($i_3 = 10$ by default),
- i_4 : if the maximum error in orbital norm is less than 10^{-i_4} for nscfextra iterations (3 by default; see initVariables), than SCF process is terminated ($i_4 = 10$ by default),
- i_5 : the verbosity of the output during SCF process
 - $-i_5 = 1$ the orbital energy, the difference between its current and previous value, the normalization error, and the (absolute) value of the largest overlap integral between the current orbital and all the lower-lying ones of the same symmetry (the value is zero for the lowest orbitals of each symmetry) is printed for every orbital in every SCF iteration

¹³S. Lehtola, Assessment of Initial Guesses for Self-Consistent Field Calculations. Superposition of Atomic Potentials: Simple yet Efficient, J. Chem. Theory Comput. 15, (2019) 1593-1604. doi:10.1021/acs.jctc.8b01089
¹⁴S. Lehtola, to be published.

- $-i_5 = 2$ the orbital energy, the difference between its current and previous value and the normalization error is printed for the worst converged orbital in energy (first line) and norm (second line) in every SCF iteration (default)
- $-i_5 = 3$ the orbital energy, the difference between its current and previous values and the normalization error is printed for the worst converged orbital in energy (first line) and norm (second line) every i_2 iterations. Printing of "... multipole moment expansion coefficients (re)calculated ..." communique is suppressed

The total energy is printed every i_2 iteration.

SLOWEXCH

Format: slowexch

This label causes the SCF process to relax the exchange potential for a given pair of orbitals twice during an SCF cycle.

SOR

Format: sor $[i_1 [i_2]]$

Selects the SOR method for solving the Poisson equations for orbitals and potentials (default) and changes the value of the micro SOR relaxation sweeps during a single SCF cycle for orbitals (i_1) and potentials (i_2) ; by default, $i_1 = i_2 = 10$.

SOR4ORB

Format: sor4orb $[i_1 [i_2]]$

Selects the SOR method for solving the Poisson equations for orbitals and changes the value of the SOR micro ((i_1) and macro (i_2) relaxation sweeps during a single SCF cycle for orbitals; by default $i_1 = 10, i_2 = 1$.

SOR4POT

Format: sor4pot $[i_1 [i_2]]$

Selects the SOR method for solving the Poisson equations for potentials and changes the value of the SOR micro (i_1) and macro (i_2) relaxation sweeps during a single SCF cycle for potentials; by default $i_1 = 10, i_2 = 1$.

TAIL

Format: tail

This label causes the examination of the tail regions of the orbitals, i.e. the regions where the μ variable has its maximum value, to find how fast the orbitals decay. These values can help choose a safe value of R_{∞} .

XALPHA

Format: xalpha α

This label allows to change the α parameter of the LDA potential (see the HFS/DFT method); by default α is set to 2/3. To set this parameter to zero use a very small but nonzero value, e.g. 1.0e-15.

2 Program's data files

There are several standard names used by the program to keep track of its input and output disk files. Normally the program writes out the data in the course of computations and upon its completion into the following disk files:

- 2dhf_output.dat (a text (ASCII) file) containing the title of a case, the time and date of its commencement, the number of mesh points, the internuclear distance, the charges of nuclei and the number of orbitals, electrons, and exchange potentials (see writeDisk for details),
- 2dhf_output.orb (a binary file) containing molecular orbitals (in the order specified by the input data following config label) followed by their normalization factors, orbital energies, Lagrange multipliers, and multipole moment expansion coefficients (see write),
- 2dhf_output.coul (a binary file) containing corresponding Coulomb potentials and
- 2dhf_output.exch (a binary file) containing all exchange potentials if the exchio [in-one|in-many] out-one card is present

These files can be used to restart a given case or run another with slightly modified parameters. If **orbpot old** card is present orbitals are retrieved from 2dhf_input.orb file, Coulomb potentials from 2dhf_input.coul and exchange potentials from 2dhf_input.exch file.

3 Running the program

To simplify the usage of the program, the xhf script (see tests/xhf) is provided to facilitate handling of the disk files. The command xhf can be invoked with one, two or three parameters. There are two basic modes of its usage:

```
xhf file1 file2
```

runs x2dhf reading input data from file1.data file and writing text data describing the case into file2.dat file and binary data with orbitals and potentials into file2.orb, file2.coul and file2.exch files.

```
xhf file1 file2 file3
```

runs x2dhf reading input data from file1.data and initial orbitals and potentials from file2.dat, file2.orb, file2.coul and file2.exch files and writing resulting data into file3.dat, file3.orb, file3.coul and file3.exch files.

If, for example, we have the following two data files:

• be.data

```
TITLE Be R_{inf}=35.0 bohr R = 2.3860 bohr
METHOD hf
        4.0 0.0 2.386
NUCLEI
CONFIG
        0
        2 sigma
                end
grid 169 35.0
orbpot hydrogen
lcao
1.0
       2 0 4.0
                   0.0
                         1 0 9.0
      1 0 4.0
1.0
                   0.0
                         1 0 9.0
SCF 300 10 4 8 1
stop
```

• be-1.data

```
TITLE Be R_{inf}=35.0 bohr R = 2.3860 bohr
METHOD hf
NUCLEI
       4.0 0.0 2.386
CONFIG
       2 sigma end
grid 169 35.0
orbpot old
lcao
1.0
      2 0 4.0
                  0.0
                        1 0 9.0 0
      1 0 4.0
                  0.0
                         1 0 9.0 0
1.0
SCF 3000 10 8 10 1
stop
```

then

xhf be be-1

starts and performs the first 300 SCF iterations. And

```
xhf be-1 be-1 be-2
```

must be used to continue the calculations. To converge the SCF process even better increase the convergence parameters (see the **scf** label) and use the following command

```
xhf be-1 be-2 be-1
```

Use testctl list to see dozens of examples of the x2dhf usage; try textctl help|-h|--help to get more details.

xhf can be used to perform a number of additional tasks; see xhf help|-h|--help.