

FIRST

```

program {id, read, write, $$}
stmt_list {id, read, write, ε}
stmt {id, read, write}
expr {(, id, literal}
term_tail {+, -, ε}
term {(, id, literal}
factor_tail {*, /, ε}
factor {(, id, literal}
add_op {+, -}
mult_op {*, /}

```

Also note that $\text{FIRST}(a) = \{a\} \forall \text{ tokens } a$.

FOLLOW

```

id {+, -, *, /, ), :=, id, read, write, $$}
literal {+, -, *, /, ), id, read, write, $$}
read {id}
write {(, id, literal}
( {(, id, literal}
) {+, -, *, /, ), id, read, write, $$}
:= {(, id, literal}
+ {(, id, literal}
- {(, id, literal}
* {(, id, literal}
/ {(, id, literal}
$$ {ε}
program {ε}
stmt_list {$$}
stmt {id, read, write, $$}

```

```

expr {), id, read, write, $$}
term_tail {), id, read, write, $$}
term {+, -, ), id, read, write, $$}
factor_tail {+, -, ), id, read, write, $$}
factor {+, -, *, /, ), id, read, write, $$}
add_op {(, id, literal}
mult_op {(, id, literal}

```

PREDICT

```

1 program → stmt_list $$ {id, read, write, $$}
2 stmt_list → stmt stmt_list {id, read, write}
3 stmt_list → ε {$$}
4 stmt → id := expr {id}
5 stmt → read id {read}
6 stmt → write expr {write}
7 expr → term term_tail {(, id, literal}
8 term_tail → add_op term term_tail {+, -}
9 term_tail → ε {), id, read, write, $$}
10 term → factor factor_tail {(, id, literal}
11 factor_tail → mult_op factor factor_tail {*, /}
12 factor_tail → ε {), id, read, write, $$}
13 factor → ( expr ) {(}
14 factor → id {id}
15 factor → literal {literal}
16 add_op → + {+}
17 add_op → - {-}
18 mult_op → * {*}
19 mult_op → / {/}

```

Figure 2.16 FIRST, FOLLOW, and PREDICT sets for the calculator language.

more serious version of the immediate error detection problem described in Section 2.2.4. There we saw that the use of context-independent FOLLOW sets could cause us to overlook a syntax error until after we had needlessly predicted one or more epsilon productions. Context-specific FOLLOW sets solved the problem, but did not change the set of *valid* programs that could be parsed with one token of look-ahead. If we define $\text{LL}(k)$ to be the set of all grammars that can be parsed predictively using the top-of-stack symbol and k tokens of look-ahead, then it turns out that for $k > 1$ we must adopt a context-specific notion of FOLLOW sets in order to parse correctly. Our previous parsing algorithm—the one based on context-independent FOLLOW sets—is really SLL, rather than true LL. For $k = 1$, the two algorithms can parse the same set of grammars. For $k > 1$, LL is strictly more powerful.

Top-of-stack nonterminal	Current input token											
	id	literal	read	write	:=	()	+	-	*	/	\$\$
<i>program</i>	1	-	1	1	-	-	-	-	-	-	-	1
<i>stmt_list</i>	2	-	2	2	-	-	-	-	-	-	-	3
<i>stmt</i>	4	-	5	6	-	-	-	-	-	-	-	-
<i>expr</i>	7	7	-	-	-	7	-	-	-	-	-	-
<i>term_tail</i>	9	-	9	9	-	-	9	8	8	-	-	9
<i>term</i>	10	10	-	-	-	10	-	-	-	-	-	-
<i>factor_tail</i>	12	-	12	12	-	-	12	12	12	11	11	12
<i>factor</i>	14	15	-	-	-	13	-	-	-	-	-	-
<i>add_op</i>	-	-	-	-	-	-	-	16	17	-	-	-
<i>mult_op</i>	-	-	-	-	-	-	-	-	-	18	19	-

Figure 2.17 LL(1) parse table for the calculator language. Table entries indicate the production to predict (as numbered in Figure 2.14). A dash indicates an error. When the top-of-stack symbol is a terminal, the appropriate action is always to match it against an incoming token from the scanner.

Writing an LL(1) Grammar

When working with a top-down parser generator, one has to acquire a certain facility in writing and modifying LL(1) grammars. The two most common obstacles to "LL(1)-ness" are *left recursion* and *common prefixes*.

Left recursion occurs when the first symbol on the right-hand side of a production is the same as the symbol on the left-hand side. Here again is the grammar from page 51, which cannot be parsed top-down:

```

id_list → id_list.prefix ;
id_list.prefix → id_list.prefix , id
               → id

```

The problem is in the second and third productions; with *id_list.prefix* at top-of-stack and an *id* on the input, a predictive parser cannot tell which of the productions it should use. (Recall that left recursion is *desirable* in bottom-up grammars, because it allows recursive constructs to be discovered incrementally, as in Figure 2.9.)

Common prefixes occur when two different productions with the same left-hand side begin with the same symbol or symbols. Here is an example that commonly appears in Algol-family languages:

```

stmt → id := expr
      → id ( argument_list )           — procedure call

```

Clearly *id* is in the FIRST set of both right-hand sides, and therefore in the PREDICT set of both productions.

Read A
Read B
sum := A + B
write sum
write sum / 2

Parse stack	Input stream	Comment
program	read A read B ...	initial stack contents
stmt_list \$\$	read A read B ...	predict program → stmt_list \$\$
stmt stmt_list \$\$	read A read B ...	predict stmt_list → stmt stmt_list
read id stmt_list \$\$	read A read B ...	predict stmt → read id
id stmt_list \$\$	A read B ...	match read
stmt_list \$\$	read B sum := ...	match id
stmt stmt_list \$\$	read B sum := ...	predict stmt_list → stmt stmt_list
read id stmt_list \$\$	read B sum := ...	predict stmt → read id
id stmt_list \$\$	B sum := ...	match read
stmt_list \$\$	sum := A + B ...	match id
stmt stmt_list \$\$	sum := A + B ...	predict stmt_list → stmt stmt_list
id := expr stmt_list \$\$	sum := A + B ...	predict stmt → id := expr
:= expr stmt_list \$\$:= A + B ...	match id
expr stmt_list \$\$	A + B ...	match :=
term term_tail stmt_list \$\$	A + B ...	predict expr → term term_tail
factor factor_tail term_tail stmt_list \$\$	A + B ...	predict term → factor factor_tail
id factor_tail term_tail stmt_list \$\$	A + B ...	predict factor → id
factor_tail term_tail stmt_list \$\$	+ B write sum ...	match id
term_tail stmt_list \$\$	+ B write sum ...	predict factor_tail → ε
add_op term term_tail stmt_list \$\$	+ B write sum ...	predict term_tail → add_op term term_tail
+ term term_tail stmt_list \$\$	+ B write sum ...	predict add_op → +
term term_tail stmt_list \$\$	B write sum ...	match +
factor factor_tail term_tail stmt_list \$\$	B write sum ...	predict term → factor factor_tail
id factor_tail term_tail stmt_list \$\$	B write sum ...	predict factor → id
factor_tail term_tail stmt_list \$\$	write sum ...	match id
term_tail stmt_list \$\$	write sum write ...	predict factor_tail → ε
stmt_list \$\$	write sum write ...	predict term_tail → ε
stmt stmt_list \$\$	write sum write ...	predict stmt_list → stmt stmt_list
write expr stmt_list \$\$	write sum write ...	predict stmt → write expr
expr stmt_list \$\$	sum write sum / 2	match write
term term_tail stmt_list \$\$	sum write sum / 2	predict expr → term term_tail
factor factor_tail term_tail stmt_list \$\$	sum write sum / 2	predict term → factor factor_tail
id factor_tail term_tail stmt_list \$\$	sum write sum / 2	predict factor → id
factor_tail term_tail stmt_list \$\$	sum write sum / 2	match id
term_tail stmt_list \$\$	write sum / 2	predict factor_tail → ε
stmt_list \$\$	write sum / 2	predict term_tail → ε
stmt stmt_list \$\$	write sum / 2	predict stmt_list → stmt stmt_list
write expr stmt_list \$\$	write sum / 2	predict stmt → write expr
expr stmt_list \$\$	sum / 2	match write
term term_tail stmt_list \$\$	sum / 2	predict expr → term term_tail
factor factor_tail term_tail stmt_list \$\$	sum / 2	predict term → factor factor_tail
id factor_tail term_tail stmt_list \$\$	sum / 2	predict factor → id
factor_tail term_tail stmt_list \$\$	/ 2	match id
mult_op factor factor_tail term_tail stmt_list \$\$	/ 2	predict factor_tail → mult_op factor factor_tail
/ factor factor_tail term_tail stmt_list \$\$	/ 2	predict mult_op → /
factor factor_tail term_tail stmt_list \$\$	2	match /
literal factor_tail term_tail stmt_list \$\$	2	predict factor → literal
factor_tail term_tail stmt_list \$\$		match literal
term_tail stmt_list \$\$		predict factor_tail → ε
stmt_list \$\$		predict term_tail → ε
\$\$		predict stmt_list → ε

Figure 2.13 Trace of a table-driven LL(1) parse of the sum-and-average program.