
Evolution of Neural Network Controllers for Gameplay Behaviours

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BSc (Hons) Games Development

School of Computing

November 2, 2017

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I, Ryan O'Flaherty, confirm that this dissertation and the work presented in it are my own achievement.

Where I have consulted the published work of others this is always clearly attributed;

Where I have quoted from the work of others the source is always given. With the exception of such quotations this dissertation is entirely my own work;

I have acknowledged all main sources of help;

If my research follows on from previous work or is part of a larger collaborative research project I have made clear exactly what was done by others and what I have contributed myself;

I have read and understand the penalties associated with Academic Misconduct.

I also confirm that I have obtained informed consent from all people I have involved in the work in this dissertation following the School's ethical guidelines.

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Abstract



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Acknowledgements

Insert acknowledgements here

I would like to thank my cat, dog and family.

1 Introduction

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1.1 Project Aims and Structure

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1.1.1 Overview Of Project Content and Milestones

This is a sub sub section with a list of bullet points.

- A working X, that will be used for this investigation.
- Investigation of current tools and their potential use during an investigation of X .
- Programming of X with related frameworks Y and Z.
- That is all.

2 Background

2.1 Introduction

The following section of this dissertation will go on to discuss the history of artificial intelligence within the context of video games, before going on to explain neural networks, evolutionary algorithms, and the NeuroEvolution of Augmenting Topologies (NEAT) library.

2.2 History of AI in Games

Video games have been a popular area of interest for artificial intelligence developers and researchers for many decades.

Over several tens of years, a large amount of research and development has been done in an attempt to perfect chess-playing artificial intelligence agents(Thrun, 1995), and work has more recently been put in to do the same with the game of Go.

In March of 2016, the goal of getting such an agent to compete and win at the highest level was reached, when AlphaGo, a program engineered by Google, managed to overcome the Go world champion human player, Lee Sedol(Kurenkov). This was then reported as a major breakthrough for the artificial intelligence field.

2.3 What is a Neural Network?

Artificial neural networks, commonly referred to simply as neural networks, are a rough representation of the human brain. Human brains can be thought of as highly complex and non-linear systems for processing information in parallel(Haykin, 1999).

To emulate this, neural networks are built using a series of layers of network nodes. These nodes are used to represent neurons in the brain. The first is an input layer, followed by two or three hidden layers before a final output layer of nodes(Wang, 2003). The connection between these nodes is representative of axons in the brain.

In an artificial neural network, the input and output layers take data in and produce results respectively, with the processing of said data being done within the hidden layers - but how does it work?

2.3.1 Perceptrons

One type of artificial neuron (or node) is known as a ‘perceptron.’ Each perceptron receives several inputs and uses them to produce one binary output(Nielsen, 2015).

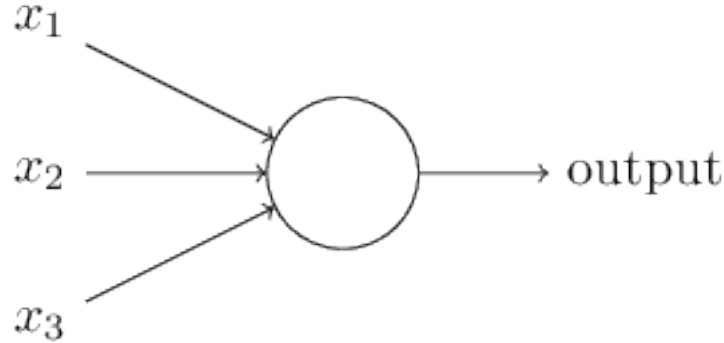


Figure 1: A Single Perceptron

Frank Rosenblatt, the scientist who developed the perceptron in the 1950s and 1960s, devised a rule for computing the output from these neurons. Using what he called 'weights,' the importance of each input is assessed and expressed. Each input has a weight assigned to it, and the resultant output from these inputs - either a 1 or 0 - is dependent on whether or not some threshold value is less than or greater than the sum of the weights from all of the inputs to that particular perceptron. Therefore, if the weighted sum is less than or equal to the threshold value, the output is a 0. Otherwise, a 1 (Nielsen, 2015). Both the threshold value and the input weights are real numbers. These can be tweaked to alter the decisions made by a neural network.

2.3.2 Sigmoid Neurons

Sigmoid neurons are akin to perceptrons, however, they are modified in such a way that marginal alterations in their weights and bias cause only a small change to their output (Nielsen, 2015). This crucial difference is what affords a network consisting of sigmoid neurons the ability to learn.

The inputs to a sigmoid neuron also differ from those of perceptrons. Rather than being binary (1 or 0), these inputs are any number *between* 1 and 0. Much like with perceptrons, these sigmoid neuron inputs are weighted, with an overall bias included. These can be denoted b, w_1, w_2, \dots, w_n where b represents the bias, and each w is an input weight. This time however, the output is non-binary. To calculate it, we use

$$\sigma(w \cdot x + b) \tag{1}$$

where σ is known as the sigmoid function, which is defined as:

$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}. \tag{2}$$

In its full extended form, with x being used to symbolise the inputs, the output of a sigmoid neuron is calculated as

$$\frac{1}{1 + \exp(-\sum_j w_j x_j - b)}. \quad (3)$$

////////////////////////////////////
 To understand the similarity to the perceptron model, suppose $z \equiv w \cdot x + b$ is a large positive number. Then $e^{-z} \approx 0$ and so $\sigma(z) \approx 1$. In other words, when $z = w \cdot x + b$ is large and positive, the output from the sigmoid neuron is approximately 1, just as it would have been for a perceptron. Suppose on the other hand that $z = w \cdot x + b$ is very negative. Then $e^{-z} \rightarrow \infty$, and $\sigma(z) \approx 0$. So when $z = w \cdot x + b$ is very negative, the behaviour of a sigmoid neuron also closely approximates a perceptron. It’s only when $w \cdot x + b$ is of modest size that there’s much deviation from the perceptron model(Nielsen, 2015).
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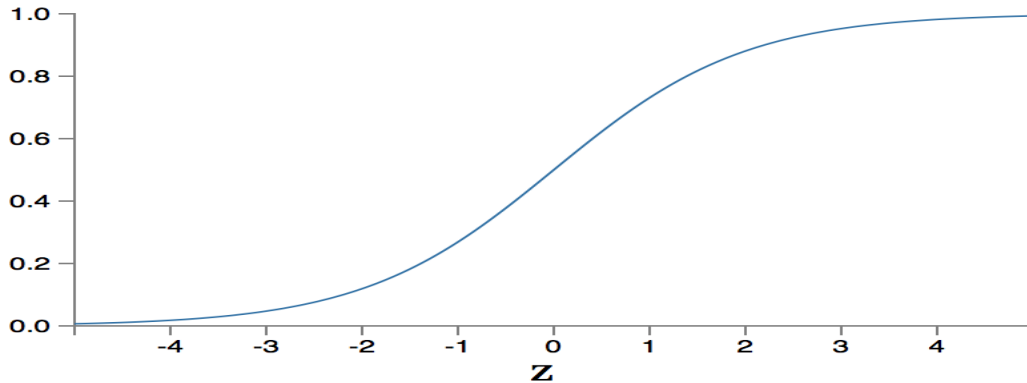


Figure 2: Sigmoid Function

The shape of a plotted σ function can be seen in Figure 2.

////////////////////////////////////
 The smooth nature of σ means that minor changes in the weights and bias - which are depicted as Δw_j and Δb_j respectively - will consequently create small changes to the output from the neuron. That change - Δoutput - can be approximated with calculus:

$$\Delta \text{output} \approx \sum_j \frac{\partial \text{output}}{\partial w_j} \Delta w_j + \frac{\partial \text{output}}{\partial b} \Delta b \quad (4)$$

The sum is over all of the weights, w_j , and $\partial \text{output} / \partial w_j$ and $\partial \text{output} / \partial b$ denote partial derivatives of the output with respect to w_j and b , respectively.

As Δoutput is a linear function of the changes Δw_j and Δb_j in the weights and bias, this linearity makes it easy to choose small changes in the weights and biases to achieve any desired small change in the output. So while sigmoid neurons have much of the same qualitative behaviour as perceptrons, they make it much easier to figure out how changing the weights and biases will change the output.

////////////////////////////////////

2.4 Evolutionary Algorithms

As the name might suggest, an evolutionary algorithm is one that evolves. It does so to encourage finding the most optimal solution to a problem. A vast amount of varying evolutionary algorithms exist, but at the core of them all is the same principal idea: “given a population of individuals the environmental pressure causes natural selection (survival of the fittest) and this causes a rise in the fitness of the population” (Eiben and Smith, 2015). As a result, the population adapts over time to its environment.

What is the process of evolution? The generational cycle works as follows:

2.4.1 Representation

Step one when defining an evolutionary algorithm is to bridge the gap between the “real world” and the “evolutionary algorithm world” (Eiben and Smith, 2015). That is, to link what are known as phenotypes, to representative genotypes.

- Phenotype:
 - A solution to a problem
- Genotype
 - Chromosome used to represent the solution to a problem

Representation refers to specifying which genotypes equate to each phenotype (Eiben and Smith, 2015). For example, if an integer is the solution to a problem, it is the phenotype, and a binary representation of that particular integer would be the genotype relating to that phenotype.

A genotype (or chromosome) is made up of genes. Values are assigned to each gene, and may be referred to as alleles. These can be of any type, or even a mixture. Types include binary strings, integers, real values, permutations and symbols. So in the example above, each gene would be either a 1 or 0, combining to form the integer as an overall chromosome.

Sometimes it may not be quite so straightforward, and genotypes need to be explicitly mapped to phenotypes, as seen in Figure 3.

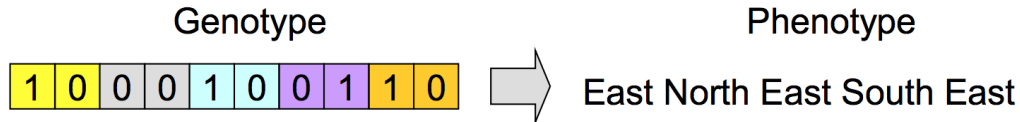


Figure 3: Genotype vs Phenotype

2.4.2 Initialisation

In the beginning, we start off with a population comprised completely of random chromosomes. This is likely to yield very poor results, however there is always a chance that some may be better. These individuals must then be evaluated.

2.4.3 Fitness

The fitness of an individual is what defines how fit for purpose it is. This measurement of quality will be defined differently for every algorithm, depending entirely on the context of problems it is being used to solve. In this project, the fitness will correlate to the amount of illegal moves the agent attempts to make, and how many times it is forced to increase its hand rather than decrease it. However, as the game of switch is largely down to luck, this will have to be taken into account to incorporate some form of leniency to fitness calculations.

The role of an evaluation function (or fitness function) to encourage improvements by defining what an improvement is (Eiben and Smith, 2015). This lays the foundation for selection.

2.4.4 Selection

The process of choosing individuals, based on their fitness, from the population to become parents to the next generation of individuals is called selection (Eiben and Smith, 2015). This is the driving force behind progressive evolution as it biases selection towards individuals of higher quality.

2.4.5 Crossover

Sometimes referred to as recombination, crossover is an operation that merges genes from two parent genotypes together into one or two offspring genotypes (Eiben and Smith, 2015).

Crossover can be defined in a few ways. There is one-point crossover, where a randomly chosen point along the length of a chromosome determines which genes are passed on from that particular genotype, and the rest will come from the other parent. This is demonstrated in Figure 4.

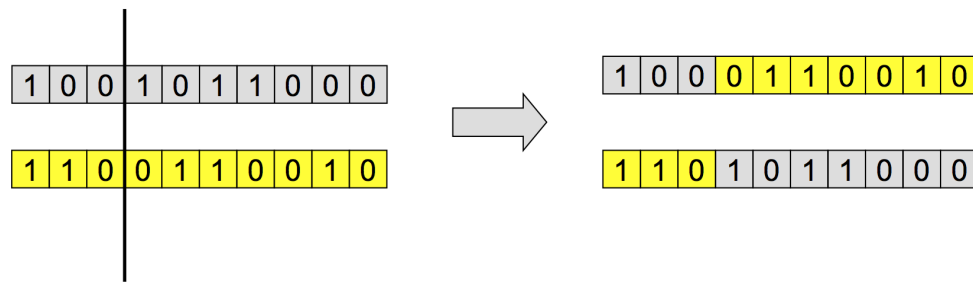


Figure 4: One-Point Crossover

Next, n-point crossover is when more than one (n) point is chosen, and chromosomes can be split up in different ways, as seen in Figure 5.

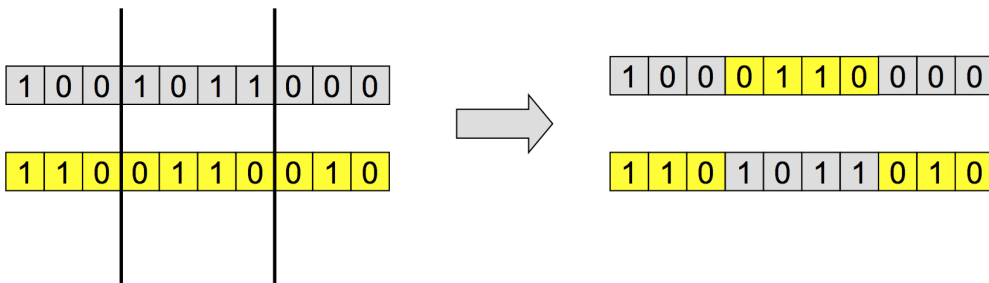


Figure 5: N-Point Crossover

Another type of crossover is called uniform. In this case, each gene of the offspring is randomly selected by deciding which of the two parents to inherit from. This is demonstrated in Figure 6.

In the case of arithmetic crossover, an average of the two parent genes is calculated and used for the child gene. This is useful if the genes consist of real numbers. Figure 7 depicts this.

All of the above techniques are used in binary and integer chromosome representations. Permutations cannot be recombined using any of these techniques, but are beyond the scope of this project.

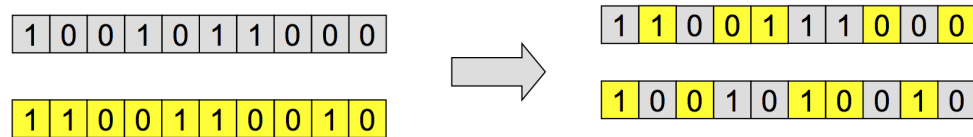


Figure 6: Uniform Crossover

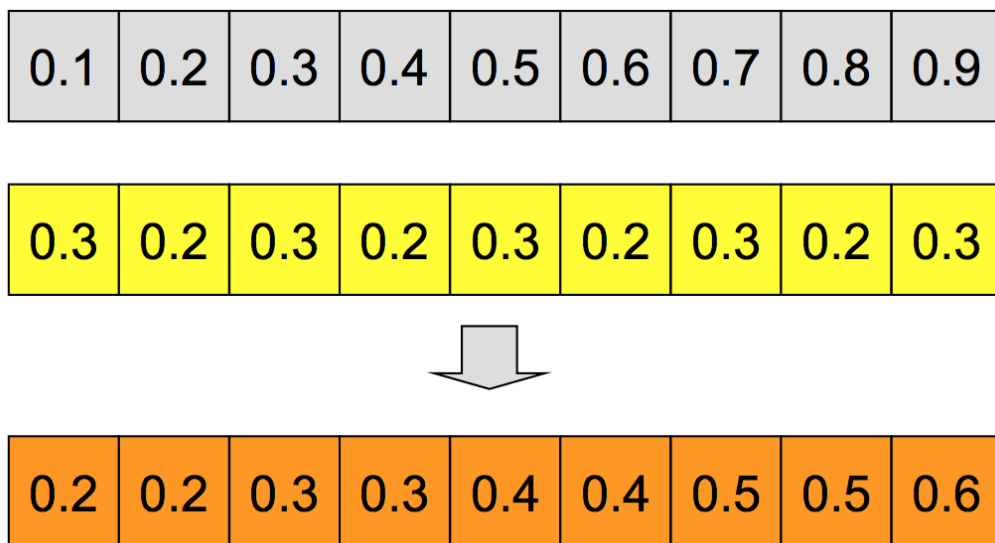


Figure 7: Arithmetic Crossover

2.4.6 Mutation

When applied to a genotype, mutation returns a slightly mutated offspring (Eiben and Smith, 2015). It can create new genes in the population, which in turn diversifies the population.

Like with crossover, there are different ways to perform mutation. In the case of binary chromosomes, we would allow each gene to 'flip' from a 1 to a 0 or vice versa, as demonstrated by Figure 8. Each gene has a probability of being mutated in this way, which will often be calculated as $1/n$ with n being representative of the chromosome length.

Integers are slightly different. The probability remains the same, but the difference is that a set of possible numbers, for example 0 to 9, is set up and when a gene is chosen for mutation, a number within that range is randomly generated and used in the offspring. This is displayed in Figure 9.

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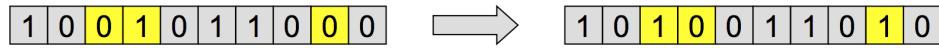


Figure 8: Binary Mutation

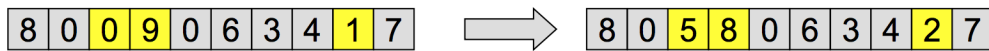


Figure 9: Integer Mutation

Again, permutations work in a completely different way, but are not considered as part of this project.

2.4.7 Replacement

This is the part where individuals are removed from the population to make way for a generation of new and hopefully improved genotypes. We could just remove the oldest genotype in the population, but this could be one with a high fitness! This can also be done randomly, but again there’s a risk that we could be removing individuals of high quality. The other way is to determine which individuals to remove using the fitness. We could just get rid of the least fit genotypes, which could lead to the population improving very quickly, however it could also lead to premature convergence.

2.5 NeuroEvolution for Augmenting Topologies (NEAT)

“NEAT is a method for evolving speciated neural networks of arbitrary structures and sizes. NEAT leverages the evolution of structure to make neuroevolution more efficient” (Stanley and Miikkulainen, 2002b).

It is claimed to result in significantly faster learning than neuroevolution techniques using fixed network topologies.

In NEAT, the mutation phase can alter network structures as well as connection weights (Stanley and Miikkulainen, 2002a). While connection weights are mutated in the same way as described in the previous section, network structure can be mutated in two ways:

- Add Connection

- A new connection gene is added, linking two nodes that were not connected beforehand
- Add Node
 - A connection that already exists is split and the new node replaces the old connection. The previous connection is disabled and the genome gains two new connections.

SOME GOOD STUFF IN (Stanley and Miikkulainen, 2004)

2.6 Summary

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3 Literature Review

Video games are a field that has been used as a catalyst for research and development in artificial intelligence due to the relatively risk-free nature of it when compared to other areas where AI might be used for quite some time now, but it was only recently that a program was able to beat a world class human player in the game of Go (Korenkov). This is despite a huge amount of work and time being injected into developing these types of game-playing agents with the desired result of beating the best human players in the world at Chess, and more recently, Go.

This project aims to create a digital version of the card game Switch. While playing, each competitor has no idea what cards their opponent(s) hold. They only know what cards they themselves hold, and what the most recently played card was. They will also know whose turn it is and what direction the play is going (if there are multiple remaining opponents).

Solutions for Chess and Go might use search trees for decision making, however this requires knowing the full state of the game, including the location of every game piece on the board. This is what is known as ‘perfect information.’ However, in card games such as Poker or Switch, there are unknowns such as the hands other players have or the value of cards that are face down. Therefore, we are faced with ‘*imperfect information.*’

This is where neural networks come in.

MIGHT DELETE THAT LINE AND PUT IT IN Why Neural Networks

3.1 AI for Playing Games

When researching neural networks in relation to games, a stand-out is MarI/O. There is a video on YouTube showcasing its solution after 34 generations using NEAT. It is described on the page of that video as the following:

“MarI/O is a program made of neural networks and genetic algorithms that kicks butt at Super Mario World” (SethBling, 2015).

Despite that description, the intelligence of MarI/O is questionable. Although it has mastered the art of manoeuvring its way across the level in question, that is all it has done. In other words, if we were to take the same agent and run it on another Super Mario level, it wouldn’t do so well. It has figured out how to pass through the level by continually moving right, and jumping at optimal times to avoid enemies and gaps in the map. Albeit successful, this is not a strategy that could be deemed as intelligent.

For Alan Turing to consider a machine intelligent, it must be able to act in a way that would be indistinguishable from the way a human would act.



Figure 10: MarI/O
(SethBling, 2015)

The Turing Test, created by Turing himself in 1950, was an imitation game whereby a human would hold textual conversations with another human, and with a computer. If the testing human is unable to successfully differentiate between the two based on interrogation within those conversations, then Turing would deem it unreasonable not to call the computer intelligent (Turing).

Although dealing in a different realm altogether, applying the same principle to MarI/O and questioning if the strategy it presents could pass a similar test of human judgement to decide whether or not it is a strategy that is likely to have been played by a human, then we cannot possibly declare MarI/O's technique as an intelligent solution.

Particularly card games

3.2 Why Neural Networks?

This project has dealt a hand presenting a problem in which a decision making process will have to make use of imperfect information. Not only can neural networks cope with this, in fact, they excel in situations of imperfect information.

Without a neural network, any given scenario within a problem would need to have some kind of hard-coded solution that is step-by-step in nature. Through a learning process, a neural network can find solutions to these scenarios on its own, via exploration of the possibilities thrown up by its decision making process over several generations.

Imagine having to write the code for a solution to every single possible game state in Chess. For every move, you would have to write a solution for it as many times as there are possible opportunities for that particular move, i.e, every possible board configuration in which that single move is legal. This would take an unthinkable amount of time, and in reality is probably not even possible.

Using a neural network and allowing it to analyse every situation it encounters on its own, decide what move to make and learn from the results is a far better idea.

Additionally, hard-coding solutions to given situations would make the game predictable, and could also lead to making moves that are not actually the best for that current game state. The flexible nature of a neural network provides the potential to reach better solutions that hard-coding might miss out on.

In our Switch card game for example, there is a rule that states if the previous player played a 2, you must pick up two cards unless you have another 2. Knowing this, and wanting to force our opponents to inherit more cards, we might hard-code a strategy that says, "if you have a 2 and it's available to be played, play it." This could cost us a chance to win the game though!

If we only had two cards left, both of the same suit and matching the suit of the most recently played card, one being a 2 and the other being a 7, we could play the 7 first, and that would allow us to play a run of that suit. Thus allowing us to play both cards and win the game. A neural network might learn that playing a 7 is better than deploying a 2, but our hard-coded strategy may not.

3.3 Why Evolve Neural Networks?

"Neuroevolution, i.e. evolving artificial neural networks with genetic algorithms, has been highly effective in reinforcement learning tasks, particularly those with hidden state information" (Stanley and Miikkulainen, 2002a).

The evolution of neural networks has demonstrated a large degree of potential when coupled with tasks solvable by reinforcement learning techniques (Stanley and Miikkulainen, 2002a). It outperforms the basic methods of reinforcement learning against tasks that are considered benchmarks, and is therefore a justifiably sought after means of decision making.

NICELY DONE x4iiiiis NOW RELATE IT TO A (CARD) GAME

3.4 Why Co-Evolve Topologies and Weights?

Much like when we compare evolving neural networks to standard reinforcement learning techniques, evolving network topologies often performs in a significantly superior manner to the alternative - in this case fixed topology neural network evolution (Stanley and Miikkulainen, 2002a).

There is always a chance with evolving topologies of making the search overly complex, but in contrast to that possibility there is also the potential to find the optimal amount of hidden nodes for any given problem by itself, which would save some time (Stanley and Miikkulainen, 2002a).

Simple networks are where NEAT begins, before expanding the search space when necessary (Stanley and Miikkulainen, 2004). This flexibility is what allows it to find far more complex controllers than evolution networks with a non-negotiable topology.

RELATE IT TO A (CARD) GAME

3.5 How intelligent is it?

What did the evolved strategy look like -Did it come up with something cheap and easy like the mario thing where it jumps all the time, or does it resemble a strategy a human player might use

3.6 Summary

4 title

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5 Additional Information / Knowledge Required

Experience with Linux and managing Virtual machines, networking. So on and so forth...

References

- A.E. Eiben and J.E. Smith. *Introduction to Evolutionary Computing*. Springer Berlin Heidelberg, 2015, 2015.
- Simon Haykin. *Neural Networks - A Comprehensive Foundation*. Prentice Hall, 1999.
- Andrey Kurenkov. A Brief History of Game AI. URL <http://www.andreykurenkov.com/writing/a-brief-history-of-game-ai/>.
- Michael A Nielsen. *Neural Networks and Deep Learning*. Determination Press, 2015.
- SethBling. MarI/O, 2015. URL <https://www.youtube.com/watch?v=qv6UV0Q0F44>.
- Kenneth O. Stanley and Risto Miikkulainen. Efficient Evolution of Neural Network Topologies. *Proceedings of the Genetic and Evolutionary Computation Conference*, 2002a.
- Kenneth O. Stanley and Risto Miikkulainen. Evolving Neural Networks through Augmenting Topologies. *Evolutionary Computation*, 2002b.
- Kenneth O. Stanley and Risto Miikkulainen. Evolving a Roving Eye for Go. *Proceedings of the Genetic and Evolutionary Computation Conference*, 2004.
- Sebastian Thrun. Learning to Play the Game of Chess. *MIT Press*, 1995.
- Alan Turing. The Alan Turing Internet Scrapbook. URL <http://www.turing.org.uk/scrapbook/test.html>.
- Sun-Chong Wang. Artificial Neural Network. *Interdisciplinary Computing in Java Programming. The Springer International Series in Engineering and Computer Science, vol 743*, 2003.

Appendices

A Project Overview

Initial Project Overview

SOC10101 Honours Project (40 Credits)

Title of Project:

Evolution of Neural Network Controllers for Gameplay Behaviours

Overview of Project Content and Milestones

The idea is to implement a card game with four players. One of the players is the human, another is an AI agent that has no idea how to play the game, and the other two are hard-coded to know the rules and how to play. The intention is for said card game to be Switch, however this is subject to change if the rules are found to be too difficult for the scale of the project – in which case a simpler game will be substituted in.

The agent then learns how to play by trying to make moves based on neural networks. Initially this will be totally random but after the first generation of the algorithm cycle, it will be based on the chromosomes with the highest fitness, which should then begin to provide better results. These moves can be blocked if they are not legal. There’ll be a scoring system for the agent that will be negatively affected by illegal moves and it will then use this to learn how to do better the next time it plays. The scoring system will also see the agent penalised for losing or not winning. This will be what our fitness is based on.

It is worth noting that how successful you are in a game of Switch depends entirely on the hand you’re dealt, and how your opponents play the hands they are dealt. A lot of the game is about luck, and so negatively affecting the agent’s score should take this into account and deploy some leniency.

The project will make use of the NeuroEvolution of Augmenting Topologies (NEAT) library and will most likely be coded in C++. It will use neural network controllers, co-evolving weights and topologies.

The Main Deliverable(s):

- A playable card game that incorporates an Artificial Intelligence agent that must learn how to play the game from scratch based on a score system that penalises the agent for illegal or costly decisions.
- Experimental research into improving the performance (in terms of score) or speeding up the learning process of the agent.
- A report into what positively or negatively affects the agent, and what causes the effects that it has including experiment results using charts and figures. Changes will be made by varying parameter settings of the evolutionary algorithm in a systematic way.

The Target Audience for the Deliverable(s):

Whilst the final product will be a playable game, it will really be aimed more at being experimental research into Artificial Intelligence techniques and, more specifically, evolving neural network controllers for playing games. Thus, the audience most likely to be interested in the project are those who also want to look into artificial intelligence agents.

The Work to be Undertaken:

- Design and build a game of Switch without the AI agent
- Thoroughly test the bare-bones game to ensure it works perfectly without bugs
- Research neural networks and evolutionary algorithms
- Implement the AI agent
- Experiment with a few different techniques and test how they perform in terms of improving or decreasing the agent's intelligence/performance in game.

Additional Information / Knowledge Required:

Neural networks and evolutionary algorithms

Information Sources that Provide a Context for the Project:

- Lubberts, & Miikkulainen (2001). Co-Evolving a Go-Playing Neural Network.
- Stanley, Bryant, & Miikkulainen (2005). Evolving Neural Network Agents in the NERO Video Game. IEEE Press.
- Thrun (1995). Learning to Play the Game of Chess. MIT Press.

The Importance of the Project:

Exploring possibilities and limits of AI in games, particularly evolved controllers which do not have to be hard-coded.

The Key Challenge(s) to be Overcome:

- Complete lack of knowledge and experience with Artificial Intelligence techniques

A.A Example sub appendices

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B Second Formal Review Output

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C Diary Sheets (or other project management evidence)

Insert diary sheets here together with any project management plan you have

D Appendix 4 and following

insert content here and for each of the other appendices, the title may be just on a page by itself, the pages of the appendices are not numbered, unless an included document such as a user manual or design document is itself page numbered.