onnx fft

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1 ONNX and FFT

ONNX does not fully support complex yet. It does not have any FFT operators either. What if we need them anyway?

[3]: '1.21.5'

1.1 Python implementation of RFFT

We try to replicate numpy.rfft.

```
[4]: import numpy
     def almost_equal(a, b, error=1e-5):
         The function compares two matrices, one may be complex. In that case,
         this matrix is changed into a new matrix with a new first dimension,
         [0,::] means real part, [1,::] means imaginary part.
         if a.dtype in (numpy.complex64, numpy.complex128):
             dtype = numpy.float64 if a.dtype == numpy.complex128 else numpy.float32
             new_a = numpy.empty((2,) + a.shape).astype(dtype)
             new a[0] = numpy.real(a)
            new_a[1] = numpy.imag(a)
             return almost_equal(new_a, b, error)
         if b.dtype in (numpy.complex64, numpy.complex128):
            return almost_equal(b, a, error)
         if a.shape != b.shape:
             raise AssertionError("Shape mismatch %r != %r." % (a.shape, b.shape))
         diff = numpy.abs(a.ravel() - b.ravel()).max()
         if diff > error:
```

```
raise AssertionError("Mismatch max diff=%r > %r." % (diff, error))
     def dft_real_cst(N, fft_length):
         n = numpy.arange(N)
         k = n.reshape((N, 1)).astype(numpy.float64)
         M = numpy.exp(-2j * numpy.pi * k * n / fft_length)
         both = numpy.empty((2,) + M.shape)
         both[0, :, :] = numpy.real(M)
         both[1, :, :] = numpy.imag(M)
         return both
     def dft_real(x, fft_length=None, transpose=True):
         if len(x.shape) == 1:
             x = x.reshape((1, -1))
             N = 1
         else:
             N = x.shape[0]
         C = x.shape[-1] if transpose else x.shape[-2]
         if fft_length is None:
             fft_length = x.shape[-1]
         size = fft_length // 2 + 1
         cst = dft_real_cst(C, fft_length)
         if transpose:
             x = numpy.transpose(x, (1, 0))
             a = cst[:, :, :fft_length]
             b = x[:fft_length]
             res = numpy.matmul(a, b)
             res = res[:, :size, :]
             return numpy.transpose(res, (0, 2, 1))
         else:
             a = cst[:, :, :fft length]
             b = x[:fft_length]
             return numpy.matmul(a, b)
     rnd = numpy.random.randn(5, 7).astype(numpy.float32)
     fft_np = numpy.fft.rfft(rnd)
     fft_cus = dft_real(rnd)
     fft_np
[4]: array([[-0.33227623+0.j
                                     , -1.53729601-0.93413037j,
              4.47973719 + 2.89019374 \mathtt{j}, \quad 1.36392938 - 2.59133368 \mathtt{j} \mathtt{]},
                                    , 0.51947711+0.624144j
            [ 0.07591467+0.j
             -2.48242622-1.56579382j, -0.98728199+2.81434946j],
            [-0.55875075+0.j
                                    , -0.83228203+2.25251549j,
              0.48281369+2.69338405j, -0.86559293+0.08437194j],
            [ 0.26185111+0.j
                                    , -1.18143684+1.73623491j,
              0.96002386+0.39340971j, 3.53861562-1.32858241j],
            [ 1.06276855+0.j
                                    , 3.07258661-2.71505518j,
             -0.82579331-1.91852778j, 4.10811113-0.46836687j]])
```

Function almost_equal verifies both functions return the same results.

```
[5]: almost_equal(fft_np, fft_cus)
    Let's do the same with fft_length < shape[1].
[6]: fft np3 = numpy.fft.rfft(rnd, n=3)
     fft_cus3 = dft_real(rnd, fft_length=3)
     fft np3
                                   , 2.20926839+0.35688821j],
[6]: array([[-0.86976612+0.j
            [ 0.33280143+0.j
                                   , -1.41451804+0.2065253j ],
                                   , 0.51297992+0.62331197i],
            [-2.30690554+0.j
                                   , 1.84198139+1.07546916j],
            [-0.72842433+0.j
            [ 4.17533261+0.j
                                   , 0.86360028+0.36508775j]])
[7]: almost equal(fft np3, fft cus3)
```

1.2 RFFT in ONNX

Let's assume first the number of column of the input matrix is fixed. The result of function dft_real_cst can be considered as constant.

```
[8]: from typing import Any
     import mlprodict.npy.numpy onnx impl as npnx
     from mlprodict.npy import onnxnumpy_np
     from mlprodict.npy.onnx_numpy_annotation import NDArrayType
     # from mlprodict.onnxrt import OnnxInference
     @onnxnumpy_np(signature=NDArrayType(("T:all", ), dtypes_out=('T',)))
     def onnx_rfft(x, fft_length=None):
         if fft_length is None:
             raise RuntimeError("fft_length must be specified.")
         size = fft_length // 2 + 1
         cst = dft real cst(fft length, fft length).astype(numpy.float32)
         xt = npnx.transpose(x, (1, 0))
         res = npnx.matmul(cst[:, :, :fft_length], xt[:fft_length])[:, :size, :]
         return npnx.transpose(res, (0, 2, 1))
     fft_onx = onnx_rfft(rnd, fft_length=rnd.shape[1])
     fft onx
```

```
[8]: array([[[-0.33227617, -1.5372959 , 4.4797373 , 1.3639294],
            [0.07591468, 0.51947707, -2.4824262, -0.98728204],
            [-0.5587506, -0.8322822, 0.48281363, -0.86559296],
            [0.26185107, -1.1814368, 0.96002394, 3.5386157],
            [1.0627685, 3.0725865, -0.8257934, 4.108111]],
           [[ 0.
                        , -0.93413043, 2.890194 , -2.5913336 ],
            [ 0.
                          0.624144 , -1.5657941 , 2.8143494 ],
            [ 0.
                        , 2.2525156 , 2.6933842 , 0.08437189],
            [ 0.
                        , 1.7362347 , 0.39340976, -1.3285824 ],
                        , -2.7150555 , -1.9185277 , -0.4683669 ]]],
            [ 0.
          dtype=float32)
```

```
[9]: almost_equal(fft_cus, fft_onx)
    The corresponding ONNX graph is the following:
[10]: %onnxview onnx_rfft.to_onnx()

[10]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x25b38b3f9d0>
[11]: fft_onx3 = onnx_rfft(rnd, fft_length=3)
    almost_equal(fft_cus3, fft_onx3)
```

1.3 FFT 2D

Below the code for complex features.

```
[12]: def _DFT_cst(N, fft_length, trunc=True):
          n = numpy.arange(N)
          k = n.reshape((N, 1)).astype(numpy.float64)
          M = numpy.exp(-2j * numpy.pi * k * n / fft_length)
          return M[:fft_length // 2 + 1] if trunc else M
      def DFT(x, fft_length=None, axis=1):
          if axis == 1:
              x = x.T
          if fft_length is None:
              fft length = x.shape[0]
          cst = _DFT_cst(x.shape[0], fft_length, trunc=axis==1)
          if axis == 1:
              return numpy.matmul(cst, x).T
          return numpy.matmul(cst, x)
      def fft2d_(mat, fft_length):
          mat = mat[:fft_length[0], :fft_length[1]]
          res = mat.copy()
          res = DFT(res, fft_length[1], axis=1)
          res = DFT(res, fft_length[0], axis=0)
          return res[:fft_length[0], :fft_length[1]//2 + 1]
      rnd = numpy.random.randn(5, 7).astype(numpy.float32)
      fft2d np = fft2d (rnd, rnd.shape)
      fft2d_np = numpy.fft.rfft2(rnd)
      fft2d_np_
```

```
[12]: array([[-4.14039719 +0.j , -1.06715605 +1.16770652j, -0.27080808 +1.93562775j, 5.28785846 +2.27915445j], [-2.57576449 +3.09907081j, -8.90391777 -5.56953367j, -1.6455202 +2.03337471j, 4.21121677 -1.85803104j], [ 1.84529583 -0.54705419j, 3.61232172 -4.11661604j, 1.00659205 +3.72264071j, -0.36878039 -8.21956881j], [ 1.84529583 +0.54705419j, -1.173484 +5.12345283j, -1.7897386 -10.15322422j, -0.17258219 +2.37388952j], [ -2.57576449 -3.09907081j, 0.58355627 +1.62293628j, 0.71779814 +4.64582025j, -6.32441255 -4.21906685j]])
```

```
[13]: almost_equal(fft2d_np_, fft2d_np)
```

It implies the computation of two FFT 1D along both axes. However, as ONNX does not support complex, it needs to be rewritten with only real numbers. The algorithm can be summarized into this formula FFT(FFT(x,axis=1),axis=0). If x is real, FFT(x,.) is complex. We still assume x is real, it then becomes (FFT is a linear operator, so FFT(ix) = iFFT(x)):

```
\begin{array}{ll} \bullet & y = FFT(x, axis = 1) \\ \bullet & z_r = FFT(Real(y), axis = 0), \ z_i = FFT(Imag(y), axis = 0) \\ \bullet & z = z_r + iz_i \end{array}
```

z is the desired output. The following implementation is probably not the most efficient one. It avoids inplace computation as ONNX does like that.

```
def fft2d(mat, fft_length):
    mat = mat[:fft_length[0], :fft_length[1]]
    res = mat.copy()

# first FFT
res = dft_real(res, fft_length=fft_length[1], transpose=True)

# second FFT decomposed on FFT on real part and imaginary part
    res2_real = dft_real(res[0], fft_length=fft_length[0], transpose=False)
    res2_imag = dft_real(res[1], fft_length=fft_length[0], transpose=False)
    res2_imag2 = numpy.vstack([-res2_imag[1:2], res2_imag[:1]])
    res = res2_real + res2_imag2
    size = fft_length[1]//2 + 1
    return res[:, :fft_length[0], :size]

fft2d_np = numpy.fft.rfft2(rnd)
fft2d_cus = fft2d(rnd, rnd.shape)
almost_equal(fft2d_np, fft2d_cus)
```

```
[15]: fft2d_np
```

```
[16]: fft2d_cus
```

```
[16]: array([[[ -4.14039719,
                             -1.06715605, -0.27080808,
                                                          5.28785846],
              [-2.57576449,
                             -8.90391777, -1.6455202,
                                                          4.21121677],
              [ 1.84529583,
                              3.61232172,
                                            1.00659205,
                                                         -0.36878039],
              [ 1.84529583,
                             -1.173484
                                           -1.7897386 ,
                                                         -0.17258219],
              [-2.57576449,
                              0.58355627,
                                            0.71779814, -6.32441255]
```

And with a different fft_length.

```
[17]: fft2d_np = numpy.fft.rfft2(rnd, (4, 6))
fft2d_cus = fft2d(rnd, (4, 6))
almost_equal(fft2d_np[:4, :], fft2d_cus)
```

1.4 FFT 2D in ONNX

We use again the numpy API for ONNX.

```
[18]: def onnx_rfft_1d(x, fft_length=None, transpose=True):
          if fft length is None:
              raise RuntimeError("fft_length must be specified.")
          size = fft_length // 2 + 1
          cst = dft_real_cst(fft_length, fft_length).astype(numpy.float32)
          if transpose:
              xt = npnx.transpose(x, (1, 0))
              res = npnx.matmul(cst[:, :, :fft_length], xt[:fft_length])[:, :size, :]
              return npnx.transpose(res, (0, 2, 1))
          else:
              return npnx.matmul(cst[:, :, :fft_length], x[:fft_length])
      @onnxnumpy_np(signature=NDArrayType(("T:all", ), dtypes_out=('T',)))
      def onnx rfft 2d(x, fft length=None):
          mat = x[:fft length[0], :fft length[1]]
          # first FFT
          res = onnx_rfft_1d(mat, fft_length=fft_length[1], transpose=True)
          # second FFT decomposed on FFT on real part and imaginary part
          res2_real = onnx_rfft_1d(res[0], fft_length=fft_length[0], transpose=False)
          res2_imag = onnx_rfft_1d(res[1], fft_length=fft_length[0], transpose=False)
          res2_imag2 = npnx.vstack(-res2_imag[1:2], res2_imag[:1])
          res = res2_real + res2_imag2
          size = fft_length[1]//2 + 1
          return res[:, :fft_length[0], :size]
      fft2d_cus = fft2d(rnd, rnd.shape)
      fft2d_onx = onnx_rfft_2d(rnd, fft_length=rnd.shape)
      almost equal(fft2d cus, fft2d onx)
```

The corresponding ONNX graph.

```
[19]: %onnxview onnx_rfft_2d.to_onnx()
```

[19]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x25b44365b50>

```
[20]: with open("fft2d.onnx", "wb") as f:
    f.write(onnx_rfft_2d.to_onnx().SerializeToString())
```

With a different fft_length.

```
[21]: fft2d_cus = fft2d(rnd, (4, 5))
fft2d_onx = onnx_rfft_2d(rnd, fft_length=(4, 5))
almost_equal(fft2d_cus, fft2d_onx)
```

This implementation of FFT in ONNX assumes shapes and fft lengths are constant. Otherwise, the matrix returned by function dft real cst must be converted as well. That's left as an exercise.

1.5 FFT2D with shape (3,1,4)

Previous implementation expects the input matrix to have two dimensions. It fails with 3.

```
[22]: shape = (3, 1, 4)
  fft_length = (1, 4)
  rnd = numpy.random.randn(*list(shape)).astype(numpy.float32)
  fft2d_numpy = numpy.fft.fft2(rnd, fft_length)
  fft2d_numpy.shape
```

```
[22]: (3, 1, 4)
```

```
[23]: fftt2d_numpy
```

```
[24]: try:
    fft2d_cus = fft2d(rnd, fft_length)
except Exception as e:
    print(e)
# fft2d_onx = onnx_rfft_2d(rnd, fft_length=fft_length)
```

axes don't match array

1.5.1 numpy version

Let's do it again with numpy first. fft2 performs fft2 on the last two axis as many times as the first axis. The goal is still to have an implementation which works for any dimension.

```
[25]: conc = []
for i in range(rnd.shape[0]):
    f2 = fft2d(rnd[i], fft_length)
    conc.append(numpy.expand_dims(f2, 0))
res = numpy.vstack(conc).transpose(1, 0, 2, 3)
almost_equal(fft2d_numpy[:, :, :3], res)
```

It works. And now a more efficient implementation. It is better to read matmul description before. To summarize, a third axis is equivalent to many matrix multiplications over the last two axes, as many as the dimension of the first axis: $matmul(A[I,J,K], B[I,K,L]) \longrightarrow C[I,J,L]$. Broadcasting also works... $matmul(A[I,J,K], B[I,K,L]) \longrightarrow C[I,J,L]$.

```
[26]: def dft_real_d3(x, fft_length=None, transpose=True):
          if len(x.shape) != 3:
              raise RuntimeError("Not implemented for shape=%r." % x.shape)
          N = x.shape[1]
          C = x.shape[-1] if transpose else x.shape[-2]
          if fft_length is None:
              fft_length = x.shape[-1]
          size = fft_length // 2 + 1
          cst = dft_real_cst(C, fft_length)
          if transpose:
              x = numpy.transpose(x, (0, 2, 1))
              a = cst[:, :, :fft_length]
              b = x[:, :fft_length, :]
              a = numpy.expand dims(a, 0)
              b = numpy.expand_dims(b, 1)
              res = numpy.matmul(a, b)
              res = res[:, :, :size, :]
              return numpy.transpose(res, (1, 0, 3, 2))
          else:
              a = cst[:, :, :fft_length]
              b = x[:, :fft_length, :]
              a = numpy.expand_dims(a, 0)
              b = numpy.expand_dims(b, 1)
              res = numpy.matmul(a, b)
              return numpy.transpose(res, (1, 0, 2, 3))
      def fft2d_d3(mat, fft_length):
          mat = mat[:, :fft_length[-2], :fft_length[-1]]
          res = mat.copy()
          # first FFT
          res = dft_real_d3(res, fft_length=fft_length[-1], transpose=True)
          # second FFT decomposed on FFT on real part and imaginary part
          res2_real = dft_real_d3(res[0], fft_length=fft_length[-2], transpose=False)
          res2_imag = dft_real_d3(res[1], fft_length=fft_length[-2], transpose=False)
          res2_imag2 = numpy.vstack([-res2_imag[1:2], res2_imag[:1]])
          res = res2_real + res2_imag2
          size = fft_length[-1]//2 + 1
          return res[:, :, :fft_length[-2], :size]
      def fft2d any(mat, fft length):
          new\_shape = (-1, ) + mat.shape[-2:]
          mat2 = mat.reshape(new shape)
          f2 = fft2d_d3(mat2, fft_length)
          new_shape = (2, ) + mat.shape[:-2] + f2.shape[-2:]
```

```
return f2.reshape(new_shape)

shape = (3, 1, 4)
fft_length = (1, 4)
rnd = numpy.random.randn(*list(shape)).astype(numpy.float32)
fft2d_numpy = numpy.fft.fft2(rnd, fft_length)
fft2d_cus = fft2d_any(rnd, fft_length)
almost_equal(fft2d_numpy[..., :3], fft2d_cus)
```

We check with more shapes to see if the implementation works for all of them.

```
[27]: for shape in [(3, 1, 4), (5, 7), (3, 5, 7), (7, 5)]:
          for fft_length in [shape[-2:], (1, shape[-1]),
                               (\min(2, \text{ shape}[-2]), \text{ shape}[-1]),
                               (shape[-2], 2),
                               (\min(3, \text{ shape}[-2]), \min(4, \text{ shape}[-2])):
              x = numpy.random.randn(*list(shape)).astype(numpy.float32)
              fnp = numpy.fft.fft2(x, fft_length)
              if len(fnp.shape) == 2:
                   fn= numpy.expand_dims(fnp, 0)
              try:
                   cus = fft2d_any(x, fft_length)
              except IndexError as e:
                   print("ERR x.shape=%r length=%r error=%r" % (x.shape, fft_length, e))
                   continue
              try:
                   almost_equal(fnp[..., :cus.shape[-1]], cus)
               except (AssertionError, IndexError) as e:
                   print("DIS x.shape=%r length=%r error=%r output shape=%r or %r" % (
                       x.shape, fft length, e, fnp.shape, cus.shape))
                   continue
              print("OK x.shape=%r length=%r output shape=%r or %r" % (
                   x.shape, fft_length, fnp.shape, cus.shape))
```

```
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 1, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 1, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 1, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 2) output shape=(3, 1, 2) or (2, 3, 1, 2)
OK x.shape=(3, 1, 4) length=(1, 1) output shape=(3, 1, 1) or (2, 3, 1, 1)
OK x.shape=(5, 7) length=(5, 7) output shape=(5, 7) or (2, 5, 4)
OK x.shape=(5, 7) length=(1, 7) output shape=(1, 7) or (2, 1, 4)
OK x.shape=(5, 7) length=(2, 7) output shape=(2, 7) or (2, 2, 4)
OK x.shape=(5, 7) length=(5, 2) output shape=(5, 2) or (2, 5, 2)
OK x.shape=(5, 7) length=(3, 4) output shape=(3, 4) or (2, 3, 3)
OK x.shape=(3, 5, 7) length=(5, 7) output shape=(3, 5, 7) or (2, 3, 5, 4)
OK x.shape=(3, 5, 7) length=(1, 7) output shape=(3, 1, 7) or (2, 3, 1, 4)
OK x.shape=(3, 5, 7) length=(2, 7) output shape=(3, 2, 7) or (2, 3, 2, 4)
OK x.shape=(3, 5, 7) length=(5, 2) output shape=(3, 5, 2) or (2, 3, 5, 2)
OK x.shape=(3, 5, 7) length=(3, 4) output shape=(3, 3, 4) or (2, 3, 3, 3)
OK x.shape=(7, 5) length=(7, 5) output shape=(7, 5) or (2, 7, 3)
OK x.shape=(7, 5) length=(1, 5) output shape=(1, 5) or (2, 1, 3)
OK x.shape=(7, 5) length=(2, 5) output shape=(2, 5) or (2, 2, 3)
OK x.shape=(7, 5) length=(7, 2) output shape=(7, 2) or (2, 7, 2)
```

```
OK x.shape=(7, 5) length=(3, 4) output shape=(3, 4) or (2, 3, 3)
```

1.5.2 ONNX version

Let's look into the differences first.

```
[28]: %load_ext pyquickhelper
[29]: %%html
     <style>
     table td, table th, table tr {text-align:left !important; white-space: pre;}
     </style>
     <IPython.core.display.HTML object>
[30]: import inspect
     text1 = inspect.getsource(dft_real)
     text2 = inspect.getsource(dft_real_d3)
     %codediff text1 text2 --verbose 1 --two 1
     100%|;;;;;;;; | 24/24 [00:00<00:00, 573.03it/s]
[30]: <IPython.core.display.HTML object>
[31]: text1 = inspect.getsource(fft2d)
     text2 = inspect.getsource(fft2d_d3)
     %codediff text1 text2 --verbose 1 --two 1
     [31]: <IPython.core.display.HTML object>
[32]: def onnx_rfft_3d_1d(x, fft_length=None, transpose=True):
         if fft_length is None:
             raise RuntimeError("fft_length must be specified.")
         size = fft_length // 2 + 1
         cst = dft_real_cst(fft_length, fft_length).astype(numpy.float32)
         if transpose:
             xt = npnx.transpose(x, (0, 2, 1))
             a = cst[:, :, :fft_length]
             b = xt[:, :fft length, :]
             a = npnx.expand_dims(a, 0)
             b = npnx.expand_dims(b, 1)
             res = npnx.matmul(a, b)
             res2 = res[:, :size, :]
             return npnx.transpose(res2, (1, 0, 3, 2))
         else:
             a = cst[:, :, :fft_length]
             b = x[:, :fft_length, :]
             a = npnx.expand_dims(a, 0)
             b = npnx.expand_dims(b, 1)
```

```
res = npnx.matmul(a, b)
        return npnx.transpose(res, (1, 0, 2, 3))
def onnx_rfft_3d_2d(x, fft_length=None):
   mat = x[:, :fft_length[-2], :fft_length[-1]]
    # first FFT
    res = onnx_rfft_3d_1d(mat, fft_length=fft_length[-1], transpose=True)
    # second FFT decomposed on FFT on real part and imaginary part
    res2_real = onnx_rfft_3d_1d(res[0], fft_length=fft_length[0], transpose=False)
    res2_imag = onnx_rfft_3d_1d(res[1], fft_length=fft_length[0], transpose=False)
   res2_imag2 = npnx.vstack(-res2_imag[1:2], res2_imag[:1])
    res = res2_real + res2_imag2
    size = fft_length[1]//2 + 1
    return res[:, :, :fft length[-2], :size]
@onnxnumpy_np(signature=NDArrayType(("T:all", ), dtypes_out=('T',)))
def onnx_rfft_2d_any(x, fft_length=None):
    new_shape = npnx.concat(
        numpy.array([-1], dtype=numpy.int64), x.shape[-2:], axis=0)
    mat2 = x.reshape(new_shape)
    f2 = onnx_rfft_3d_2d(mat2, fft_length)
    new_shape = npnx.concat(
        numpy.array([2], dtype=numpy.int64), x.shape[:-2], f2.shape[-2:])
    return f2.reshape(new_shape)
shape = (3, 1, 4)
fft_length = (1, 4)
rnd = numpy.random.randn(*list(shape)).astype(numpy.float32)
fft2d cus = fft2d any(rnd, fft length)
fft2d_onx = onnx_rfft_2d_any(rnd, fft_length=fft_length)
almost_equal(fft2d_cus, fft2d_onx)
```

Let's do the same comparison.

```
except IndexError as e:
    print("ERR x.shape=%r length=%r error=%r" % (x.shape, fft_length, e))
    continue

try:
    almost_equal(onx, cus)
except (AssertionError, IndexError) as e:
    print("DIS x.shape=%r length=%r error=%r output shape=%r or %r" % (
        x.shape, fft_length, e, fnp.shape, cus.shape))
    continue
print("OK x.shape=%r length=%r output shape=%r or %r" % (
    x.shape, fft_length, fnp.shape, cus.shape))
```

```
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 4) output shape=(3, 4) or (2, 3, 1, 3)
OK x.shape=(3, 1, 4) length=(1, 2) output shape=(3, 4) or (2, 3, 1, 2)
OK x.shape=(3, 1, 4) length=(1, 1) output shape=(3, 4) or (2, 3, 1, 1)
OK x.shape=(5, 7) length=(5, 7) output shape=(3, 4) or (2, 5, 4)
OK x.shape=(5, 7) length=(1, 7) output shape=(3, 4) or (2, 1, 4)
OK x.shape=(5, 7) length=(2, 7) output shape=(3, 4) or (2, 2, 4)
OK x.shape=(5, 7) length=(5, 2) output shape=(3, 4) or (2, 5, 2)
OK x.shape=(5, 7) length=(3, 4) output shape=(3, 4) or (2, 3, 3)
OK x.shape=(3, 5, 7) length=(5, 7) output shape=(3, 4) or (2, 3, 5, 4)
OK x.shape=(3, 5, 7) length=(1, 7) output shape=(3, 4) or (2, 3, 1, 4)
OK x.shape=(3, 5, 7) length=(2, 7) output shape=(3, 4) or (2, 3, 2, 4)
OK x.shape=(3, 5, 7) length=(5, 2) output shape=(3, 4) or (2, 3, 5, 2)
OK x.shape=(3, 5, 7) length=(3, 4) output shape=(3, 4) or (2, 3, 3, 3)
OK x.shape=(7, 5) length=(7, 5) output shape=(3, 4) or (2, 7, 3)
OK x.shape=(7, 5) length=(1, 5) output shape=(3, 4) or (2, 1, 3)
OK x.shape=(7, 5) length=(2, 5) output shape=(3, 4) or (2, 2, 3)
OK x.shape=(7, 5) length=(7, 2) output shape=(3, 4) or (2, 7, 2)
OK x.shape=(7, 5) length=(3, 4) output shape=(3, 4) or (2, 3, 3)
```

There is one issue with fft_length=(1, 1) but that case is out of scope.

1.5.3 ONNX graph

[34]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x25b44556730>

```
[35]: with open("fft2d_any.onnx", "wb") as f:
    key = list(onnx_rfft_2d_any.signed_compiled)[0]
    f.write(onnx_rfft_2d_any.signed_compiled[key].compiled.onnx_.SerializeToString())
```

Let's check the intermediate results.

```
[36]: key = list(onnx_rfft_2d_any.signed_compiled)[0]
key
```

[36]: FctVersion((numpy.float32,), ((1, 4),))

```
[37]: from mlprodict.onnxrt import OnnxInference
      x = numpy.random.randn(3, 1, 4).astype(numpy.float32)
      onx = onnx_rfft_2d_any.signed_compiled[key].compiled.onnx_
      oinf = OnnxInference(onx)
      oinf.run({'x': x}, verbose=1, fLOG=print)
     +ki='init': (1,) (dtype=int64 min=0 max=0)
     +ki='init_1': (1,) (dtype=int64 min=-2 max=-2)
     +ki='init_3': (1,) (dtype=int64 min=-1 max=-1)
     +ki='init_4': (2,) (dtype=int64 min=0 max=0)
     +ki='init_5': (2,) (dtype=int64 min=1 max=4)
     +ki='init_6': (2,) (dtype=int64 min=1 max=2)
     +ki='init_8': (1,) (dtype=int64 min=4 max=4)
     +ki='init_9': (1,) (dtype=int64 min=1 max=1)
     +ki='init_b11': (2, 4, 4) (dtype=float32 min=-1.0 max=1.0)
     +ki='init_b14': (1,) (dtype=int64 min=3 max=3)
     +ki='init_b16': () (dtype=int64 min=1 max=1)
     +ki='init b21': (2, 1, 1) (dtype=float32 min=0.0 max=1.0)
     +ki='init_b23': () (dtype=int64 min=0 max=0)
     +ki='init_b28': (1,) (dtype=int64 min=2 max=2)
     +ki='init_b37': (2,) (dtype=int64 min=1 max=3)
     +ki='init_b38': (2,) (dtype=int64 min=2 max=3)
     -- OnnxInference: run 38 nodes
     Onnx-Shape(x) -> out_sha_0
                                   (name='_shape')
     +kr='out_sha_0': (3,) (dtype=int64 min=1 max=4)
     Onnx-Shape(out_sha_0) -> out_sha_0_1
                                              (name='_shape_1')
     +kr='out_sha_0_1': (1,) (dtype=int64 min=3 max=3)
     Onnx-Gather(out_sha_0_1, init) -> out_gat_0
                                                     (name='_gather')
     +kr='out_gat_0': (1,) (dtype=int64 min=3 max=3)
     Onnx-Slice(out_sha_0, init_1, out_gat_0, init) -> out_sli_0
                                                                     (name='_slice')
     +kr='out_sli_0': (2,) (dtype=int64 min=1 max=4)
     Onnx-Concat(init_3, out_sli_0) -> out_con_0
                                                     (name='_concat')
     +kr='out_con_0': (3,) (dtype=int64 min=-1 max=4)
     Onnx-Reshape(x, out_con_0) -> out_res_0
                                                (name='_reshape')
     +kr='out_res_0': (3, 1, 4) (dtype=float32 min=-2.0340726375579834
     max=2.391742706298828)
     Onnx-Slice(out_res_0, init_4, init_5, init_6) -> out_sli_0_1
     (name='_slice_1')
     +kr='out_sli_0_1': (3, 1, 4) (dtype=float32 min=-2.0340726375579834
     max=2.391742706298828)
     Onnx-Transpose(out_sli_0_1) -> out_tra_0
                                                  (name='_transpose')
     +kr='out_tra_0': (3, 4, 1) (dtype=float32 min=-2.0340726375579834
     max=2.391742706298828)
     Onnx-Slice(out_tra_0, init, init_8, init_9) -> out_sli_0_2
                                                                    (name='_slice_2')
     +kr='out_sli_0_2': (3, 4, 1) (dtype=float32 min=-2.0340726375579834
     max=2.391742706298828)
     Onnx-Unsqueeze(out_sli_0_2, init_9) -> out_uns_0
                                                          (name='_unsqueeze')
     +kr='out_uns_0': (3, 1, 4, 1) (dtype=float32 min=-2.0340726375579834
     max=2.391742706298828)
     Onnx-Unsqueeze(init_b11, init) -> out_uns_0_1
                                                       (name='_unsqueeze_1')
     +kr='out_uns_0_1': (1, 2, 4, 4) (dtype=float32 min=-1.0 max=1.0)
     Onnx-MatMul(out_uns_0_1, out_uns_0) -> out_mat_0
                                                         (name=' matmul')
     +kr='out_mat_0': (3, 2, 4, 1) (dtype=float32 min=-2.188795566558838
```

```
max=3.3646905422210693)
Onnx-Slice(out mat 0, init, init b14, init 9) -> out sli 0 3
(name=' slice 3')
+kr='out_sli_0_3': (3, 2, 4, 1) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Transpose(out sli 0 3) -> out tra 0 1
                                            (name=' transpose 1')
+kr='out tra 0 1': (2, 3, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Gather(out_tra_0_1, init_b16) -> out_gat_0_1
                                                    (name='_gather_1')
+kr='out_gat_0_1': (3, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Slice(out_gat_0_1, init, init_9, init_9) -> out_sli_0_4
(name='_slice_4')
+kr='out_sli_0_4': (3, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Unsqueeze(out_sli_0_4, init_9) -> out_uns_0_2
                                                     (name='_unsqueeze_2')
+kr='out_uns_0_2': (3, 1, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Unsqueeze(init_b21, init) -> out_uns_0_3
                                               (name=' unsqueeze 3')
+kr='out_uns_0_3': (1, 2, 1, 1) (dtype=float32 min=0.0 max=1.0)
Onnx-MatMul(out_uns_0_3, out_uns_0_2) -> out_mat_0_1
                                                       (name=' matmul 1')
+kr='out_mat_0_1': (3, 2, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Gather(out tra 0 1, init b23) -> out gat 0 2
                                                    (name=' gather 2')
+kr='out gat 0 2': (3, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
+kr='out_tra_0_2': (2, 3, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Slice(out_gat_0_2, init, init_9, init_9) -> out_sli_0_5
(name='_slice_5')
+kr='out_sli_0_5': (3, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Slice(out_tra_0_2, init_9, init_b28, init) -> out_sli_0_6
(name=' slice 6')
+kr='out_sli_0_6': (1, 3, 1, 4) (dtype=float32 min=0.0 max=0.0)
Onnx-Unsqueeze(out sli 0 5, init 9) -> out uns 0 4 (name=' unsqueeze 4')
+kr='out_uns_0_4': (3, 1, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Slice(out_tra_0_2, init, init_9, init) -> out_sli_0_7
                                                            (name='_slice_7')
+kr='out sli 0 7': (1, 3, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Neg(out sli 0 6) -> out neg 0
                                   (name=' neg')
+kr='out_neg_0': (1, 3, 1, 4) (dtype=float32 min=-0.0 max=-0.0)
Onnx-MatMul(out_uns_0_3, out_uns_0_4) -> out_mat_0_2
                                                       (name='_matmul_2')
+kr='out_mat_0_2': (3, 2, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Concat(out_neg_0, out_sli_0_7) -> out_con_0_1
                                                     (name=' concat 1')
+kr='out_con_0_1': (2, 3, 1, 4) (dtype=float32 min=-2.054079532623291
max=2.054079532623291)
Onnx-Transpose(out_mat_0_2) -> out_tra_0_3
                                             (name='_transpose_3')
+kr='out_tra_0_3': (2, 3, 1, 4) (dtype=float32 min=-2.188795566558838
max=3.3646905422210693)
Onnx-Add(out tra 0 3, out con 0 1) -> out add 0 (name=' add')
```

```
+kr='out_add_0': (2, 3, 1, 4) (dtype=float32 min=-2.188795566558838
     max=3.3646905422210693)
     Onnx-Slice(out_add_0, init_4, init_b37, init_b38) -> out_sli_0_8
     (name='_slice_8')
     +kr='out_sli_0_8': (2, 3, 1, 3) (dtype=float32 min=-2.188795566558838
     max=3.3646905422210693)
     Onnx-Shape(out sli 0 8) -> out sha 0 2
                                                (name=' shape 2')
     +kr='out_sha_0_2': (4,) (dtype=int64 min=1 max=3)
     Onnx-Shape(out_sha_0_2) -> out_sha_0_3
                                                (name='_shape_3')
     +kr='out_sha_0_3': (1,) (dtype=int64 min=4 max=4)
     Onnx-Gather(out_sha_0_3, init) -> out_gat_0_3
                                                       (name='_gather_3')
     +kr='out_gat_0_3': (1,) (dtype=int64 min=4 max=4)
     Onnx-Slice(out_sha_0_2, init_1, out_gat_0_3, init) -> out_sli_0_9
     (name='_slice_9')
     +kr='out_sli_0_9': (2,) (dtype=int64 min=1 max=3)
     Onnx-Slice(out_sha_0, init, init_1, init) -> out_sli_0_b10
     (name='_slice_b10')
     +kr='out_sli_0_b10': (1,) (dtype=int64 min=3 max=3)
     Onnx-Concat(init_b28, out_sli_0_b10, out_sli_0_9) -> out_con_0_2
     (name=' concat 2')
     +kr='out_con_0_2': (4,) (dtype=int64 min=1 max=3)
     Onnx-Reshape(out_sli_0_8, out_con_0_2) -> y
                                                     (name='_reshape_1')
     +kr='y': (2, 3, 1, 3) (dtype=float32 min=-2.188795566558838
     max=3.3646905422210693)
[37]: {'y': array([[[-8.3439898e-01, 6.9026375e-01, 3.2907667e+00]],
               [[3.3646905e+00, -2.9031307e-01, -2.0941215e+00]],
               [[ 2.1246734e+00, 5.1293659e-01, -2.1887956e+00]]],
              [[[ 0.0000000e+00, -2.0055625e+00, 8.1667386e-16]],
               [[ 0.0000000e+00, 2.0540795e+00, -8.0671079e-16]],
               [[ 0.0000000e+00, -3.2617974e-01, -5.5504507e-16]]]],
             dtype=float32)}
[38]:
```