

c) Transition table: Looking at the STG and knowing the transition table of a D-flip-flop. (3)

Q_0	Q_1	X	Q_0'	Q_1'	D_0	D_1	Y
0	0	0	0	0	0	0	0
0	0	1	0	1	0	1	0
0	1	0	1	0	1	0	0
0	1	1	0	1	0	1	0
1	0	0	0	0	0	0	0
1	0	1	1	1	1	1	0
1	1	0	1	0	1	0	0
1	1	1	0	1	0	1	1

from the STG
from the transition table of a D flip-flop
from the STG

D	Q'
0	0
1	1

d)

→ The state functions are the next ones: $D_0 = \bar{Q}_0 \cdot \bar{Q}_1 \cdot \bar{X} + \bar{Q}_0 \cdot \bar{Q}_1 \cdot X + \bar{Q}_0 \cdot Q_1 \cdot \bar{X}$

$$D_1 = \bar{Q}_0 \cdot \bar{Q}_1 \cdot X + \bar{Q}_0 \cdot Q_1 \cdot X + Q_0 \cdot \bar{Q}_1 \cdot X + Q_0 \cdot Q_1 \cdot X$$

→ The output function is the next one: $Y = Q_0 \cdot Q_1 \cdot X$

* The reduction for D_0 is:

$X \backslash Q_0 Q_1$	00	01	11	10
0		1	1	
1				1

$\bar{X} \cdot Q_1$

$$\Rightarrow D_0 = Q_1 \bar{X} + \bar{Q}_0 \bar{Q}_1 X$$

* The reduction for D_1 is:

$X \backslash Q_0 Q_1$	00	01	11	10
0				
1	1	1	1	1

$\rightarrow X$

$$\Rightarrow D_1 = X$$

* There is no reduction for the output function, so: $Y = Q_0 \cdot Q_1 \cdot X$