NLP and the Web - WS 2024/2025



Lecture 3
Information Retrieval I



Ubiquitous Knowledge Processing Lab Technische Universität Darmstadt







Syllabus (tentative)

Nr.	<u>Lecture</u>
01	Introduction / NLP basics
02	Foundations of Text Classification
03	IR – Introduction, Evaluation
04	IR – Word Representation, Data Collection
05	IR – Re-Ranking Methods
06	IR – Language Domain Shifts, Dense / Sparse Retrieval
07	LLM – Language Modeling Foundations
08	LLM – Neural LLM, Tokenization
09	LLM – Transformers, Self-Attention
10	LLM – Adaption, LoRa, Prompting
11	LLM – Alignment, Instruction Tuning
12	LLM – Long Contexts, RAG
13	LLM – Scaling, Computation Cost
14	Review & Preparation for the Exam

Today

IR – Introduction, Evaluation

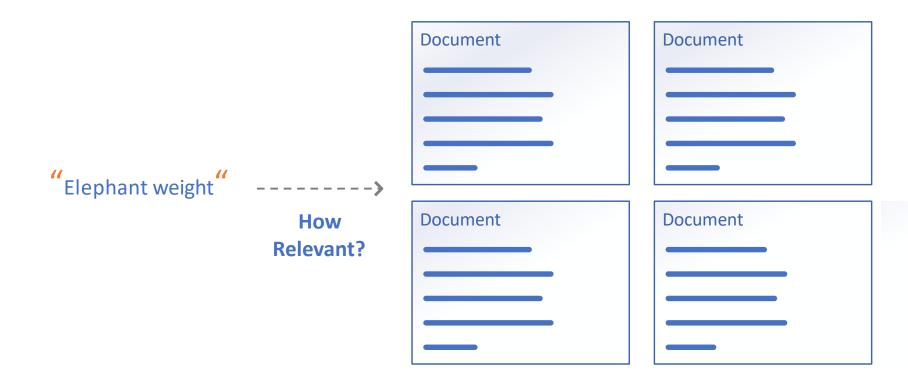
- Introduction
 - Inverted Index
 - Search & Relevance
 - TF-IDF & BM25
- 2 Evaluation
 - Precision & Recall
 - MRR & MAP
 - nDCG



Information Retrieval



Information Retrieval (finding the needle in the haystack)

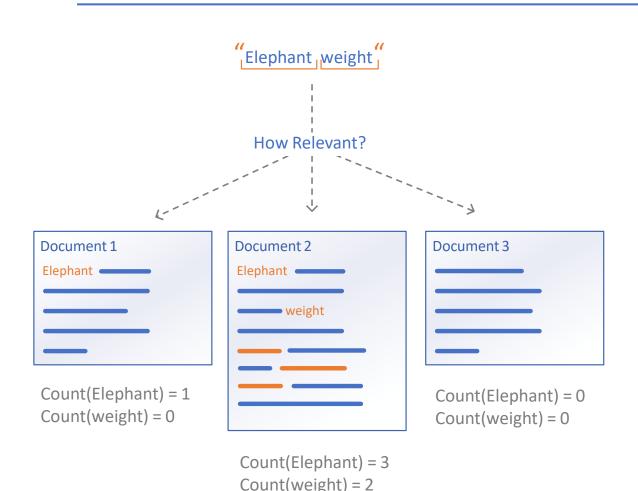


Notes on terminology

- **Documents** can be anything: a web page, word file, text file, article ... (we assume it to be text for the moment)
 - A lot of details to look out for: encoding, language, hierarchy, fields, ...
- Collection: A set of documents (we assume it to be static for the moment)

• **Relevance**: Does a document satisfy the information need of the user and does it help complete the user's task?

Relevance (based on text content)



- If a word appears more often -> more relevant
- Solution: count the words
- If a document is longer, words will tend to appear more often -> take into account the document length
- Counting only when we have a query is inefficient

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Inverted Index

- Inverted index allows to efficiently retrieve documents from large collections
- Inverted index stores all statistics per term (that the scoring model needs)
 - **Document frequency:** how many documents contain the term
 - Term frequency per document: how often does the term appear per document
 - Document length
 - Average document length
- Save statistics in a format that is accessible by a given term
- Save metadata of a document (Name, location of the full text, etc..)

Inverted Index

Document data

Term data

```
Document Ids & Metadata:

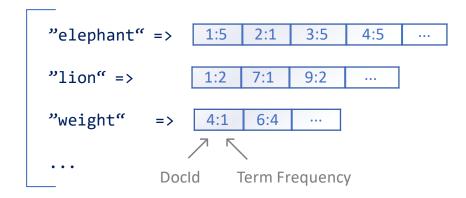
[0] = ("Wildlife", "location",...)

[1] = ("Zoo Vienna",...)

...

Document Lengths:

[0] = 231 [1] = 381 ...
```

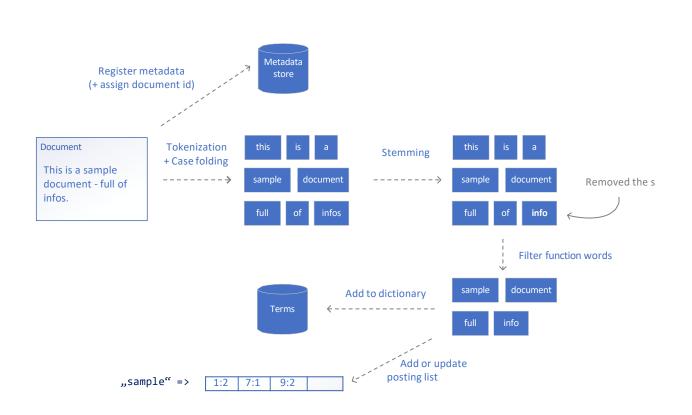


Every document gets an internal document id

 Term dictionary is saved as a search friendly data structure (more on that later)

 Term Frequencies are stored in a "posting list" = a list of doc id, frequency pairs

Creating the Inverted Index



Simplified example pipeline

Linguistic models are language dependent

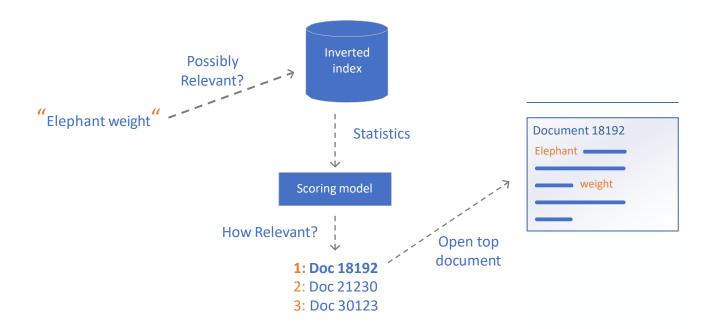
 A query text and a document text both have to undergo the same steps

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Querying the Inverted Index



No need to read full documents

 Only operate on frequency numbers of potentially relevant documents*

 Sort documents based on relevance score – retrieve most relevant documents

^{*} it's not that easy because a document could be relevant without containing the exact query terms – but for now keep it simple

Types of queries (including, but not limited to)

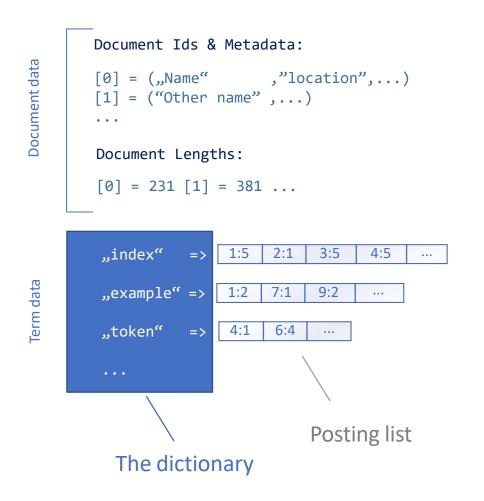
• Exact matching: match full words and concatenate multiple query words with "or"

Boolean queries: "and" / "or" / "not" operators between words

• **Expanded queries**: automatically incorporate synonyms and other similar or relevant words into the query

• Wildcard queries, phrase queries, phonetic queries (e.g. Soundex) ...

Inverted Index: Dictionary



- Dictionary<T> maps text to T
 - T is a posting list or potentially other data about the term depending on the index
- Wanted properties:
 - Random lookup
 - Fast (creation & especially lookup)
 - Memory efficient (keep the complete dictionary in memory)
- Naturally, there are a lot of choices

Scoring model

• Input: statistics, Output: floating point value (i.e. the score)

• Evaluated pairwise – 1 query, 1 document: score(q, d)

Capture the notion of relevance in a mathematical model

Today we focus on free-text queries & "ad-hoc" document retrieval

(document content only)

Search algorithm

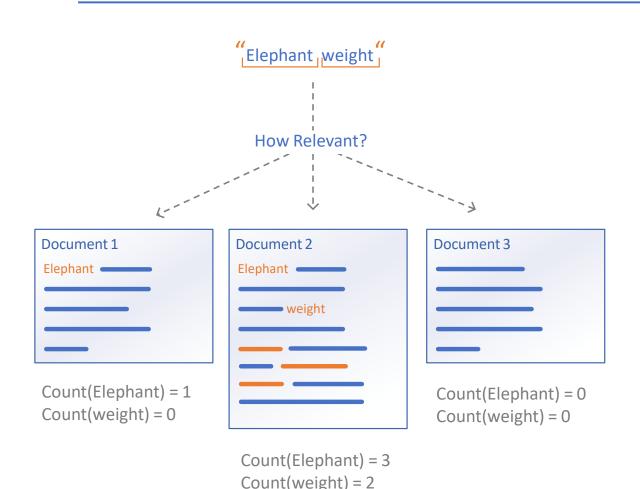
```
float Scores={}
```

for each query term qfetch posting list for qfor each pair(d, $tf_{t,d}$) in posting list if d not in Scores do Scores[d]=0 $Scores[d] += score(q, d, tf_{t,d}, ...)$

We transform information back to a document centric view (from the term centric view in the inverted index)

return Top *K* entries of *Scores*

Relevance



 If a word appears more often → more relevant

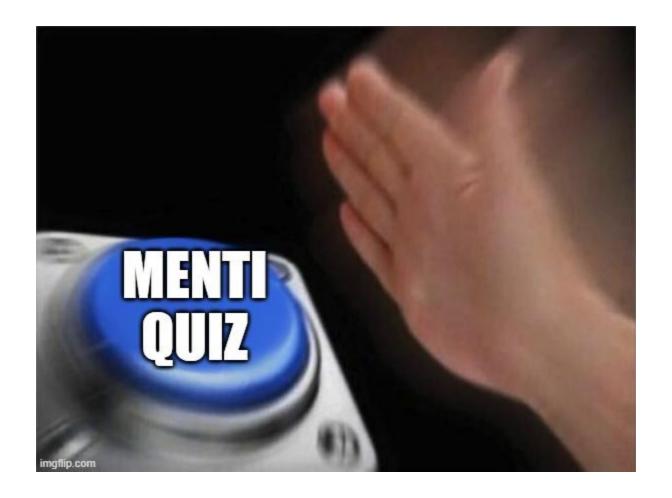
Solution: count the words

 If a document is longer, words will tend to appear more often → take into account the document length

Relevance limitations

- "Relevance" means relevance to the need rather than to the query
 - "Query" is shorthand for an instance of information need, its initial verbalized presentation by the user
- Relevance is assumed to be a binary attribute
 - A document is either relevant to a query/need or it is not
- We need these oversimplifications to create & evaluate mathematical models

From: A probabilistic model of information retrieval: development and comparative experiments, Spärck Jones et al. http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.134.6108&rep=rep1&type=pdf



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Term Frequency – conceptional data view

- Bag of words: word order is not important
- First step for a retrieval model: number of occurrences counts!
- $tf_{t,d}$ number of occurrences of term t in document d

		Documents					
		Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Terms	Antony	157	73	0	0	0	0
	Brutus	4	157	0	1	0	0
	Caesar	231	227	0	2	1	1
	Calpurnia	0	10	0	0	0	0
	Cleopatra	57	0	0	0	0	0
	mercy	2	0	3	5	5	1
	worser	2	0	1	1	1	0

Term Frequency – actual data storage

- Inverted index saves only non-0 entries, not the whole matrix
 - Otherwise we would waste a lot of storage capacity
- Therefore not good at random lookups into the document column
 - Needs to iterate through the posting list to find the correct document
 - However, for scoring models $tf_{t,d}$ with 0 can be skipped

```
      "elephant" =>
      1:5
      2:1
      3:5
      4:5
      ...

      "lion" =>
      1:2
      7:1
      9:2
      ...

      "weight" =>
      4:1
      6:4
      ...

      Docld
      Term Frequency
```

TF - Term Frequency

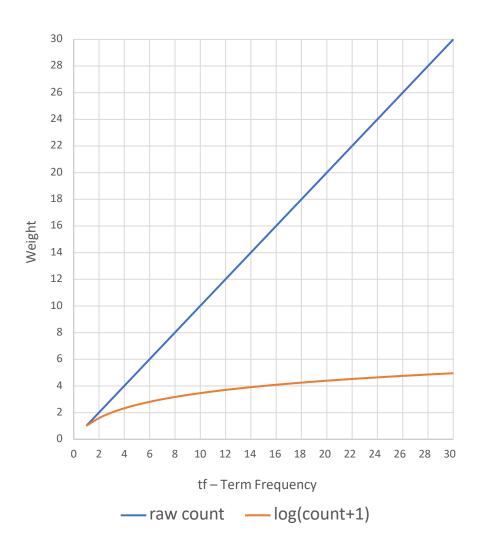
• $tf_{t,d}$ = how often does term t appear in document d

Powerful starting point for many retrieval models

Main point of our intuition at the beginning

- Using the raw frequency is not the best solution
 - Use relative frequencies
 - Dampen the values with logarithm

Term Frequency & Logarithm



- In long documents, a term may appear hundred of times.
- Retrieval experiments show that using the logarithm of the number of term occurrences is more effective than raw counts.
- Commonly used approach: apply logarithm

$$\log(1 + t f_{t,d})$$

Document Frequency

- df_t = in how many documents does term t appear in
- Rare terms are more informative than frequent terms
 - Recall function words (and, or, the, ...)
- Consider a term in the query that is rare in the collection
 - e.g., Darmstadt in a news corpora
- A document containing this term is very likely to be relevant to the query TU Darmstadt
- → We want a high weight for rare terms like *Darmstadt*.

IDF – Inverse Document Frequency

• A common way of defining the inverse document frequency of a term is as follows:

$$idf(t) = log \frac{|D|}{df_t}$$

- df_t is an inverse measure of the "informativeness" of the term
- $df_t \leq |D|$
- Logarithm is used also for idf to "dampen" its effect.

|D| Total # of documents

 df_t # of Documents with $tf_{t_-} > 0$

TF-IDF

$$TF_IDF(q,d) = \sum_{t \in T_d \cap T_q} \frac{\log(1 + tf_{t,d})}{df_t} * \frac{\log(\frac{|D|}{df_t})}{df_t}$$

increases with the number of occurrences within a document

increases with the rarity of the term in the collection

- A rare word (in the collection) appearing a lot in one document creates a high score
- Common words are downgraded

 $\sum_{t \in T_d \cap T_q}$ Sum over all query terms, that are in the index $f_{t,d}$ Term frequency $f_{t,d}$ Total # of documents

of Documents

with $tf_{t,d} > 0$

For more variations: https://en.wikipedia.org/wiki/Tf-idf

TF-IDF — Usage

- Useful not only as a standalone model in document retrieval
- Weights used as a base for many other retrieval models
 - Example: Vector Space Model (VSM) works better with tf-idf weights
- Also useful as a generic word weighting mechanism for NLP
 - Task agnostic importance of a word in a document in a collection
 - Assign every word in a collection its tf-idf score

BM25

- Created 1994 by Robertson et al.
- Grounded in probabilistic retrieval

• In general, BM25 improves on TF-IDF results

But only set as a default scoring in Lucene in 2015

Original paper: http://www.staff.city.ac.uk/~sb317/papers/robertson_walker_sigir94.pdf

TF-IDF vs BM25 in Lucene https://opensourceconnections.com/blog/2015/10/16/bm25-the-next-generation-of-lucene-relevation/

BM25 (as defined by Robertson et al. 2009)

$$BM25(q,d) = \sum_{t \in T_d \cap T_q} \frac{tf_{t,d}}{k_1((1-b) + b\frac{dl_d}{avgdl}) + tf_{t,d}} * log \frac{|D| - df_t + 0.5}{df_t + 0.5}$$

- Simpler than the original formula
 - Over time it was shown that more complex parts not needed

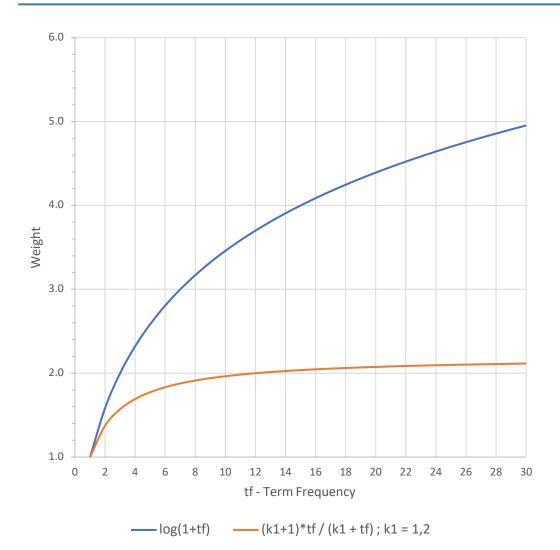
$\sum_{t \in T_d \cap T_q}$	Sum over all query terms, that are in the index
$tf_{t,d}$	Term frequency
dl_d	Document length
avgdl	Average document length in index
<i>D</i>	Total # of documents
df_t	# of Documents with $tf_{t,}>0$
k_1 , b	Hyperparameters

BM25 vs. TF-IDF

Simple case of BM25 looks a lot like TF-IDF

- 1 main difference: BM25 tf component contains saturation function
 - Therefore works better in practice
- BM25 variants can be adapted to:
 - Incorporate additional reference information
 - Long(er) queries
 - multiple fields

BM25 vs. TF-IDF - Saturation



 TF-IDF: weight is always increasing (even with log)

• **BM25:** diminishing returns quickly = asymptotically approaches $k_1 + 1$

Note: we added (k_1+1) to the numerator to make tf@1 = 1, but it does not change the ranking because it is added to every term

Note: we assume the doc length = avgdl

BM25 vs. TF-IDF - Example

- Suppose your query is "machine learning"
- Suppose you have 2 documents with term counts:
 - doc1: learning 1024; machine 1
 - doc2: learning 16; machine 8
- TF-IDF: $\log(tf) * \log(|D|/df)$ BM25: $k_1 = 2$
 - doc1: 11 * 7 + 1 * 10 = 87
 - doc2: 5*7+4*10=75

- doc1: 3*7+1*10=31
- doc2: 2.67*7 + 2.4*10 = 42.7

Hyperparameters

- k_1 , b are hyperparameters = they are set by us, the developers
- k_1 controls term frequency scaling
 - k_1 = 0 is binary model; k_1 large is raw term frequency
- b controls document length normalization
 - b = 0 is no length normalization; b = 1 is relative frequency (fully scale by document length)
- Common ranges: 0.5 < b < 0.8 and $1.2 < k_1 < 2$

Summary: Part 1

1 We save statistics about terms in an inverted index

2 The statistics in the index can be access by a given term (query)

3 TF-IDF & BM25 use term and document frequencies to score a query & doc

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Evaluation

- We evaluate systems to observe concrete evidence for a hypothesis
 - Is our system better than the other one?
- IR systems are hard to evaluate
 - Ambiguity what is relevant? In which context? Humans differ a lot ...
 - Collection size explosion of query-document pairs
- Different types of result quality evaluation:
 - Intrinsic: Fixed set: same collection, query set & labels
 - Extrinsic: Observe behavior of users (in production system)*

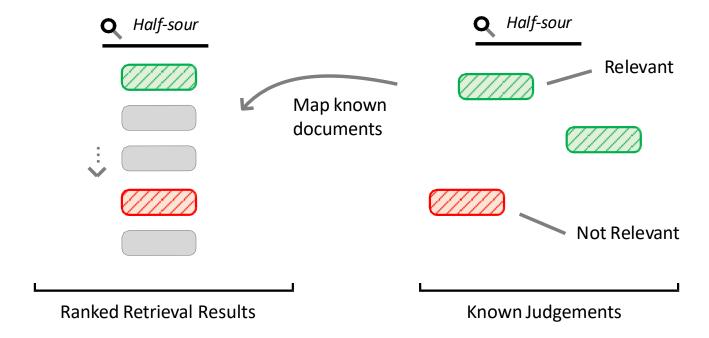
^{*} Could also be a user study, beta version, etc...

The World of Evaluation

- Today we focus on evaluating the result quality of our own IR system
 - Does a document contain the answer for our query?
- Many other possibilities:
 - Efficiency
 - How fast can we index, return results for a query, how large becomes our index on disk?
 - Fairness, diversity, content quality, source credibility, effort, ...
 - Retrieval in the context of a larger goal
 - How many products, services do we sell through search
 - How well does our website integrate with Google, Bing, etc.. (SEO)
 - Optimizing a Blackbox

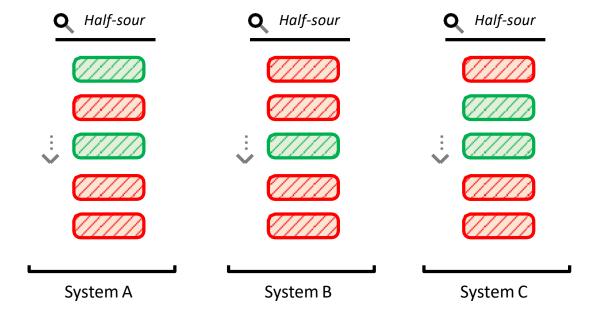
Extrinsic Evaluation Setup

- Quality of systems, that produce ranked list of documents
- Compared by a pool of judgements (does not necessarily cover the whole list)
 - Missing judgements are often considered as non-relevant



Comparing Systems

- We have multiple IR systems running on the same documents & same query
- How to compare them? Evaluation metrics to the rescue!

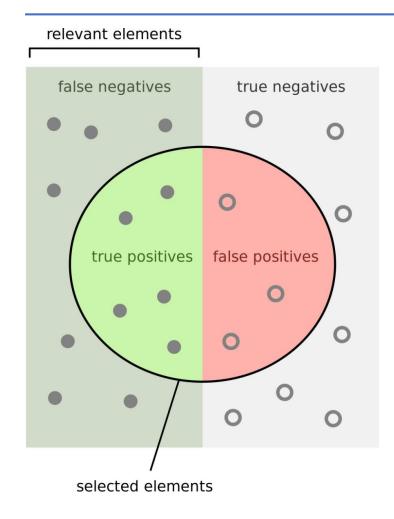


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Precision & Recall



How many selected items are relevant?

How many relevant items are selected?

From: Wikipedia https://en.wikipedia.org/wiki/Precision and recall

Precision/recall tradeoff

- You can increase recall (R) by returning more documents
 - Recall is a non-decreasing function of the number of documents retrieved
 - A system that returns all docs has 100% recall!
- The converse is also true: It's easy to get high precision (P) for very low recall
- Combined measure F-score:
- allows us to trade off precision against recall
- Mostly used measure: F1 or the harmonic mean of P and R

$$F_1 = 2 \times \frac{P \times R}{P + R}$$

Example for precision, recall, F1

	Relevant	Non-relevant	
Retrieved	20	40	60
Not retrieved	60	1,000,000	1,000,060
	80	1,000,040	1,000,120

$$P = \frac{20}{(20 + 40)} = \frac{1}{3}$$

$$R = \frac{20}{(20 + 60)} = \frac{1}{4}$$

$$F1 = 2 \times \frac{\frac{1}{3} \times \frac{1}{4}}{\frac{1}{3} + \frac{1}{4}} = \frac{2}{7}$$

Not retrieved FN TN $P = \frac{TP}{TP + FP}$						

$$P = \frac{TP}{TP + FP}$$

$$R = \frac{TP}{TP}$$

$$F_1 = 2 \times \frac{P \times R}{P + R}$$

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Ranking List Evaluation Metrics

- Binary labels
 - MRR: Mean Reciprocal Rank
 - MAP: Mean Average Precision
- Graded labels
 - nDCG: normalized Discounted Cumulative Gain

- Typically we measure at a cutoff @k of the top retrieved documents
 - MAP, Recall: @100, @1000
 - Precision, MRR, nDCG: @5, @10, @20

MRR: Mean Reciprocal Rank

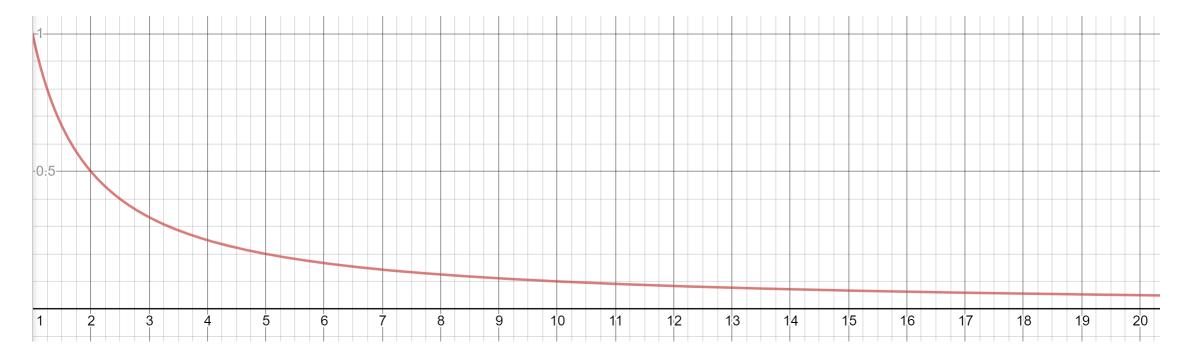
Users look at results from the top; gets annoyed pretty fast; stops once they found the first relevant; doesn't care about the rest

$$MRR(Q) = \frac{1}{|Q|} * \sum_{q \in Q} \frac{1}{FirstRank(q)}$$
 Reciprocal Rank

- MRR puts the focus on the first relevant document
- Applicable with sparse judgements or assuming users are satisfied with one relevant document

MRR: The Reciprocal Rank

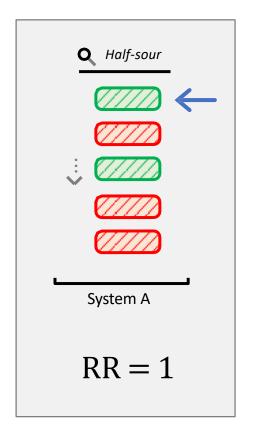
- Reciprocal Rank: $\frac{1}{x}$
- Very strongly emphasis the first position

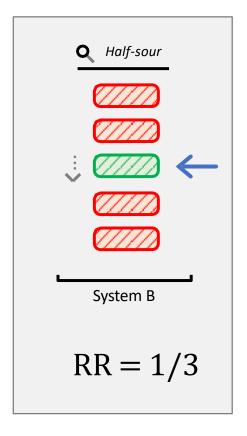


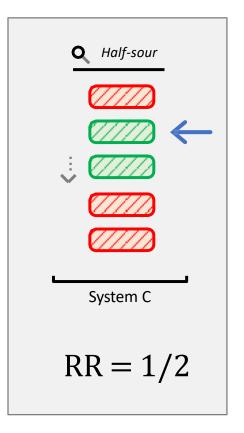
^{*} x is plotted continuously, but in MRR x is discrete with the position in step size of 1

MRR: An Example

• Example for Reciprocal Rank:







MAP: Mean Average Precision

Users look at results closely, every time they find a new relevant document, they look at the full picture of what has been before

Mean over all queries Precision per relevant doc
$$MAP(Q) = \frac{1}{|Q|} * \sum_{q \in Q} \frac{\sigma_{i=1}^k \ P(q)_{@i} * rel(q)}{|rel(q)|}$$
 Average Precision

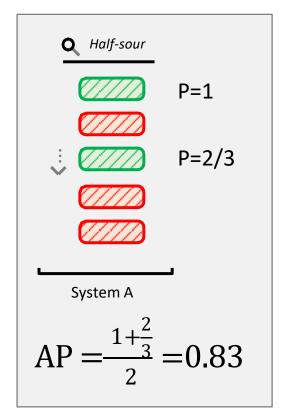
- MAP squeezes complex evaluation into a single number
- Hard to interpret
- MAP corresponds to the area under the Precision-Recall curve

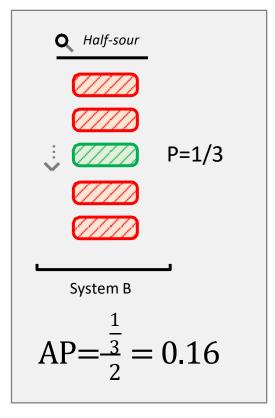
19

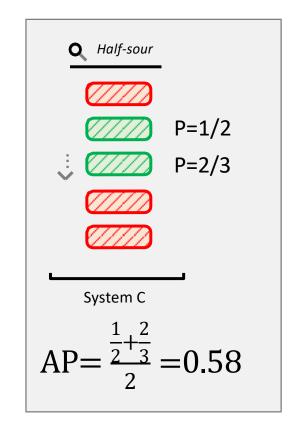
Q | Q | $P(q)_{@}$ | rel(q) | rel(q) | rel(q) | Query Set Number of Queries | Precision of query q | Binary Relevance of | Number of relevant | doc at position i | documents

MAP: Mean Average Precision

- Example for Average Precision (2 relevant docs)
 - Mean is then calculated for multiple queries, for each system







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Graded Relevance

- Previous metrics all use binary relevance labels
 - Simple enough or too simple?
- Major problem: Of course there can be a difference in importance of relevance
 - Binary labels can not distinguish
- Graded relevance allows to assign different values of relevance
 - Can be floating point or fixed set of classes for manual annotation
 - Fixed set of classes for manual annotation
 - Floating point can be used when relevance inferred from logs

Common Graded TREC Relevance Labels

- [3] Perfectly relevant: Document is dedicated to the query, it is worthy of being a top result in a search engine.
- [2] Highly relevant: The content of this document provides substantial information on the query.
- [1] Relevant: Document provides some information relevant to the query, which may be minimal.
- [0] Irrelevant: Document does not provide any useful information about the query

nDCG: normalized Discounted Cumulative Gain

Users take for each document the relevance grade and position into account, normalize by best possible ranking per query

$$DCG(D) = \sum_{\substack{d \in D, i=1}} \frac{rel(d)}{log_2(i+1)}$$

$$nDCG(Q) = \frac{1}{|Q|} * \sum_{q \in Q} \frac{DCG(q)}{DCG(sorted(rel(q)))}$$

- nDCG compares actual results with maximum per query
- Relevance is graded
- nDCG@10 most commonly used in modern offline web search evaluation

Q	Q	D	rel(d)	rel(q)	sorted()	
Query Set	# of Queries	Single Doc. Result list	Relevance grade for single query-doc pair	List of all relevance grades for a query	Return graded documents by descending relevance	24

nDCG: A Closer Look

Discounted cumulative gain

$$\overline{DCG(D)} = \sum_{d \in D, i=1}^{\sum} \frac{rel(d)}{log_2(i+1)}$$
 Gain (relevance value, commonly 0 -> 3)

Position Discounting

$$nDCG(Q) = \frac{1}{|Q|} * \sum_{q \in Q} \frac{DCG(q)}{DCG(sorted(rel(q)))}$$
Best possible sorting (ground truth)

Mean over all queries

Q |Q| Query Set # of Queries

*D*Single Doc.

Result list

rel(d)Relevance grade for single query-doc pair

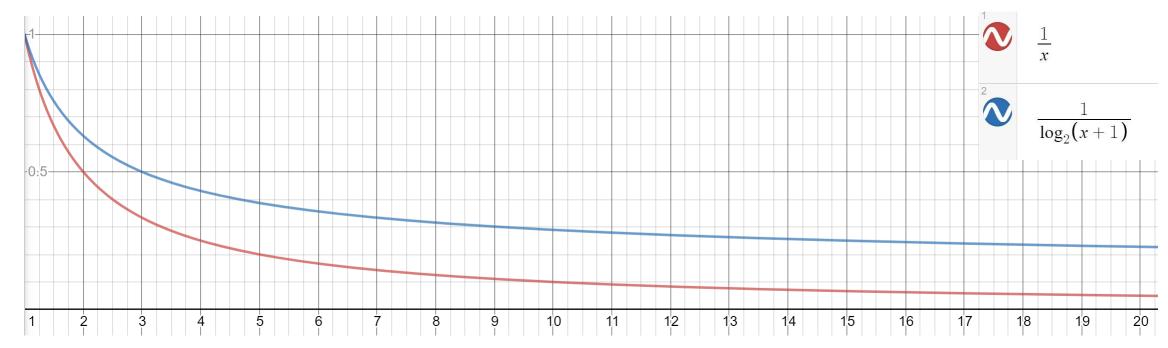
rel(q)List of all relevance grades for a query

Return graded documents by descending relevance

sorted()

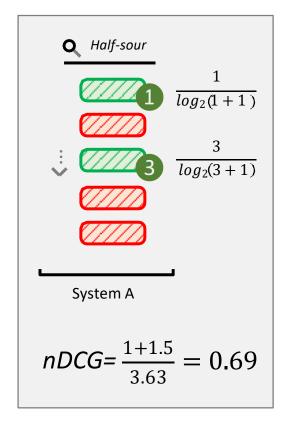
nDCG: Position Discounting

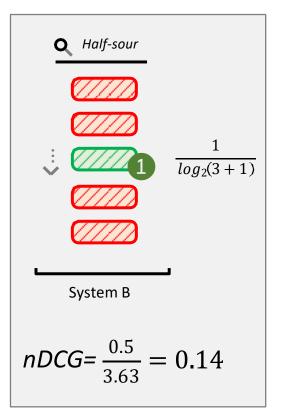
- Comparing the document position discount with reciprocal rank
 - Only for binary case rel=1
- nDCG discounts less than MRR

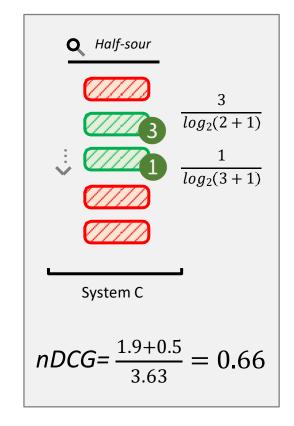


nDCG: Example

- Assuming two differently relevant docs (rel = 3 & 1)
 - Ideal DCG = $\frac{3}{\log_2(1+1)} + \frac{1}{\log_2(2+1)} = 3.63$







Summary: Part 2

1 We compare systems with a set of query and document relevance labels

2 Binary metrics (MRR & MAP) are a solid foundation for evaluation

3 Graded relevance allows for more fine-grained metrics (nDCG)