

PROBLEMA 7.9

$$f(x) ; x_0 = 1$$

$$P_4(x|f, 1) = 2(x-1)^3 - 3(x-1)^4$$

Puesto que:

$$P_4(x|f, 1) = f(1) + f'(1)(x-1) + \frac{f''(1)}{2!}(x-1)^2 + \frac{f'''(1)}{3!}(x-1)^3 + \frac{f^{(4)}(1)}{4!}(x-1)^4$$

$$\Rightarrow f(1) = 0 ; f'(1) = 0 ; f''(1) = 0 ;$$

$$f'''(1) = 3! \cdot 2 = 12$$

$$f^{(4)}(1) = -4! \cdot 3 = -72$$

- La recta tangente a la gráfica de $x_0 = 1$ es la recta $y = 0$ (recta de pendiente 0 que pasa por $y_0 = 0$)

$$\begin{aligned} \bullet \lim_{x \rightarrow 1} \frac{f(x)}{(x-1)^3} &= \lim_{x \rightarrow 1} \frac{2(x-1)^3 - 3(x-1)^4 + o((x-1)^4)}{(x-1)^3} = \\ &= 2 \end{aligned}$$

- $f^{(4)}(1) = -72$