onnx discrepencies

April 5, 2022

1 Discrepencies with ONNX

The notebook shows one example where the conversion leads with discrepencies if default options are used. It converts a pipeline with two steps, a scaler followed by a tree.

The bug this notebook is tracking does not always appear, it has a better chance to happen with integer features but that's not always the case. The notebook must be run again in that case.

```
[1]: from jyquickhelper import add_notebook_menu add_notebook_menu()
```

[1]: <IPython.core.display.HTML object>

```
[2]: %matplotlib inline
```

1.1 Data and first model

We take a random datasets with mostly integers.

```
[3]: import math
import numpy
from sklearn.datasets import make_regression
from sklearn.model_selection import train_test_split

X, y = make_regression(10000, 10)
X_train, X_test, y_train, y_test = train_test_split(X, y)

Xi_train, yi_train = X_train.copy(), y_train.copy()
Xi_test, yi_test = X_test.copy(), y_test.copy()
for i in range(X.shape[1]):
    Xi_train[:, i] = (Xi_train[:, i] * math.pi * 2 ** i).astype(numpy.int64)
    Xi_test[:, i] = (Xi_test[:, i] * math.pi * 2 ** i).astype(numpy.int64)
```

```
model.fit(Xi_train, yi_train)
[4]: Pipeline(steps=[('scaler', StandardScaler()),
                     ('dt', DecisionTreeRegressor(max_depth=10))])
[5]: model.predict(Xi_test[:5])
[5]: array([-283.03708629, 263.17931397, -160.34784206, -126.59514441,
            -150.1963714 ])
    Other models:
[6]: model2 = Pipeline([
         ('scaler', StandardScaler()),
         ('dt', DecisionTreeRegressor(max_depth=max_depth))
     ])
     model3 = Pipeline([
         ('scaler', StandardScaler()),
         ('dt', DecisionTreeRegressor(max_depth=3))
    ])
     models = \Gamma
         ('bug', Xi_test.astype(numpy.float32), model),
         ('no scaler', Xi_test.astype(numpy.float32),
         DecisionTreeRegressor(max_depth=max_depth).fit(Xi_train, yi_train)),
         ('float', X_test.astype(numpy.float32),
         model2.fit(X_train, y_train)),
         ('max_depth=3', X_test.astype(numpy.float32),
          model3.fit(X_train, y_train))
    ]
    1.2 Conversion to ONNX
[7]: import numpy
     from mlprodict.onnx_conv import to_onnx
     onx = to_onnx(model, X_train[:1].astype(numpy.float32))
[8]: from mlprodict.onnxrt import OnnxInference
     oinfpy = OnnxInference(onx, runtime="python_compiled")
     print(oinfpy)
    OnnxInference(...)
        def compiled_run(dict_inputs):
            # inputs
            X = dict inputs['X']
            (variable1, ) = n0_scaler(X)
            (variable, ) = n1_treeensembleregressor(variable1)
            return {
                'variable': variable,
            }
```

```
[9]: import pandas

X32 = Xi_test.astype(numpy.float32)
y_skl = model.predict(X32)

obs = [dict(runtime='sklearn', diff=0)]
for runtime in ['python', 'python_compiled', 'onnxruntime1']:
    oinf = OnnxInference(onx, runtime=runtime)
    y_onx = oinf.run({'X': X32})['variable']
    delta = numpy.abs(y_skl - y_onx.ravel())
    am = delta.argmax()
    obs.append(dict(runtime=runtime, diff=delta.max()))
    obs[-1]['v[%d]' % am] = y_onx.ravel()[am]
    obs[0]['v[%d]' % am] = y_skl.ravel()[am]

pandas.DataFrame(obs)
```

```
[9]: runtime diff v[1583]
0 sklearn 0.000000 -439.590635
1 python 133.641599 -305.949036
2 python_compiled 133.641599 -305.949036
3 onnxruntime1 133.641599 -305.949036
```

The pipeline shows huge discrepencies. They appear for a pipeline StandardScaler + DecisionTreeRegressor applied in integer features. They disappear if floats are used, or if the scaler is removed. The bug also disappear if the tree is not big enough (max_depth=4 instread of 5).

```
obs = [dict(runtime='sklearn', diff=0, name='sklearn')]
for name, x32, mod in models:
    for runtime in ['python', 'python_compiled', 'onnxruntime1']:
        lonx = to_onnx(mod, x32[:1])
        loinf = OnnxInference(lonx, runtime=runtime)
        y_skl = mod.predict(X32)
        y_onx = loinf.run({'X': X32})['variable']
        delta = numpy.abs(y_skl - y_onx.ravel())
        am = delta.argmax()
        obs.append(dict(runtime=runtime, diff=delta.max(), name=name))
        obs[-1]['v[%d]' % am] = y_onx.ravel()[am]
        obs[0]['v[%d]' % am] = y_skl.ravel()[am]

df = pandas.DataFrame(obs)
df
```

```
[10]:
                   runtime
                                   diff
                                                 name
                                                           v[1583]
                                                                        v[1109]
      0
                   sklearn
                               0.000000
                                              sklearn -439.590635
                                                                     516.084502
                                                   bug -305.949036
      1
                    python 133.641599
                                                                             NaN
      2
           python_compiled
                            133.641599
                                                  bug -305.949036
                                                                             NaN
      3
              onnxruntime1
                            133.641599
                                                  bug -305.949036
                                                                            NaN
      4
                    python
                               0.000029
                                            no scaler
                                                               NaN
                                                                     516.084473
      5
           python_compiled
                               0.000029
                                            no scaler
                                                               {\tt NaN}
                                                                     516.084473
      6
              onnxruntime1
                               0.000029
                                            no scaler
                                                               NaN
                                                                     516.084473
      7
                    python
                               0.000029
                                                float
                                                               {\tt NaN}
                                                                            NaN
          python_compiled
                               0.000029
                                                float
                                                                            NaN
      8
                                                               NaN
              onnxruntime1
                               0.000029
                                                float
                                                               NaN
                                                                             NaN
```

```
10
                              0.000003 max_depth=3
                                                              NaN
                                                                          NaN
                    python
          python_compiled
                              0.000003
                                        max depth=3
                                                              NaN
                                                                          NaN
      12
             onnxruntime1
                                        max_depth=3
                              0.000003
                                                              NaN
                                                                          NaN
               v[19]
                            v[4]
         -549.753386 -97.726497
                 NaN
                             NaN
      1
      2
                  NaN
                             NaN
      3
                 NaN
                             NaN
      4
                 NaN
                             NaN
      5
                  NaN
                             NaN
      6
                 NaN
                             NaN
      7
         -549.753357
                             NaN
      8
        -549.753357
                             NaN
        -549.753357
                             NaN
      9
      10
                 NaN -97.726494
                 NaN -97.726494
      11
      12
                 NaN -97.726494
[11]: df.pivot("runtime", "name", "diff")
[11]: name
                                        float max_depth=3 no scaler
                               bug
      runtime
      onnxruntime1
                        133.641599
                                    0.000029
                                                  0.000003
                                                              0.000029
                                                                             NaN
                                                                            NaN
                                    0.000029
                                                  0.000003
                                                              0.000029
      python
                        133.641599
      python_compiled 133.641599
                                    0.000029
                                                  0.000003
                                                              0.000029
                                                                            NaN
      sklearn
                                                       NaN
                                                                             0.0
                               NaN
                                          NaN
                                                                   NaN
```

1.3 Other way to convert

ONNX does not support double for TreeEnsembleRegressor but that a new operator TreeEnsembleRegressorDouble was implemented into mlprodict. We need to update the conversion.

```
[12]: %load_ext mlprodict
[13]: onx32 = to_onnx(model, X_train[:1].astype(numpy.float32))
      onx64 = to_onnx(model, X_train[:1].astype(numpy.float64),
                      rewrite_ops=True)
      %onnxview onx64
[13]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x1c394fc1048>
[14]: X32 = Xi_test.astype(numpy.float32)
      X64 = Xi test.astype(numpy.float64)
      obs = [dict(runtime='sklearn', diff=0)]
      for runtime in ['python', 'python_compiled', 'onnxruntime1']:
          for name, onx, xr in [('float', onx32, X32), ('double', onx64, X64)]:
              try:
                  oinf = OnnxInference(onx, runtime=runtime)
              except Exception as e:
                  obs.append(dict(runtime=runtime, error=str(e), real=name))
                  continue
              y_skl = model.predict(xr)
```

```
y_onx = oinf.run({'X': xr})['variable']
delta = numpy.abs(y_skl - y_onx.ravel())
am = delta.argmax()
obs.append(dict(runtime=runtime, diff=delta.max(), real=name))
obs[-1]['v[%d]' % am] = y_onx.ravel()[am]
obs[0]['v[%d]' % am] = y_skl.ravel()[am]
pandas.DataFrame(obs)
```

```
Γ14]:
                 runtime
                                 diff
                                           v[1583]
                                                           v[0]v
                                                                   real \
      0
                  sklearn
                             0.000000 -439.590635 -283.037086
                                                                    NaN
      1
                  python
                           133.641599 -305.949036
                                                                  float
                                                            NaN
      2
                  python
                             0.000000
                                               NaN -283.037086
                                                                 double
      3
        python_compiled
                           133.641599 -305.949036
                                                            NaN
                                                                  float
         python_compiled
                             0.000000
                                               NaN -283.037086
                                                                 double
      5
            onnxruntime1
                           133.641599 -305.949036
                                                            NaN
                                                                  float
      6
            onnxruntime1
                                  NaN
                                               NaN
                                                            NaN
                                                                 double
                                                        error
      0
                                                         NaN
      1
                                                         NaN
      2
                                                         NaN
      3
                                                         NaN
      4
                                                         NaN
      5
                                                         NaN
         Unable to create InferenceSession due to '[ONN...
```

We see that the use of double removes the discrepencies.

1.4 OnnxPipeline

Another way to reduce the number of discrepencies is to use a pipeline which converts every steps into ONNX before training the next one. That way, every steps is either trained on the inputs, either trained on the outputs produced by ONNX. Let's see how it works.

C:\xavierdupre__home_\github_fork\scikit-learn\sklearn\base.py:209:
FutureWarning: From version 0.24, get_params will raise an AttributeError if a parameter cannot be retrieved as an instance attribute. Previously it would return None.

FutureWarning)

[15]: OnnxPipeline(steps=[('scaler',

 $\label{lem:connx_bytes=b'} OnnxTransformer(onnx_bytes=b'\x08\x06\x12\x08skl2onnx\x1a\x 081.7.1076"\x07ai.onnx(\x002\x00:\xf6\x01\n\xa6\x01\n\x01X\x12\x08variable\x1a\x 06Scaler"\x06Scaler*=\n\x06offset=>\xc3:;=+=\xc0;=|\xf2\xb0<=\xcd`\xf9>=\x89\xad 3\xbd=RL\xab\xbf=V\xc4V\xbe=6<\x9d\xc0=B>\xa0@=\xbb\x93\xea@\xa0\x01\x06*<\n\x05$

We see that the first steps was replaced by an object *OnnxTransformer* which wraps an ONNX file into a transformer following the *scikit-learn* API. The initial steps are still available.

```
[16]: model_onx.raw_steps_
[16]: [('scaler', StandardScaler()), ('dt', DecisionTreeRegressor(max_depth=10))]
[17]: models = [
          ('bug', Xi_test.astype(numpy.float32), model),
          ('OnnxPipeline', Xi_test.astype(numpy.float32), model_onx),
      ]
[18]: obs = [dict(runtime='sklearn', diff=0, name='sklearn')]
      for name, x32, mod in models:
          for runtime in ['python', 'python_compiled', 'onnxruntime1']:
              lonx = to_onnx(mod, x32[:1])
              loinf = OnnxInference(lonx, runtime=runtime)
              y_skl = model_onx.predict(X32) # model_onx is the new baseline
              y_onx = loinf.run({'X': X32})['variable']
              delta = numpy.abs(y_skl - y_onx.ravel())
              am = delta.argmax()
              obs.append(dict(runtime=runtime, diff=delta.max(), name=name))
              obs[-1]['v[%d]' \% am] = y_onx.ravel()[am]
              obs[0]['v[%d]' % am] = y_skl.ravel()[am]
      df = pandas.DataFrame(obs)
```

```
[18]:
                  runtime
                                   diff
                                                            v [2276]
                                                                         v[1109]
                                                  name
                              0.000000
                                               sklearn 272.784708 516.084502
      0
                  sklearn
                   python
                            234.930666
                                                   bug
                                                          37.854042
                                                                             NaN
      1
         python_compiled
                            234.930666
                                                          37.854042
      2
                                                   bug
                                                                             NaN
      3
             onnxruntime1
                            234.930666
                                                   bug
                                                          37.854042
                                                                             NaN
                   python
      4
                              0.000029
                                         OnnxPipeline
                                                                {\tt NaN}
                                                                     516.084473
         python_compiled
                              0.000029
                                         OnnxPipeline
                                                                     516.084473
                                                                \mathtt{NaN}
                                         OnnxPipeline
             onnxruntime1
                              0.000029
                                                                {\tt NaN}
                                                                     516.084473
```

Training the next steps based on ONNX outputs is better. This is not completely satisfactory... Let's check the accuracy.

```
[19]: model.score(Xi_test, yi_test), model_onx.score(Xi_test, yi_test)
```

[19]: (0.6492778377907853, 0.6536515451871481)

Pretty close.

1.5 Final explanation: StandardScalerFloat

We proposed two ways to have an ONNX pipeline which produces the same prediction as *scikit-learn*. Let's now replace the StandardScaler by a new one which outputs float and not double. It turns out that

class StandardScaler computes X /= self.scale_ but ONNX does X *= self.scale_inv_. We need to implement this exact same operator with float32 to remove all discrepencies.

```
[20]: class StandardScalerFloat(StandardScaler):
          def __init__(self, with_mean=True, with_std=True):
              StandardScaler.__init__(self, with_mean=with_mean, with_std=with_std)
          def fit(self, X, y=None):
              StandardScaler.fit(self, X, y)
              if self.scale_ is not None:
                  self.scale_inv_ = (1. / self.scale_).astype(numpy.float32)
              return self
          def transform(self, X):
              X = X.copy()
              if self.with_mean:
                  X -= self.mean
              if self.with_std:
                  X *= self.scale inv
              return X
      model_float = Pipeline([
          ('scaler', StandardScalerFloat()),
          ('dt', DecisionTreeRegressor(max_depth=max_depth))
      ])
      model_float.fit(Xi_train.astype(numpy.float32), yi_train.astype(numpy.float32))
[20]: Pipeline(steps=[('scaler', StandardScalerFloat()),
                      ('dt', DecisionTreeRegressor(max depth=10))])
[21]: try:
          onx_float = to_onnx(model_float, Xi_test[:1].astype(numpy.float))
      except RuntimeError as e:
          print(e)
     Unable to find a shape calculator for type '<class
     '__main__.StandardScalerFloat'>'.
     It usually means the pipeline being converted contains a
     transformer or a predictor with no corresponding converter
     implemented in sklearn-onnx. If the converted is implemented
     in another library, you need to register
     the converted so that it can be used by sklearn-onnx (function
     update_registered_converter). If the model is not yet covered
     by sklearn-onnx, you may raise an issue to
     https://github.com/onnx/sklearn-onnx/issues
     to get the converter implemented or even contribute to the
     project. If the model is a custom model, a new converter must
     be implemented. Examples can be found in the gallery.
```

We need to register a new converter so that *sklearn-onnx* knows how to convert the new scaler. We reuse the existing converters.

```
[22]: from skl2onnx import update_registered_converter
      from skl2onnx.operator_converters.scaler_op import convert_sklearn_scaler
      from skl2onnx.shape_calculators.scaler import calculate_sklearn_scaler_output_shapes
      update registered converter(
          StandardScalerFloat, "SklearnStandardScalerFloat",
          calculate sklearn scaler output shapes,
          convert_sklearn_scaler,
          options={'div': ['std', 'div', 'div cast']})
\lceil 23 \rceil : | models = \lceil
          ('bug', Xi_test.astype(numpy.float32), model),
          ('FloatPipeline', Xi_test.astype(numpy.float32), model_float),
      ]
[24]: obs = [dict(runtime='sklearn', diff=0, name='sklearn')]
      for name, x32, mod in models:
          for runtime in ['python', 'python_compiled', 'onnxruntime1']:
              lonx = to_onnx(mod, x32[:1])
              loinf = OnnxInference(lonx, runtime=runtime)
              y_skl = model_float.predict(X32) # we use model_float as a baseline
              y_onx = loinf.run({'X': X32})['variable']
              delta = numpy.abs(y_skl - y_onx.ravel())
              am = delta.argmax()
              obs.append(dict(runtime=runtime, diff=delta.max(), name=name))
              obs[-1]['v[\%d]' \% am] = y onx.ravel()[am]
              obs[0]['v[%d]' % am] = y_skl.ravel()[am]
      df = pandas.DataFrame(obs)
```

```
[24]:
                runtime
                                                       v[1489]
                                                                   v[1109]
                               diff
                                              name
                           0.000000
                                           sklearn 378.038116 516.084493
     0
                sklearn
     1
                 python 273.322334
                                               bug 104.715782
                                                                      NaN
     2 python compiled 273.322334
                                               bug 104.715782
                                                                      NaN
           onnxruntime1
     3
                         273.322334
                                               bug 104.715782
                                                                      NaN
                           0.000020 FloatPipeline
                                                          NaN 516.084473
     4
                 python
        python_compiled
                           0.000020 FloatPipeline
                                                          NaN 516.084473
           onnxruntime1
                           0.000020
                                    FloatPipeline
                                                          NaN 516.084473
```

That means than the differences between float32(X / Y) and float32(X) * float32(1 / Y) are big enough to select a different path in the decision tree. float32(X) / float32(Y) and float32(X) * float32(1 / Y) are also different enough to trigger a different path. Let's illustrate that on example:

```
[25]: a1 = numpy.random.randn(100, 2) * 10
a2 = a1.copy()
a2[:, 1] *= 1000
a3 = a1.copy()
a3[:, 0] *= 1000

for i, a in enumerate([a1, a2, a3]):
    a = a.astype(numpy.float32)
    max_diff32 = numpy.max([
```

```
0 1.9073486e-06 7.105427357601002e-15
1 3.7252903e-09 3.469446951953614e-18
2 0.00390625 7.275957614183426e-12
```

The last random set shows very big differences, obviously big enough to trigger a different path in the graph. The difference for double could probably be significant in some cases, not enough on this example.

1.6 Change the conversion with option div

Option 'div' was added to the converter for StandardScaler to change the way the scaler is converted.

[27]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x1c3955e75c0>

[28]: <jyquickhelper.jspy.render_nb_js_dot.RenderJsDot at 0x1c3943bd518>

[29]: <jyquickhelper.jspy.render nb js dot.RenderJsDot at 0x1c3955fc2e8>

The ONNX graph is different and using division. Let's measure the discrepencies.

```
obs = [dict(runtime='sklearn', diff=0, name='sklearn')]
for name, mod, onx in models:
    for runtime in ['python', 'python_compiled', 'onnxruntime1']:
        oinf = OnnxInference(onx, runtime=runtime)
        y_sk132 = mod.predict(X32)
        y_sk164 = mod.predict(X64)
        y_onx = oinf.run({'X': X32})['variable']
        delta32 = numpy.abs(y_skl32 - y_onx.ravel())
        am32 = delta32.argmax()
        delta64 = numpy.abs(y_skl64 - y_onx.ravel())
        am64 = delta64.argmax()
        obs.append(dict(runtime=runtime, diff32=delta32.max(),
                         diff64=delta64.max(), name=name))
        obs[0]['v32[\%d]' % am32] = y_sk132.ravel()[am32]
        obs[0]['v64[\%d]' \% am64] = y skl64.ravel()[am64]
        obs [-1] ['v32[%d]' % am32] = y_onx.ravel() [am32]
        obs[-1]['v64[\%d]' \% am64] = y_onx.ravel()[am64]
df = pandas.DataFrame(obs)
```

```
[30]:
                   runtime
                            diff
                                                v32[1583]
                                                             v64[1246]
                                                                          v32[1246]
                                        name
      0
                             0.0
                                    sklearn -439.590635 -364.555875 -203.438616
                   sklearn
      1
                   python
                             NaN
                                         bug -305.949036 -203.438614
                                                                                 NaN
      2
         python_compiled
                             NaN
                                         bug -305.949036 -203.438614
                                                                                 NaN
      3
             onnxruntime1
                              NaN
                                         bug -305.949036 -203.438614
                                                                                 NaN
                    python
                                                                    NaN -364.555878
      4
                              NaN
                                         div
                                                      NaN
         python_compiled
      5
                             NaN
                                         div
                                                      NaN
                                                                    NaN -364.555878
      6
             onnxruntime1
                                         div
                                                      NaN
                                                                    NaN -364.555878
                              NaN
      7
                   python
                              NaN
                                   div_cast
                                                      NaN
                                                                    NaN -364.555878
      8
         python_compiled
                              {\tt NaN}
                                   div_cast
                                                      NaN
                                                                    NaN -364.555878
      9
             onnxruntime1
                                                                    NaN -364.555878
                             {\tt NaN}
                                   div_cast
                                                      NaN
           v64[2080]
                        v64[1109]
                                         diff32
                                                      diff64
         171.604023
                       516.084502
      0
                                            NaN
                                                          NaN
                                   133.641599
                                                  161.117261
      1
                 NaN
                               {\tt NaN}
      2
                 NaN
                               NaN
                                   133.641599
                                                  161.117261
      3
                                    133.641599
                                                  161.117261
                 NaN
                               NaN
      4
         329.592377
                                    161.117261
                                                  157.988354
                               NaN
      5
         329.592377
                                    161.117261
                                                  157.988354
                               \mathtt{NaN}
         329.592377
                                                  157.988354
      6
                               {\tt NaN}
                                    161.117261
      7
                                    161.117261
                 {\tt NaN}
                       516.084473
                                                    0.000029
      8
                 NaN
                       516.084473
                                                    0.000029
                                    161.117261
      9
                                                    0.000029
                 \mathtt{NaN}
                       516.084473
                                   161.117261
```

The only combination which works is the model converted with option div_cast (use of division in double precision), float input for ONNX, double input for scikit-learn.

1.7 Explanation in practice

Based on previous sections, the following example buids a case where discreprencies are significant.

```
[31]: std = StandardScaler()
    std.fit(Xi_train)
    xt32 = Xi_test.astype(numpy.float32)
    xt64 = Xi_test.astype(numpy.float64)
    pred = std.transform(xt32)
```

```
[32]: from onnxruntime import InferenceSession

onx32 = to_onnx(std, Xi_train[:1].astype(numpy.float32))
sess32 = InferenceSession(onx32.SerializeToString())
got32 = sess32.run(0, {'X': xt32})[0]
d32 = numpy.max(numpy.abs(pred.ravel() - got32.ravel()))
d32
```

[32]: 2.3841858e-07

```
[33]: oinf32 = OnnxInference(onx32.SerializeToString())
gotpy32 = oinf32.run({'X': xt32})['variable']
dpy32 = numpy.max(numpy.abs(pred.ravel() - gotpy32.ravel()))
dpy32
```

[33]: 2.3841858e-07

We tried to cast float into double before applying the normalisation and to cast back into single float. It does not help much.

[34]: 2.3841858e-07

Last experiment, we try to use double all along.

```
[35]: from onnxruntime.capi.onnxruntime_pybind11_state import InvalidGraph
  onx64_2 = to_onnx(std, Xi_train[:1].astype(numpy.float64))
  try:
     sess64_2 = InferenceSession(onx64_2.SerializeToString())
  except InvalidGraph as e:
     print(e)
```

[ONNXRuntimeError] : 10 : INVALID_GRAPH : This is an invalid model. Error in Node:Scaler : Mismatched attribute type in 'Scaler : offset'

onnxruntime does not support this. Let's switch to mlprodict.

```
[36]: onx64_2 = to_onnx(std, Xi_train[:1].astype(numpy.float64))
sess64_2 = OnnxInference(onx64_2, runtime="python")
pred64 = std.transform(xt64)
got64_2 = sess64_2.run({'X': xt64})['variable']
d64_2 = numpy.max(numpy.abs(pred64.ravel() - got64_2.ravel()))
```

```
d64_2
```

[36]: 4.440892098500626e-16

Differences are lower if every operator is done with double.

1.8 Conclusion

```
Maybe the best option is just to introduce a transform which just cast inputs into floats.
[37]: model1 = Pipeline([
          ('scaler', StandardScaler()),
          ('dt', DecisionTreeRegressor(max_depth=max_depth))
      ])
      model1.fit(Xi_train, yi_train)
[37]: Pipeline(steps=[('scaler', StandardScaler()),
                      ('dt', DecisionTreeRegressor(max_depth=10))])
[38]: from skl2onnx.sklapi import CastTransformer
      model2 = Pipeline([
          ('cast64', CastTransformer(dtype=numpy.float64)),
          ('scaler', StandardScaler()),
          ('cast', CastTransformer()),
          ('dt', DecisionTreeRegressor(max_depth=max_depth))
      ])
      model2.fit(Xi_train, yi_train)
[38]: Pipeline(steps=[('cast64', CastTransformer(dtype=<class 'numpy.float64'>)),
                       ('scaler', StandardScaler()), ('cast', CastTransformer()),
                      ('dt', DecisionTreeRegressor(max_depth=10))])
[39]: X32 = Xi_test.astype(numpy.float32)
      models = [('model1', model1, X32), ('model2', model2, X32)]
      options = [('-', None),
                 ('div_cast', {StandardScaler: {'div': 'div_cast'}})]
      obs = [dict(runtime='sklearn', diff=0, name='model1'),
             dict(runtime='sklearn', diff=0, name='model2')]
      for name, mod, x32 in models:
          for no, opts in options:
              onx = to_onnx(mod, Xi_train[:1].astype(numpy.float32),
                            options=opts)
              for runtime in ['python', 'python_compiled', 'onnxruntime1']:
                      oinf = OnnxInference(onx, runtime=runtime)
                  except Exception as e:
                      obs.append(dict(runtime=runtime, err=str(e),
                                       name=name, options=no))
                      continue
                  y_skl = mod.predict(x32)
```

```
try:
                       y_onx = oinf.run({'X': x32})['variable']
                   except Exception as e:
                       obs.append(dict(runtime=runtime, err=str(e),
                                        name=name, options=no))
                       continue
                   delta = numpy.abs(y_skl - y_onx.ravel())
                   am = delta.argmax()
                   obs.append(dict(runtime=runtime, diff=delta.max(),
                                    name=name, options=no))
                   obs[-1]['v[\%d]' \% am] = y_onx.ravel()[am]
                   if name == 'model1':
                       obs[0]['v[\%d]' \% am] = y_skl.ravel()[am]
                       obs[1]['v[%d]' % am] = model2.predict(Xi_test).ravel()[am]
                   elif name == 'model2':
                       obs[0]['v[%d]' % am] = model1.predict(Xi_test).ravel()[am]
                       obs[1]['v[%d]' % am] = y_skl.ravel()[am]
      df = pandas.DataFrame(obs)
      df
[39]:
                   runtime
                                   diff
                                           name
                                                     v[1583]
                                                                  v[1246]
                                                                               v[1109]
                               0.000000
                                                                           516.084502
      0
                   sklearn
                                         model1 -439.590635 -162.952888
      1
                   sklearn
                              0.000000
                                         model2 -439.590635 -364.555875
                                                                           516.084502
                    python 133.641599
      2
                                         model1 -305.949036
                                                                                   NaN
                                                                      NaN
      3
          python_compiled
                            133.641599
                                         model1 -305.949036
                                                                      NaN
                                                                                   NaN
                                         model1 -305.949036
      4
              onnxruntime1
                            133.641599
                                                                                   NaN
                                                                      NaN
      5
                            201.602989
                                         model1
                                                         NaN -364.555878
                                                                                   NaN
                    python
      6
          python_compiled
                            201.602989
                                         model1
                                                         NaN -364.555878
                                                                                   NaN
      7
             onnxruntime1
                            201.602989
                                                         NaN -364.555878
                                         model1
                                                                                   NaN
      8
                    python
                              0.000029
                                         model2
                                                         NaN
                                                                      {\tt NaN}
                                                                           516.084473
      9
          python_compiled
                               0.000029
                                         model2
                                                         NaN
                                                                      NaN
                                                                           516.084473
      10
              onnxruntime1
                                    NaN
                                         model2
                                                         NaN
                                                                      NaN
                                                                                   NaN
                    python
      11
                               0.000029
                                         model2
                                                         NaN
                                                                      {\tt NaN}
                                                                           516.084473
          python_compiled
                               0.000029
                                         model2
                                                         NaN
                                                                           516.084473
      12
                                                                      {\tt NaN}
      13
             onnxruntime1
                              0.000029
                                         model2
                                                         NaN
                                                                      NaN
                                                                           516.084473
           options
                                                                      err
      0
                NaN
                                                                      NaN
                NaN
                                                                      NaN
      1
      2
                                                                      NaN
      3
                                                                      NaN
      4
                                                                      NaN
      5
          div_cast
                                                                      NaN
      6
          div_cast
                                                                      NaN
      7
          div_cast
                                                                      NaN
      8
                                                                      NaN
      9
                                                                      NaN
      10
                     Unable to create InferenceSession due to '[ONN...
      11
          div_cast
                                                                      NaN
```

NaN

12

div_cast

13 div_cast NaN

It seems to work that way.

[40]: