

1. Construct a truth table for the following:

a.  $(x + y)(x + z)(x' + z)$

**Ans**

x	y	z	x'	x + y	x + z	x' + z	$(x + y)(x + z)(x + z)$
0	0	0	1	0	0	1	0
0	0	1	1	0	1	1	0
0	1	0	1	1	0	1	0
0	1	1	1	1	1	1	1
1	0	0	0	1	1	0	0
1	0	1	0	1	1	1	1
1	1	0	0	1	1	0	0
1	1	1	0	1	1	1	1

2. Show that  $x = xy + xy'$

a. Using truth tables

x	y	y'	xy	xy'	xy + xy'
0	0	1	0	0	0
0	1	0	0	0	0
1	0	1	0	1	1
1	1	0	1	0	1

b. Using Boolean identities

$$x = xy + xy' = x(y+y') \text{ \# Distributive Law}$$

$$= x(1) \text{ \# Inverse Law}$$

$$= x \text{ \# Identity Law}$$

Ans  $\therefore x = xy + xy'$

2. Given the function:  $F(x,y,z) = xy'z + x'y'z + xyz$

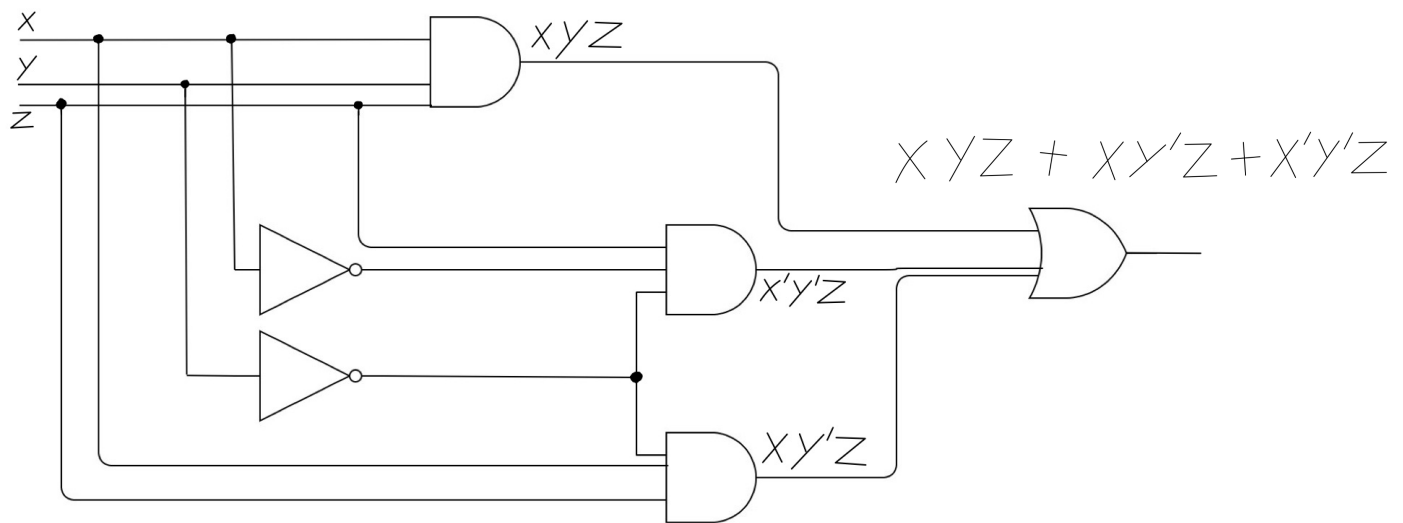
a. List the truth table for F.

**Ans**

x	y	z	x'	y'	xyz	xy'z	x'y'z	xy'z + x'y'z + xyz
0	0	0	1	1	0	0	0	0
0	0	1	1	1	0	0	1	1
0	1	0	1	0	0	0	0	0
0	1	1	1	0	0	0	0	0
1	0	0	0	1	0	0	0	0
1	0	1	0	1	0	1	0	1
1	1	0	0	0	0	0	0	0
1	1	1	0	0	1	0	0	1

b. Draw the logic diagram using the original Boolean expression

**Ans**



c. Simplify the expression using Boolean algebra and identities.

Ans

$$F(x,y,z) = xy'z + x'y'z + xyz \text{ \# Idempotent Law}$$

$$= z(xy' + x'y' + xy) \text{ \# Distributive Law}$$

$$= z(x(y + y') + x'y') \text{ \# Commutative \& Distributive Laws}$$

$$= z(x(1) + x'y') \text{ \# Inverse Law}$$

$$= z(x + x'y') \text{ \# Identity Law}$$

$$= z((x + x')(x + y')) \text{ \# Distributive Law}$$

$$= z((1)(x + y')) \text{ \# Inverse Law}$$

$$= z(x + y') \text{ \# Identity Law}$$

$$= xz + y'z \text{ \# Distributive Law}$$

d. Simplify the expression using KMap

Ans

x \ yz	00	01	11	10
0	0	1	0	0
1	0	1	1	0

$xy'z$

$xy'z$

$x'y'z$

$xyz$



$y'z + xz \longrightarrow y'z + xz \text{ \# Simplified}$

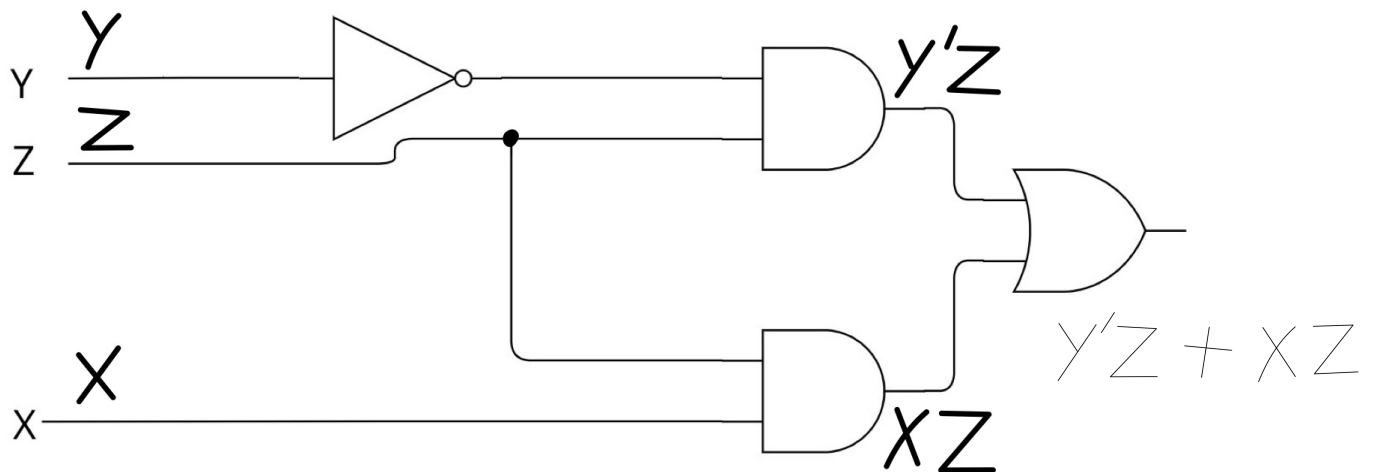
e. List the truth table for your answer in Part d.

**Ans**

x	y	z	y'	xz	y'z	y'z + xz
0	0	0	1	0	0	0
0	0	1	1	0	1	1
0	1	0	0	0	0	0
0	1	1	0	0	0	0
1	0	0	1	0	0	0
1	0	1	1	1	1	1
1	1	0	0	0	0	0
1	1	1	0	1	0	1

f. Draw the logic diagram for the simplified expression in Part d.

**Ans**



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