The Task of Text Classification

Naïve Bayes (I)

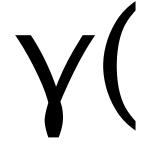


#### **Naïve Bayes Intuition**

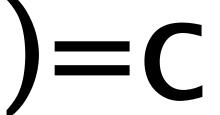
- Simple ("naïve") classification method based on Bayes rule
- Relies on very simple representation of document
  - Bag of words



#### The bag of words representation



I love this movie! It's sweet, but with satirical humor. The dialogue is great and the adventure scenes are fun... It manages to be whimsical and romantic while laughing at the conventions of the fairy tale genre. I would recommend it to just about anyone. I've seen it several times, and I'm always happy to see it again whenever I have a friend who hasn't seen it yet.

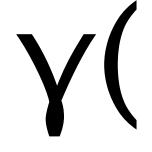




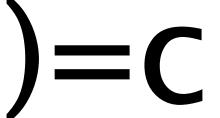




#### The bag of words representation



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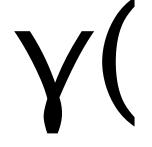




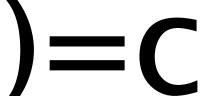




## The bag of words representation: using a subset of words



x love xxxxxxxxxxxxxx sweet xxxxxxx satirical xxxxxxxxxx xxxxxxxxxxx **great** xxxxxxx xxxxxxxxxxxxxxxxx fun xxxxxxxxxxxx whimsical xxxx romantic xxxx laughing \*\*\*\*\*\*\*\*\*\*\* xxxxxxxxxxxxxx **recommend** xxxxx xx several xxxxxxxxxxxxxxxxx happy xxxxxxxxx again xxxxxxxxxxxxxxxxxx

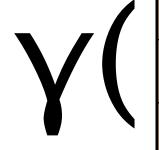








### The bag of words representation



| great     | 2     |
|-----------|-------|
| love      | 2     |
| recommend | 1     |
| laugh     | 1     |
| happy     | 1     |
| • • •     | • • • |









#### Bag of words for document classification

Test document

parser language label translation

. . .

Machine Learning learning training algorithm shrinkage network...

**NLP** parser tag training translation

<u>language</u>...

Collection garbage collection memory

region...

Garbage

planning temporal reasoning optimization plan

language...

Planning

GUI

Naïve Bayes (I)

Formalizing the Naïve Bayes
Classifier



## Bayes' Rule Applied to Documents and Classes

For a document d and a class c

$$P(c \mid d) = \frac{P(d \mid c)P(c)}{P(d)}$$





### Naïve Bayes Classifier (I)

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(c \mid d)$$

MAP is "maximum a posteriori" = most likely class

$$= \underset{c \in C}{\operatorname{argmax}} \frac{P(d \mid c)P(c)}{P(d)}$$

**Bayes Rule** 

$$= \underset{c \in C}{\operatorname{argmax}} P(d \mid c) P(c)$$

Dropping the denominator

Dan Jurafsky



### Naïve Bayes Classifier (II)

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(d \mid c) P(c)$$

$$= \underset{c \in C}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n \mid c) P(c)$$

Document d represented as features x1..xn



### Naïve Bayes Classifier (IV)

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n \mid c) P(c)$$

 $O(|X|^n \bullet |C|)$  parameters

How often does this class occur?

Could only be estimated if a very, very large number of training examples was available.

We can just count the relative frequencies in a corpus



## Multinomial Naïve Bayes Independence Assumptions

$$P(x_1,x_2,...,x_n \mid c)$$

- Bag of Words assumption: Assume position doesn't matter
- Conditional Independence: Assume the feature probabilities  $P(x_i|c_i)$  are independent given the class c.

$$P(x_1,...,x_n \mid c) = P(x_1 \mid c) \cdot P(x_2 \mid c) \cdot P(x_3 \mid c) \cdot ... \cdot P(x_n \mid c)$$



### Multinomial Naïve Bayes Classifier

$$c_{MAP} = \underset{c \in C}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n \mid c) P(c)$$

$$c_{NB} = \underset{c \in C}{\operatorname{argmax}} P(c_j) \prod_{x \in X} P(x \mid c)$$



## **Applying Multinomial Naive Bayes Classifiers to Text Classification**

positions ← all word positions in test document

$$c_{NB} = \underset{c_{j} \in C}{\operatorname{argmax}} P(c_{j}) \prod_{i \in positions} P(x_{i} \mid c_{j})$$

Formalizing the Naïve Bayes
Classifier

Naïve Bayes: Learning



#### Learning the Multinomial Naïve Bayes Model

- First attempt: maximum likelihood estimates
  - simply use the frequencies in the data

$$\hat{P}(c_j) = \frac{doccount(C = c_j)}{N_{doc}}$$

$$\hat{P}(w_i \mid c_j) = \frac{count(w_i, c_j)}{\sum_{w \in V} count(w, c_j)}$$



#### **Parameter estimation**

$$\hat{P}(w_i \mid c_j) = \frac{count(w_i, c_j)}{\sum_{w \in V} count(w, c_j)}$$
 fraction of times word  $w_i$  appears among all words in documents of topic  $c_j$ 

- Create mega-document for topic j by concatenating all docs in this topic
  - Use frequency of w in mega-document



#### **Problem with Maximum Likelihood**

 What if we have seen no training documents with the word fantastic and classified in the topic positive (thumbs-up)?

$$\hat{P}(\text{"fantastic" | positive}) = \frac{count(\text{"fantastic", positive})}{\sum_{w \in V} count(w, \text{positive})} = 0$$

 Zero probabilities cannot be conditioned away, no matter the other evidence!

$$c_{MAP} = \operatorname{argmax}_{c} \hat{P}(c) \prod_{i} \hat{P}(x_{i} \mid c)$$



### Laplace (add-1) smoothing for Naïve Bayes

$$\hat{P}(w_i \mid c) = \frac{count(w_i, c) + 1}{\sum_{w \in V} (count(w, c)) + 1}$$

$$= \frac{count(w_i, c) + 1}{\left(\sum_{w \in V} count(w, c)\right) + |V|}$$



### **Multinomial Naïve Bayes: Learning**

- From training corpus, extract *Vocabulary*
- Calculate  $P(c_i)$  terms
  - For each  $c_j$  in C do  $docs_j \leftarrow \text{all docs with class} = c_j$

$$P(c_j) \leftarrow \frac{|docs_j|}{|total \# documents|}$$

- Calculate  $P(w_k \mid c_i)$  terms
  - $Text_j \leftarrow single doc containing all <math>docs_j$
  - For each word  $w_k$  in *Vocabulary*  $n_k \leftarrow \#$  of occurrences of  $w_k$  in  $Text_j$

$$P(w_k \mid c_j) \leftarrow \frac{n_k + \alpha}{n + \alpha \mid Vocabulary \mid}$$