Statistics - Exam preparation

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Contents

1 Introduction

Statistics is a fairly big field. Therefore this paper will only include the absolutely necessary topics for passing the university class.

2 Abstract

This paper starts of with symbols used in the field of statistics, their meaning and in what context they are commonly used. Following Combinatorics is thematized.

3 Symbols and special characters

- $n!$ Faculty / Fakultät
- $\binom{n}{k}$ Binomial Coefficient / Binomialkoeffizient
- Ω Event set / Ergebnismenge
- ω Result / Ergebnis
- $A \subseteq \Omega$ Event / Ereignis
- $\{\omega\}$ Elementary event / Elementarereignis
- $\mathbb{P}$ Probability measure / Wahrscheinlichkeitsmaß
- $\mathbb{P}(A)$ Event propability / Wahrscheinlichkeit eines Ereignisses
- $\mathbb{E}(X), \mu_x, \mu$ Expected value / Erwartungswert
- σ Deviation from the mean / Standardabweichung
- $\mathrm{Var}(X), \sigma_x^2$ Variance / Varianz
- $\mathrm{Cov}(X, Y), \sigma_{XY}$ Kovarianz von X und Y
- $\mathcal{N}(\mu, \sigma^2)$ Normal distribution / Normalverteilung
- φ Bell curve / Glockenkurve
- Φ Error function / Fehlerintegral
- X Random variable / Zufallsvariable
- Z Standard score / standard-normalverteilte Zufallsvariable [1]
- $\mathrm{Bin}(n, p)$ Binomial distribution / Binomialverteilung
- $\mathrm{Pois}(\lambda)$ Poisson distribution / Poission-Verteilung
- $\mathrm{Exp}(\lambda)$ Exponential distribution / Exponentialverteilung

4 Combinatorics

This chapter will introduce the Binomial Coefficient, Faculty, Pascal's triangle and the binomial Theorem.

4.1 Binomial Coefficient

n choose k; used to calculate the Amount of Sets in $\{1, ..., n\}$ with exactly k Elements. n needs to be positive and k and n have to meet the following criteria: $n \in \mathbb{N}, 0 \leq k \leq n$.

$$\binom{n}{k} = \frac{n!}{k! \cdot (n-k)!} \tag{1}$$

Choosing k different Numbers from $\{1, ..., n\}$, there are n possibilities for the first number, $n-1$ possibilities for the second, and so forth.

[1] read more: wikipedia

4.2 Faculty

This can be described with $n!$. The faculty is defined as the product of decrementing n by an increasing subtrahend:

$$n! := n \cdot (n-1) \cdot (n-2)... \tag{2}$$

If $n = k$, there are $n!$ possibilities to choose k Elements from n. $0! = 1$.

4.3 Pascal's triangle

The pascal's triangle can be used to visualize the binomial coefficient.[2]

$$\binom{n+1}{k+1} = \binom{n}{k} + \binom{n}{k+1} \tag{3}$$

4.4 Binomial Theorem

Allows for expressing the exponents of $(x+y)^n, n \in \mathbb{N}$ as a polynomial with the degree of n.

$$(x+y)^n = \sum_{k=0}^{n} \binom{n}{k} \cdot x^k \cdot y^{n-k} \tag{4}$$

5 Probability theory

This chapter contains information on how to calculate probabilites.

5.1 Event set

The set containing results of the *experiment* E is notated via the *event set* (Ω). Sub sets of Ω are *events* (ω). *Events* with one entry are *elementary events* $\{\omega\}$. If Ω is finite: $\forall \omega \in \Omega, \mathbb{P}(\omega) \geq 0$. The sum of all propabilities of $\omega \in \Omega$ is 1[3].

5.2 Random variable

$X : \Omega \to \mathbb{R}$ we define $\{X = x\} := \{\omega | X(\omega) = x\}$ and can therefore shorten our definition of the propability that X is x to: $P(X = x) := P(\{X = x\})$

$$x \to \mathbb{P}(X = x) \tag{5}$$
$$x \to \mathbb{P}(X \leq x) \tag{6}$$

[2]read more about *pascal's triangle* here: wikipedia
[3]$\sum_{\omega \in \Omega} \mathbb{P}(\omega) = 1$

The equation 5 defines the density / probability function of X and the equation 6 the distribution function of X.