## Exam - Computer Architecture Unit I [06/02/2025] (B)

Surname:	Name:	
Student ID Number (Matricola):		

DSA Students should solve only the first 4 exercises (grade will be scaled accordingly)

**Exercise 1 (7 points)** Design a sequential circuit with two inputs x1, x0, that encode the characters T, O, S as shown on the table on the right. The circuit has 2 outputs z1 and z0. The circuit outputs z1=1 when it receives the sequence TOST, and z0=1 when it receives the sequence TOT. Overlaps are allowed. Draw the FSM diagram, the state transition table, and the circuit.

x1, x0	character
00	T
01	0
1-	S

matricola	
-----------	--

Exercise 2 (4 points) Design a circuit that computes how many days are in a given month. The month is specified by a 4-bit input  $a_3a_2a_1a_0$ . For example, if the inputs are (0001), the month is January, and if the inputs are (1100), the month is December. The output of the circuit  $Y_1$   $Y_0$ , must be equal to 00 only when the month specified on the input has 31 days, they must be equal to 01 when the input month has 30 days, and they must be equal to 10 when the input month has 28 days. The outputs must be equal to 11 in the remaining cases. Write down the truth table, and the minimal SOP and POS forms.

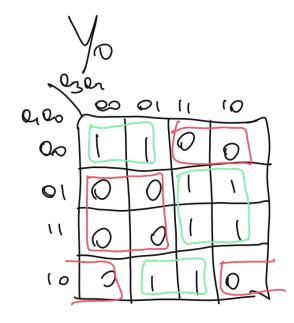
\$ 1/2/20/20/20/20/20/20/20/20/20/20/20/20/2	l <sub>3</sub>	QL	Q,		<del>}</del> o	4		40			
//	0	0	0	<u> </u> @	)	١	4	<del></del>	•		
31	6	0	0	(		Q	۱ (	0			
45	Q	0	(	£	)	(	$\forall$	0			
31	0	0	-	+	(	တ	$\Box$	0	_		
70	0	١	0	0		(	긔				
31	0	١	0	1		0		$\bigcirc$			
30	0		1	2	)	(E	4	(			
31	0	\_	10	4		C	<u> </u>	0	_		
7	(	0	0	1	>	6		<b>⊘</b>			
20	(	0	0		(	•	)	(			
3,	1	0	1	/ (	)	0	)	0			
\ \ -	17	70	\	1)	(	10	9	1	•		
20	<del>                                     </del>	1,		0	0	7	S	0			
31	1-			$\overline{}$	1	$\top$	(	$T_{T}$		>	
//		11	`	<u> </u>	\	+	_	+			_
11	$\top$	1		(	0			( )			
//				(	(		(				

4	3Q r			
0.00	8	01	11	(O
00 CO		0	0	0
ا _ ا©	0	0	1	0
( )	0	0	M	0
10	$\overline{l}$	0		0
,		•	(	

SOP= Q3Q2Q0+ Q3Q2Q1

$$POS = \left( Q_3 + \overline{Q}_0 \right) \left( Q_3 + \overline{Q}_1 \right) \left( \overline{Q}_3 + \overline{Q}_1 \right)$$

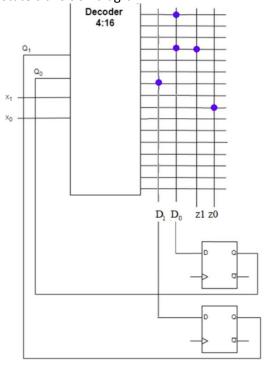
$$\left( Q_3 + \overline{Q}_1 + \overline{Q}_0 \right)$$



$$POS = \left(Q_3 + \overline{Q_0}\right)\left(\overline{Q_3} + \overline{Q_1} + \overline{Q_0}\right)\left(Q_2 + \overline{Q_1} + \overline{Q_0}\right)$$

**Exercise 3 (5 points)** Analyze the sequential circuit in the figure below. Write down the next state table and the

state transition diagram.



O <sub>i</sub>	Q <sub>o</sub>	Х		Vο	Ī	)(	D			5/2	<u>'</u>
0	0	0	1	0	0	_	(	$\perp$	0	To	<u></u>
0	0	Q	1	١	0	1	6	<	5	7	_
0	0	(	4	0	ଦ	4	Ø	[	2	b	
0	O	l	L	1	0	L	(	<u> </u>		þ	
0000000	1	0	k	2	Ø	L	٥	0	_ {	つ	
0	١	0		(	Ð	L	0	0	$\int$	9	_
0	1	(	1	2		c	<u>)</u>	2		D	_
_	1	1	T	\	D	4	<u>ව</u>	D	$\neg$	<u>つ</u>	
9		10	1	C	D	2	2_	۵	_		_
$\rightarrow$	<u> </u>	10	;†	1	0		0	0		٥	-
1	0	+	ナ	<del>`</del>	0	Ċ		୍ଚ	7	0	_
	р 	+	4	1	0		O	0	7	5	
(	1	1	5	9	S	τ	>	5	7		
_	1,	10	 5	\	O	J	)	ō		$\mathcal{L}$	-
	t	$\top$	(	p	2		2	િ	7	>	
_	$+ \tau$	$\top$	<u> </u>	$\overline{}$	٥	C		O	0	)	
			`			•					

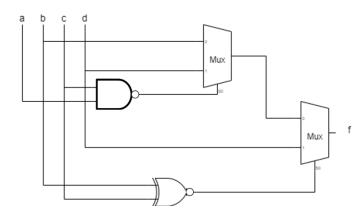
11 UNREDMARKE

11/19/ 0/00 0//00 11/00

> 0/0/ 0/160

## Exercise 4 (6 points)

- Consider the circuit depicted below and write down the boolean expression for the function *f*
- Transform the expression, using Boole's algebra axioms and theorems, to SOP form
- Write down the truth table for *f*
- Write down the minimal POS form for f



$$\int = (B\Phi C)D + (B\Phi C)[\overline{AC}D + ACB]^{-1}$$

$$= (\overline{BC} + B\overline{C})D + (B\overline{C} + \overline{BC})((\overline{A} + \overline{C})D + ABC)^{-1}$$

$$= (\overline{BC} \overline{BC})D + (B\overline{C} + \overline{BC})(\overline{AD + CD + ABC})^{-1}$$

= (B+c)(B+c)D+ABCD+BCD=

$$= BCD + \overline{B}CD + \overline{A} \overline{B}CD + \overline{B}CD + \overline{B}CD =$$

$$= BD (C + \overline{A}\overline{C} + \overline{C}) + \overline{B}CD + \overline{A}\overline{B}CD =$$

$$= BD + \overline{B}CD + \overline{A}\overline{B}CD = D(B + \overline{B}C) + \overline{A}\overline{B}CD =$$

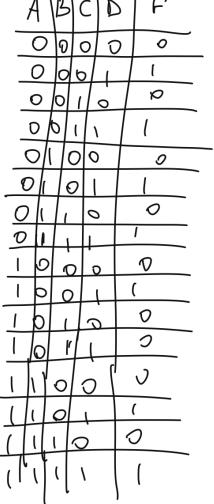
$$= BD + \overline{C}D + \overline{A}\overline{B}CD = BD + D(\overline{C} + \overline{A}\overline{B}C) =$$

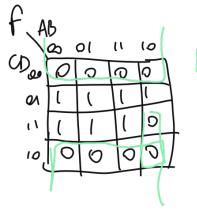
$$= BD + \overline{C}D + \overline{A}\overline{B}D = D(B + \overline{A}\overline{B}) + \overline{C}D =$$

$$= BD + \overline{C}D + \overline{A}\overline{B}D = D(B + \overline{A}\overline{B}) + \overline{C}D =$$

$$= BD + \overline{A}D + \overline{C}D =$$

$$= BD + \overline{A}D + \overline{C}D =$$





PoS=(D)(A+B+C)

**Exercise 5 (4 points)** Convert the base 10 number X = -304 in the IEEE 754 half-precision format and convert those 16 bits to a base-16 number. Then, convert the base-16 number Y = 5A00 to a binary string, and interpret that string as an IEEE 754 half-precision number. Compute X+Y in IEEE 754 half-precision, and convert the resulting 16 bits to a base-16 number.

$$V = 5A00 = 0101 1010 0000 0000$$
  
Sign 6. exp. mention  
 $C = 72 \rightarrow 24p = 7$ 

$$y = +2^{4} \cdot 1.1 = 0.11 \cdot 2^{8} = 1100000 = 192_{10}$$

matrico	la

**Exercise 6 (4 points)** Given the expression  $f = (\bar{x} + \overline{y(y + \overline{zw})}) \oplus (\bar{x} + zw)$  simplify it and bring it to normal SOP form. Write the canonical form for f and implement f using NAND only.

CANGONICAL: XYZW+XJZW+XJZW+XJZW

matricola	
matricola	

ATTENTION: You can detach and use this page as scratchpad. Whatever you write here will be ignored during the correction of the exam. The solution must fit all within the previous pages.

matricola	
matricola	

ATTENTION: You can detach and use this page as scratchpad. Whatever you write here will be ignored during the correction of the exam. The solution must fit all within the previous pages.