

Algorithms for linear regression

Exploratory variables are geometry coefficients and the Froude number:

1. Longitudinal position of the center of buoyancy, adimensional.
2. Prismatic coefficient, adimensional.
3. Length-displacement ratio, adimensional.
4. Beam-draught ratio, adimensional.
5. Length-beam ratio, adimensional.
6. Froude number, adimensional.

The target histogram negative variable is the residuary resistance per unit weight of displacement:

7. Resistance: Residuary resistance per unit weight of displacement, adimensional.

Take the log of the target?

Yes, if we plot *Resistance* we see a significant right skew. However if we plot the histogram of the logarithm of *Resistance*, we see a distribution that looks much more like a normal distribution:

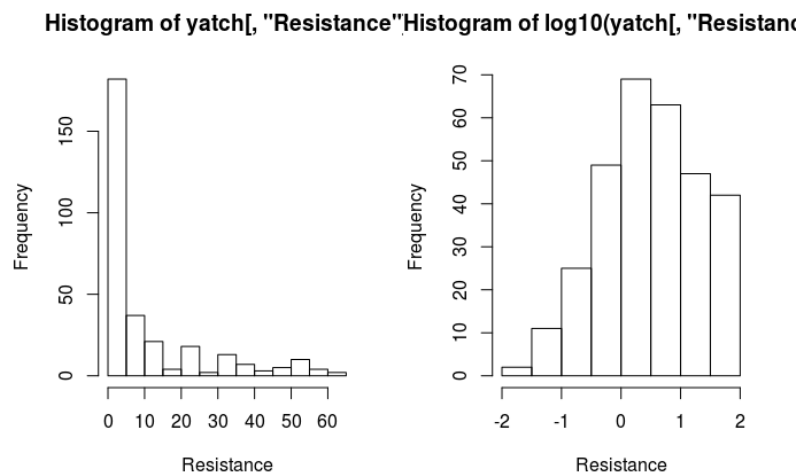


Figure 1 - log of the target

LINEAR REGRESSION

Only correlation *Froude.No* – *Resistance* seems significant, other columns are omitted.

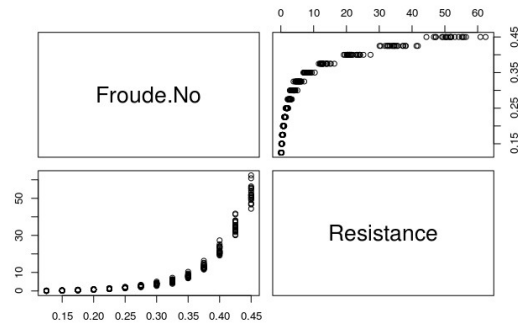


Figure 2 - correlations

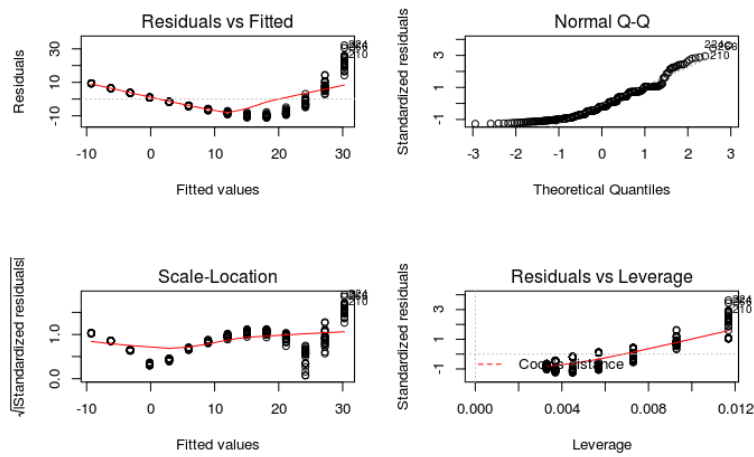


Figure 3 - model main plots

Independent variables, as well as dependent, are transformed:

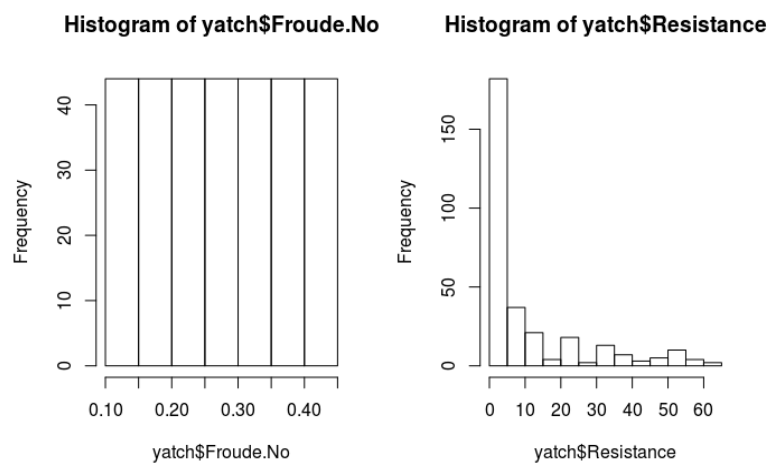


Figure 4 - original histogram independent/dependant var

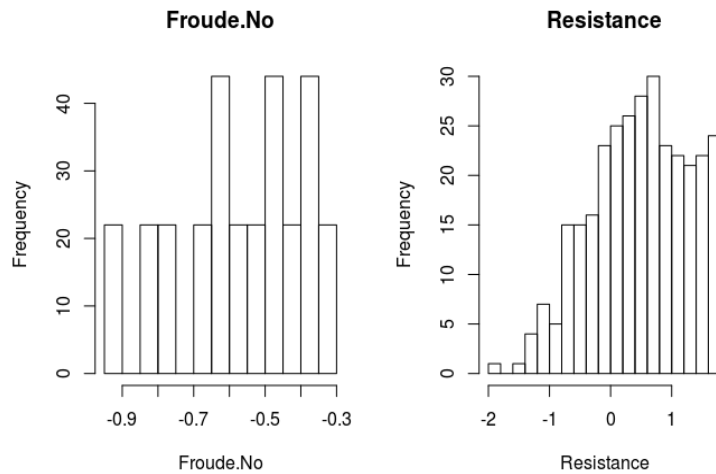


Figure 5 - histogram transformed variables - $\log_{10}(x)$

```
Call:
lm(formula = yacht$Resistance ~ ., data = yacht)

Residuals:
    Min       1Q   Median       3Q      Max
-11.240  -7.669  -1.726   6.404  32.154

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  -24.484     1.534  -15.96  <2e-16 ***
Froude.No    121.668     5.034   24.17  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.903 on 306 degrees of freedom
Multiple R-squared:  0.6562, Adjusted R-squared:  0.6551
F-statistic: 584.2 on 1 and 306 DF, p-value: < 2.2e-16
```

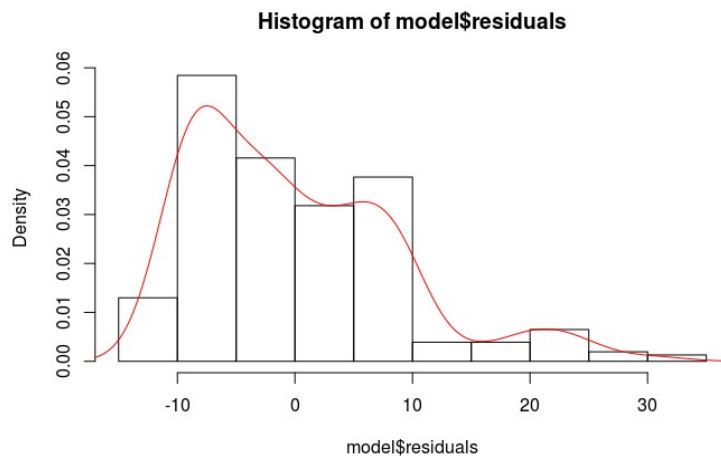


Figure 6 - Histogram of model residuals

Taking the whole variables does not provide any special benefit:

```
Call:
lm(formula = yacht$Resistance ~ ., data = yacht)

Residuals:
    Min       1Q   Median       3Q      Max
-11.770  -7.565  -1.881   6.112  31.572

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)    -19.2367    27.1133  -0.709   0.479
Longitudinal.pos      0.1938     0.3381   0.573   0.567
Prismatic.coeff    -6.4194    44.1590  -0.145   0.885
Length.displ       4.2330    14.1651   0.299   0.765
Beam.draught..... -1.7657     5.5212  -0.320   0.749
Length.beam       -4.5164    14.2000  -0.318   0.751
Froude.No        121.6676     5.0658  24.018 <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.96 on 301 degrees of freedom
Multiple R-squared:  0.6576,    Adjusted R-squared:  0.6507
F-statistic: 96.33 on 6 and 301 DF,  p-value: < 2.2e-16
```

Our model does not look fine, even with centering, scaling, or with the already applied *log* transform, results do not improve much.

RIDGE REGRESSION

Find lambdas:

```
> lambdes <- seq(0.001,0.5,0.001)
> select(lm.ridge(model, lambda = lambdes))
```

Get model:

```
> lambdes[which.min(model.ridge$GCV)]
0.001
> model.ridge<-lm.ridge(model, lambda = 0.001)
```

Prediction error:

```
> norm.root.mse.LOOCV
> sqrt(model.ridge$GCV)
0.5147124
```

...